

Bibliographical references

Recurrence Quantification Analysis (RQA) and Cross-Recurrence Quantification Analysis (CRQA) are nonlinear methods for the analysis of nonstationary time series. They offer the quantification of the recurring patterns in phase space trajectories [19, 20]. Introduced by Trulla et al.[19] (directly built on quantifying recurrence plots[24]) and expanded by Webber and Zbilut[20], RQA measures metrics like recurrence rate, determinism, and laminarity to capture dynamic system behavior. Thomasson et al.[21] in their work, demonstrated RQA’s applicability on EEG data, mentioning the robustness it shows in accordance to noise and nonstationarity. Marwan et al.[22] further advanced recurrence plot techniques, emphasizing on developing a confidence measure of RQA in detecting dynamic transitions. Works like these, serve as a foundation of applying RQA and CRQA on EEG studies in various conditions such as epilepsy, cognitive disorders and more as explored in this review.

Frolov et al.[1] proposed an approach to analyze frequency based multiplex brain networks using recurrence quantification analysis (RQA) on EEG data, and demonstrated the way that recurrence-based synchronization indices can effectively capture both within-frequency (intralayer) and cross-frequency (interlayer) functional connectivity during cognitive tasks. Their work showed that RQA is particularly suitable for analyzing non-stationary EEG signals and revealed important insights about the evolution of functional connectivity patterns during cognitive tasks. In addition the dataset used in this research are openly available in a Figshare repository.

Núñez et al. [16] worked with resting-state EEG recordings from subjects with mild cognitive impairment(MCI), Alzheimer’s disease(AD), and healthy ground truth controls in order to detect frequency based changes into their brain dynamics. By blending wavelet based Kullback–Leibler divergence (KLD) for capturing non-stationarity, and two RQA metrics(*entropy of the recurrence point density* and the *median of the recurrence point density*) insights have been extracted related to neurodegeneration presence. Research’s findings show that MCI and AD are presenting notable changes in the recurrence structure and non-stationarity of EEG signals, and more specifics on the theta and beta frequency bands. Therefore, recurrence based dynamics show a capability as potential biomarkers for monitoring and detecting early Alzheimer’s disease and its progression.

MCI has also been investigated by Timothy et al.[25], where researchers have focused on the classification of MCI using EEG signals and combining RQA and CRQA methods. Analysis has been performed on both resting-state (eyes closed) and task-based (short-term memory) EEG data, focusing on complexity (via RQA) and synchronization (via CRQA) features. Their results indicate that MCI patients exhibit lower complexity and higher inter- and intra-hemispheric synchronization compared to healthy controls, particularly during memory tasks. The study also proposes a novel feature space approach using RQA and CRQA measures, achieving high classification accuracy (91.7%) under task conditions.

Fan and Chou [15] have also proposed an approach for real-time epileptic seizure detection using as a method the analysis of temporal synchronization patterns of EEG signals with recurrence networks and spectral graph theory. Recurrence plots were used for the modeling of the EEG dynamics, extracting graph theory's features for quantifying the synchronization. Results showed high sensitivity of 98.48% and low latency (6 seconds) for detecting seizure on the CHB-MIT dataset, performing better than other RQA measures.

Heunis and co-authors[23] have utilized resting state EEG and RQA in order to distinguish individuals of ages 0-18 of two categories; ASD (autism spectrum disorder) and typically developing. RQA features were extracted and tested on various linear and nonlinear classifiers achieving 92.9% classification accuracy with nonlinear SVM classifier.

Author in [6], investigated changes related to aging in brain sensorimotor systems using RQA and theta-band functional connectivity in EEG signals. In the study a VR experimental paradigm was utilized with auditory stimulus across different age groups (young and elder subjects). Key findings include that elder subjects present decreased EEG complexity during motor preparation stages as measured by RQA metrics (ΔRR and ΔRTE), and had increased theta band functional connectivity highlighting the potential of RQA in detecting age related biomarkers that were not detectable using standalone signal spectral analysis.

Guglielmo et al. [7] utilized RQA features extracted by EEG signals for the purpose of classification of cognitive performance during mental arithmetic tasks. They used frontal and parietal EEG signals and analyzed them, from 36 participants by extracting six RQA metrics (*recurrence rate, determinism, laminarity, entropy, maximum diagonal line length and average diagonal line length*) from four electrodes (F7, Pz, P4, Fp1). Afterwards by applying machine learning classifiers (SVM, Random Forest, and Gradient Boosting) and they reached accuracy of classification above 0.85, showing the potential that RQA holds for generalizing on nonlinear dynamics.

Mihajlović [33] studied the discriminative efficiency of traditional spectral features in comparison to RQA-derived nonlinear metrics for the cognitive effort classification purposes. Utilizing a 4-channel wearable EEG headset, data was recorded while subjects perform tasks having variable cognitive load such as relaxation, math, reading. The key finding was that while spectral features alone often yielded higher classification accuracy, RQA features such *recurrence rate, determinism ratio* were consistently ranked among the most important features for discrimination task. A conjunction of a hybrid model using both spectral and RQA features achieved the best overall performance, showing the complementary nature of the methods in brain dynamics exploration.

Yang and co-authors [17], examined stereo electroencephalography (sEEG) recordings of 10 patients with refractory focal epilepsy for analyzing dynamical differences among discrete epileptic phases/states (inter-ictal, pre-ictal, and ictal) and regions. Using recurrence plots and CRQA, they identified epileptogenic channels with longer diagonal structures in RPs, which is a sign of more deterministic and recurrent dynamics. Their findings point out that the

synchronization among the epileptogenic channels strengthened while seizures events occur, suggesting that these regions dominate the network’s dynamics.

Lopes et al. [8] have proposed a combinatorial framework by mixing RQA with dynamic functional network (dFN) analysis, applying it to both MEG and stereo EEG data. The methodology they described is split into five steps: data segmentation, functional network inference, distance computation alongside networks, recurrence plot construction and finally RQA. The study demonstrated that functional networks in epilepsy patients recur more quickly than in healthy controls, suggesting RQA on dFNs could play the role of a potential biomarker. For the EEG dataset investigation, they have showed that the pre-ictal networks shown higher recurrence rates than post-ictal periods, with the τ -recurrence rate (RR_τ) proving particularly effective for seizure detection.

Rangaprakash [18] have proposed an application of RQA for the study of brain connectivity using multichannel EEG signals. In its work, a new CRQA-based feature was proposed (Correlation between Probabilities of Recurrence (CPR)), a nonlinear and non-parametric phase synchronization technique. Afterwards it was utilized for the analysis of functional connectivity in epilepsy subjects during eyes-open/eyes-closed conditions. The results demonstrated that CPR outperformed other known traditional linear methods on distinguishing seizure and pre-seizure states, identifying epileptic foci, and differentiating alongside eyes-open and eyes-closed conditions.

In another study which demonstrates the effectiveness of RQA in analyzing EEG signals for epilepsy detection, Gruszczyńska et al.[11] applied RQA on such signals in order to distinguish epileptic from healthy patients using recordings from frontal and temporal lobe electrodes (Fp1, Fp2, T3, T4). In their findings they have showed that the epileptic signals present more periodic dynamics in comparison to healthy controls, by producing higher values of RQA parameters such as determinism, laminarity, and longest diagonal line. The combination of RQA with Principal Component Analysis for dimensionality reduction and visualization, achieved 86.8% classification accuracy with SVM. Authors also demonstrated RQA’s capability to identify pathological patterns in EEG signals without the requirement of seizure events during recording which have bad impact on the subject’s health.

Another study utilizing advanced nonlinear analysis techniques for neural correlation investigation to cognitive functions [12] used *stereoelectroencephalography (sEEG)* combined alongside RQA for the examination of the relationship of the DMN and empathy. Correlations have been detected relating specific RQA metrics (mean diagonal line length, entropy of diagonal line lengths, trapping time) and empathy scores, particularly within DMN subsystems.

Regarding epilepsy diagnosis, authors in [13] proposed a new framework utilizing the combination of RQA with genetic algorithms and Bayesian classifiers for identifying corresponding biomarkers for seizure detection. They utilized five distance norms (e.g., Euclidean, Mahalanobis) and multiple thresholds for extracting recurrence features from EEG signals, achieving 100% classification accuracy. More specific, the *transitivity* feature has shown capability of a highly discriminative biomarker, performing better compared to traditional

linear methods.

Ngamga et al.[14] studied the performance achieved of RQA and Recurrence Network (RN) measures in identifying pre-seizure states from multi-day, multi-channel intracranial EEG (iEEG) recordings of epilepsy patients. Results highlighted the correlation among RQA measures (determinism, laminarity, and mean recurrence time) in detecting seizure precursors, while RN measures (average shortest path length and network transitivity) provided complementary but not so consistent insights than using the application of RQA measures alone.

Researchers in [3], have applied RQA on resting-state fMRI data from TgF344-AD rats(a transgenic rat model which will eventually develop Alzheimer’s disease) and their healthy-control counterparts wild-type rats(WT), in order to detect early stage biomarkers for the disease. By analyzing Default Mode-Like Network (DMLN) using RQA metrics(*entropy, recurrence rate, determinism and average diagonal line length*) changes have been detected in regions of the basal forebrain, hippocampal fields (CA1, CA3), and visual cortices (V1, V2). Also on the study’s findings include reduced predictability in WT rats with aging, while AD rats exhibited less decline in predictability, suggesting some unknown yet countereacting mechanisms. This study highlights RQA’s sensitivity for nonlinear dynamics in preclinical AD and the code used is also publicly available.

Lombardi et al.[5] investigated the nonlinear properties in fMRI BOLD signals during a working memory task in schizophrenic patients and healthy controls. They have attempted by using RQA, to analyze recurrence plots for quantifying determinism, trapping time, and maximal vertical line length in functionally relevant brain clusters. Outcome revealed differences in the dynamics between the two groups, and more specific in working memory and DMN areas. While their work have focused on fMRI, the methodology can be adapted also into EEG signals, which can offer a higher resolution for capturing rapid neural dynamics.

Kang et al. [2], in their study explore the dynamics and functional connectivity of the Default Mode Network (DMN) in schizophrenia, applying RQA-CRQA on resting-state fMRI data. Findings include decreased *determinism* between specific DMN regions (vMPFC-posterior cingulate and vMPFC-precuneus) in first-episode schizophrenia patients, as a signal of disturbed predictability of functional interactions. Moreover, their results achieve to correctly classify using SVM(support vector machine) schizophrenia patients from healthy controls with 77% classification accuracy.

In their research, Pentari et al.[9] have applied CRQA to resting-state fMRI data for examining the dynamic functional connectivity on patients with neuropsychiatric systemic lupus erythematosus (NPSLE). Results contain the fact that CRQA metrics, such as determinism, appear more sensitive than conventional static functional connectivity methods in order to identify aberrant connectivity patterns that correlated with visuomotor performance. The study focused on 16 frontoparietal regions and found that CRQA could detect both increased and decreased connectivity in NPSLE patients compared against the healthy controls. Building on these findings, Pentari et al.[10] subsequently ex-

panded the investigation to whole brain network analysis in a larger cohort. In this study they demonstrate the capability of CRQA to integrate multiple recurrence metrics for revealing both hyperconnectivity in parietal regions (angular gyrus and superior parietal lobule) and hypoconnectivity in medial temporal structures (hippocampus and amygdala).

In addition there have been works where simulated data have been used in conjunction with RQA. Lameu et al.[4], investigated burst phase synchronization in neural networks using RQA. They analyzed two network types; a small-world network and a network of networks (to mimic better the real human brain), using coupled Rulkov maps to model bursting neurons. By applying RQA, they identified synchronized neuron groups and quantified their sizes during synchronization transitions. The study showed that RQA measures (*recurrence rate*, *laminarity inspired*(custom feature), and *average structure size*) complement traditional order parameters by revealing localized synchronization patterns, such as the formation and growth of synchronized clusters. Kashyap and Keilholz[26] conducted a comprehensive comparison between simulated brain network models (BNMs) and real rs-fMRI data using dynamic analysis techniques, including Recurrence Quantification Analysis (RQA). In the study they employed two BNMs, the Kuramoto oscillator model and the Firing Rate model, for simulating the whole-brain activity, which was then compared to human rs-fMRI data. Among the compared dynamic analysis methods, RQA was proved particularly effective in distinguishing between the models and empirical data, demonstrating that RQA metrics (*recurrence rate*, *entropy*, and *average diagonal length*) could robustly separate the empirical data from simulations.

Shalbaf et al. [28] investigated the synchronization of EEG signals between frontal and temporal regions during propofol anesthesia using *Order Patterns Cross Recurrence Analysis* (OPCR). Their study introduced a novel index, *Order Pattern Laminarity* (OPL), for the quantification of neuronal synchronization and compared its performance with the traditional Bispectral Index (BIS). The results demonstrated that OPL correlated more strongly with propofol concentration ($P_k = 0.9$) and exhibited faster response times to transient changes in consciousness compared to BIS. Additionally, OPL showed lower variability at the point of loss of consciousness (LOC), suggesting its robustness as a measure of anesthetic depth. This work highlights the potential of recurrence-based methods (e.g., CRQA) for analyzing brain network dynamics under anesthesia, particularly in noisy, non-stationary EEG data.

Table 1: Comparison among the retrieved studies using recurrence analysis

#	Reference	Modality	Analysis Methods	Network Type
1	Frolov et al. (2020)	EEG	RQA, CRQA	Multiplex functional networks
2	Kang et al. (2023)	fMRI	RQA, CRQA	DMN, schizophrenia
3	Rezaei et al. (2023)	fMRI	RQA	Default model-like network, AD
4	Lameu et al. (2018)	—	RQA	Small-world & cluster network
5	Lombardi et al. (2014)	fMRI	RQA	schizophrenia, working memory
6	Pitsik E. (2025)	EEG	RQA	aging
7	Guglielmo et al. (2022)	EEG	RQA	cognitive tasks
8	Lopes et al. (2020)	sEEG, MEG	RQA	epilepsy
9	Pentari et al. (2022)	fMRI	RQA, CRQA	NPSLE
10	Pentari et al. (2023)	fMRI	CRQA	NPSLE
11	Gruszczyńska et al. (2019)	EEG	RQA	epilepsy
12	Mo et al. (2022)	sEEG	RQA	DMN, epilepsy
13	Palanisamy et al. (2024)	EEG	RQA	epilepsy
14	Ngamga et al. (2016)	EEG	RQA, RN	epilepsy
15	Fan and Chou (2019)	EEG	RQA, RN	epilepsy, seizure detection
16	Nunez et al. (2020)	EEG	RQA	AD
17	Yang et al. (2019)	sEEG	RQA, CRQA	epilepsy
18	Rangaprakash (2014)	EEG	CPR(CRQA-based)	epilepsy
19	Heunis et al. (2018)	rsEEG	RQA	autism spectrum disorder
20	Timothy et al. (2017)	EEG	RQA-CRQA	MCI
21	Kashyap et al. (2019)	fMRI	RQA	distinguish BNMs
22	Shalbaf et al. (2014)	EEG	CRQA(OPL)	Anesthesia depth monitoring
23	Mihajlović. (2019)	EEG	RQA	cognitive tasks

1 Filtering

Electroencephalogram signals in most cases are contaminated by noise and artifacts from physiological (eye blinks, muscle or cardiac activity) and non-physiological sources (powerline interference). In general, artifacts consist of all the non-neural signals that contaminate the recorded EEG data.

Preprocessing is required in order to increase the quality of the signal (signal-to-noise) for boosting further analysis in various application domains like brain-computer interfaces (BCIs) or clinical diagnostics [29-32].

Common preprocessing techniques include:

- **Filtering** (e.g., Butterworth, Chebyshev) to remove unwanted frequency bands.
- **Regression methods** for correcting ocular artifacts using reference channels.
- **Blind Source Separation (BSS)** (e.g., ICA, CCA) to decompose and isolate neural activity from artifacts.

- **Wavelet/EMD-based methods** for non-stationary artifact removal.

Also hybrid approaches (e.g., wavelet-ICA) combine multiple techniques for improved artifact rejection. The choice of method depends on computational constraints, artifact type, and real-time processing needs. Effective preprocessing is a key that ensures reliable feature extraction for later analysis.

1.1 Evaluation metrics for EEG denoising in the CHB-MIT dataset

In order to evaluate the performance of different wavelet-based filters for EEG denoising, quantitative metrics have been computed over entire recordings per channel and filter configuration. Metrics used were:

- **Signal-to-Noise Ratio (SNR, dB)**: Measures the ratio between the power of the clean signal and the power of the noise. Higher values indicate better noise suppression while preserving the structure of the signal.
- **Root Mean Square Error (RMSE, μV)**: This metric quantifies the average deviation between the denoised and reference signals in microvolts. Lower values indicate closer similarity to the original signal.
- **Normalized RMSE (NRMSE, %)**: RMSE normalized by the dynamic range of the reference signal, expressed as a percentage. Lower values represent better performance.
- **Correlation Coefficient**: Pearson’s correlation between the denoised and reference signals, assessing how similar the two compared waveforms are. Values close to 1 indicate high waveform preservation.
- **Percent Root-mean-square Difference (PRD, %)**: Measures the relative distortion introduced by the denoising process. Lower values indicate less distortion.

For each one of the filters configuration, metrics were computed channel-wise and then averaged across all channels in order to calculate their global performance score.

1.2 Filter Selection Criteria

The selection of the optimal filter was based on a multi-criteria ranking strategy, where:

1. Metrics where *higher* values indicate better performance (**SNR, Correlation**) were ranked in descending order.
2. Metrics where *lower* values indicate better performance (**RMSE, NRMSE, PRD**) were ranked in ascending order.

3. The ranks from all metrics were averaged to obtain an overall performance rank for each filter.

The filter with the lowest average rank was considered the best compromise between noise reduction and signal fidelity. According to this evaluation, the **SYM8, level 4, threshold 0.5, hard thresholding** filter presented the highest overall performance, exhibiting:

- the highest SNR values,
- one of the lowest RMSE and the lowest NRMSE value,
- the highest correlation coefficient,
- and the lowest PRD.

This indicates that the chosen filter effectively suppressed noise while preserving the morphological features of the EEG signal, making it the most suitable choice for subsequent analysis. The results of the benchmarking those metrics in 5 EDF recording files which include seizures are presented in the following figure.

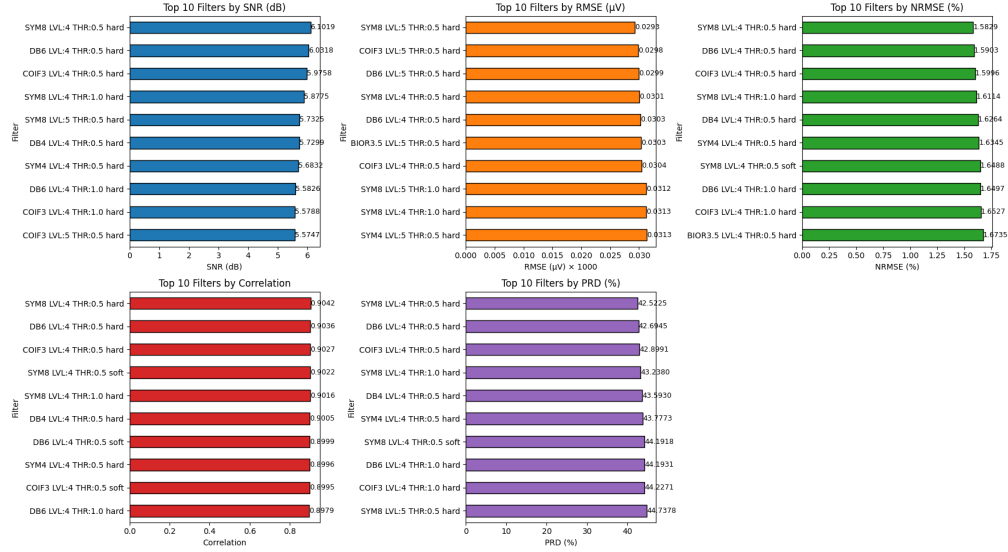


Figure 1: The top 10 filter configurations per EEG metric. RMSE values scaled.

In the following figures we present a visualization using the recording named *chb01_03.edf* comparing the original 10 first EEG channels against the filtered ones with the respective wavelets filters.

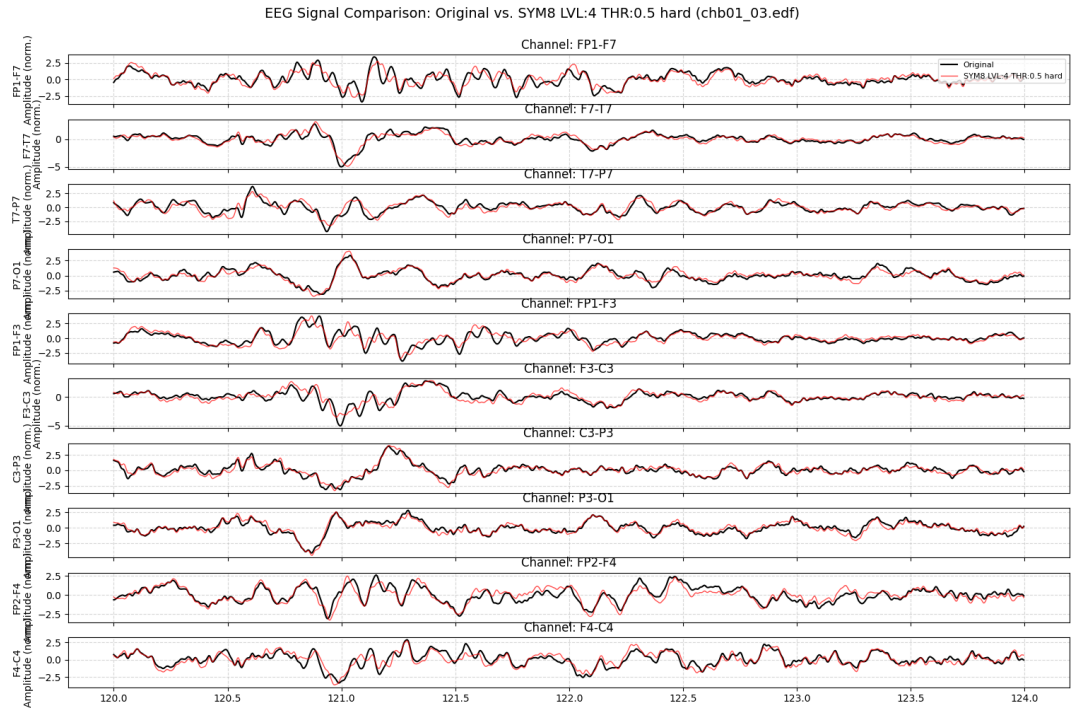


Figure 2

EEG Signal Comparison: Original vs. DB6 LVL:4 THR:0.5 hard (chb01_03.edf)

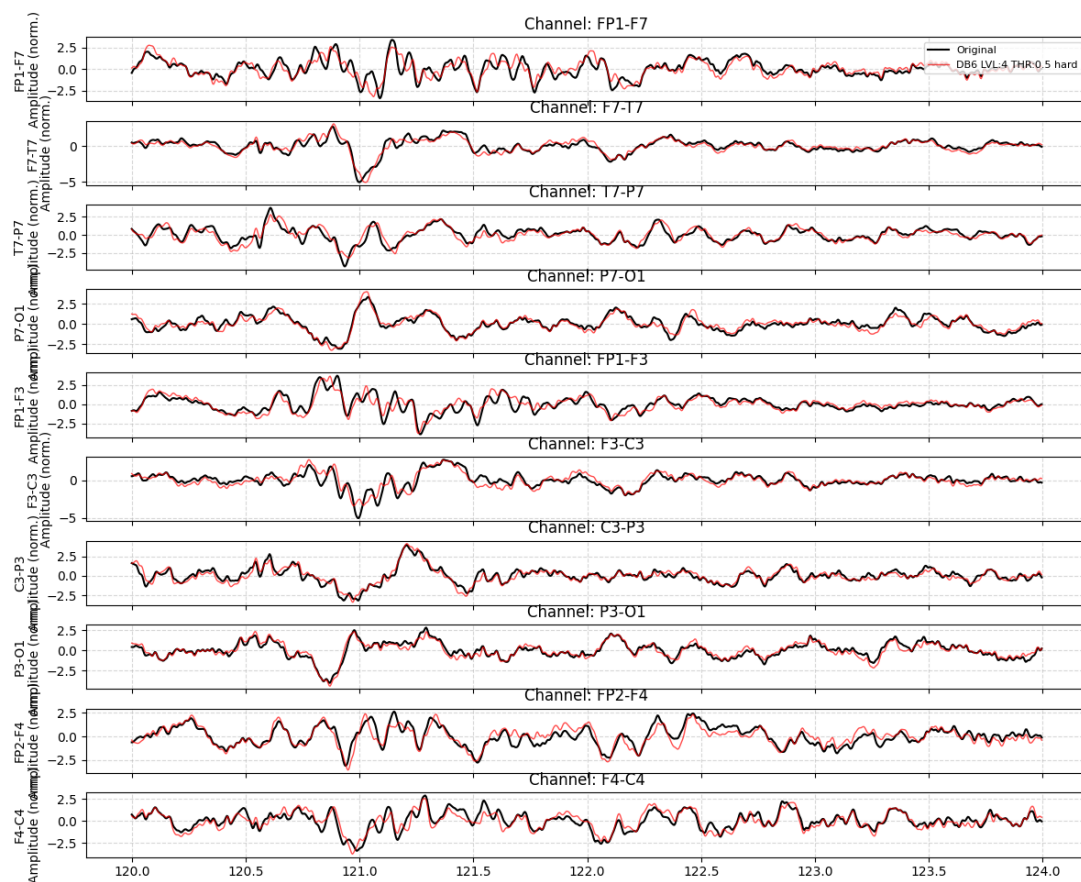


Figure 3

2 Phase space reconstruction of EEG signals

The analysis of nonlinear dynamical systems from experimental time series, such as EEG recordings, requires the reconstruction of the underlying phase space from the scalar measurements of each channel. According to Takens' embedding theorem [34], a time series $x(t)$ can be embedded in an m -dimensional space using time-delay coordinates:

$$\vec{y}(t) = [x(t), x(t + \tau), x(t + 2\tau), \dots, x(t + (m - 1)\tau)] \quad (1)$$

where m is the embedding dimension and τ is the time delay. The critical challenge lies in determining the appropriate values for these parameters to faithfully reconstruct the system's dynamics without distortion.

2.1 Determination of Embedding Parameters

The reconstruction of the phase space from a single time series $x(t)$ requires the specification of two parameters: the time delay τ and the embedding dimension m . These two parameters determine how the reconstruction will represent and how close reveals the underlying dynamics without distortion.

2.1.1 Calculation of time delay τ utilizing mutual information

The time delay τ can be estimated by applying the *Average Mutual Information* (AMI) method, a concept which was first introduced by Fraser and Swinney [36]. In contrast to linear autocorrelation, mutual information has the ability to capture both linear and nonlinear dependencies among the original time series $x(t)$ and its delayed version $x(t + \tau)$.

The mutual information $I(\tau)$ between $x(t)$ and $x(t + \tau)$ is defined as:

$$I(\tau) = \sum_{x(t), x(t+\tau)} P(x(t), x(t + \tau)) \log_2 \left(\frac{P(x(t), x(t + \tau))}{P(x(t)) P(x(t + \tau))} \right)$$

where $P(\cdot)$ denotes probability.

The optimal time delay τ is chosen as the value at which $I(\tau)$ reaches its *first minimum*. This value indicates a good compromise between independence (too small τ) and irrelevance (too large τ) of the coordinates in the embedding vector.

2.1.2 Estimating embedding dimension m using false nearest neighbors approach

When the embedding dimension m is too small, the phase space becomes *projected* rather than properly *embedded*. This projection can create artificial neighborhoods where points appear to be close due to geometrical constraints of the space rather than their actual dynamical similarity. These are named as *false nearest neighbors* [35].

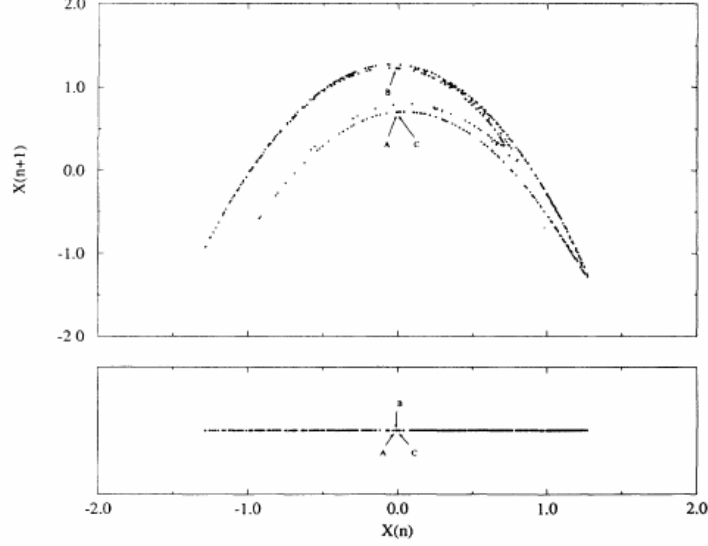


Figure 4: Schematic illustration of false neighbors. In insufficient embedding dimension (down), points A and B appear neighbors due to projection. When proper embedding is employed(up), their true separation is revealed.

Mathematically, two points \vec{y}_i and \vec{y}_j are false neighbors if their distance increases significantly when embedded in higher dimension:

$$\frac{\|\vec{y}_i^{(m+1)} - \vec{y}_j^{(m+1)}\|}{\|\vec{y}_i^{(m)} - \vec{y}_j^{(m)}\|} > R_{\text{tol}} \quad (2)$$

where R_{tol} is a tolerance threshold (typically 10–15).

The False Nearest Neighbors(FNN) method [35] provides a systematic approach in order to determine the minimal sufficient embedding dimension. The method's steps are:

1. For each point in dimension m , identify its nearest neighbor.
2. Embed the data in dimension $m + 1$.
3. Calculation the relative distance increase between each point and its former neighbor.
4. If the increase exceeds predetermined thresholds, the neighbor point is classified as a false neighbor
5. The optimal m is the smallest dimension where the fraction of false neighbors drops below an acceptable level (typically 1–5%)

Both relative and absolute criteria are included in the algorithm:

$$\text{Relative: } \frac{\|\vec{y}_i^{(m+1)} - \vec{y}_j^{(m+1)}\|}{\|\vec{y}_i^{(m)} - \vec{y}_j^{(m)}\|} > R_{\text{tol}} \quad (3)$$

$$\text{Absolute: } \|\vec{y}_i^{(m+1)} - \vec{y}_j^{(m+1)}\| > A_{\text{tol}} \cdot \sigma_x \quad (4)$$

where σ_x is the standard deviation of the time series.

Applying FNN to EEG data is particularly important for several reasons. EEG signals exhibit nonstationary characteristics, making fixed embedding parameters suboptimal and contain measurement noise and artifacts that can distort phase space reconstruction. In addition the optimal embedding may vary across subjects, brain states, and recording conditions and FNN provides a data-driven approach that adapts to individual recordings.

References

- [1] Frolov, N., Maksimenko, V. and Hramov, A. (2020), Revealing a multiplex brain network through the analysis of recurrences *Chaos: An Interdisciplinary Journal of Nonlinear Science* 30(12), 121108.
- [2] Recurrence quantification analysis of periodic dynamics in the default mode network in first-episode drug-naïve schizophrenia. *Psychiatry Research: Neuroimaging*, 329, 111583.
- [3] Recurrence quantification analysis of rs-fMRI data: A method to detect subtle changes in the TgF344-AD rat model. *Computer Methods and Programs in Biomedicine*, 257, 108378.
- [4] Lameu, E. L., Yanchuk, S., Macau, E. E. N., Borges, F. S., Iarosz, K. C., Caldas, I. L., Protachevich, P. R., Borges, R. R., Viana, R. L., Szezech, J. D., Batista, A. M. and Kurths, J. (2018). Recurrence quantification analysis for the identification of burst phase synchronisation. *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 28(8), 085701. <https://doi.org/10.1063/1.5024324>
- [5] Lombardi, A., Guccione, P. and Mascolo, L. (2014). Analysis of fMRI data using the complex systems approach. In *20th IMEKO TC4 International Symposium and 18th International Workshop on ADC Modelling and Testing* (pp. 293-298). Benevento, Italy.
- [6] Pitsik, E. (2025). Recurrence quantification analysis and theta-band functional networks detect age-related changes in brain sensorimotor system: VR-based approach. *The European Physical Journal Special Topics*. <https://doi.org/10.1140/epjs/s11734-025-01509-y>
- [7] Guglielmo, G., Wiltshire, T. J. and Louwerse, M. (2022). Training machine learning models to detect group differences in neurophysiological data using recurrence quantification analysis based features. *ICAART 2022 - 14th International Conference on Agents and Artificial Intelligence*, 430-434.
- [8] Lopes, M. A., Zhang, J., Krzeminski, D., Hamandi, K., Chen, Q., Livi, L. and Masuda, N. (2020). Recurrence quantification analysis of dynamic brain networks. *European Journal of Neuroscience*, 00, 1-20. <https://doi.org/10.1111/ejn.14960>
- [9] Pentari, A., Tzagkarakis, G., Tsakalides, P., Simos, P., Bertstas, G., Kavroulakis, E., Marias, K., Simos, N. J. and Papadaki, E. (2022). Changes in resting-state functional connectivity in neuropsychiatric lupus: A dynamic approach based on recurrence quantification analysis. *Biomedical Signal Processing and Control*, 72, 103285. <https://doi.org/10.1016/j.bspc.2021.103285>
- [10] Pentari, A., Simos, N., Tzagarakis, G., Kagialis, A., Bertstas, G., Kavroulakis, E., Gratsia, E., Sidiropoulos, P., Boumpas, D. T. and Papadaki, E. (2023). Altered hippocampal connectivity dynamics predicts

- memory performance in neuropsychiatric lupus: A resting-state fMRI study using cross-recurrence quantification analysis. *Lupus Science & Medicine*, 10(1), e000920. <https://doi.org/10.1136/lupus-2023-000920>
- [11] Gruszczyńska, I., Mosdorf, R., Sobaniec, P., Żochowska-Sobaniec, M. and Borowska, M. (2019). Epilepsy identification based on EEG signal using RQA method. *Advances in Medical Sciences*, 64(1), 58-64. <https://doi.org/10.1016/j.advms.2018.08.003>
 - [12] Mo, J., Zhang, J., Hu, W., Wang, X., Zhao, B., Zhang, K. and Zhang, C. (2022). Neural underpinnings of default mode network on empathy revealed by intracranial stereoelectroencephalography. *Psychiatry and Clinical Neurosciences*, 76(12), 659-666. <https://doi.org/10.1111/pcn.13470>
 - [13] Vanithamani Palanisamy, A. Ranichitra, and Radhamani Ellapparaj, A differential biomarker based on recurrence quantification analysis of EEG signal and genetic algorithm for epilepsy diagnosis. *Journal of Artificial Intelligence and System Modelling*, 2(2):74–85, 2024. 10.22034/jaism.2024.450400.1046
 - [14] Ngamga, E. J., Bialonski, S., Marwan, N., Kurths, J., Geier, C. and Lehnertz, K. (2016). Evaluation of selected recurrence measures in discriminating pre-ictal and inter-ictal periods from epileptic EEG data. *Physics Letters A*, 380(16), 1419–1425. <https://doi.org/10.1016/j.physleta.2016.02.024>
 - [15] Fan, M. and Chou, C.-A. (2019). Detecting abnormal pattern of epileptic seizures via temporal synchronization of EEG signals. *IEEE Transactions on Biomedical Engineering*, 66(3), 601-608. <https://doi.org/10.1109/TBME.2018.2850959>
 - [16] P. Núñez, J. Poza, C. Gómez, V. Barroso-García, A. Maturana-Candelas, M. A. Tola-Arribas, M. Cano, and R. Hornero, Characterization of the dynamic behavior of neural activity in Alzheimer’s disease: exploring the non-stationarity and recurrence structure of EEG resting-state activity, *Journal of Neural Engineering*, vol. 17, no. 1, p. 016071, 2020, doi: <https://doi.org/10.1088/1741-2552/ab71e9>.
 - [17] Yang, C., Luan, G., Liu, Z. and Wang, Q. (2019). Dynamical analysis of epileptic characteristics based on recurrence quantification of SEEG recordings. *Physica A: Statistical Mechanics and its Applications*, 523, 507–515. <https://doi.org/10.1016/j.physa.2019.02.017>
 - [18] Rangaprakash, D. (2014). Connectivity analysis of multichannel EEG signals using recurrence based phase synchronization technique. *Computers in Biology and Medicine*, 46, 11-21. <https://doi.org/10.1016/j.combiomed.2013.10.025>

- [19] Trulla, L. L., Giuliani, A., Zbilut, J. P., and Webber, C. L., “Recurrence Quantification Analysis of the Logistic Equation with Transients,” *Physics Letters A*, vol. 223, no. 4-5, pp. 255–260, 1996. doi: 10.1016/S0375-9601(96)00741-4
- [20] Webber, C. L. and Zbilut, J. P., “Recurrence Quantification Analysis of Nonlinear Dynamical Systems,” in *Tutorials in Contemporary Nonlinear Methods for the Behavioral Sciences*, pp. 26–94, 2005.
- [21] Thomasson, N., Hoeppner, T. J., Webber, C. L., and Zbilut, J. P., “Application of Recurrence Quantification Analysis to EEG Signals,” *International Journal of Computer Research*, 2002.
- [22] Marwan, N., Schinkel, S., and Kurths, J., “Recurrence Plots 25 Years Later – Gaining Confidence in Dynamical Transitions,” *EPL (Europhysics Letters)*, vol. 101, no. 2, p. 20007, 2013. doi: 10.1209/0295-5075/101/20007
- [23] Heunis, T., Aldrich, C., Peters, J. M., Jeste, S. S., Sahin, M., Scheffer, C., and de Vries, P. J., “Recurrence quantification analysis of resting state EEG signals in autism spectrum disorder – a systematic methodological exploration of technical and demographic confounders in the search for biomarkers,” *BMC Medicine*, vol. 16, no. 1, p. 101, 2018.
- [24] Eckmann, J.-P., Kamphorst, S. O. and Ruelle, D. (1987). Recurrence plots of dynamical systems. *Europhysics Letters*, 4(9), 973–977.
- [25] Timothy, L. T., Krishna, B. M. and Nair, U. (2017). Classification of mild cognitive impairment EEG using combined recurrence and cross recurrence quantification analysis. *International Journal of Psychophysiology*, 120, 86–95. <https://doi.org/10.1016/j.ijpsycho.2017.07.006>
- [26] Kashyap, A. and Keilholz, S. (2019). Dynamic properties of simulated brain network models and empirical resting-state data. *Network Neuroscience*, 3(2), 405–426. https://doi.org/10.1162/netn.a_00070
- [27] Carrubba, S., Frilot, C. and Marino, A. A. (2019). Optimization of recurrence quantification analysis for detecting the presence of multiple sclerosis. *Journal of Medical and Biological Engineering*, 39(6), 806–815. <https://doi.org/10.1007/s40846-019-00462-1>
- [28] Shalbaf, R., Behnam, H., Sleight, J. W., Steyn-Ross, D. A., & Steyn-Ross, M. L. (2014). Frontal-temporal synchronization of EEG signals quantified by order patterns cross recurrence analysis during propofol anesthesia. *IEEE Transactions on Neural Systems and Rehabilitation Engineering*, 22(6), 1164–1174. <https://doi.org/10.1109/TNSRE.2014.2350537>
- [29] Jiang, X., Bian, G.-B., and Tian, Z. (2019). Removal of Artifacts from EEG Signals: A Review. *Sensors*, 19(5), 987. <https://doi.org/10.3390/s19050987>

- [30] Dhanaseivam, P. S., and Chellam, C. N. (2023). A review on preprocessing of EEG signal. In *2023 9th International Conference on Biosignals, Images and Instrumentation (ICBSII 23)*. Madurai, India.
- [31] Jiang, X., Bian, G.-B., and Tian, Z. (2019). Removal of artifacts from EEG signals: A review. *Sensors*, 19(5), 987. <https://doi.org/10.3390/s19050987>
- [32] Sen, D., Mishra, B. B., and Pattnaik, P. K. (2023). A review of the filtering techniques used in EEG signal processing. In *Proceedings of the 7th International Conference on Trends in Electronics and Informatics (ICOEI 2023)* (pp. 270–278). Bhubaneswar, India.
- [33] Mihajlović, D. (2019). EEG Spectra vs Recurrence Features in Understanding Cognitive Effort. In *Proceedings of the 2019 International Symposium on Wearable Computers (ISWC '19)*, September 9–13, 2019, London, United Kingdom. ACM, New York, NY, USA, 6 pages. <https://doi.org/10.1145/3341163.3347746>
- [34] Takens, F. (1981). Detecting strange attractors in turbulence. In *Lecture Notes in Mathematics* (Vol. 898, pp. 366–381). Springer.
- [35] Kennel, M. B., Brown, R., & Abarbanel, H. D. I. (1993). Determining embedding dimension for phase-space reconstruction using a geometrical construction. *Physical Review A*, 45(6), 3403–3411.
- [36] Fraser, A. M., & Swinney, H. L. (1986). Independent coordinates for strange attractors from mutual information. *Physical Review A*, 33(2), 1134–1140. <https://doi.org/10.1103/PhysRevA.33.1134>
- [37] Rosenstein, M. T., Collins, J. J., & De Luca, C. J. (1993). A practical method for calculating largest Lyapunov exponents from small data sets. *Physica D: Nonlinear Phenomena*, 65(1-2), 117–134. [https://doi.org/10.1016/0167-2789\(93\)90009-P](https://doi.org/10.1016/0167-2789(93)90009-P)