

Lab 2

Q₁)

$$a) R = \begin{bmatrix} k \cos \theta & -k \sin \theta & \bar{t}_x \\ k \sin \theta & k \cos \theta & \bar{t}_y \\ 0 & 0 & 1 \end{bmatrix}$$

\rightarrow scale = 0.5
 \rightarrow Rotation = $\frac{3\pi}{8}$
 \rightarrow Translation = (20, 30)

$$= \begin{bmatrix} 0.5 \cos \frac{3\pi}{8} & -0.5 \sin \frac{3\pi}{8} & 20 \\ 0.5 \sin \frac{3\pi}{8} & 0.5 \cos \frac{3\pi}{8} & 30 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.19134172 & -0.46193977 & 20 \\ 0.46193977 & 0.19134172 & 30 \\ 0 & 0 & 1 \end{bmatrix}$$

Q₃)

$$A = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

$$A \cup B \text{ (union)} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

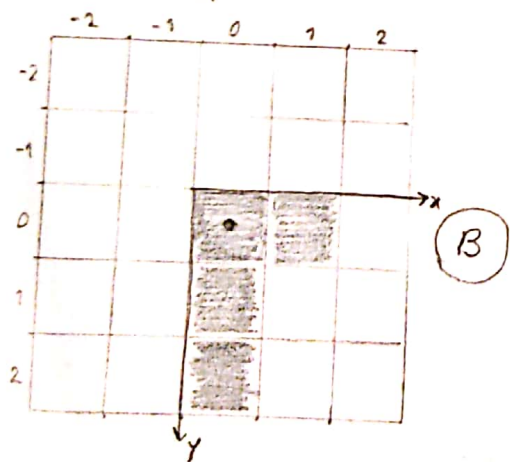
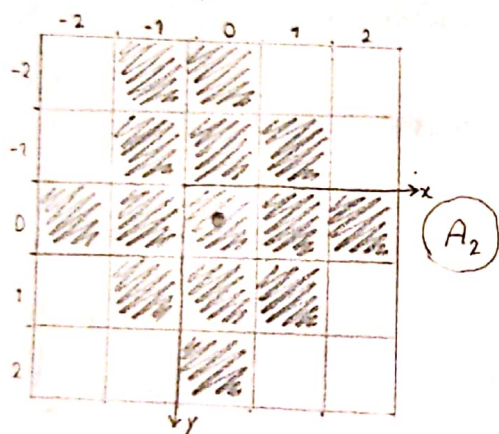
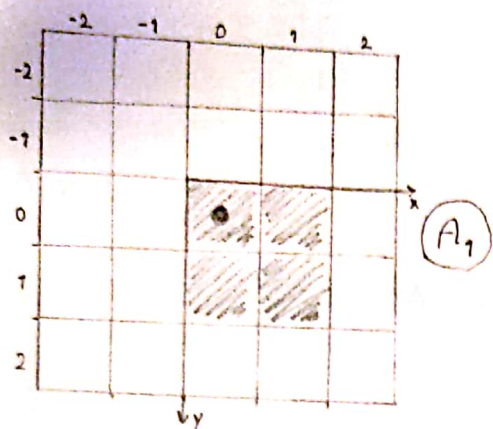
$$\bar{B} \text{ (reflection)} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A \cap B \text{ (intersection)} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\neg A \text{ (complement)} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

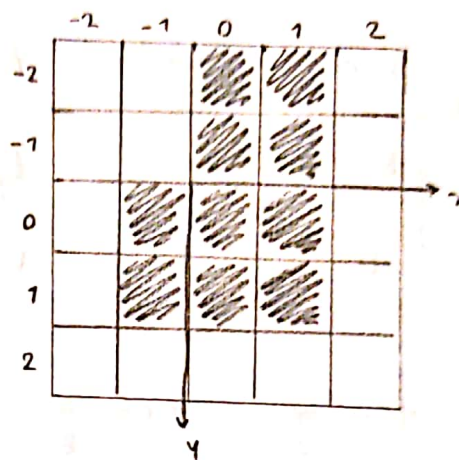
$$A \setminus B \text{ (set difference)} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Q4)



Dilation

$$A_1 \oplus B$$



Erosion

$$A_2 \ominus B$$

