

1.

Determine the DFA schematic for  $M = (Q, \Sigma, \delta, q, F)$

where  $Q = \{q_1, q_2, q_3\}$ ,  $\Sigma = \{0, 1\}$ ,  $q_1$  is the start state,  $F = \{q_2\}$  and  $\delta$  is given by the table below.

Initial state $q$	Symbol $\sigma$	Final state $\delta(q, \sigma)$
$q_1$	0	$q_1$
$q_1$	1	$q_2$
$q_2$	0	$q_3$
$q_2$	1	$q_2$
$q_3$	0	$q_2$
$q_3$	1	$q_2$

Also determine a Language  $L$  recognized by the DFA.

2.

Obtain the DFA that accepts/recognizes the language

$$L(M) = \{w \mid w \in \{a, b, c\}^* \text{ and } w \text{ contains the pattern } abac\}$$

3.

Design a DFA, the language recognized by the

Automaton being

$$L = \{a^n b : n \geq 0\}$$

4.

Determine an NFA accepting the language

$$L_2 = \{a^* \cup b^*\}$$

5.

Given the NDA as shown in Fig. (a), with  $\delta$  as shown in

Fig. (b).

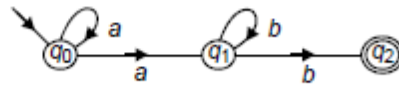


Fig. (a)

	$a$	$b$
$q_0$	$\{q_0, q_1\}$	$\emptyset$
$q_1$	$\emptyset$	$\{q_1, q_2\}$
$q_2$	$\emptyset$	$\emptyset$

Fig. (b)

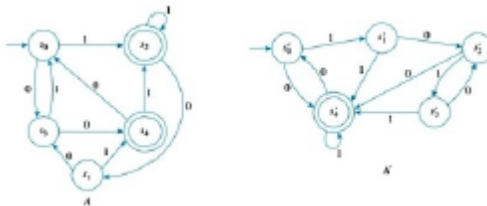
Determine the equivalent DFA for the above given NDA.

6.

Given  $L_1 = \{a, ab, a^2\}$  and  $L_2 = \{b^2, aba\}$  are the languages over  $A = \{a, b\}$ , determine  $\{a\} \bar{L}_1 L_2$  (b)  $\bar{L}_2 L_2$ .

7.

Are the automata  $A$  and  $A'$  shown below equivalent?



8

(a) design an automaton with the given input alphabet that accepts the given set of strings, and (b) find a regular expression that defines the language accepted by the automaton.

Input alphabet =  $\{a, b\}$ ; Accepts the set of all strings of length at least 2 for which the final two input symbols are the same.