

**2023**

*Time : 3 hours*

*Full Marks : 70*

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Answer from **all** the Sections as directed.*

**Section – A**

**(Objective Type Questions)**

1. Select the correct answer of the following :

$$1 \times 5 = 5$$

- (a) The following is an example of a linear function :

(i)  $f : \mathbb{R}^2 \rightarrow \mathbb{R}$  given as  $f(x, y) = 2x + 3y$

(ii)  $f : \mathbb{R}^2 \rightarrow \mathbb{R}$  given as  $f(x, y) = 2x + 3y - 1$

(iii)  $f : \mathbb{R}^2 \rightarrow \mathbb{R}$  given as  $f(x, y) = 2x + 3y + 1$

~~(iv) None of these~~

- (b) The feasible region of an LPP is a :

~~(i) Convex set~~

- (ii) Non-convex set
  - (iii) Both (i) & (ii)
  - (iv) None of these
- (c) The objective function of an LPP is a :
- ~~(i)~~ Linear function
  - (ii) Non-linear function
  - (iii) Both (i) and (ii)
  - (iv) None of these
- (d) Feasible region is the set of points which satisfies :
- (i) The objective function
  - (ii) Some of the given constraints
  - ~~(iii)~~ All of the given constraints
  - (iv) None of these
- (e) The feasible solution of an LPP which gives the best value to the objective function is called :
- (i) General solution
  - ~~(ii)~~ Optimal solution
  - (iii) Particular solution
  - (iv) None of these

2. Fill in the blanks of the following :  $1 \times 5 = 5$

(a) The region inside a circle is an example of a \_\_\_\_\_ set.

(b) The full form of PERT is \_\_\_\_\_.

(c) The Floyd algorithm is used to find \_\_\_\_\_.

(d) The Ford-Fulkerson algorithm is used to find \_\_\_\_\_.

(e) The set of constraints in an LPP identify the \_\_\_\_\_ region.

### Section – B

#### (Short-answer Type Questions)

3. Answer any four questions of the following :

$5 \times 4 = 20$

(a) Solve the linear system :

$$x + y + z = 4$$

$$3x - y - z = 2$$

$$x + 3y + 3z = 8$$

(b) Find the rank of the matrix

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ -1 & -2 & -2 \end{bmatrix}$$

KV – 3/3

(3)

(Turn over)

(c) Solve the following  $2 \times 2$  game :

		Player B	
		Strategy I	Strategy II
Player A	Strategy I	1	7
	Strategy II	6	2

(d) Show that the union of two convex sets need not be convex.

(e) What are the differences between PERT and CPM ?

(f) Write a short note on Fulkerson Algorithm with an example.

### Section - C

#### (Long-answer Type Questions)

4. Answer any four questions of the following :

$$10 \times 4 = 40$$

(a) Solve the LPP graphically :

$$\text{Max } Z = 5x + 3y \text{ subject to } x + y \leq 300$$

$$2x + y \leq 360$$

$$x, y \geq 0$$

(b) Solve the LPP by simplex method :

$$\text{Max } Z = 5x + 7y$$

$$\text{subject to } 2x + 3y \leq 13$$

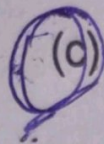
$$3x + 2y \leq 12$$

$$x, y \geq 0$$

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(4)

Contd.



(c) Show that the intersection of two convex sets is also a convex set.

(d) Solve the following game using principle of dominance method :

Player B	Strategy I	Strategy II	Strategy III	Strategy IV
Player A	I	II	III	IV
Strategy I	3	2	4	0
Strategy II	3	4	2	4
Strategy III	4	2	4	0
Strategy IV	0	4	0	8

(e) Obtain the initial basic feasible solution of the given transportation problem whose cost and requirement table is given below using least cost method :

Destination	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	Supply
origin				
O <sub>1</sub>	2	7	4	5
O <sub>2</sub>	3	3	1	8
O <sub>3</sub>	5	4	7	7
O <sub>4</sub>	1	6	2	14
Demand	7	9	18	34

(f) Write short note on PERT and CPM.

