

2023

Time : 3 hours

Full Marks : 70

*Candidates are required to give their answers in
their own words as far as practicable.*

The figures in the margin indicate full marks.

Answer from all the Sections as directed.

Section – A

(Objective Type Questions)

1. Select the correct answer of the following :

$1 \times 5 = 5$

(a) The following is an example of a linear function :

- (i) $f: R^2 \rightarrow R$ given as $f(x, y) = 2x + 3y$
- (ii) $f: R^2 \rightarrow R$ given as $f(x, y) = 2x + 3y - 1$
- (iii) $f: R^2 \rightarrow R$ given as $f(x, y) = 2x + 3y + 1$
- (iv) None of these

(b) The feasible region of an LPP is a :

- (i) Convex set

- (ii) Non-convex set
 - (iii) Both (i) & (ii)
 - (iv) None of these
- (c) The objective function of an LPP is a :
- (i) Linear function
 - (ii) Non-linear function
 - (iii) Both (i) and (ii)
 - (iv) None of these
- (d) Feasible region is the set of points which satisfies :
- (i) The objective function
 - (ii) Some of the given constraints
 - (iii) All of the given constraints
 - (iv) None of these
- (e) The feasible solution of an LPP which gives the best value to the objective function is called :
- (i) General solution
 - (ii) Optimal solution
 - (iii) Particular solution
 - (iv) None of these

2. Fill in the blanks of the following : $1 \times 5 = 5$

- (a) The region inside a circle is an example of a _____ set.
- (b) The full form of PERT is _____.
- (c) The Floyd algorithm is used to find _____.
- (d) The Ford-Fulkerson algorithm is used to find _____.
- (e) The set of constraints in an LPP identify the _____ region.

Section - B

(Short-answer Type Questions)

3. Answer any four questions of the following :

$5 \times 4 = 20$

~~(a)~~ Solve the linear system :

$$x + y + z = 4$$

$$3x - y - z = 2$$

$$x + 3y + 3z = 8$$

~~(b)~~ Find the rank of the matrix

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ -1 & -2 & -2 \end{bmatrix}$$

KV - 3/3 (3) (Turn over)

(c) Solve the following 2×2 game:

Player B

		Strategy I	Strategy II
Player A		Strategy I	7
		Strategy II	2
		1	
		6	

(d) Show that the union of two convex sets need not be convex.

(e) What are the differences between PERT and CPM ?

(f) Write a short note on Fulkerson Algorithm with an example.

Section - C

(Long-answer Type Questions)

4. Answer any four questions of the following :

$$10 \times 4 = 40$$

(a) Solve the LPP graphically :

$$\text{Max } Z = 5x + 3y \text{ subject to } x + y \leq 300$$

D $\geq 0, 300$ B $\geq 300, 0$ $2x + y \leq 360$
C $\geq 10, 240$ $x, y \geq 0$

(b) Solve the LPP by simplex method :

$$\text{Max } Z = 5x + 7y$$

$$\text{subject to } 2x + 3y \leq 13$$

$$3x + 2y \leq 12$$

$$x, y \geq 0$$

(c)

Show that the intersection of two convex sets is also a convex set.

(d) Solve the following game using principle of dominance method :

Player B	Strategy I	Strategy II	Strategy III	Strategy IV
Player A	1			
Strategy I	3	2	4	0
Strategy II	3	4	2	4
Strategy III	4	2	4	0
Strategy IV	0	4	0	8

(e)

Obtain the initial basic feasible solution of the given transportation problem whose cost and requirement table is given below using least cost method :

Destination	D ₁	D ₂	D ₃	Supply
origin				
O ₁	2	7	4	5
O ₂	3	3	1	8
O ₃	5	4	7	7
O ₄	1	6	2	14
Demand	7	9	18	34

(f)

Write short note on PERT and CPM.

