#### Aufgabe 1:

(a)

$$Y = [(A \wedge \overline{B}) \vee (\overline{C} \wedge D) \vee \overline{E} \vee F] \wedge G$$
$$\overline{Y} = [(\overline{A} \vee B) \wedge (C \vee \overline{D}) \wedge E \wedge \overline{F}] \vee \overline{G}$$

**(b)** 

0000000: 
$$Y = [(0 \land \overline{0}) \lor (\overline{0} \land 0) \lor \overline{0} \lor 0] \land 0$$
  
 $= [(0 \land 1) \lor (1 \land 0) \lor 1 \lor 0] \land 0$   
 $= [(0) \lor (0) \lor 1 \lor 0] \land 0$   
 $= [1] \land 0$   
 $= 0$   
 $\overline{Y} = [(\overline{0} \lor 0) \land (0 \lor \overline{0}) \land 0 \land \overline{0}] \lor \overline{0}$   
 $= [(1 \lor 0) \land (0 \lor 1) \land 0 \land 1] \lor 1$   
 $= [(1) \land (1) \land 0 \land 1] \lor 1$   
 $= [0] \lor 1$   
 $= 1$ 

1010101: 
$$Y = [(1 \wedge \overline{0}) \vee (\overline{1} \wedge 0) \vee \overline{1} \vee 0] \wedge 1$$
  
 $= [(1 \wedge 1) \vee (0 \wedge 0) \vee 0 \vee 0] \wedge 1$   
 $= [(1) \vee (0) \vee 0 \vee 0] \wedge 1$   
 $= [1] \wedge 1$   
 $= 1$   
 $\overline{Y} = [(\overline{1} \vee 0) \wedge (1 \vee \overline{0}) \wedge 1 \wedge \overline{0}] \vee \overline{1}$   
 $= [(0 \vee 0) \wedge (1 \vee 1) \wedge 1 \wedge 1] \vee 0$   
 $= [(0) \wedge (1) \wedge 1 \wedge 1] \vee 0$   
 $= [0] \vee 0$   
 $= 0$ 

1111111: 
$$Y = [(1 \land \overline{1}) \lor (\overline{1} \land 1) \lor \overline{1} \lor 1] \land 1$$
  
 $= [(1 \land 0) \lor (0 \land 1) \lor 0 \lor 1] \land 1$   
 $= [(0) \lor (0) \lor 0 \lor 1] \land 1$   
 $= [1] \land 1$   
 $= 1$   
 $\overline{Y} = [(\overline{1} \lor 1) \land (1 \lor \overline{1}) \land 1 \land \overline{1}] \lor \overline{1}$   
 $= [(0 \lor 1) \land (1 \lor 0) \land 1 \land 0] \lor 0$   
 $= [(1) \land (1) \land 1 \land 0] \lor 0$   
 $= [0] \lor 0$   
 $= 0$ 

0101010: 
$$Y = [(0 \land \overline{1}) \lor (\overline{0} \land 1) \lor \overline{0} \lor 1] \land 0$$
  
 $= [(0 \land 0) \lor (1 \land 1) \lor 1 \lor 1] \land 0$   
 $= [(0) \lor (1) \lor 1 \lor 1] \land 0$   
 $= [1] \land 0$   
 $= 0$   
 $\overline{Y} = [(\overline{0} \lor 1) \land (0 \lor \overline{1}) \land 0 \land \overline{1}] \lor \overline{0}$   
 $= [(1 \lor 1) \land (0 \lor 0) \land 0 \land 0] \lor 1$   
 $= [(1) \land (0) \land 0 \land 0] \lor 1$   
 $= [0] \lor 1$   
 $= 1$ 

### Aufgabe 2:

$$Y = (\overline{A} \wedge (\overline{B} \vee \overline{C})) \vee (D \wedge \overline{E} \wedge F)$$

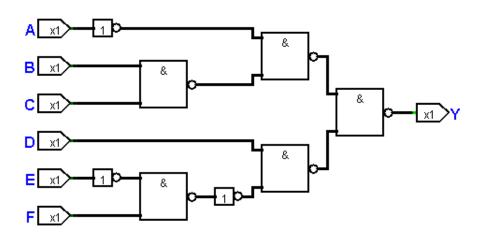
(a)

$$\begin{split} Y &= (\overline{A} \wedge (\overline{B} \vee \overline{C})) \vee (D \wedge \overline{E} \wedge F) \\ &= (\overline{A} \wedge \overline{(B \wedge C)}) \vee \overline{(D \wedge \overline{E} \wedge F)} \\ &= \overline{(\overline{A} \wedge \overline{(B \wedge C)})} \vee \overline{(D \wedge \overline{E} \wedge F)} \\ &= \overline{(\overline{A} \wedge \overline{(B \wedge C)})} \wedge \overline{(D \wedge \overline{E} \wedge F)} \\ &= \overline{\overline{A} \wedge \overline{B \wedge C}} \wedge \overline{D \wedge \overline{E} \wedge F} \end{split}$$

**(b)** 

$$Y = \overline{\overline{A} \wedge \overline{B} \wedge \overline{C}} \wedge \overline{D \wedge \overline{E} \wedge F}$$
$$= \overline{(\overline{A}) \wedge (\overline{B} \wedge \overline{C})} \wedge (\overline{D} \wedge (\overline{\overline{E} \wedge F}))$$

(c)

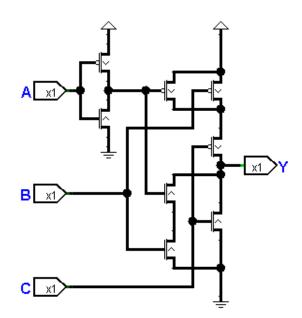


# Aufgabe 3:

$$Y = (A \vee \overline{B}) \wedge \overline{C}$$
$$h(A,B,C) = (A \vee \overline{B}) \wedge \overline{C}$$
$$= (\overline{A} \vee \overline{B}) \wedge \overline{C}$$

$$g(A,B,C) = \overline{h(A,B,C)}$$
$$= (\overline{A} \land B) \lor C$$

nach Shannonsches Gesetz:



# Aufgabe 4:

$$F = (F1 \lor F2 \lor F3) \land F4$$

$$F1 = \overline{A} \land B$$

$$F2 = A \land B$$

$$F3 = A \land \overline{B} \land \overline{C}$$

$$F4 = \overline{A} \lor C \lor A$$

$$F1 \lor F2 = (\overline{A} \land B) \lor (A \land B)$$

$$= B$$

$$F4 = \overline{A} \lor C \lor A$$

$$= 1$$

$$\Rightarrow F = (F1 \lor F2 \lor F3) \land F4$$

$$= B \lor F3$$

	A	B	C	$\overline{B}$	$\overline{C}$	$F3 = A \wedge \overline{B} \wedge \overline{C}$	$F = B \lor F3$
•	0	0	0	1	1	0	0
	0	0	1	1	0	0	0
	0	1	0	0	1	0	1
	0	1	1	0	0	0	1
	1	0	0	1	1	1	1
	1	0	1	1	0	0	0
	1	1	0	0	1	0	1
	1	1	1	0	0	0	1

#### **Aufgabe 5:**

A	В	С	Y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

(a)

folgende Minterme sind hier relevant:

$$m_1 = \overline{A} \wedge \overline{B} \wedge C$$

$$m_2 = \overline{A} \wedge B \wedge \overline{C}$$

$$m_7 = A \wedge B \wedge C$$

**(b)** 

Die DNF ist dann die Disjunktion der Minterme:

$$Y = m_1 \vee m_2 \vee m_7$$
  
=  $(\overline{A} \wedge \overline{B} \wedge C) \vee (\overline{A} \wedge B \wedge \overline{C}) \vee (A \wedge B \wedge C)$ 

(c)

folgende Maxterme sind hier relevant:

$$M_0 = \overline{A} \wedge \overline{B} \wedge \overline{C}$$

$$M_3 = \overline{A} \wedge B \wedge C$$

$$M_4 = A \wedge \overline{B} \wedge \overline{C}$$

$$M_5 = A \wedge \overline{B} \wedge C$$

$$M_6 = A \wedge B \wedge \overline{C}$$

Die KNF ist dann die Konjunktion der Maxterme:

$$Y = M_0 \wedge M_3 \wedge M_4 \wedge M_5 \wedge M_6$$
  
=  $(\overline{A} \wedge \overline{B} \wedge \overline{C}) \wedge (\overline{A} \wedge B \wedge C) \wedge (A \wedge \overline{B} \wedge \overline{C}) \wedge (A \wedge \overline{B} \wedge C) \wedge (A \wedge B \wedge \overline{C})$ 

**(d)** 

A	B	C	Y	$m_1$	$m_2$	$m_7$
0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	0	1	0	1	0
0	1	1	0	0	0	0
1	0	0	0	0	0	0
1	0	1	0	0	0	0
1	1	0	0	0	0	0
1	1	1	1	0	0	1

**(e)** 

A	B	C	Y	$M_0$	$M_3$	$M_4$	$M_5$	$M_6$
0	0	0	0	0	1	1	1	1
0	0	1	1	1	1	1	1	1
0	1	0	1	1	1	1	1	1
0	1	1	0	1	0	1	1	1
1	0	0	0	1	1	0	1	1
1	0	1	0	1	1	1	0	1
1	1	0	0	1	1	1	1	0
1	1	1	1	1	1	1	1	1