

# Differences-in-Differences & two-way fixed effects

Nils Droste

2021 ClimBEco course



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**Synopsis**: Today, we will be looking into *the* classical research design for inferring causal effects from observational data (i.e. when experiments are unethical or infeasible), and its recent developments

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**Synopsis:** Today, we will be looking into *the* classical research design for inferring causal effects from observational data (i.e. when experiments are unethical or infeasible), and its recent developments

In particular, we will develop an understanding of

quasi / natural experiments

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- quasi / natural experiments
  - Difference-in-Differences

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- quasi / natural experiments
  - Difference-in-Differences
  - (two-way) fixed-effects regressions

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- quasi / natural experiments
  - Difference-in-Differences
  - (two-way) fixed-effects regressions
  - staggered treatment

# Definition

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### **Quasi-** / natural experiment:

A setting where a subpopulation is treated with an intervention of sorts that occurs due to non-random assignment processes (outside of the researchers influence if its called *natural*).

# Recall potential outcome approximation

### Diff-in-Diff



We may choose to infer an average treatment effect (ATE) I: i.e.  $I = \{A, B...\}$ by comparing the average outcomes of treated individuals a from A with the one of untreated individuals  $b \in B$ .

$$E\{\Delta Y_i\} \approx E\{Y_a(1)\} - E\{Y_b(0)\} \tag{1}$$

For such a case we can exploit *random chance* within sufficiently large samples to make these groups comparable.

# Recall potential outcome approximation

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$$E\{\Delta Y_i\} \approx E\{Y_a(1)\} - E\{Y_b(0)\} \tag{1}$$

For such a case we can exploit *random chance* within sufficiently large samples to make these groups comparable.

**But what if we do not have a random assignment** (and there may be a selection-bias and / or substantial differences between groups)?

# a famous case

By comparing a treated with an untreated group over 2+ periods, we can control for (time-constant) differences between groups.

DAGs



## a famous case



By comparing a treated with an untreated group over 2+ periods, we can control for (time-constant) differences between groups.

A classic example is the Card and Krueger (AER, 1994), comparing fast-food worker employment in Pennsylvania (PA) and New Jersey (NJ) before and after a minimum wage raise in NJ in 1992.

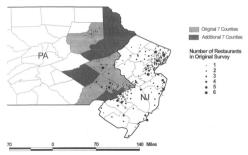


FIGURE 1. AREAS OF NEW JERSEY AND PENNSYLVANIA COVERED BY ORIGINAL SURVEY AND BLS DATA

Image source: Card and Krueger 2000

## results

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## Here is a (tweaked) version of Card and Krueger 1994, Figure 1.

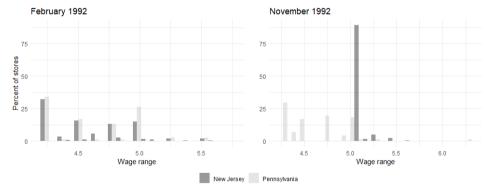


Image source: Card and Krueger 1994

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Here, we are interested in the average treatment effect on the treated (ATT)

$$ATT = E[Y_i(1) - Y_i(0)|D = 1]$$
 (2)

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For this to be a consistent estimator, we will need a set of conditions to hold, some of which we can test, others we will need to assume.

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For this to be a consistent estimator, we will need a set of conditions to hold, some of which we can test, others we will need to assume.

In particular, the parallel-trends assumption:

$$E[Y_{it}(0) - Y_{it-1}(0)|D = 1] = E[Y_{it}(0) - Y_{it-1}(0)|D = 0]$$
(3)

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$$E[\mathbf{Y}_{it}(0) - \mathbf{Y}_{it-1}(0)|D=1] = E[\mathbf{Y}_{it}(0) - \mathbf{Y}_{it-1}(0)|D=0]$$
 (3)

because then, we can assume

$$ATT = E[Y_t - Y_{t-1}|D=1] - E[Y_t - Y_{t-1}|D=0]$$
 (4)

# Directed acyclic graphs

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## Difference-in-Differences (DID)

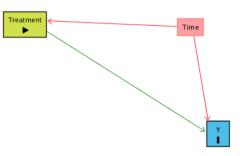


Image source: Huntington-Klein 2018

# Directed acyclic graphs

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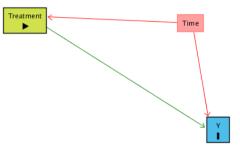
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### Difference-in-Differences (DID)



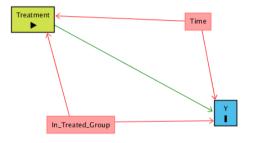


Image source: Huntington-Klein 2018

# Directed acyclic graphs

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## Difference-in-Differences (DID)

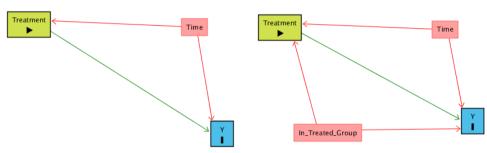


Image source: Huntington-Klein 2018

 $\rightarrow$  Accounting for differences between groups over time enables not just the estimation of time and group effects but also the differences-in-differences (i.e. the interaction of time and group effects).

## **Estimation**

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### **DID** Estimator

assume n individual units i, and t = 2 time periods, we can estimate the effect of a treatment ocurring at  $P_{t=1}$ , affecting the treated subpopulation  $D_i = 1$ 

$$Y_{i} = \beta_{0} + \beta_{1}D_{i} + \beta_{2}P_{t} + \beta_{3}D_{i} \times P_{t} + \varepsilon_{i}$$
 (5)

with  $D_i$  = Treatment,  $P_t$  = Period Dummy.

 $\beta_3$  gives us an estimate of the diff-in-diff treatment effect.

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## Estimation

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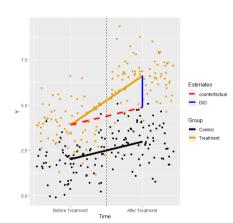
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# regression

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## To estimate an example ATT, we can use the Card and Krueger (1994) data

> summary(did\_model)

### Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) 23.331 1.072 21.767 <2e-16 \*\*\* -2.1661.516 -1.429 0.1535 time 1.194 -2.423 0.0156 \* treated -2.892 2.754 1.688 1.631 0.1033 time:treated

Note: heteroskedasticity and autocorrelation robust standard errors should be computed

# intermediate summary

estimation



A difference-in-differences approach allows us to

- compare a treatment group with an untreated quasi-counterfactual
- even under conditions of a non-random assignment
- assuming that the groups behave comparably enough

## Panel Data

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Let us suppose a situation with repeated measurements for multiple individual(s) (units), i.e. cross-sectional time-series, or panel data.

### An example panel data structure

individual	time	Υ	X	D
Α	1	0.8	0.3	0
Α	2	0.7	0.2	0
Α	3	0.5	0.2	1
В	1	1.2	0.4	0
В	2	1.1	0.5	0
В	3	0.9	0.6	1

## An exemplary study



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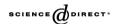
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ECOLOGICAL ECONOMICS

Ecological Economics 55 (2005) 527-538

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### ANALYSIS

# Environmental pressure group strength and air pollution: An empirical analysis

Seth Binder, Eric Neumayer\*

Department of Geography and Environment and Center for Environmental Policy and Governance (CEPG), London School of Economics and Political Science, Houghton Street, London WC2A 2AE, UK

Received 7 December 2003; received in revised form 22 October 2004; accepted 14 December 2004 Available online 24 February 2005

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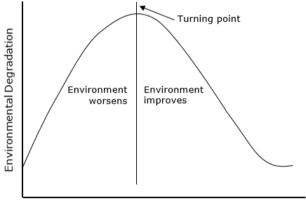
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## An exemplary study



Per Capita Income

Theoretical underpinning for Binder and Neumayer 2005: Environmental Kuznets Curve. Image source: Wikipedia

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## Replicated results from table 1, model 1 Binder and Neumayer 2005

### Coefficients:

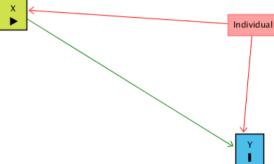
	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-57.55012	16.60671	-3.465	0.000548	***
lnengopc	-0.51121	0.11878	-4.304	1.82e-05	***
lnenergy	1.00887	0.60455	1.669	0.095425	
lngdp	13.81819	4.17975	3.306	0.000975	***
lngdpsq	-0.88657	0.27384	-3.238	0.001239	**
polity	-0.05079	0.03023	-1.680	0.093135	

Note: This is not a fixed effects regression but an OLS

# Panel Data

## One way fixed-Effects (FE) structure





Accounting for individual fixed effects. Image source: Huntington-Klein 2018

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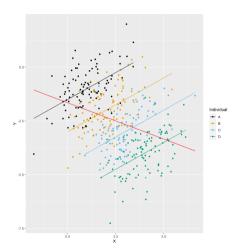
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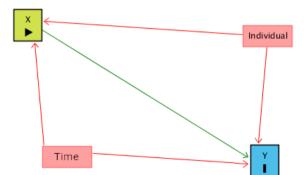


### FE Estimator

$$Y_i = \alpha_i + \beta X_{it} + \varepsilon_{it}$$
 (6)

with  $\alpha_i$  = individual, time-invariant effect, and  $X_i$  = a variable of interest. The so called *within* transformation accounts for  $\alpha_i$  through demeaning such that we can consistently estimate  $\partial Y/\partial X$ 

## Two way fixed-effects



Accounting for individual and time (two-way) fixed effects. Image source: Huntington-Klein 2018

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# **Estimator**

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The two-way fixed effects model can be formulated as

$$Y_{it} = \alpha_i + \theta_t + T_{it} + X_{it} + \epsilon_i \tag{7}$$

where  $\alpha$  individual and  $\theta$  time fixed effects, T a binary treatment indicator ( $T = D \times P$ ), possibly a controls vector  $X_i$ , and error term  $\epsilon_i$ , assumed to be normally distributed and centered around 0, independent of everything else.

## time-trends

### This allows to take both individual differences and shocks in time into account

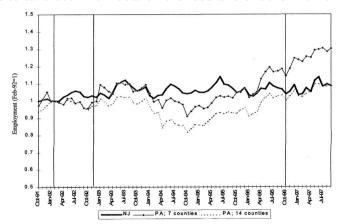


FIGURE 2. EMPLOYMENT IN NEW JERSEY AND PENNSYLVANIA FAST-FOOD RESTAURANTS, OCTOBER 1991 TO SEPTEMBER 1997

Note: Vertical lines indicate dates of original Card-Krueger survey and the October 1996 federal minimum-wage increase.

Source: Authors: calculations based on BLS ES-202 data.

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A two-way fixed effects approach allows us to

- control for time-constant, unobserved heterogeneity between individuals
- control for common time shocks, that affect all individuals
- a multi-period 2WFE approach resembles DiD when
  - treatment is simultaneous
  - effects are homogeneous

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Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

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Over the last 6 or so years, DiD methdology has seen quite some development.

I will briefly introduce

staggered treatment / event-time studies

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Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

- staggered treatment / event-time studies
- non-parallel trend corrections

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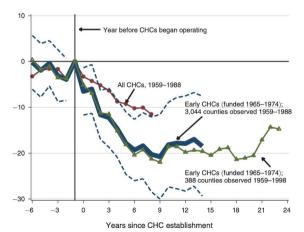


Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

- staggered treatment / event-time studies
- non-parallel trend corrections
- heterogeneous treatment corrections

# What if treatment happened at different times?



Reduction in mortality by Community Health Centers (CHC), Image source: Bailey and Goodman-Bacon 2015

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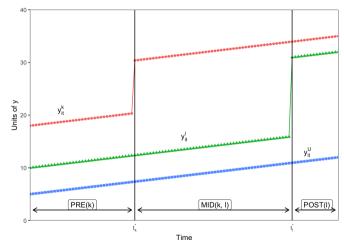
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# We may run into time series length related weighting problems





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DiD with variations in treatment timing. Image source: Goodman-Bacon 2018, as reproduced by <u>A.C. Baker</u>
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Recall,

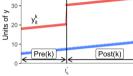
$$ATT = E[Y_t - Y_{t-1}|D = 1] - E[Y_t - Y_{t-1}|D = 0]$$

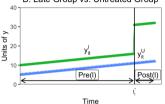
which is a comparison of mean differences between groups over time. Straightforward for 2 periods.

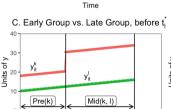
Now, we have multiple periods.

# Picture a case with multiple periods, three groups, and thus four comparisons

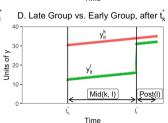








Time







DiD with variations in treatment timing. Image source: Goodman-Bacon 2018, as reproduced by A.C. Baker

# notation

# Turns out the 2WFE DiD estimator is a weighted average of all these comparisons

# Theorem 1. Difference-in-Differences Decomposition Theorem

Assume that the data contain k=1,...,K groups of units ordered by the time when they receive a binary treatment,  $\mathbf{t}_k \in (1,T]$ . There may be one group,  $\mathbf{U}$ , that never receives treatment. The OLS estimate,  $\hat{\boldsymbol{\beta}}^D$ , in a two-way fixed-effects model (2) is a weighted average of all possible two-by-by DD estimators.

$$\widehat{\beta}^{DD} = \sum_{k \neq U} s_{kU} \widehat{\beta}_{kU}^{2x2} + \sum_{k \neq U} \sum_{\ell > k} s_{k\ell} \left[ \mu_{k\ell} \widehat{\beta}_{k\ell}^{2x2,k} + (1 - \mu_{k\ell}) \widehat{\beta}_{k\ell}^{2x2,\ell} \right]$$
(7)

Where the two-by-two DD estimators are:

$$\begin{split} \widehat{\boldsymbol{\beta}}_{kU}^{22,2} &= \left(\overline{\boldsymbol{y}}_{k}^{POST(k)} - \overline{\boldsymbol{y}}_{k}^{PRE(k)}\right) - \left(\overline{\boldsymbol{y}}_{U}^{POST(j)} - \overline{\boldsymbol{y}}_{U}^{PRE(j)}\right) \\ \widehat{\boldsymbol{\beta}}_{k\ell}^{22,2k} &= \left(\overline{\boldsymbol{y}}_{k}^{MID(k,\ell)} - \overline{\boldsymbol{y}}_{k}^{PRE(k)}\right) - \left(\overline{\boldsymbol{y}}_{\ell}^{MID(k,\ell)} - \overline{\boldsymbol{y}}_{\ell}^{PRE(k)}\right) \\ \widehat{\boldsymbol{\beta}}_{k\ell}^{22,2k} &= \left(\overline{\boldsymbol{y}}_{\ell}^{POST(\ell)} - \overline{\boldsymbol{y}}_{\ell}^{MID(k,\ell)}\right) - \left(\overline{\boldsymbol{y}}_{k}^{POST(\ell)} - \overline{\boldsymbol{y}}_{\ell}^{MID(k,\ell)}\right) \end{split}$$

the weights are:

$$s_{kU} = \frac{n_k n_U \overline{b}_k (1 - \overline{b}_k)}{v \overline{w}_i C(\overline{b}_i)}$$

$$s_{k\ell} = \frac{n_k n_\ell (\overline{b}_k - \overline{b}_\ell) (1 - (\overline{b}_k - \overline{b}_\ell))}{v \overline{w}_i C(\overline{b}_i)}$$

$$v \overline{w}_i C(\overline{b}_i)$$

$$\mu_{k\ell} = \frac{1 - \overline{b}_k}{1 - (\overline{b}_k - \overline{b}_\ell)}$$
and  $\sum_{k \in U} S_{kU} + \sum_{k \in V} S_{kV} S_{k\ell} = 1$ .

Proof: See appendix A.

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Bacon decomposition theorem. Image source: Goodman-Bacon 2018, see also his tweet-thread

# notation

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DAGs estimation

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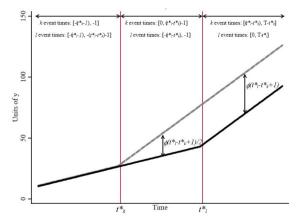
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Even worse, a positive but staggered slope change, can even change the sign of the DD estimate



Staggered treatment with linear slope change. Image source: Goodman-Bacon 2018, see also his tweet-thread

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# Several works on the issue:

- Athey and Imbens 2020
  - under random adoption dates, the DID is unbiased
  - comparing treated with not-yet treated

Causal Inference 2021 ClimBEco course 28/33

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- Athey and Imbens 2020
  - under random adoption dates, the DID is unbiased
  - comparing treated with not-yet treated
- Goodman-Bacon 2018
  - a time-in-treatment weighted DiD

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- Athey and Imbens 2020
  - under random adoption dates, the DID is unbiased
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- Goodman-Bacon 2018
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- Callaway and Sant'Anna 2020
  - semiparametric, bootstrapped inference with pre-intervention conditioning on co-variates
  - R package did

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- Callaway and Sant'Anna 2020
  - semiparametric, bootstrapped inference with pre-intervention conditioning on co-variates
  - R package did
- Sun and Abraham 2020
  - a time-to-treatment (cohort) weighted approach
  - implemented in fixest R package

# Heterogeneous Treatment

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# Further works on DiD design / application issues:

- Chaisemartin and D'Haultfœuille 2020
  - allowing for treatment effects "heterogeneous across groups and over time periods"
  - R package <u>DIDmultiplegt</u>
- Imai and Kim 2020
  - identify some proplematic negative weigthing in 2WFE
  - they propose weighting or matching <u>Imai 2020</u>

# Non-parallel trends

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However, all these approaches, assume (to some extent) parallel trends

- Roth
  - test for parallel-trends, R package pretends
  - robust inference strategy under non-parralel trends Rambachan and Roth 2020, R package <u>HonestDiD</u>

# Summary

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Re: DiD and (adjusted) 2WFE estimators

- compare treated individual (units) with a reference group
- who we compare to whom deserves special attention
- constantly being developed further

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