

Modelling ultrafast magnetization dynamics in Fe, Ni, Co with the Microscopic Three Temperature model

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Midterm presentation for Master thesis

Introduction

The Microscopic Three temperature Model

Experimental Data

Implemented Model

Discussion of parameters

Results

## Introduction

The Microscopic Three temperature Model

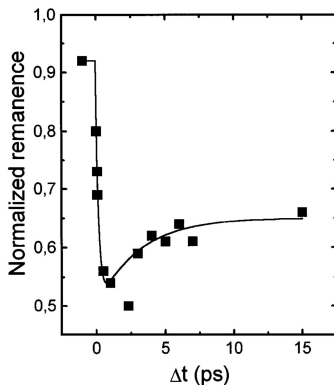
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- ▶ Beaurepaire et al. 1996: UFD in Nickel
- ▶ optically excite sample with fs laser pulse
- ▶ measure magnetization by probing at different delays
- ▶ microscopic processes?



UFD in Nickel, captured by Beaurepaire et al. <sup>1</sup>

<sup>1</sup>Beaurepaire et al., PRL 76, 1996

Introduction

**The Microscopic Three temperature Model**

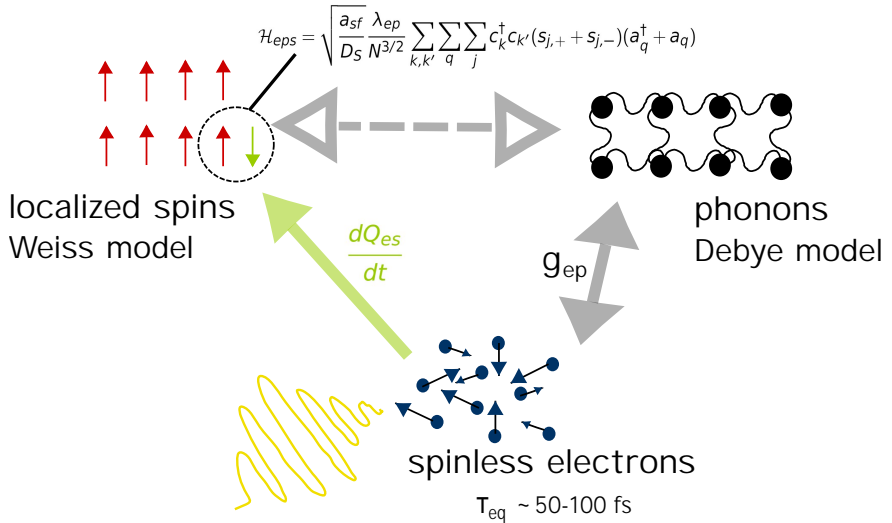
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# Sketch of Interactions



Dynamics of electronic, lattice and spin subsystems <sup>2</sup>

$$C_e \frac{dT_e}{dt} = g_{e-p}(T_p - T_e) + S(z, t) + \nabla(\kappa \nabla T_e)$$

$$C_p \frac{dT_p}{dt} = -g_{e-p}(T_p - T_e)$$

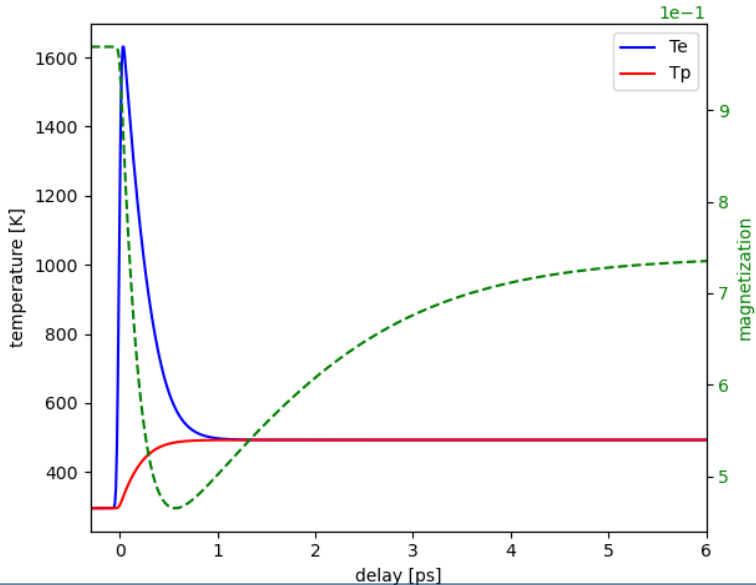
$$\frac{dm}{dt} = Rm \frac{T_p}{T_C} \left( 1 - \frac{m}{B_{1/2} \left( \frac{Jm}{k_B T_e} \right)} \right)$$

$$R = a_{sf} 8g_{ep} k_B T_C^2 V_{at} / (\mu_{at} E_D^2)$$

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<sup>2</sup>Koopmans et al., NMat 2593, 2009

# Dynamics of the subsystems in the M3TM

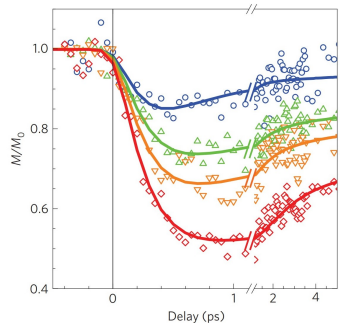




## Koopmans' estimation of $a_{sf}$

- fit parameters  $\mathbf{c_e, c_p, g_{ep}, S_0, a_{sf}}$
- spin flip probability found by Koopmans very high
- Carva et al.<sup>3</sup> retrieved  $a_{sf}$  from DFT calculations

Sample	$a_{sf}$	Koopmans
Nickel	0.04 – 0.09	0.17 – 0.2
Cobalt	0.01 – 0.022	0.135 – 0.165
Iron	0.04 – 0.07	



simulation fits for low fluences,  
reprinted from <sup>3</sup>

<sup>3</sup>Carva et al., PRB 87, 2013

<sup>4</sup>Koopmans et al., NMat 2593, 2009

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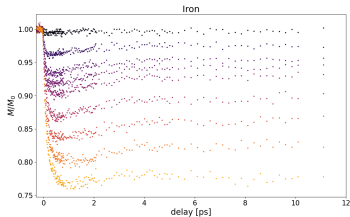
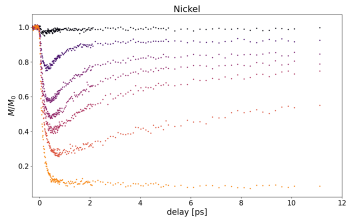
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**Experimental Data**

Implemented Model

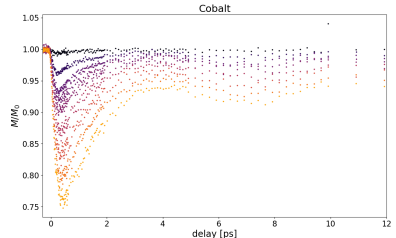
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Results



- ▶ Ni, Fe, Co thin films ( $d = 15$  nm) on glass wafers
- ▶ room temperature, fluence  $0.5 - 15 \frac{\text{mJ}}{\text{cm}^2}$
- ▶ magnetization measured under same conditions for several pump fluences

Borchert et al., arXiv:2008.12612, 2020



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## Dynamics of electronic, lattice and spin subsystems<sup>4</sup>

$$C_e \frac{dT_e}{dt} = g_{e-p}(T_p - T_e) + S(z, t) + \frac{dQ_{se}}{dt}$$

$$C_p \frac{dT_p}{dt} = -g_{e-p}(T_p - T_e)$$

$$\frac{dm}{dt} = Rm \frac{T_p}{T_C} \left( 1 - \frac{m}{B_{1/2} \left( \frac{Jm}{k_B T_e} \right)} \right)$$

$$\frac{dQ_{se}}{dt} = Jm \frac{dm}{dt}$$

$$R = a_{sf} 8g_{ep} k_B T_C^2 V_{at} / (\mu_{at} E_D^2)$$

\*Ab initio parameters<sup>5</sup>

<sup>4</sup>Koopmans et al., Nmat 2593, 2009

<sup>5</sup>Zahn et al., PRR 3, 2020

# M-Dynamics for arbitrary spin

material	$S_{\text{eff}}^6$
Nickel	0.5
Iron	2
Cobalt	1.5

## Arbitrary Spin Rate Equations <sup>7</sup>

$$\frac{dm}{dt} = -\frac{1}{S} \sum_{m_s=-S}^{m_s=+S} m_s \frac{df_{m_s}}{dt}$$

$$\frac{df_{m_s}}{dt} = -(W_{m_s}^+ + W_{m_s}^-)f_{m_s} + W_{m_s-1}^+ f_{m_s-1} + W_{m_s+1}^- f_{m_s+1}$$

$$W_{m_s}^{\pm} = R \frac{Jm}{4Sk_B T_c} \frac{T_p}{T_c} \frac{e^{\mp \frac{Jm}{2Sk_B T_e}}}{\sinh(\frac{Jm}{2Sk_B T_e})} (S(S+1) - m_s(m_s \pm 1))$$

<sup>6</sup>Köbler et al., Condensed matter, 2003

<sup>7</sup>Beens et al., Phys. Rev. B, 2019

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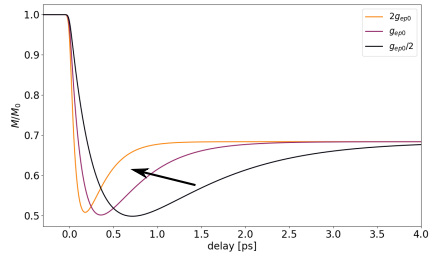
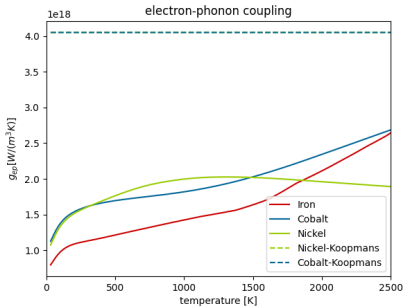
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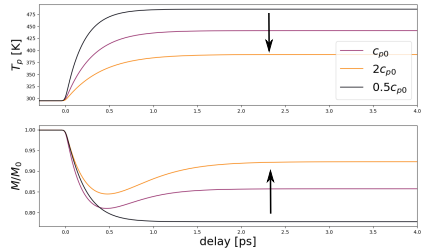
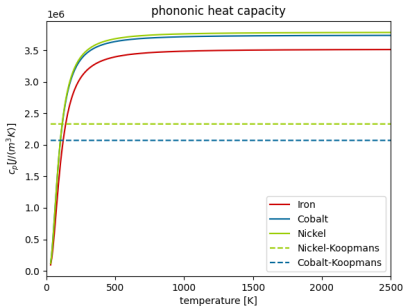
# Electron phonon coupling $g_{ep}$



fixed  $\frac{R}{g_{ep}}, c_e, c_p$   
vary  $g_{ep}$

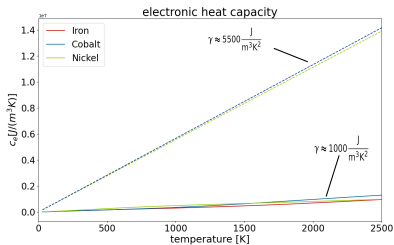


# Phononic specific heat $c_p$

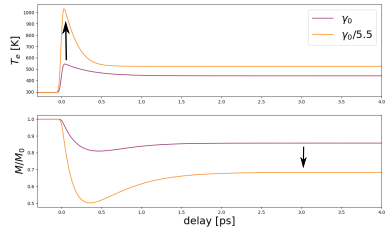


fixed  $R, c_e, g_{ep}$ ,  
vary  $c_p$

# Electronic specific heat $c_e$

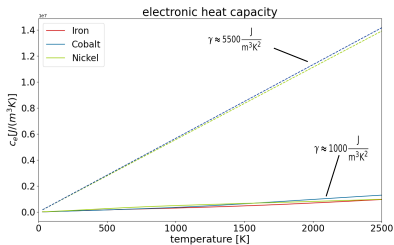


$$c_e = \gamma T_e$$

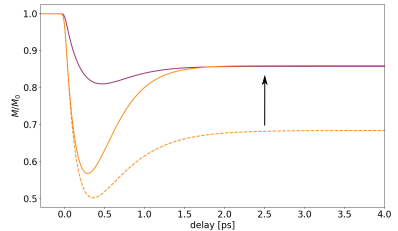


fixed  $R, c_p, g_{ep}$ ,  
decrease  $c_e$

# Electronic specific heat $c_e$

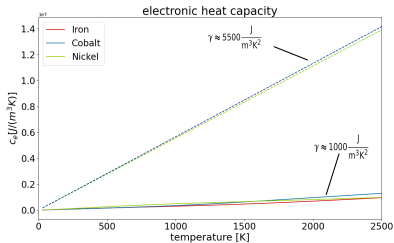


$$c_e = \gamma T_e$$

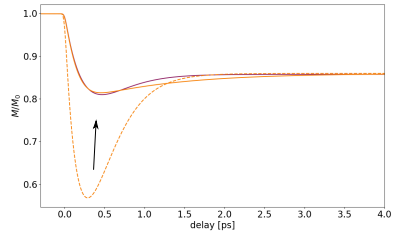


$$\text{fixed } R, g_{ep} \\ \approx 2c_p$$

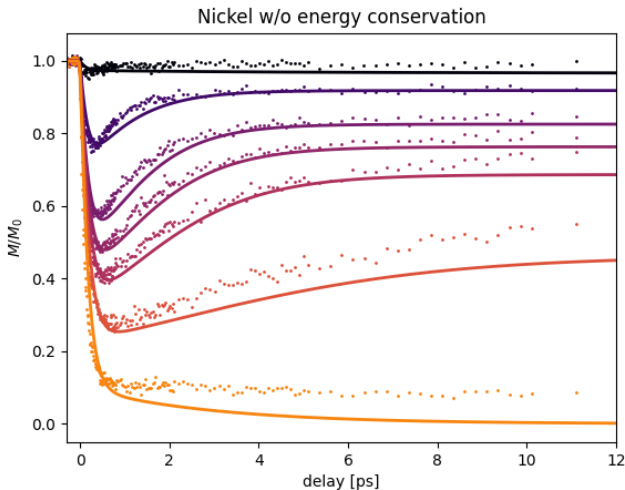
# Electronic specific heat $c_e$



$$c_e = \gamma T_e$$

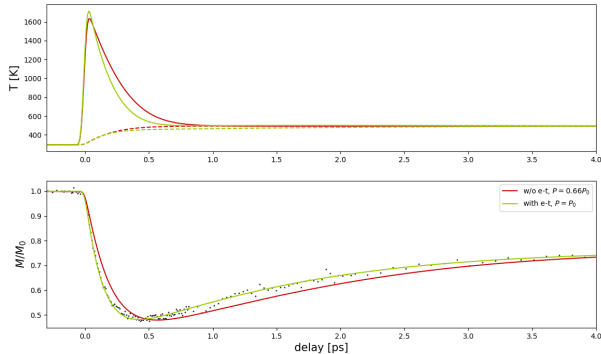


fixed  $g_{ep}$   
 $\approx 0.4R$



$$a_{sf} \approx 0.05$$

# Influence of e-s energy flow



$$\frac{dQ_{es}}{dt} = Jm \frac{dm}{dt} \quad (1)$$

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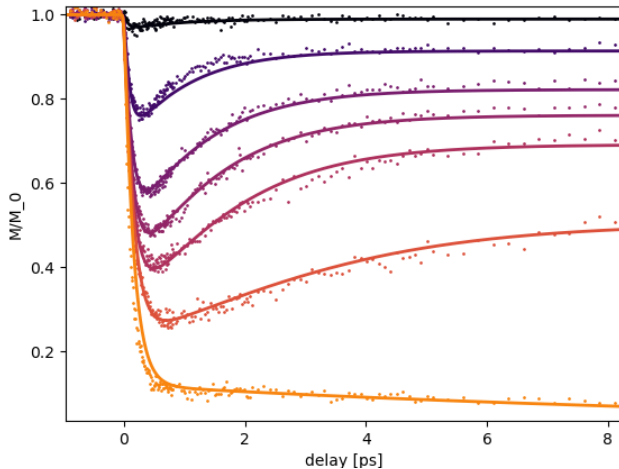
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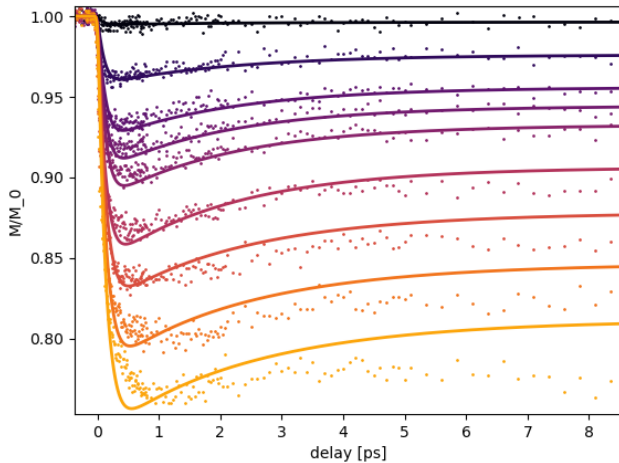
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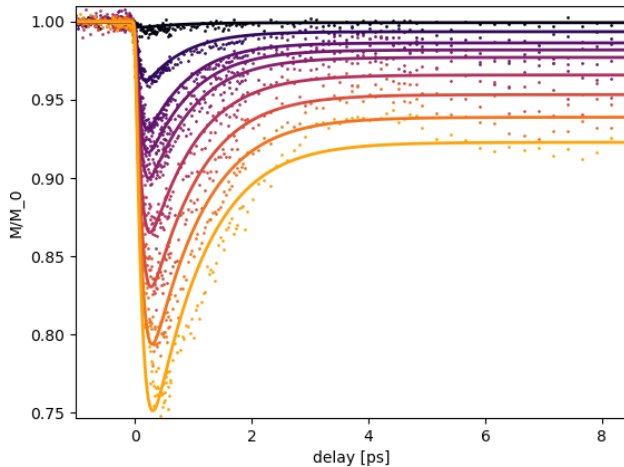


$P_s$	Koopmans	simulated
0.04 – 0.09	0.17 – 0.2	0.05 – 0.06





$P_s$	Koopmans	simulated
0.04 – 0.07		0.03 – 0.035



$P_s$	Koopmans	simulated
0.01 – 0.022	0.135 – 0.165	0.04 – 0.05

# Thanks

Thank you for your attention

fluence [ $\frac{mj}{cm^2}$ ]	$P_0$ [ $10^{21} \frac{W}{m^3}$ ] Nickel	$P_0$ [ $10^{21} \frac{W}{m^3}$ ] Iron	$P_0$ [ $10^{21} \frac{W}{m^3}$ ] Cobalt
0.5	1.68	1.33	1.33
3	10.08	8	8
5	16.8	13.3	13.3
6	20.3	16	16
7	23.7	18.6	18.6
9	30.5	23.9	23.9
11	38.5	29	29
13		34.2	34.2
15		39.4	39.4

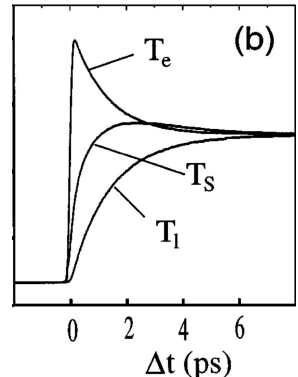
## Three temperature model

$$C_e \partial_t T_e = -g_{ep}(T_e - T_p) - g_{es}(T_e - T_s) + S(t) \quad (2)$$

$$C_p \partial_t T_p = g_{ep}(T_e - T_p) - g_{ps}(T_p - T_s)$$

$$C_s \partial_t T_s = g_{es}(T_e - T_s) + g_{ps}(T_p - T_s)$$

- ▶  $C_i$  heat capacity of subsystem  $i$
- ▶  $g_{ij}$  coupling constant of systems  $i, j$
- ▶  $g_{ps} \ll g_{es}$
- ▶  $C_s \ll C_p$
- ▶ spin system not in internal equilibrium <sup>8</sup>
- ▶ energy redistribution within sample
- ▶ microscopic processes behind spin flip events?



# Landau-Lifshitz-Bloch description

$$\partial_t \mathbf{n} = \gamma [\mathbf{n} \times \mathbf{H}_{\text{eff}}] - \frac{\gamma \alpha_{\perp}}{n^2} [\mathbf{n} \times [\mathbf{n} \times \mathbf{H}_{\text{eff}}]] + \frac{\gamma \alpha_{\parallel}}{n^2} [\mathbf{n} \cdot \mathbf{H}_{\text{eff}}] \mathbf{n}^9 \quad (3)$$

$\gamma$  gyromagnetic ratio

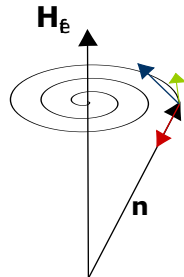
$$\mathbf{n} = \frac{\langle \mathbf{S} \rangle}{m_e(T_e)}$$

$$\alpha_{\perp} = \frac{\lambda}{m_e} \left[ \frac{\tanh(q_s)}{q_s} - \frac{T}{3T_C} \right]$$

$$\alpha_{\parallel} = \frac{2\lambda T}{3m_e T_C} \frac{2q_s}{\sinh(2q_s)}$$

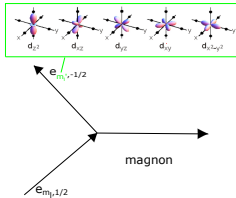
$\lambda$  dissipation constant

$$\mathbf{H}_{\text{eff}} = \mathbf{H}_{\text{int}} + \frac{m_e(T)}{2\chi_{\parallel}} (1 - n^2) \mathbf{n}$$

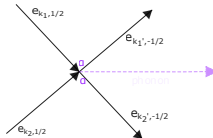


<sup>9</sup>Atxitia et al., PRB 84, 2011

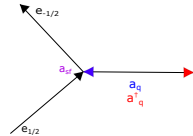
# Proposed Elliott-Yafet like spin flip interactions



e-m scattering,  
*Carpene et al., PRB 78, 2008*



Coulomb-scattering,  
*Krauß et al., PRB 80, 2009*



e-p scattering,  
*Koopmans et al., Nmat 2593, 2009*

- low energy magnon excitations
- inelastic scattering leads to Stoner excitations
- angular momentum not explicitly considered
- lattice = sink for angular momentum

## Elliott-Yafet spin flips

- ▶ SOC couples majority and minority bands, thus <sup>10</sup>

$$|\psi_{k,n}^{\uparrow}\rangle = a_{k,n}^{\uparrow} |\uparrow\rangle + b_{k,n}^{\uparrow} |\downarrow\rangle$$

- ▶ spin transitions upon spin-diagonal interactions yield finite

$$\langle \psi_{k,n}^{\uparrow} | \mathcal{H}_{\text{int}} | \psi_{k',n}^{\downarrow} \rangle$$

Proposed mechanisms include

- ▶ electron-magnon-scattering
- ▶ Coulomb scattering
- ▶ electron phonon-scattering

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<sup>10</sup>Elliott<sup>†</sup>, PR 96, 1954