

Differences-in-Differences & two-way fixed effects

Nils Droste

2021 ClimBEco course



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Synopsis: Today, we will be looking into *the* classical research design for inferring causal effects from observational data (i.e. when experiments are unethical or infeasible), and its recent developments

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Synopsis: Today, we will be looking into *the* classical research design for inferring causal effects from observational data (i.e. when experiments are unethical or infeasible), and its recent developments

In particular, we will develop an understanding of

quasi / natural experiments

Introduction



Synopsis: Today, we will be looking into the classical research design for inferring causal effects from observational data (i.e. when experiments are unethical or infeasible), and its recent developments

- quasi / natural experiments
 - Difference-in-Differences

Introduction



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- quasi / natural experiments
 - Difference-in-Differences
 - (two-way) fixed-effects regressions

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- quasi / natural experiments
 - Difference-in-Differences
 - (two-way) fixed-effects regressions
 - staggered treatment

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Quasi- / natural experiment:

A setting where a subpopulation is treated with an intervention of sorts that occurs due to non-random assignment processes (outside of the researchers influence if its called *natural*).

Recall potential outcome approximation

Diff-in-Diff



We may choose to infer an average treatment effect (ATE) I: i.e. $I = \{A, B...\}$ by comparing the average outcomes of treated individuals a from A with the one of untreated individuals $b \in B$.

$$E\{\Delta Y_i\} \approx E\{Y_a(1)\} - E\{Y_b(0)\} \tag{1}$$

For such a case we can exploit *random chance* within sufficiently large samples to make these groups comparable.

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For such a case we can exploit *random chance* within sufficiently large samples to make these groups comparable.

But what if we do not have a random assignment (and there may be a selection-bias and / or substantial differences between groups)?

a famous case

By comparing a treated with an untreated group over 2+ periods, we can control for (time-constant) differences between groups.

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a famous case

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By comparing a treated with an untreated group over 2+ periods, we can control for (time-constant) differences between groups.

A classic example is the Card and Krueger (AER, 1994), comparing fast-food worker employment in Pennsylvania (PA) and New Jersey (NJ) before and after a minimum wage raise in NJ in 1992.

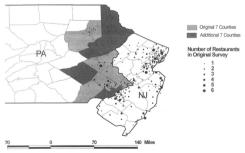


FIGURE 1. AREAS OF NEW JERSEY AND PENNSYLVANIA COVERED BY ORIGINAL SURVEY AND BLS DATA

Image source: Card and Krueger 2000

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Here is a (tweaked) version of Card and Krueger 1994, Figure 1.

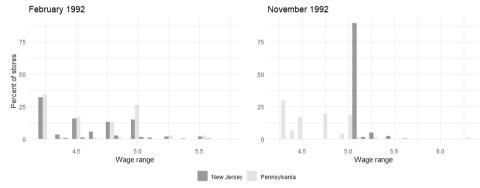


Image source: Card and Krueger 1994

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Here, we are interested in the average treatment effect on the treated (ATT)

$$ATT = E[Y_i(1) - Y_i(0)|D = 1]$$
 (2)

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For this to be a consistent estimator, we will need a set of conditions to hold, some of which we can test, others we will need to assume.

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In particular, the parallel-trends assumption:

$$E[Y_{it}(0) - Y_{it-1}(0)|D = 1] = E[Y_{it}(0) - Y_{it-1}(0)|D = 0]$$
(3)

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In particular, the parallel-trends assumption:

$$E[Y_{it}(0) - Y_{it-1}(0)|D = 1] = E[Y_{it}(0) - Y_{it-1}(0)|D = 0]$$
(3)

because then, we can assume

$$ATT = E[Y_t - Y_{t-1}|D=1] - E[Y_t - Y_{t-1}|D=0]$$
 (4)

Directed acyclic graphs

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Difference-in-Differences (DID)

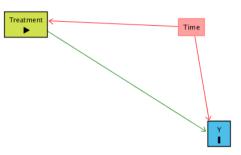


Image source: Huntington-Klein 2018

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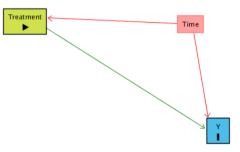
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Difference-in-Differences (DID)



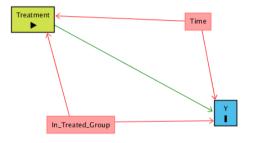


Image source: Huntington-Klein 2018

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Difference-in-Differences (DID)

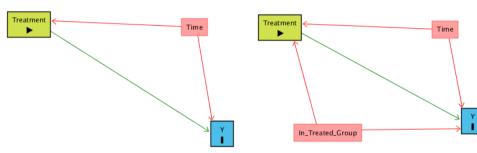


Image source: Huntington-Klein 2018

 \rightarrow Accounting for differences between groups over time enables not just the estimation of time and group effects but also the differences-in-differences (i.e. the interaction of time and group effects).

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DID Estimator

assume n individual units i, and t = 2 time periods, we can estimate the effect of a treatment ocurring at $P_{t=1}$, affecting the treated subpopulation $D_i = 1$

$$Y_{i} = \beta_{0} + \beta_{1}D_{i} + \beta_{2}P_{t} + \beta_{3}D_{i} \times P_{t} + \varepsilon_{i}$$
 (5)

with D_i = Treatment, P_t = Period Dummy.

 β_3 gives us an estimate of the diff-in-diff treatment effect.

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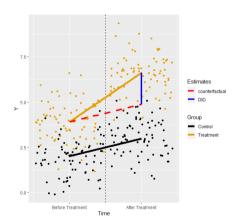
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DID Estimator

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 β_3 gives us an estimate of the diff-in-diff treatment effect.

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To estimate an example ATT, we can use the Card and Krueger (1994) data

> summary(did_model)

Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) 23.331 1.072 21.767 <2e-16 *** -2.1661.516 -1.429 0.1535 time 1.194 -2.423 0.0156 * treated -2.892 2.754 1.688 1.631 0.1033 time:treated

Note: heteroskedasticity and autocorrelation robust standard errors should be computed

intermediate summary

estimation



A difference-in-differences approach allows us to

- compare a treatment group with an untreated quasi-counterfactual
- even under conditions of a non-random assignment
- assuming that the groups behave comparably enough

Panel Data

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Let us suppose a situation with repeated measurements for multiple individual(s) (units), i.e. cross-sectional time-series, or panel data.

An example panel data structure

| individual | time | Υ | X | D |
|------------|------|-----|-----|---|
| Α | 1 | 0.8 | 0.3 | 0 |
| Α | 2 | 0.7 | 0.2 | 0 |
| Α | 3 | 0.5 | 0.2 | 1 |
| В | 1 | 1.2 | 0.4 | 0 |
| В | 2 | 1.1 | 0.5 | 0 |
| В | 3 | 0.9 | 0.6 | 1 |
| | | | | |

An exemplary study



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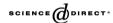
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ECOLOGICAL ECONOMICS

Ecological Economics 55 (2005) 527-538

www.elsevier.com/locate/ecolecon

ANALYSIS

Environmental pressure group strength and air pollution: An empirical analysis

Seth Binder, Eric Neumayer*

Department of Geography and Environment and Center for Environmental Policy and Governance (CEPG), London School of Economics and Political Science, Houghton Street, London WC2A 2AE, UK

Received 7 December 2003; received in revised form 22 October 2004; accepted 14 December 2004 Available online 24 February 2005

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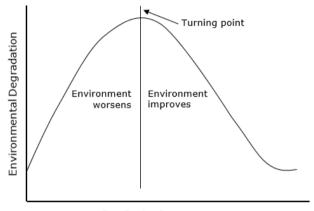
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An exemplary study



Per Capita Income

Theoretical underpinning for Binder and Neumayer 2005: Environmental Kuznets Curve. Image source: Wikipedia

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Replicated results from table 1, model 1 Binder and Neumayer 2005

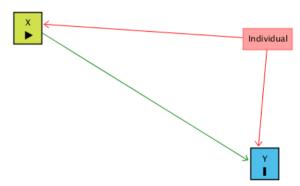
Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) | |
|-------------|-----------|------------|---------|----------|-----|
| (Intercept) | -57.55012 | 16.60671 | -3.465 | 0.000548 | *** |
| lnengopc | -0.51121 | 0.11878 | -4.304 | 1.82e-05 | *** |
| lnenergy | 1.00887 | 0.60455 | 1.669 | 0.095425 | |
| lngdp | 13.81819 | 4.17975 | 3.306 | 0.000975 | *** |
| lngdpsq | -0.88657 | 0.27384 | -3.238 | 0.001239 | ** |
| polity | -0.05079 | 0.03023 | -1.680 | 0.093135 | |

Note: This is not a fixed effects regression but an OLS

Panel Data

One way fixed-Effects (FE) structure



Accounting for individual fixed effects. Image source: Huntington-Klein 2018

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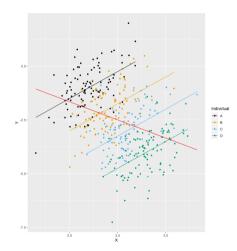
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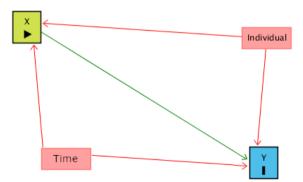


FE Estimator

$$Y_i = \alpha_i + \beta X_{it} + \varepsilon_{it}$$
 (6)

with α_i = individual, time-invariant effect, and X_i = a variable of interest. The so called *within* transformation accounts for α_i through demeaning such that we can consistently estimate $\partial Y/\partial X$

Two way fixed-effects



Accounting for individual and time (two-way) fixed effects. Image source: Huntington-Klein 2018

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The two-way fixed effects model can be formulated as

$$Y_{it} = \alpha_i + \theta_t + T_{it} + X_{it} + \epsilon_i \tag{7}$$

where α individual and θ time fixed effects, T a binary treatment indicator ($T = D \times P$),

possibly a controls vector X_i ,

and error term ϵ_i , assumed to be normally distributed and centered around 0, independent of everything else.

time-trends

This allows to take both individual differences and shocks in time into account

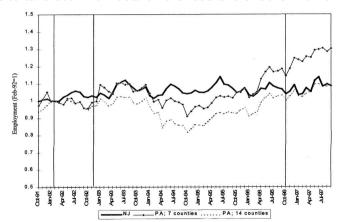


FIGURE 2. EMPLOYMENT IN NEW JERSEY AND PENNSYLVANIA FAST-FOOD RESTAURANTS, OCTOBER 1991 TO SEPTEMBER 1997

Note: Vertical lines indicate dates of original Card-Krueger survey and the October 1996 federal minimum-wage increase.

Source: Authors: calculations based on BLS ES-202 data.

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A two-way fixed effects approach allows us to

- control for time-constant, unobserved heterogeneity between individuals
- control for common time shocks, that affect all individuals
- a multi-period 2WFE approach resembles DiD when
 - treatment is simultaneous
 - effects are homogeneous

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Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

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Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

staggered treatment / event-time studies

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Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

- staggered treatment / event-time studies
- non-parallel trend corrections

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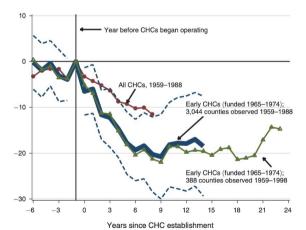


Over the last 6 or so years, DiD methology has seen quite some development.

I will briefly introduce

- staggered treatment / event-time studies
- non-parallel trend corrections
- heterogeneous treatment corrections

What if treatment happened at different times?



Reduction in mortality by Community Health Centers (CHC). Image source: Bailey and Goodman-Bacon 2015

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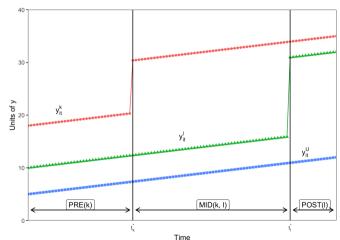
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We may run into time series length related weighting problems



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DiD with variations in treatment timing. Image source: Goodman-Bacon 2018, as reproduced by <u>A.C. Baker</u>
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Recall,

$$ATT = E[Y_t - Y_{t-1}|D = 1] - E[Y_t - Y_{t-1}|D = 0]$$

which is a comparison of mean differences between groups over time. Straightforward for 2 periods.

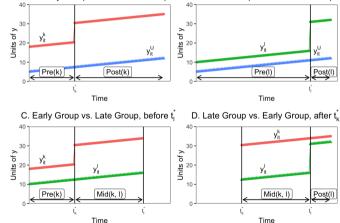
Now, we have multiple periods.

Picture a case with multiple periods, three groups, and thus four comparisons









DiD with variations in treatment timing. Image source: Goodman-Bacon 2018, as reproduced by A.C. Baker

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notation

Turns out: 2WFE DiD estimator is a weighted average of these comparisons

Theorem 1. Difference-in-Differences Decomposition Theorem

Assume that the data contain k = 1, ..., K groups of units ordered by the time when they receive a binary treatment, $t_i^* \in (1,T]$. There may be one group, U, that never receives treatment. The OLS estimate. \widehat{B}^{DD} in a two-way fixed-effects model (2) is a weighted average of all possible twoby-two DD estimators

$$\widehat{\beta}^{DD} = \sum_{k \neq U} s_{kU} \widehat{\beta}_{kU}^{2x2} + \sum_{k \neq U} \sum_{\ell \geq k} s_{k\ell} \left[\mu_{k\ell} \widehat{\beta}_{k\ell}^{2x2,k} + (1 - \mu_{k\ell}) \widehat{\beta}_{k\ell}^{2x2,\ell} \right]$$
(7)

Where the two-by-two DD estimators are:

$$\begin{split} \widehat{\boldsymbol{\beta}}_{kU}^{2X2,E} &= \left(\overline{\boldsymbol{y}}_{k}^{POST(\ell)} - \overline{\boldsymbol{y}}_{k}^{PRE(k)} \right) - \left(\overline{\boldsymbol{y}}_{u}^{POST(f)} - \overline{\boldsymbol{y}}_{u}^{PRE(f)} \right) \\ \widehat{\boldsymbol{\beta}}_{k\ell}^{2X2,E} &= \left(\overline{\boldsymbol{y}}_{k}^{MD(k,\ell)} - \overline{\boldsymbol{y}}_{k}^{PRE(k)} \right) - \left(\overline{\boldsymbol{y}}_{\ell}^{MD(k,\ell)} - \overline{\boldsymbol{y}}_{\ell}^{PRE(k)} \right) \\ \widehat{\boldsymbol{\beta}}_{k\ell}^{2X2,E} &= \left(\overline{\boldsymbol{y}}_{\ell}^{POST(\ell)} - \overline{\boldsymbol{y}}_{k}^{MD(k,\ell)} - \left(\overline{\boldsymbol{y}}_{k}^{POST(\ell)} - \overline{\boldsymbol{y}}_{k}^{MD(k,\ell)} \right) \right) \\ \widehat{\boldsymbol{\beta}}_{k\ell}^{2X2,E} &= \left(\overline{\boldsymbol{y}}_{\ell}^{POST(\ell)} - \overline{\boldsymbol{y}}_{k}^{MD(k,\ell)} - \overline{\boldsymbol{y}}_{\ell}^{POST(\ell)} - \overline{\boldsymbol{y}}_{k}^{MD(k,\ell)} \right) \end{split}$$

the weights are:

$$s_{RV} = \frac{n_{k}n_{U}\overline{D}_{k}(1-\overline{D}_{k})}{v\overline{ar}\cdot(\overline{D}_{t})}$$

$$s_{k\ell} = \frac{n_{k}n_{\ell}(\overline{D}_{k}-\overline{D}_{\ell})(1-(\overline{D}_{k}-\overline{D}_{\ell}))}{v\overline{ar}\cdot(\overline{D}_{t})}$$

$$\mu_{k\ell} = \frac{1-\overline{D}_{k}}{1-(\overline{D}_{k}-\overline{D}_{\ell})}$$
and $\sum_{k\in I} S_{kU} + \sum_{k\in I} S_{kU} = 1$

Proof: See appendix A.

Bacon decomposition theorem. Image source: Goodman-Bacon 2018, see also his tweet-thread

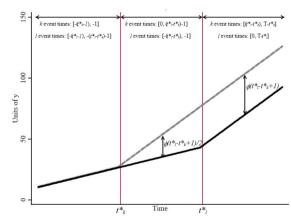
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Even worse, a positive but staggered slope change, can even change the sign of the DD estimate



Staggered treatment with linear slope change. Image source: Goodman-Bacon 2018, see also his tweet-thread

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Several works on the issue:

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Several works on the issue:

- Athey and Imbens 2020
 - under random adoption dates, the DID is unbiased
 - comparing treated with not-yet treated

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Reference



Several works on the issue:

- Athey and Imbens 2020
 - under random adoption dates, the DID is unbiased
 - comparing treated with not-yet treated
- Goodman-Bacon 2018
 - a time-in-treatment weighted DiD, fixing the weights to gain balance
 - R package bacondecomp

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Several works on the issue:

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Several works on the issue:

- Callaway and Sant'Anna 2020
 - bootstrapped inference with pre-intervention conditioning on co-variates
 - R package did

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Several works on the issue:

- Callaway and Sant'Anna 2020
 - bootstrapped inference with pre-intervention conditioning on co-variates
 - R package <u>did</u>
- Sun and Abraham 2020
 - time-to-treatment (cohort) weighted approach, comparing to never-treated
 - implemented in <u>fixest</u> R package

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Further works on DiD design / application issues:

- Chaisemartin and D'Haultfœuille 2020
 - allowing for treatment effects "heterogeneous across groups and over time periods"
 - R package <u>DIDmultiplegt</u>
 - Imai and Kim 2020
 - identify some proplematic negative weigthing in 2WFE
 - they propose weighting or matching <a href="Imailto:Imailto

Non-parallel trends



However, all these approaches, assume (to some extent) parallel trends

- Jonathan Roth 2021
 - test for parallel-trends, R package pretends
 - robust inference strategy under non-parralel trends Rambachan and Roth 2020. R package HonestDiD

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Re: DiD and (adjusted) 2WFE estimators

- compare treated individual (units) with a reference group
- who we compare to whom deserves special attention
- software solutions available

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