

Quantum Networking: Creating the Future Landscape of Refined Classical Communication

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Abstract—The landscape of communication sits on the edge of a quantum leap. Harnessing the paradoxical rules of quantum mechanics, quantum networks promise the ability to shatter the boundaries of traditional systems, ushering in an age of extraordinary speed, security, and computational powers. This research dives into the unexplored domain of quantum networking, clarifying its transformational potential and charting a course toward its practical realization.

Crucially, the research transcends ordinary simulations by offering conceptual blueprints for a revolutionary quantum-based network architecture. This innovative concept presents entanglement distribution and quantum key distribution as applications built upon the network itself, rather than demanding bespoke network infrastructures. To painstakingly investigate this proposed model, quantum circuits were meticulously simulated, and their results juxtaposed with established quantum algorithms, revealing vital insights into its performance and potential.

This research establishes the framework for the quantum Internet, not as a distant goal but as an attainable future. By delving into the integration of the proposed model with existing network topologies, the path towards a unified quantum environment is paved. The consequences of this study reach far beyond theoretical advances; they beckon a future where unbreakable encryption preserves sensitive information, communication spans vast distances with amazing speed, and distributed quantum computers unleash previously inconceivable frontiers.

Keywords: *Quantum Networking, Quantum Signal Processing, Quantum Key Distribution, Bell state measurements, Quantum Error Correction, BB84, Grover's Algorithm, Quantum Circuit, Data Transmission, Quantum Security.*

I. INTRODUCTION

In the ever-evolving environment of information technology, the limitations of conventional communication systems have become increasingly evident, encouraging the study of alternative techniques to answer the growing need for quicker, more secure data transfer. Classical networking, while robust, confronts issues such as limited capacity, sensitivity to eavesdropping, and latency concerns. In response to these obstacles, the integration of quantum methods and techniques has emerged as a possible route to better classical communication systems.

The primary challenge addressed by this research revolves around the hunt for enhanced communication strategies. By utilizing the principles of quantum mechanics, we aspire to surpass the limitations of classical communication, introducing a new era of quantum networks that boast exceptional speed and security. Quantum significant Distribution (QKD), quantum encoding,

entanglement, packet switching, and quantum teleportation constitute significant principles researched in this quest, each contributing uniquely to the broader objective of revolutionizing data transport [1,4].

Quantum Key Distribution (QKD) acts as a cornerstone in quantum communication, ensuring secure transmission by exploiting the principles of quantum superposition and quantum entanglement [5]. The application of quantum encoding permits the representation and transmission of information in quantum bits or qubits, giving a powerful alternative to classical bits. Additionally, the entanglement phenomenon, which Einstein famously referred to as "spooky action at a distance," enables the correlation of quantum states between distant particles, allowing for instantaneous communication [2].

In the world of packet switching, the classical paradigm encounters difficulties due to the sequential structure of information transport. Quantum packet switching introduces the ability to process information concurrently, possibly improving the efficiency and speed of data transmission. Furthermore, the exciting concept of quantum teleportation, wherein the quantum state of a particle is conveyed instantaneously across large distances, shows promise for accelerating information transport [9].

This research study addresses the practical implementation of these quantum principles through the building of real-time quantum circuits employing quantum algorithms. Through simulations and empirical validations using IBM's Quantum Composer and Google's quantum circuits, we hope to give tangible evidence proving the feasibility and efficacy of adding quantum approaches into classical communication systems. By delving into the nuances of quantum networking, our research attempts to contribute to the growing narrative of quantum technologies as essential enablers of faster and more secure data transfer in our linked world.

II. LITERATURE REVIEW

The continual growth of information technology has witnessed a dramatic shift with the emergence of quantum networking, ushering in a new age for classical communication systems. This comprehensive literature review digs into seminal publications, key concepts, current breakthroughs, and persisting issues in the realm of quantum networks. By analyzing the possible benefits and uses of integrating quantum technologies into standard communication infrastructures, this review seeks to provide a nuanced perspective on the emerging topic.

A. Quantum Key Distribution (QKD):

Quantum Key Distribution marks a milestone achievement in quantum communication research. The seminal work of Bennett and Brassard in 1984 developed the concept of quantum cryptography, paving the path for secure communication through quantum entanglement. The Ekert protocol in 1991 established the viability of secure key exchange based on quantum principles. QKD has since evolved, with advances including the BBM92 protocol by Bennett, Brassard, and Mermin in 1992, enabling better security protections against potential eavesdropping. This foundational work highlights the vital significance of QKD in constructing secure communication channels, forming the groundwork for the exploration of quantum networking [10].

B. Quantum Encoding and Packet Switching:

Quantum encoding techniques, employing qubits instead of classical bits, have gained substantial attention for their potential to revolutionize information representation and transmission. The work of Nielsen and Chuang in 2000 on quantum information theory set the framework for quantum encoding, highlighting the unique features of qubits. The concept of quantum packet switching, developed by Tang et al. (2014), marks a paradigm change in concurrent data processing. This research intends to explore the possible efficiency benefits given by quantum encoding and packet switching, hoping to redefine the speed and efficacy of data transmission.

C. Entanglement and Quantum Teleportation:

Entanglement, a cornerstone of quantum communication, has been widely researched since its conceptualization. Notable work by Aspect and Zeilinger has expanded our understanding of entanglement, emphasizing its potential for instantaneous correlation of quantum states over great distances. Quantum teleportation, as postulated by Bennett et al. in 1993, provides exciting possibilities for the fast transmission of quantum states across networks. The research of these phenomena is vital to uncovering the full potential of quantum networking in speeding data transfer.

D. Real-Time Quantum Circuits and Algorithm Testing:

Recent breakthroughs in quantum computing have led to the creation of real-time quantum circuits, simplifying the practical implementation and testing of quantum algorithms. The work of Arute et al. (2019) on quantum supremacy using Google's Sycamore processor highlights the capability of quantum processors to solve complicated problems. IBM's Quantum Composer and Google's quantum circuits have emerged as crucial instruments for verifying the feasibility and efficacy of quantum approaches in communication systems. This study attempts to exploit real-time quantum circuits to empirically test and validate quantum algorithms for real-world applications.

Quantum Node and Repeater Integration: Quantum node and repeater integration offers a vital field of investigation to overcome distance limits and signal attenuation in quantum communication. Briegel et al. (1998) and Sangouard et al. (2011) have produced seminal papers exploring the significance of quantum repeaters in extending the reach of quantum communication. These activities are vital for boosting the scalability and practical application of quantum networks.

Scalability is a fundamental factor for the practical deployment of quantum networks. Recent studies by Preskill (2018) and Z look into the scalability difficulties and potential solutions for quantum networks. Understanding the scalability of quantum networks is vital for their integration into current communication infrastructures. Moreover, investigating prospective applications of quantum networks, spanning from distributed quantum computing to secure communication in the era of quantum computing, adds dimension to the ongoing topic. The need for communication systems capable of handling vast data while ensuring heightened security is pressing. This study merges quantum technology's potential with classical communication, aiming to transcend existing constraints and set new benchmarks for data transmission and network stability [20].

III. METHODOLOGY USED

This study employs a comprehensive methodology utilizing a synergistic blend of platform exploration, programming languages, and simulation tools to examine, understand, and benefit from the numerous concepts of quantum networks.

A. Platforms and Tools used:

1. IBM Quantum Composer: Leveraging the intuitive interface of IBM's Quantum Composer, complicated quantum circuits were constructed and analyzed, offering practical insights into their real-world application potential. [12]
2. Google Colab: Facilitating code creation and thorough data analysis, Google Colab acted as a helpful tool for deriving probabilities and predictions from complicated quantum circuits.
3. IBM Quantum Lab: Providing an accessible platform for hands-on experimentation, IBM's Quantum Lab was leveraged to mimic quantum circuits and algorithms, enabling greater knowledge via interactive exploration.

B. Language used:

1. Qiskit: This open-source software framework facilitates access to quantum technologies, streamlining device interface and offering full tools for creating, performing, and evaluating quantum experiments. Researchers benefit from an intuitive interface and comprehensive libraries, offering the opportunity to examine quantum circuits and algorithms without requiring specific hardware.
2. QASM: Serving as the lingua franca for expressing quantum processes, QASM enables the definition and manipulation of quantum gates and circuits. Its clear syntax and potent capabilities permit researchers to develop complicated quantum algorithms, unleashing the tremendous potential of these difficult theoretical structures.

By applying these rigorous techniques, the study efficiently bridges the gap between theoretical notions and practical implementation, setting the framework for continued inquiry and progress in the intriguing subject of quantum networking.

IV. QUANTUM CIRCUITS: QUANTUM BLUEPRINTS

Quantum circuits, like the blueprints for quantum calculations, give a visual and logical depiction of the complicated operations conducted on qubits. Quantum circuits are basic to quantum computation, permitting the manipulation and change of quantum states using quantum gates [25]. They operate as a bridge between conceptual quantum algorithms and actual implementations on quantum hardware.

A. Quantum Circuit Elements:

1. **Qubits (Quantum Bits):** These constitute the basic units of quantum information, equivalent to classical bits. Qubits may exist in a superposition of states, allowing for simultaneous processing.
2. **Quantum Gates:** Quantum gates are the essential building blocks of quantum circuits, which are accountable for manipulating qubits. Notable gates include Hadamard (H), Pauli-X (X), Pauli-Y (Y), Pauli-Z (Z), and Controlled-NOT (CNOT) some of them are shown in (Fig. 1).
3. **Classical Bits (c-bits):** Classical bits serve the purpose of classical transmission and measurements. The outputs of quantum calculations are typically measured and stored in traditional bits.
4. **Quantum Registers:** A set of qubits that are controlled as a unit during quantum calculations.
5. **Quantum Measurement:** This technique includes retrieving classical information from qubits, forcing the breakdown of the quantum state into a classical state. M in (Fig. 1) depicts quantum measurement units.

B. Notations:

1. **Ket Notation ($|\Psi\rangle$):** This notation has been used to depict the state of a qubit or a quantum system. For instance, $|0\rangle$ and $|1\rangle$ indicate the classical bit states, while superposition states are designated as $\alpha|0\rangle + \beta|1\rangle$.
2. **Quantum Gate Notation:** Gates are expressed using matrix notation. For example, the Hadamard gate is represented as: $H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
3. **Qiskit:** This open-source toolkit offers a Python-based interface for creating and modeling quantum circuits. A qiskit circuit code is shown in (Fig. 2).
4. **QASM:** The Quantum Assembly Language provides a more hardware-centric vocabulary for describing quantum circuits. An example of QASM code is shown in (Fig. 3)

Quantum circuits are commonly shown as schematics with horizontal lines representing qubits and other symbols representing quantum gates. Arrows show the flow of information, while measurement findings are often presented as classical bits [13].

By comprehending these concepts and notations, researchers may successfully design and implement quantum algorithms, utilizing the incredible capability of quantum

computing to handle challenging issues across many domains [21].

Simulators such as IBM Quantum Composer overcome the gap between theoretical principles and actual experimentation by delivering a visual, intuitive interface for constructing and assessing quantum circuits. Researchers may quickly create circuits using a drag-and-drop technique using pre-built components, access real-time visualization for rapid feedback, and conduct simulations to investigate probability distributions and study circuit behaviour. Built-in error-checking and debugging tools further expedite the process, permitting researchers to explore and modify their concepts without relying on constrained quantum hardware.

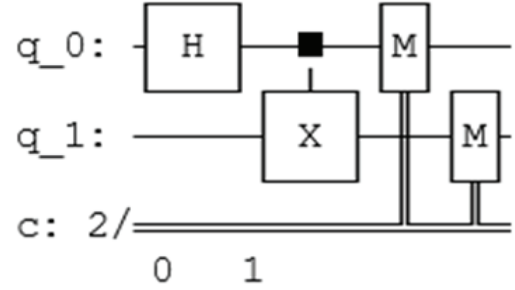


Fig. 1. A Quantum circuit diagram.

```
from qiskit import QuantumCircuit
qc = QuantumCircuit(2)
qc.h(0)
qc.cx(0, 1)
qc.measure_all()
```

Fig. 2. Qiskit (Python-based).

```
OPENQASM 2.0;
include "qelib1.inc";
qreg q[2];
h q[0];
cx q[0], q[1];
measure q[0] -> c[0];
measure q[1] -> c[1];
```

Fig. 3. QASM (Quantum Assembly Language).

V. BELL STATE CIRCUIT & MEASUREMENTS

The Bell state, a key concept in quantum information theory, is a unique entangled quantum state that shows correlations exceeding classical bounds. The production and manipulation of Bell states are key components in the construction of quantum circuits, particularly those designed for quantum communication [19,22].

A. Bell State Circuits:

The best-known Bell state is the maximally entangled state referred to as the Bell state $|\Phi^+\rangle$, which is formed using a Hadamard gate (H) and a Controlled-NOT (CNOT) gate as shown in (Fig. 4). The circuit for producing $|\Phi^+\rangle$ may be stated as follows:

q_0: ---H---@---
 |
 q_1: -----X---

Fig. 4. In this circuit, the Hadamard gate brings the qubit q0 into a superposition, while the CNOT gate forms an entangled state between q0 and q1. Additional Bell states, such as $|\Phi-\rangle$, $|\Psi+\rangle$, and $|\Psi-\rangle$, can be generated using equivalent quantum circuits with suitable gate operations.

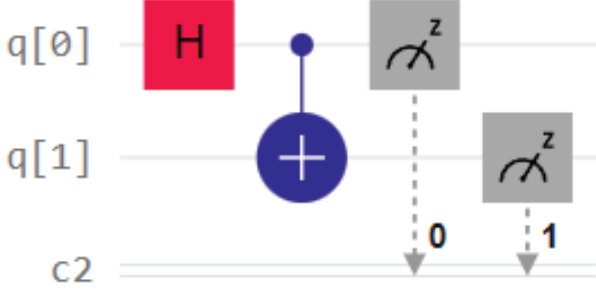


Fig. 4. Simulated diagram of a Bell State circuit.

B. Measurements and Bell State Correlations:

When analyzing the two qubits of a Bell state, the outputs become linked in a manner that defies the conventional explanation. As an example, if q0 is measured using the computational basis ($|0\rangle$ or $|1\rangle$), the state of q1 becomes immediately identified, regardless of the physical gap between them. The Bell state measurements yield pairs of results that are associated, showing the unique and non-local character of entanglement [17].

C. Crucial Role in Quantum Networks:

The production and usage of Bell states are important for the creation of quantum communication protocols. By communicating entangled Bell states between distant participants, a safe and instantaneous link may be formed. This is particularly crucial in the context of quantum networks because information sharing requires both speed and security.

D. Correlation between Sender and Receiver:

Utilizing Bell states in quantum communication permits the formation of a unique correlation between the transmitter and receiver. If a pair of particles are entangled in a Bell state, the measurement outcomes of one particle immediately identify the state of the other, regardless of the distance between them. This connection is the foundation for quantum key distribution (QKD) protocols, guaranteeing a secure and tamper-evident communication channel.

VI. QKD USING BELL STATE MEASUREMENTS

Bell states enable the creation of quantum key distribution methods, an essential component of quantum cryptography. The BB84 and BBM92 protocols, among others, leverage Bell states to ease the production of secret shared encryption keys between communication parties, often designated as Alice and Bob. These keys constitute the basis for powerful encryption, delivering secure communication channels inside traditional communication systems.

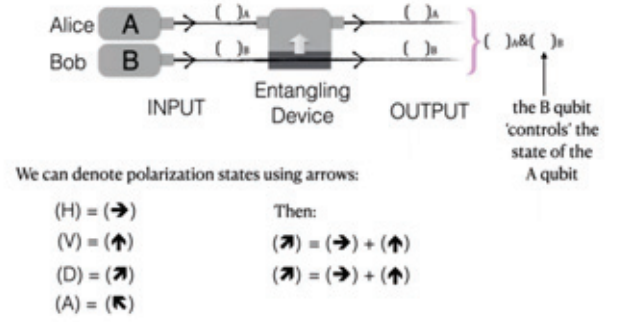


Fig. 5. Qubit polarization states for the selection of measurement basis.

A. Bell State Measurements (BSM) for Key Generation:

To produce a shared encryption key, Alice and Bob execute Bell state measurements on entangled pairs of particles. The source creates Bell states, and the measurement outcomes of these entangled particles reveal quantum correlations that challenge conventional interpretations [17]. This connection is the basis for safe key distribution, allowing Alice and Bob to construct a shared key with a level of security unreachable in traditional cryptography.

Even in the presence of faulty sources and measurement equipment, Bell state measurements contribute to the resilience of quantum key distribution. If Alice and Bob can verify that the measurement outcome statistics violate the Bell inequality, it shows the presence of quantum entanglement. This breach acts as a reliable criterion for identifying eavesdropping attempts, assuring the security of the shared key.

B. Overcoming Faults and Verifying Quantum Correlation:

Sources of data and measuring instruments may be prone to failures, however the verification of measurement outcome metrics through the violation of the Bell inequality allows Alice and Bob to discover such difficulties. By harnessing the unique qualities of entangled particles, scientists can identify true quantum correlations from those created by external sources, boosting the dependability of the shared key generation process.

C. Creating Bell State& Measurements:

1) . Preparation of Entangled Qubits:

The method commences with the creation of two qubits that are already entangled in one of the four unique Bell states [20]. These Bell states, indicated as Bell states 0, 1, 2, and 3, each demonstrate distinct correlations:

- Bell state 0: Both qubits are found in either the $|00\rangle$ or $|11\rangle$ states, suggesting a common quantum state.
- Bell state 1: The qubits reside in opposing states, with one in the $|0\rangle$ state and the other in the $|1\rangle$ state.
- Bell state 2: The qubits are in a superposition of $|00\rangle$ and $|11\rangle$ states.
- Bell state 3: The qubits reside in a superposition of $|01\rangle$ and $|10\rangle$ states.

These established correlations set the foundation for further experiments, enabling the characterization of the entangled qubits.

2) Selection of Measurement Basis:

The determination of the Bell state seen directs the selection of measurement basis for each qubit as shown in (Fig. 5) where an entangling device is used to entangle the qubits. Different measurement bases give diverse viewpoints for evaluating the entangled system [18]. This decision is critical for collecting precise information regarding the entangled states of the qubits.

3) Measurement and Correlation Analysis:

After the selection of measurement basis, each qubit undergoes measurement using its chosen basis. Two often adopted bases are the Rectilinear (H/V or 0/1) basis and the Diagonal (D/A or +/−) basis, as seen in Figure 16. The measurement outputs indicate correlations between the qubits, illuminating the complex structure of the entanglement.

Polarization states are also defined as the H/V basis, where photons are polarized horizontally (|H⟩) or vertically (|V⟩), and the D/A basis, where they are polarized on the diagonal (|D⟩) or antidiagonal (|A⟩) directions as shown in (Fig. 6).

Bell states may be characterized using polarization states. Specifically, the Bell states are commonly stated in terms of the polarization states of photons.

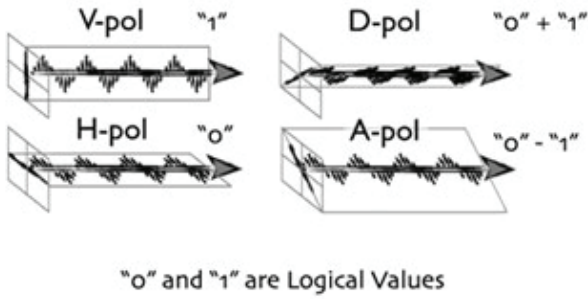


Fig. 6. H/V and D/A basis polarization.

Defined Bell States using polarization are:

- $|\Phi^+\rangle = \frac{1}{\sqrt{2}}(|H\rangle \otimes |V\rangle + |V\rangle \otimes |H\rangle)$
- $|\Phi^-\rangle = \frac{1}{\sqrt{2}}(|H\rangle \otimes |V\rangle - |V\rangle \otimes |H\rangle)$
- $|\Psi^+\rangle = \frac{1}{\sqrt{2}}(|H\rangle \otimes |H\rangle + |V\rangle \otimes |V\rangle)$
- $|\Psi^-\rangle = \frac{1}{\sqrt{2}}(|H\rangle \otimes |H\rangle - |V\rangle \otimes |V\rangle)$

This correlation analysis is crucial in understanding the quantum entanglement between the qubits. The measurement outputs give insights into the shared quantum states, superpositions, or opposing states, depending on the Bell state detected. The capacity to recognize these correlations is crucial for quantum communication protocols, quantum key distribution, and quantum information processing in general. The complicated interplay of entangled qubits, governed by preset Bell states, lays the basis for utilizing the unique capabilities of quantum mechanics in the area of quantum information science.

VII. QUANTUM NETWORKS (MERGING OF QKD & PACKET SWITCHING)

The convergence of quantum key distribution (QKD) with conventional packet switching offers a hybrid network design, leveraging the specific benefits of both quantum and conventional networking paradigms.

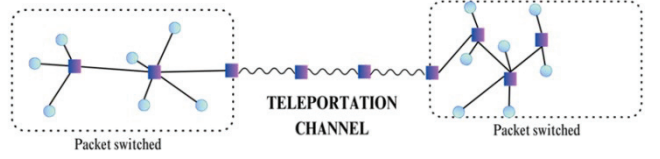


Fig. 7. Two packet-switched networks are coupled via an entanglement-based teleportation route.

A. Quantum-Secured Communication Channels:

The integration of QKD generates quantum-secured communication channels as depicted in (Fig. 9). within the conventional packet-switched network. Utilizing the features of quantum entanglement and teleportation, these channels demonstrate resistance to eavesdropping efforts, increasing the security of the network [33].

B. QKD Devices:

Strategic installation of QKD devices inside the network facilitates the establishment of reliable quantum communication links as depicted in (Fig. 7). These devices readily integrate into routers and switches, ensuring the synthesis and distribution of quantum keys while data packets transit the regular network[36].Data from one network is packet-switched to an exit of one subnetwork and is teleported to the inlet of another via an entanglement-based network, employing Bell State entanglement swapping as depicted in (Fig. 8) to build end-to-end entanglement among the subnetwork edge nodes [5].

C. Quantum Repeaters for Long-range Communication:

Quantum repeaters establish a natural location inside the integrated network, enhancing the range of quantum communication. Particularly helpful for generating secure communications across great distances using teleportation and entanglement swapping as shown in (Fig. 8), quantum repeaters eliminate a key issue experienced solely by quantum networks [14].

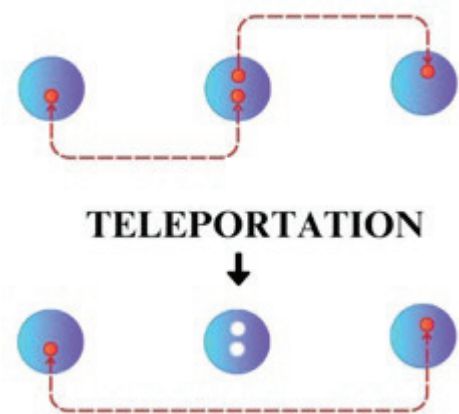


Fig. 8. Entanglement swapping where data bits are teleported between two entangled repeaters.

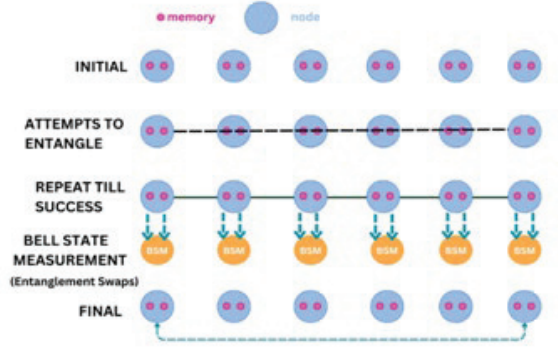


Fig. 9. Creating a Chain Network of Entangled Repeaters.

VIII. SIMULATION RESULTS

The project has successfully explored the potential of quantum technology for enhancing classical communication results were achieved:

The simulation of the Bell state circuit employing the IBM Quantum Composer has generated enlightening results, exhibiting success state probabilities favorable to Quantum Key Distribution (QKD) propagation. In a series of 1024 shots, the observed probabilities for two states were as follows: "0000": 0.501953125 and "0011": 0.498046875. These conclusions demonstrate the possibility of utilizing entanglement enabling secure quantum communication, and establishing the framework for the development of a quantum-enabled network infrastructure that offers security, reliability, speed, and scalability.

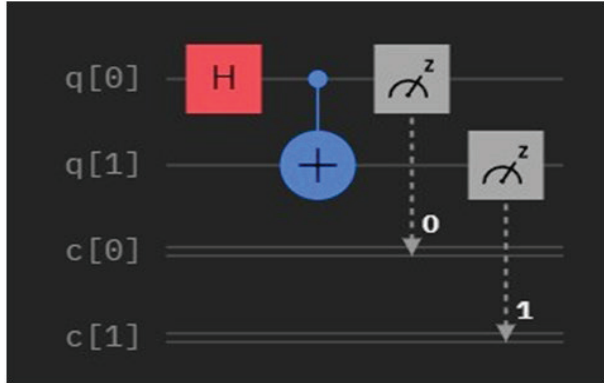


Fig. 10. Transpiled Bell State Circuit is a code version of the original circuit formed after running the Qiskit code in the simulator.

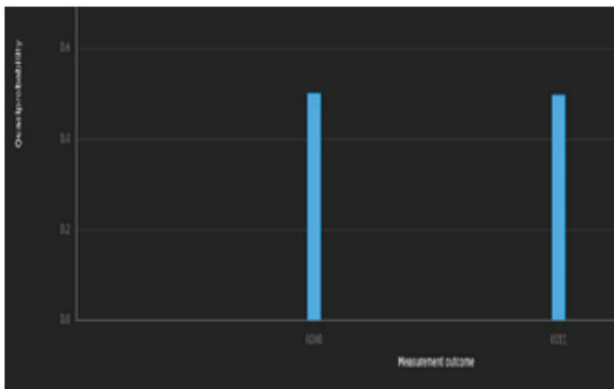


Fig. 11. The probability distribution of the Bell State circuit indicates a quantum state in a bar graph, and the horizontal axis indicates the computational base states. The vertical axis measures the probability in terms of percentages.

A. Entanglement-Secured Transmission:

The success state probability shown in (Fig. 12) derived from the Bell state circuit simulation underlines the relevance of entanglement in safeguarding quantum communication. The observed probabilities correspond with the theoretical assumptions, strengthening the dependability of entanglement-based transmission [23].

B. Probability Distribution:

The probability distribution generated from the simulation, shown in (Fig. 11) symbolizes the stable and balanced nature of entanglement-based communication. The measured probabilities of "0000" and "0011" contribute to a richer knowledge of the statistical properties of quantum states during the transmission process. The graphical representation of the quantum state with one or more qubits by assigning each computational basis state to a point on a sphere's surface called the Q-sphere is depicted in (Fig. 13).

C. Quantum-Enabled Network System:

These results contribute to the knowledge of entanglement-based transmission and underline the possibility of a quantum-enabled network that is safe, fast, scalable, and well-suited to the needs of current communication technology.

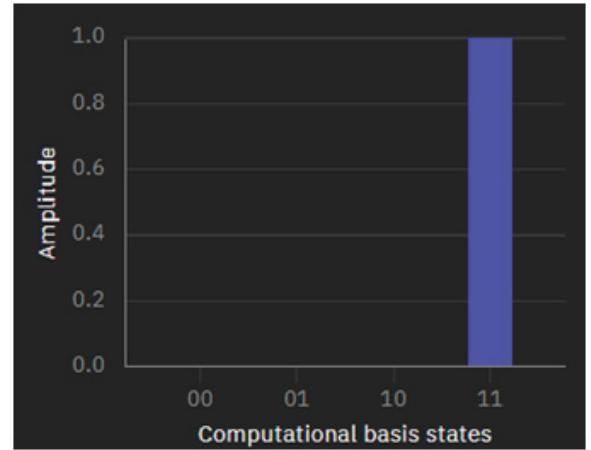


Fig. 12. The Statevector simulation output of the Bell State circuit which measures the amplitude of base state of the qubits in the circuit.

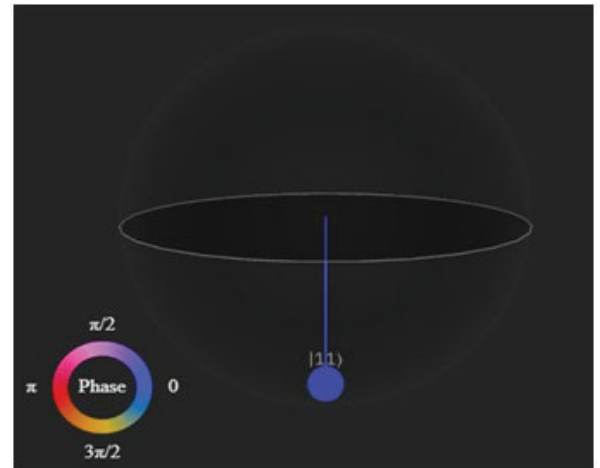


Fig. 13. Q-sphere representing the state the Bell State circuit creates with the state $|11\rangle$ and a phase angle of 0° .

IX. CONCLUSION& OUTLOOK

The research work along with the simulation of the Bell state circuit using the IBM Quantum Composer, has offered vital insights into the possible integration of Quantum Key Distribution (QKD) with conventional packet switching systems for secure quantum communication. The measured success state probabilities of "0000": 0.501953125 and "0011": 0.498046875 in 1024 shots support the viability of leveraging entanglement for quantum transmission within a network system. This research lays the basis for the construction of a quantum-enabled network that offers promising security, speed, and sustainability.

To develop a resilient quantum network system, it is important to combine bell-state circuits inside an interconnected architecture of quantum nodes, repeaters, and memory, reinforced by classical networking approaches [26,27]. This comprehensive technique gives a roadmap towards a more controllable and efficient quantum network system. The integration of quantum networking into standard communication networks has the potential to bring about major advances in data security, processing capacity, and fault-tolerance mechanisms by exploiting the unique features of quantum physics.

Exploring Bell states will pave the route for enhanced quantum networks that may leverage entanglement principles for secure data transport and communication. The benefits extend beyond the problems, giving the promise of drastically enhancing data security, processing capacity, and fault-tolerance mechanisms within the larger landscape of communication networks.

Intending to improve quantum networking, the academic and scientific community needs to confront these difficulties collectively. Increased access to resources and facilities, together with continued research and development, will help to unlock the full potential of quantum networking and its smooth integration into traditional communication networks. The voyage towards a quantum-enabled future holds the potential for dramatic breakthroughs in communication technology, opening the way for secure, efficient, and scalable networking that utilizes the power of quantum physics [30].

The research additionally provides a platform for working and predictions of the quantum networks which give optimal results that can be used for future implementations. Finding sophisticated ideal protocols and algorithms for constructing fast, frictionless, and secure future networks which will assume the face of Quantum Internet.

REFERENCES

- [1] Pravinkumar, P. (2023). Quantum random number generator on IBM QX. *Journal of Cryptographic Engineering*, 1-7.
- [2] Barthe, A., Grossi, M., Dunjko, V., & Tura, J. (2023). arXiv: Bloch Sphere Binary Trees: A method for the visualization of sets of multi-qubit systems pure states (No. arXiv: 2302.02957).
- [3] Sun, S., & Huang, A. (2022). A review of security evaluation of practical quantum key distribution system. *Entropy*, 24(2), 260.
- [4] Zhang, W., van Leent, T., Redeker, K., Garthoff, R., Schwonnek, R., Fertig, F., ... & Weinfurter, H. (2022). A device-independent quantum key distribution system for distant users. *Nature*, 607(7920), 687-691.
- [5] Adu-Kyere, A., Nigussie, E., & Isoaho, J. (2022). Quantum key distribution: Modeling and simulation through bb84 protocol using python3. *Sensors*, 22(16), 6284.
- [6] Qiu, D., Luo, L., & Xiao, L. (2022). Distributed Grover's algorithm. arXiv preprint arXiv:2204.10487.
- [7] Wang, L. J., Zhang, K. Y., Wang, J. Y., Cheng, J., Yang, Y. H., Tang, S. B., ... & Pan, J. W. (2021). Experimental authentication of quantum key distribution with post-quantum cryptography. *npj quantum information*, 7(1), 67.
- [8] Tsai, C. W., Yang, C. W., Lin, J., Chang, Y. C., & Chang, R. S. (2021). Quantum key distribution networks: challenges and future research issues in security. *Applied Sciences*, 11(9), 3767.
- [9] Amer, O., Garg, V., & Krawec, W. O. (2021). An introduction to practical quantum key distribution. *IEEE Aerospace and Electronic Systems Magazine*, 36(3), 30-55.
- [10] Basso Basset, F., Valeri, M., Rocca, E., Muredda, V., Poderini, D., Neuwirth, J., ... & Trotta, R. (2021). Quantum key distribution with entangled photons generated on demand by a quantum dot. *Science advances*, 7(12), eabe6379.
- [11] Hietala, K., Rand, R., Hung, S. H., Wu, X., & Hicks, M. (2021). A verified optimizer for quantum circuits. *Proceedings of the ACM on Programming Languages*, 5(POPL), 1-29.
- [12] Nadlinger, D. P., Drmota, P., Nichol, B. C., Aranedo, G., Main, D., Srinivas, R., ... & Bancal, J. D. (2021). Device-independent quantum key distribution. arXiv preprint arXiv:2109.14600.
- [13] Das, S., Bäuml, S., Winczewski, M., & Horodecki, K. (2021). Universal limitations on quantum key distribution over a network. *Physical Review X*, 11(4), 041016.
- [14] Riedel Gårding, E., Schwaller, N., Chan, C. L., Chang, S. Y., Bosch, S., Gessler, F., ... & Macris, N. (2021). Bell Diagonal and Werner state generation: Entanglement, non-locality, steering and discord on the IBM quantum computer. *Entropy*, 23(7), 797.
- [15] Jing, Y. (2021). Quantum key distribution over quantum repeaters with encoding (Doctoral dissertation, University of Leeds).
- [16] Khanal, B., Rivas, P., Orduz, J., & Zhakubayev, A. (2021, December). Quantum machine learning: A case study of Grover's algorithm. In *2021 International Conference on Computational Science and Computational Intelligence (CSCI)* (pp. 79-84). IEEE.
- [17] Pires, O. M., Duzzioni, E. I., Marchi, J., & Santiago, R. (2021). Quantum circuit synthesis of Bell and GHZ states using projective simulation in the NISQ era. arXiv preprint arXiv:2104.13297.
- [18] Piroli, L., Styliaris, G., & Cirac, J. I. (2021). Quantum circuits assisted by local operations and classical communication: Transformations and phases of matter. *Physical Review Letters*, 127(22), 220503.
- [19] Song, D., & Chen, D. (2020). Quantum key distribution based on random grouping bell state measurement. *IEEE Communications Letters*, 24(7), 1496-1499.
- [20] Mehic, M., Niemiec, M., Rass, S., Ma, J., Peev, M., Aguado, A., ... & Voznak, M. (2020). Quantum key distribution: a networking perspective. *ACM Computing Surveys (CSUR)*, 53(5), 1-41.
- [21] Bravyi, S., Gosset, D., Koenig, R., & Tomamichel, M. (2020). Quantum advantage with noisy shallow circuits. *Nature Physics*, 16(10), 1040-1045.
- [22] Yang, C. W., & Tsai, C. W. (2020). Efficient and secure dynamic quantum secret sharing protocol based on bell states. *Quantum Information Processing*, 19, 1-14.
- [23] Shannon, K., Towe, E., & Tonguz, O. K. (2020). On the use of quantum entanglement in secure communications: a survey. arXiv preprint arXiv:2003.07907.
- [24] Wong, H. Y. (2023). Shor's Algorithm. In *Introduction to Quantum Computing: From a Layperson to a Programmer in 30 Steps* (pp. 289-298). Cham: Springer International Publishing.
- [25] Gunkel, M., Wissel, F., & Poppe, A. (2019, May). Designing a quantum key distribution network-Methodology and challenges. In *Photonic Networks; 20th ITG-Symposium* (pp. 1-3). VDE.
- [26] Liu, Y.; Yu, Z.-W.; Zhang, W.; Guan, J.-Y.; Chen, J.-P.; Zhang, C.; Hu, X.-L.; Li, H.; Jiang, C.; Lin, J.; et al. Experimental Twin-Field Quantum Key Distribution through Sending or Not Sending. *Phys. Rev. Lett.* 2019, 123, 100505.
- [27] Wehner, S., Elkouss, D., & Hanson, R. (2018). Quantum internet: A vision for the road ahead. *Science*, 362(6412), eaam9288.
- [28] Stockill, R., Stanley, M. J., Huthmacher, L., Clarke, E., Hugues, M., Miller, A. J., ... & Atatüre, M. (2017). Phase-tuned entangled state generation between distant spin qubits. *Physical review letters*, 119(1), 010503.1
- [29] Tanizawa, Y.; Takahashi, R.; Sato, H.; Dixon, A.R.; Kawamura, S. A Secure Communication Network Infrastructure Based on Quantum

- Key Distribution Technology. *IEICE Trans. Commun.* (2016), 99, 1054–1069.
- [30] Van Meter, R. (2014). *Quantum networking*. John Wiley & Sons.
 - [31] Goldner, P., Ferrier, A., & Guillot-Noël, O. (2015). Chapter 267: Rare earth-doped crystals for quantum information. *Handbook on the Physics and Chemistry of Rare Earths*, 46, 1.
 - [32] Devitt, S. J., Munro, W. J., & Nemoto, K. (2013). Quantum error correction for beginners. *Reports on Progress in Physics*, 76(7), 076001.
 - [33] Van Meter, R. (2012). Quantum networking and internetworking. *IEEE Network*, 26(4), 59-64.
 - [34] John Preskill. 2018. Quantum computing in the NISQ era and beyond. *Quantum* 2 (Aug. 2018), 79. <https://doi.org/10.22331/q2018-08-06-79>.
 - [35] Arute, F., Arya, K., Babbush, R., Bacon, D., Bardin, J. C., Barends, R., ... & Martinis, J. M. (2019). Quantum supremacy using a programmable superconducting processor. *Nature*, 574(7779), 505-510.
 - [36] Briegel, H. J., Dür, W., Cirac, J. I., & Zoller, P. (1998). Quantum repeaters: the role of imperfect local operations in quantum communication. *Physical Review Letters*, 81(26), 5932.
 - [37] Sangouard, N., Simon, C., De Riedmatten, H., & Gisin, N. (2011). Quantum repeaters based on atomic ensembles and linear optics. *Reviews of Modern Physics*, 83(1), 33.