## MATH 450 Seminar in Proof

Every integer greater than 1 is expressible as a product of primes.

Proof. Let us proceed by contradiction. Let n>1 be the least integer that cannot be expressed as a product of primes. By construction, n has no divisors that are prime, so n is not a prime number. Thus n is composite number. Thus, there exists an integer a where 1 < a < n such that, a divides n. Since a divides n we can write n as n = ab where 1 < b < n. Since n is the smallest number that does not have prime factors, we can say that  $a = p_1 \cdot p_2 \cdot p_3 \cdot \ldots \cdot p_n$  and  $b = q_1 \cdot q_2 \cdot q_3 \cdot \ldots \cdot q_n$  where  $p_i, q_i$ , where  $p_i \in \mathbb{N}$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  and  $p_i$  and  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  and  $p_i$  are prime factors of  $p_i$  and  $p_i$  are prime fa

A little awkwardly written since it's not the i that are the prime factors