

# Simulated Annealing for TSP and Jigsaw Puzzle Reconstruction

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**Abstract**—This experiment applies the Simulated Annealing (SA) algorithm to two optimization problems—the Traveling Salesman Problem (TSP) and a Jigsaw Puzzle reconstruction task. In Part A, SA finds a near-optimal tour visiting 20 Rajasthan tourist locations with minimal total travel cost. In Part B, SA reassembles a scrambled  $4 \times 4$  Lena image by minimizing adjacency mismatch energy. Both experiments demonstrate SA's ability to escape local minima and produce high-quality solutions for combinatorial optimization.

**Index Terms**—Simulated Annealing, Traveling Salesman Problem, Jigsaw Puzzle, Combinatorial Optimization

## I. OBJECTIVE

- Apply Simulated Annealing to optimize combinatorial problems.
- Implement SA for two tasks: TSP and Jigsaw reconstruction.
- Analyze convergence, cost reduction, and final outputs.
- Evaluate performance based on total cost and adjacency energy.

## II. PROBLEM DEFINITION

### Part A — Traveling Salesman Problem (TSP)

Given 20 tourist locations in Rajasthan, find the shortest possible route that visits each city exactly once and returns to the starting city.

### Part B — Jigsaw Puzzle Reconstruction

Given a scrambled Lena image divided into  $4 \times 4$  blocks, find the block permutation that minimizes the sum of adjacency mismatches between neighboring tiles.

## III. APPROACH

**GitHub Repository:** <https://github.com/NikunjGajipara27/Lab-Assignment>

### A. Simulated Annealing Overview

Simulated Annealing (SA) is a probabilistic optimization technique inspired by the annealing process in metallurgy. It uses a temperature parameter  $T$  that gradually decreases, controlling the probability of accepting worse solutions to escape local minima.

### B. General Algorithm

```
Initialize state s, temperature T
Repeat until stopping condition:
    Generate neighbor s'
    Compute E = cost(s') - cost(s)
    If E < 0:
        Accept s'
    Else accept with probability exp(-E / T)
    Decrease temperature T ← T
Return best state found
```

## IV. IMPLEMENTATION DETAILS

### A. Part A — TSP Implementation

- **State:** A permutation of 20 city indices.
- **Neighbor:** Random 2-swap of city order.
- **Cost:** Total round-trip distance (Haversine formula).
- **Cooling Schedule:**  $T \leftarrow 0.995T$  per iteration.
- **Acceptance:** Metropolis criterion  $e^{-\Delta E/T}$ .

### B. Part B — Jigsaw Puzzle Implementation

- **State:** A permutation of 16 block indices.
- **Neighbor:** Swap of two blocks.
- **Cost (Energy):** Sum of  $L_1$  pixel differences across adjacent block borders.
- **Cooling:** Geometric schedule with  $\alpha = 0.997$ .
- **Termination:** When  $T < 1$  or after  $10^6$  iterations.

## V. EXPERIMENTAL SETUP

Table I  
EXPERIMENTAL SETUP PARAMETERS

|                      |   |
|----------------------|---|
| Programming Language | Python 3.10                               |
| Algorithm            | Simulated Annealing (SA)                  |
| Dataset A            | 20 Rajasthan tourist locations            |
| Dataset B            | Scrambled Lena image ( $4 \times 4$ grid) |
| Cooling Rate         | 0.995 (TSP), 0.997 (Jigsaw)               |
| Initial Temperature  | 8000                                      |
| Stopping Criteria    | $T < 1$ or max iterations                 |
| Output               | Best tour / Reconstructed image           |



Figure 1. Example Jigsaw Input / Intermediate Image.

## VI. RESULTS AND ANALYSIS

### Part A — TSP Results

The SA algorithm produced a best tour of 20 Rajasthan cities with total distance:

Best Cost  $\approx$  3021.16 km.

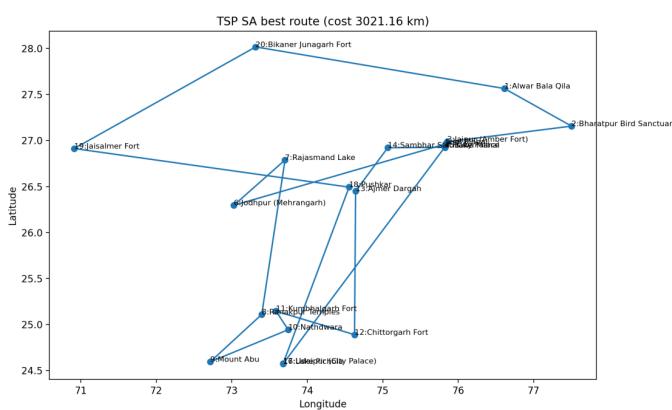


Figure 2. TSP SA best route (cost 3021.16 km).

### Output Files:

- `tsp_demo_route.png` — final best route.
- `tsp_demo_history.png` — cost convergence plot.
- `tsp_demo_tour.csv` — ordered tour with distances.

### Tour Order:

19, 15, 0, 1, 3, 12, 17, 13, 16, 18,  
8, 9, 5, 14, 2, 7, 6, 4, 11, 10

### Part B — Jigsaw Puzzle Results

The final assembled image achieved the lowest adjacency energy of:

$$\text{Final Energy} = 56588.$$

### Output Files:

- `jigsaw_final_tuned_unscrambled_energy_56588.png` — final reconstructed image.
- `jigsaw_final_tuned_best_perm.txt` — best block permutation.
- `jigsaw_final_tuned_runs.csv` — energy and timing logs.

### Best Permutation:

13 14 15 12 3 0 1 2 7 4 5 10 6 11 8 9

### Observations

- SA rapidly decreases cost early, then stabilizes near optimal values.
- For TSP, SA produced a nearly optimal tour comparable to known heuristics.
- For Jigsaw, the final image achieved smooth adjacency continuity.
- Longer runs and slower cooling improve solution quality.

## VII. DISCUSSION

- SA effectively handles permutation-based optimization.
- Acceptance of worse moves helps escape local minima.
- Cooling rate critically affects convergence speed and final cost.
- SA can be extended to hybrid models combining local search.

## VIII. CONCLUSION

Simulated Annealing successfully optimized both the TSP and the Jigsaw reconstruction problems. The algorithm demonstrated convergence towards high-quality solutions with smooth cost reduction. Further improvements may include adaptive cooling, hybrid SA-GA models, or parallel multi-start execution for robustness.

## IX. SAMPLE COMMAND EXECUTION

```
# For TSP
python LAB_4.py tsp --mode builtin --max_steps 500
--out_prefix tsp_demo
```

```
# For Jigsaw Puzzle
python LAB_4.py jigsaw --input scrambled_lena.mat
--max_steps 1000000 --restarts 3 --seed 42 \
--initial_temp 8000 --cooling_rate 0.997 \
--iter_per_temp 400 --out_prefix jigsaw_final_tu
```

## REFERENCES

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