

# Lambda Grammar

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May 28, 2023

## 1 Grammar

$\langle \text{program} \rangle ::= \text{let } \langle \text{variable} \rangle = \langle \text{term} \rangle \mid \langle \text{term} \rangle$   
 $\langle \text{term} \rangle ::= \langle \text{application} \rangle \mid \langle \text{term}' \rangle$   
 $\langle \text{term}' \rangle ::= \langle \text{variable} \rangle \mid \langle \text{abstraction} \rangle \mid "(" \langle \text{term} \rangle ")"$   
 $\langle \text{applique} \rangle ::= \langle \text{term}' \rangle \langle \text{term}' \rangle \{ \langle \text{term}' \rangle \}$   
 $\langle \text{abstraction} \rangle ::= \backslash \langle \text{variable} \rangle \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\langle \text{variable} \rangle ::= \langle \text{keyword} - \text{exception} \rangle \mid \langle \text{letter} \rangle \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \}$   
 $\langle \text{keyword} - \text{exception} \rangle ::= \text{let}$   
 $\langle \text{letter} \rangle ::= a \mid \dots \mid z \mid A \mid \dots \mid Z$   
 $\langle \text{digit} \rangle ::= 1 \mid \dots \mid 9$

## 2 Examlpe 1

$\text{let } K = \backslash x y.x \implies$   
 $\langle \text{program} \rangle$   
 $\text{let } \langle \text{variable} \rangle = \langle \text{term} \rangle$   
 $\text{let } \langle \text{letter} \rangle \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} = \langle \text{term} \rangle$   
 $\text{let } K \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} = \langle \text{term} \rangle$   
 $\text{let } K = \langle \text{term} \rangle$   
 $\text{let } K = \langle \text{term}' \rangle$   
 $\text{let } K = \langle \text{abstraction} \rangle$   
 $\text{let } K = \backslash \langle \text{variable} \rangle \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash \langle \text{letter} \rangle \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash \langle \text{letter} \rangle \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x \langle \text{variable} \rangle \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x \langle \text{letter} \rangle \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x y \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x y \{ \langle \text{variable} \rangle \}. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x y. \langle \text{term} \rangle$   
 $\text{let } K = \backslash x y. \langle \text{term}' \rangle$   
 $\text{let } K = \backslash x y. \langle \text{variable} \rangle$   
 $\text{let } K = \backslash x y. \langle \text{letter} \rangle \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \}$   
 $\text{let } K = \backslash x y.x \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \}$   
 $\text{let } K = \backslash x y.x$

## 3 Example 2

$\text{let } gg = (\backslash l o.l) e z \implies$   
 $\langle \text{program} \rangle$   
 $\text{let } \langle \text{letter} \rangle \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} = \langle \text{term} \rangle$   
 $\text{let } g \{ \langle \text{letter} \rangle \mid \langle \text{digit} \rangle \} = \langle \text{term} \rangle$

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let g < letter > { < letter > | < digit > } = < term >
let gg { < letter > | < digit > } = < term >
let gg = < term >
let gg = < applique >
let gg = < term' > < term' > { < term' > }
let gg = (< term >) < term' > { < term' > }
let gg = (< term' >) < term' > { < term' > }
let gg = (< abstraction >) < term' > { < term' > }
let gg = (\ < variable > { < variable > }. < term >) < term' > { < term' > }
let gg = (\ < letter > { < letter > | < digit > } { < variable > }. < term >) < term' > { < term' > }
let gg = (\ { < letter > | < digit > } { < variable > }. < term >) < term' > { < term' > }
let gg = (\ { < variable > }. < term >) < term' > { < term' > }
let gg = (\ < variable > { < variable > }. < term >) < term' > { < term' > }
let gg = (\ < letter > { < letter > | < variable > } { < variable > }. < term >) < term' > { < term' > }
let gg = (\ o { < letter > | < variable > } { < variable > }. < term >) < term' > { < term' > }
let gg = (\ o { < variable > }. < term >) < term' > { < term' > }
let gg = (\ o. < term >) < term' > { < term' > }
let gg = (\ o. < term' >) < term' > { < term' > }
let gg = (\ o. < variable >) < term' > { < term' > }
let gg = (\ o. < letter > { < letter > | < digit > }) < term' > { < term' > }
let gg = (\ o.l { < letter > | < digit > }) < term' > { < term' > }
let gg = (\ o.l) < term' > { < term' > }
let gg = (\ o.l) < variable > { < term' > }
let gg = (\ o.l) < letter > { < letter > | < digit > } { < term' > }
let gg = (\ o.l) e { < letter > | < digit > } { < term' > }
let gg = (\ o.l) e { < term' > }
let gg = (\ o.l) e < term' > { < term' > }
let gg = (\ o.l) e < variable > { < term' > }
let gg = (\ o.l) e < letter > { < letter | < digit > } { < term' > }
let gg = (\ o.l) e z { < letter | < digit > } { < term' > }
let gg = (\ o.l) e z { < term' > }
let gg = (\ o.l) e z

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