

- 1) Write an algorithm that given an unsorted array returns whether an increasing subsequence of length 3 exists or not in the array. Your algorithm should run in $O(n)$ time complexity and $O(1)$ space complexity.

15 points

- 2) Consider the following multithreaded algorithm for performing pairwise multiplication on n -element arrays $A[1..n]$ and $B[1..n]$, storing the multiplications in $C[1..n]$:

```
MUL-ARRAYS (A, B, C)
1   parallel for i = 1 to A.length
2       C[i] = A[i] * B[i]
```

Analyze the work, span and parallelism of this algorithm.

15 points

- 3) Design a dynamic programming algorithm for the version of the knapsack problem in which there are unlimited quantities of copies for each of the n item kinds given. Indicate the time efficiency of the algorithm.

20 points