




# Business Intelligence

## 09 Predictive Modeling I

Prof. Dr. Bastian Amberg  
(summer term 2024)  
7.6.2024

# Schedule

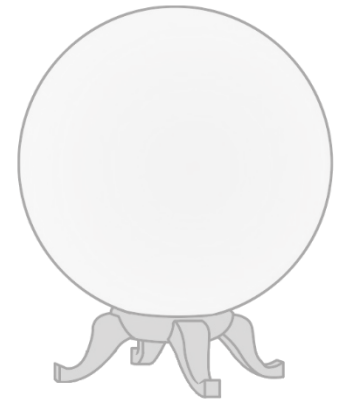
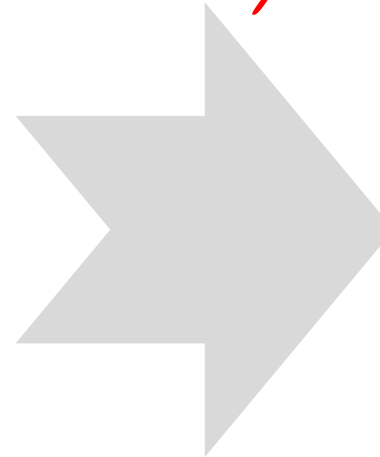
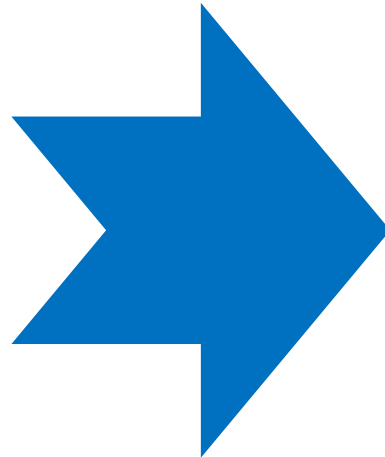
		Wed., 10:00-12:00		Fr., 14:00-16:00 (Start at 14:30)		Self-study
Basics	W1	17.4.	(Meta-)Introduction	19.4.		Python-Basics Chap. 1
	W2	24.4.	Data Warehouse – Overview & OLAP	26.4.	[Blockveranstaltung SE Prof. Gersch]	Chap. 2
	W3	1.5.		3.5.		Chap. 3
	W4	8.5.	Data Warehouse Modeling I & II	10.5.	Data Mining Introduction	
Main Part	W5	15.5.	CRISP-DM, Project understanding	17.5.	Python-Basics-Online Exercise	Python-Analytics Chap. 1
	W6	22.5.	Data Understanding, Data Visualization I	24.5.	No lectures, but bonus tasks 1.) Co-Create your exam 2.) Earn bonus points for the exam	Chap. 2
	W7	29.5.	Data Visualization II	31.5.		
	W8	5.6.	Data Preparation	7.6.	Predictive Modeling I (10:00 -12:00)	BI-Project Start
	W9	12.6.	Predictive Modeling II, Fitting a Model I	14.6.	Python-Analytics-Online Exercise	
	W10	19.6.	Guest Lecture Dr. Ionescu	21.6.	Fitting a Model II	
	W11	26.6.	How to avoid overfitting	28.6.	What is a good Model?	
Deepening	W12	3.7.	Project status update Evidence and Probabilities	5.7.	Similarity (and Clusters) From Machine to Deep Learning I	
	W13	10.7.		12.7.	From Machine to Deep Learning II	
	W14	17.7.	Project presentation	19.7.	Project presentation	End
Ref.					Klausur 1. Termin, 31.7. '24 Klausur 2. Termin, 2.10. '24	Projektbericht

# Agenda

→ MCD ✓  
→ MAD ✓  
Nonignorable ✓

Data Preparation

Predictive Modeling I



- ✓ Data selection
- ✓ Data cleansing
- **Data transformation**
- ✓ Data integration

Introductory example  
Attribute Selection,  
Decision Trees

# Data transformation

## Categorical -> Numerical attributes

Some models can only handle numerical attributes, other models only categorical attributes.

In such cases, categorical attributes must be transformed into numerical ones or vice versa.

"Winfo"  $\rightarrow 1$   
 $\rightarrow 0$

## Categorical attribute -> Numerical attribute:

A binary attribute can be turned into a numerical attribute with the values 0 and 1 (aka dummy variable)

A categorical attribute with more than two values, say  $a_1, \dots, a_k$ , should not be turned into a single numerical attribute with the values  $1, \dots, k$ , unless the attribute is an ordinal attribute. It should be turned into  $k$  attributes  $A_1, \dots, A_k$  with values 0 and 1 (dummies).  $a_1$  is represented by  $A_i = 1$  and  $A_j = 0$  for  $i \neq j$ .

Handwritten notes and table illustrating categorical attribute transformation:

Left side (crossed out):

"Winfo"	1
"Facts"	2
"MRM"	3

Right side (correct transformation):

Winfo (ja/nein)	Facts	MRM
0 oder 1	0 oder 1	0 oder 1

# Data transformation

Discretization: Numerical -> Categorical attributes

Discretization techniques refer to splitting a numerical range into a number of finite bins.

Equi-width discretization. Splits the range into intervals (bins) of the *same width*.

Equi-frequency discretization. Splits the range into intervals such that each interval (bin) contains (roughly) the *same number of records*.

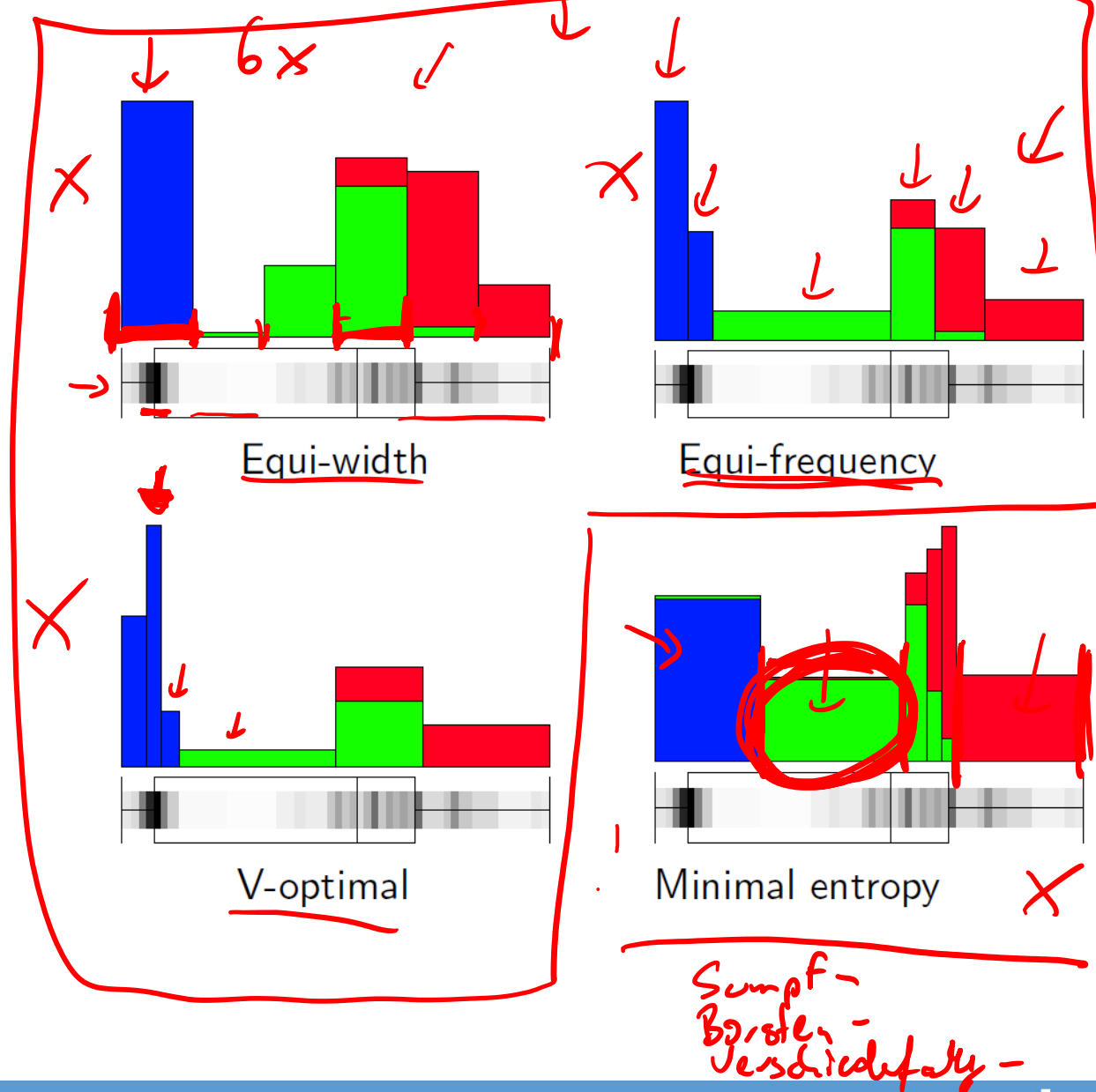
V-optimal discretization. Minimizes  $\sum_i n_i V_i$  where  $n_i$  is the *number of data objects* in the  $i$ th interval and  $V_i$  is the *sample variance* of the data in this interval.

Minimal entropy discretization. Minimizes the *entropy*. (Only applicable in the case of classification problems, we'll dive deeper into this with decision trees)

Ref.

Größe

Sumf  
Kellstlänge

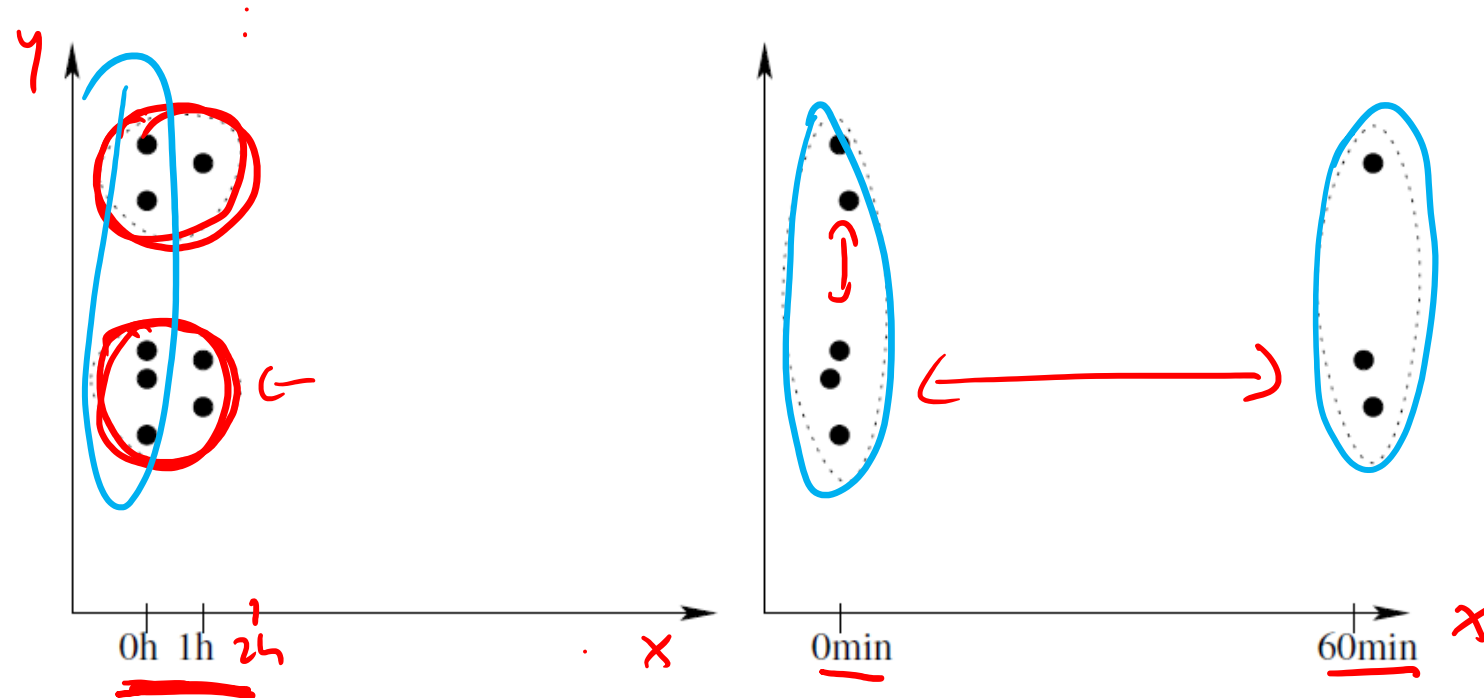


# Normalization | Standardization (1/2)

[0...1]

For some data analysis techniques (PCA, MDS, cluster analysis) the influence of an attribute depends on the scale or measurement unit.

To guarantee impartiality, some kind of standardization or normalization should be applied.



## Min-max normalization:

For a numerical attribute  $X$  with  $\min_x$  and  $\max_x$  being the minimum and maximum value in the sample, the min-max normalization is defined as

$$n: \text{dom}X \rightarrow [0,1], \quad x \rightarrow \frac{x - \min_x}{\max_x - \min_x}$$

## Z-score standardization:

For a numerical attribute  $X$  with sample mean  $\hat{\mu}_X$  and empirical standard deviation  $\hat{\sigma}_X$ , the z-score standardization is defined as

$$s: \text{dom}X \rightarrow \mathbb{R}, \quad x \rightarrow \frac{x - \hat{\mu}_X}{\hat{\sigma}_X}$$



## Robust z-score standardization:

The sample mean and empirical standard deviation are easily affected by outliers. A more robust alternative is (see also boxplots):

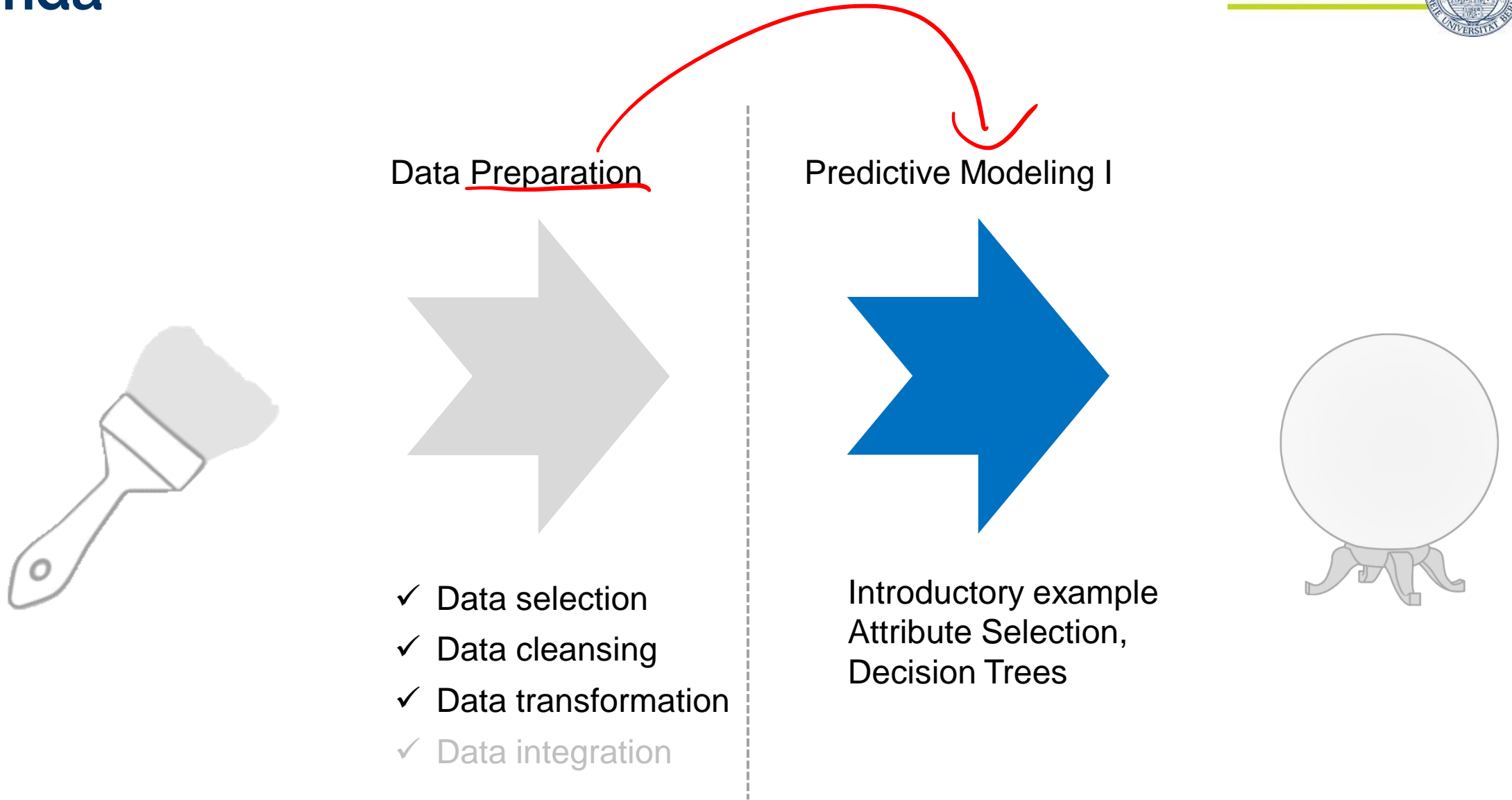
$$s: \text{dom}X \rightarrow \mathbb{R}, \quad x \rightarrow \frac{x - \tilde{x}}{IQR_X}$$

## Decimal scaling:

For a numerical attribute  $X$  and the smallest integer value  $s$  that is larger than  $\log_{10}(\max_x)$ , the decimal scaling is defined as

$$d: \text{dom}X \rightarrow [0,1], \quad x \rightarrow \frac{x}{10^s}$$

# Agenda



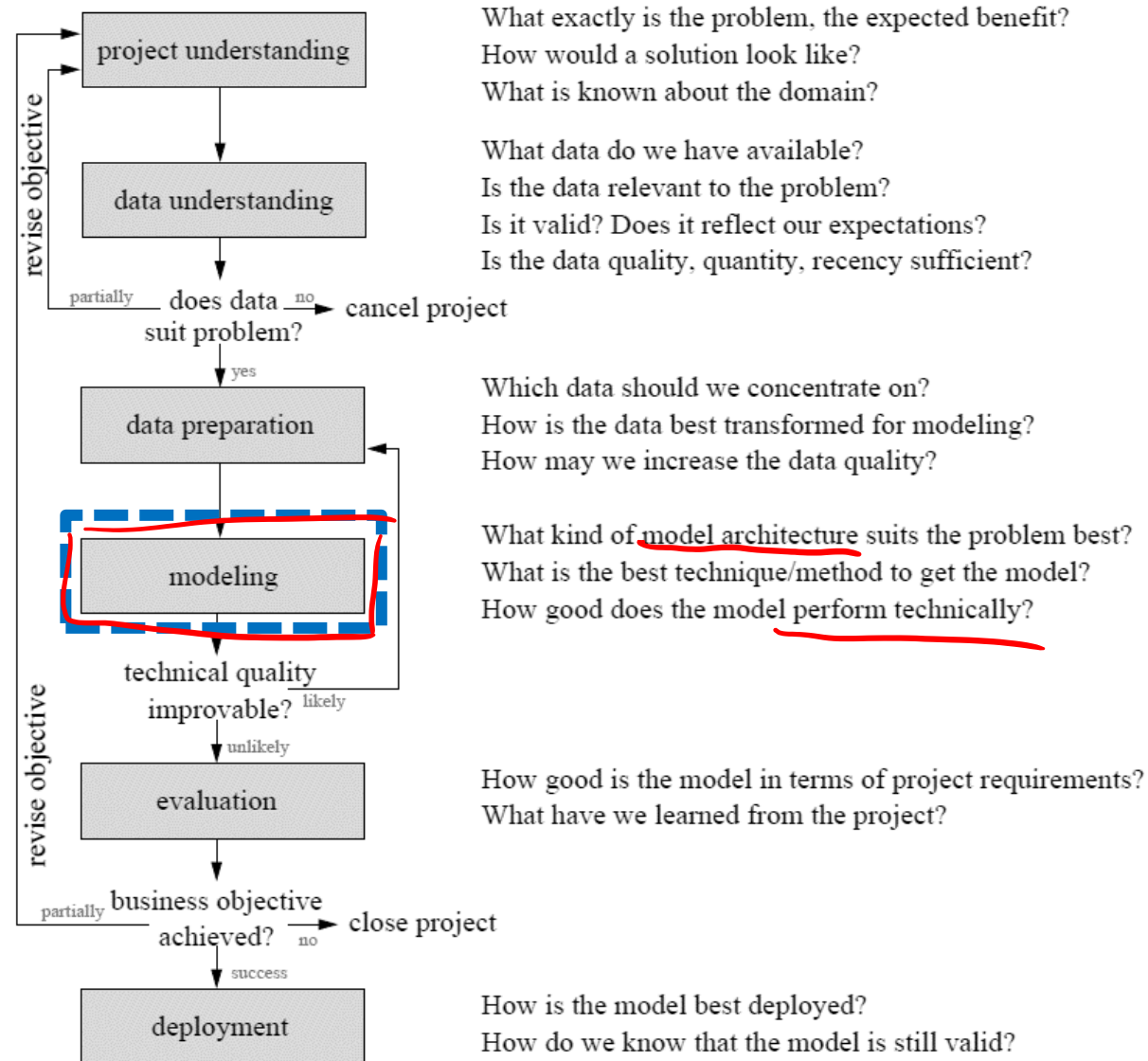


Cross  
Industry  
Standard  
Process for  
Data  
Mining

Iteration as  
a rule

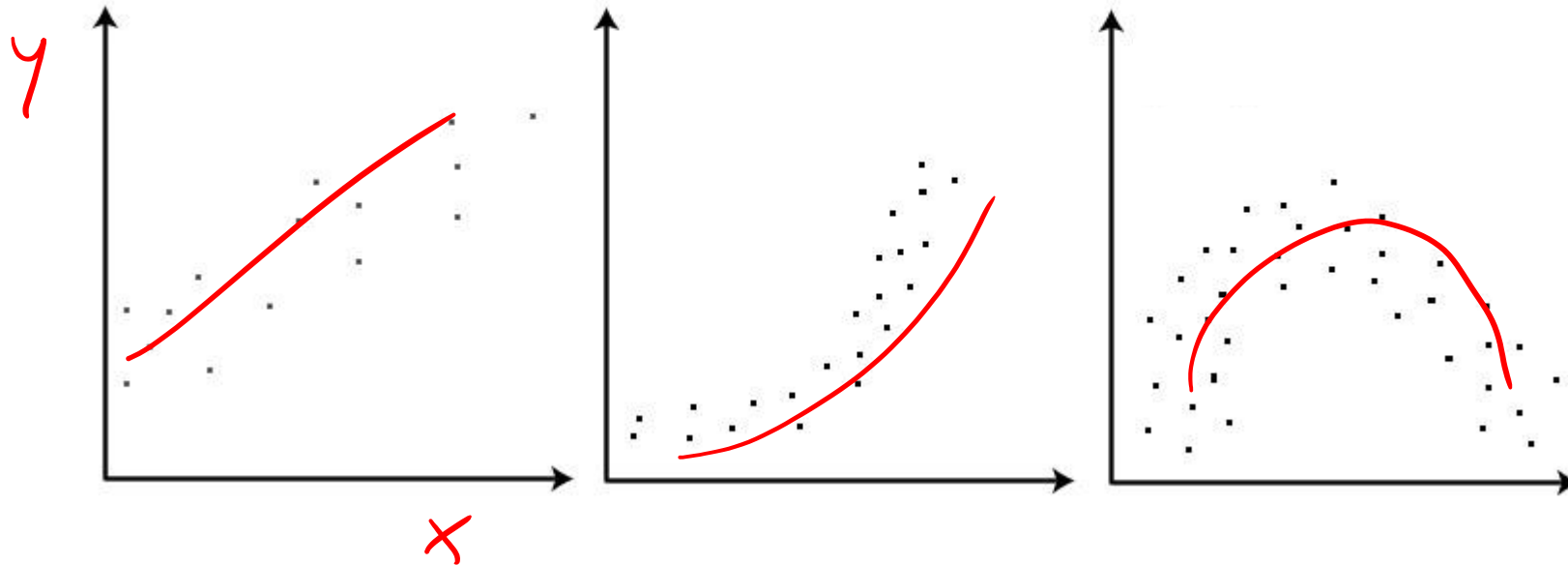
Process of data  
exploration

Implementation of the  
KDD Process



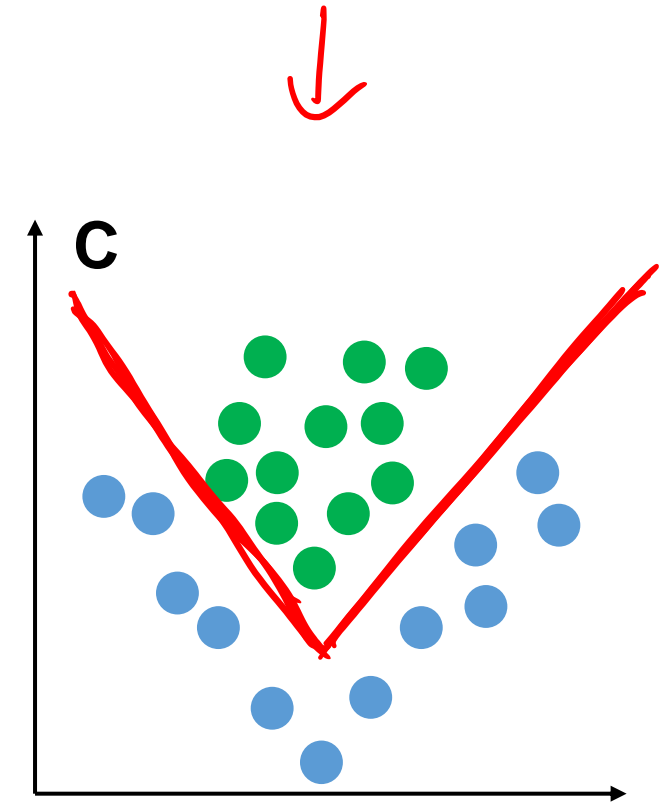
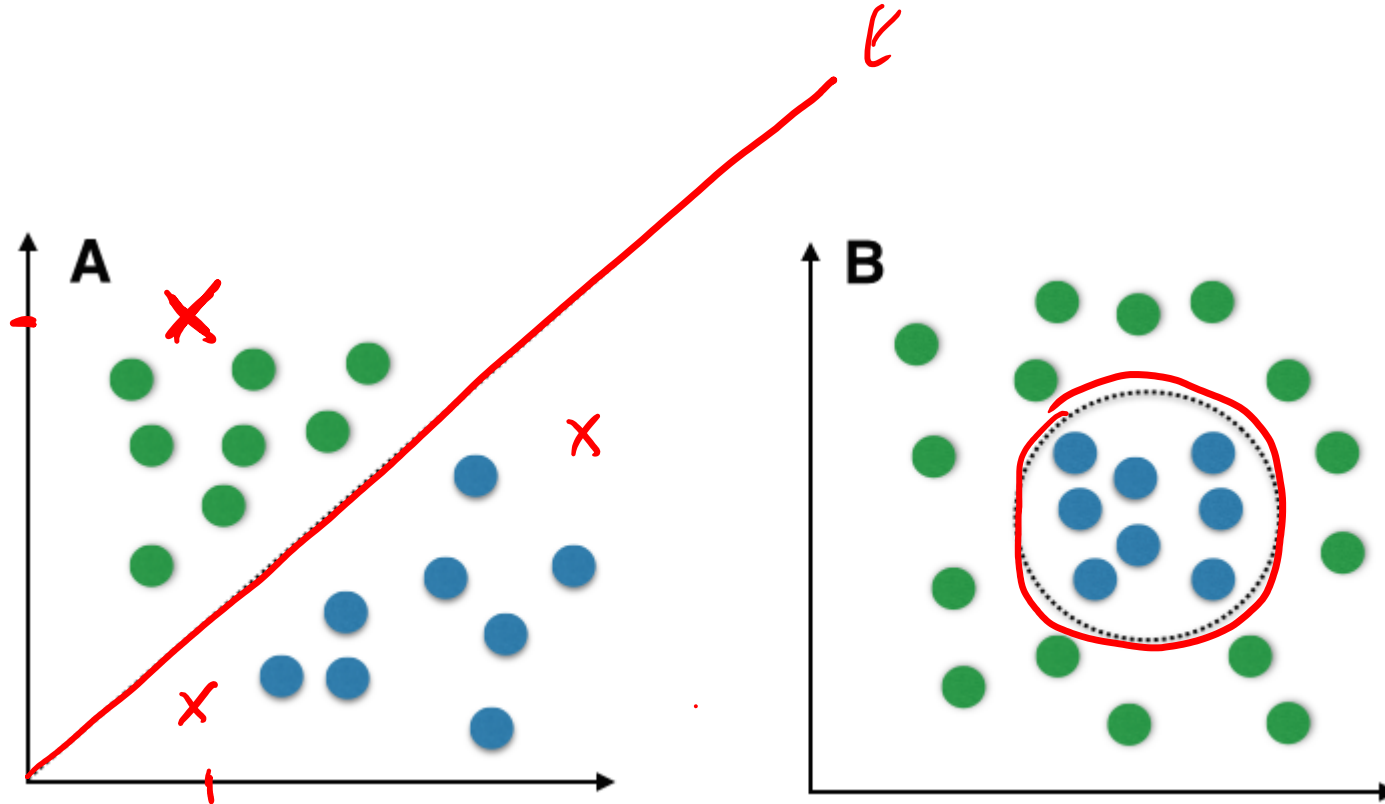
# Let's revisit data understanding

Types of relationships



# Let's revisit data understanding


On our way to classification problems



Decision Tree  
SUM

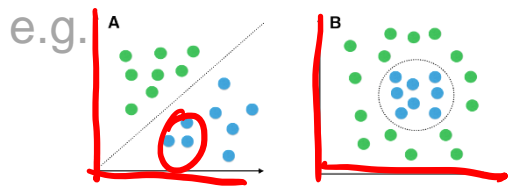
# Introduction

$$\begin{array}{cccc} \overset{L}{A} & \overset{L}{B} & C & D \\ + & - & & \end{array}$$
$$\begin{array}{r} \textcircled{AB} \\ ++ \\ -- \\ \hline +- \\ +- \end{array} \Rightarrow \text{yes}$$
$$\begin{array}{r} +- \\ +- \end{array} \Rightarrow \text{no}$$

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Fundamental concept of DM: **predictive modeling**

Supervised segmentation: how can we segment the population with respect to something that we would like to predict or estimate



- „Which customers are likely to leave the company when their contracts expire?“
- „Which potential customers are likely not to pay off their account balances?“

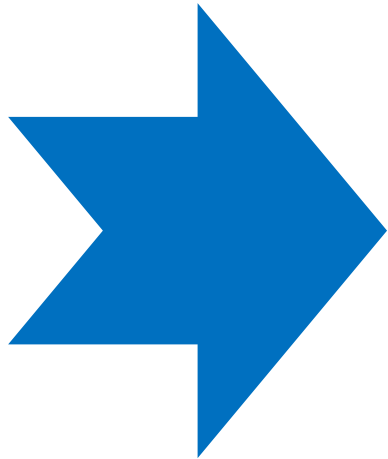
Technique: find or **select important, informative variables / attributes** of the entities with respect to a target

Is there one or more other variables that reduces our uncertainty about the value of the target?

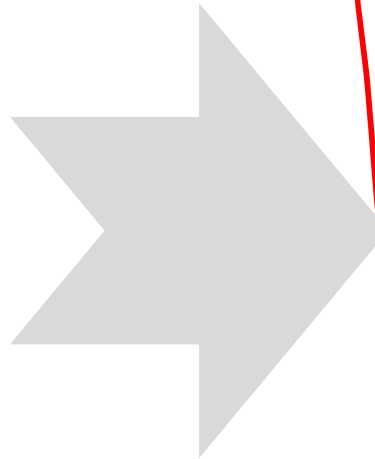
Select **informative subsets** in large databases



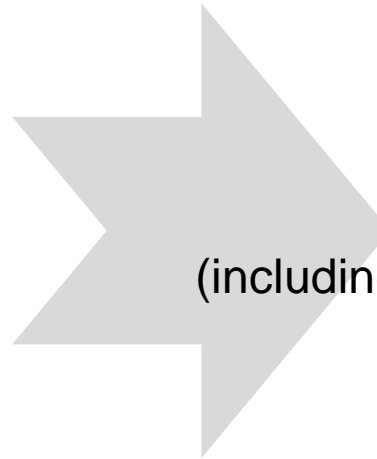
Ref.



(1) Models and Induction



(2) Attribute Selection



(3a) Decision Trees  
Algorithmic View



(3b) Probability Estimation



(3c) Decision Tree Examples

Next week  
(including the Python-exercise on Friday)

# Models and Supervised Learning

OR

A model is a simplified representation of reality created to serve a purpose

A predictive model is a formula for **estimating the unknown value of interest**: the target

Classification/class-probability estimation and regression models

**Prediction = estimate an unknown value**

Credit scoring, spam filtering, fraud detection

Descriptive modeling: gain insight into the underlying phenomenon or process

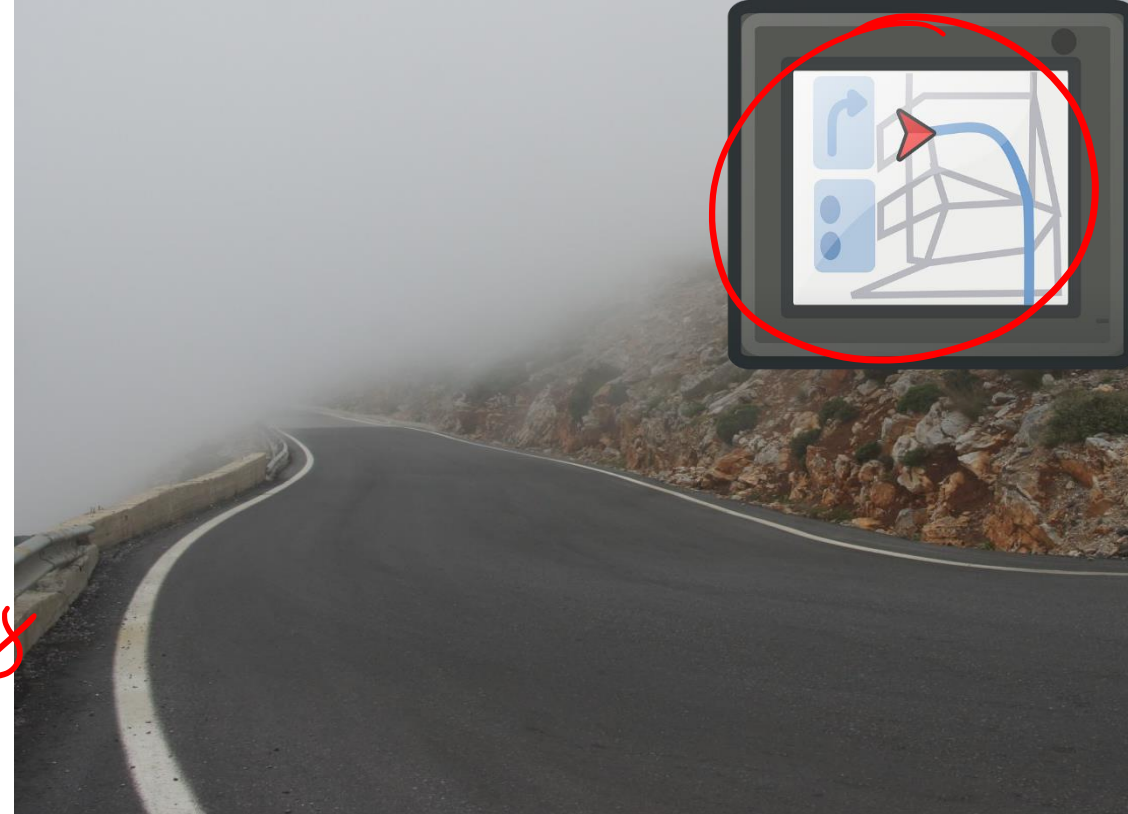
→ Clustering  
Unsupervised

## Supervised learning

Model creation where the model describes a relationship between a set of selected variables (attributes/features) and a **predefined variable** (target)

The model estimates the value of the target variable as a function of the features

Ref.





## Supervised learning

Model creation where the model describes a relationship between a set of selected variables (attributes/features) and a **predefined variable** (target)

The model estimates the value of the target variable as a function of the features

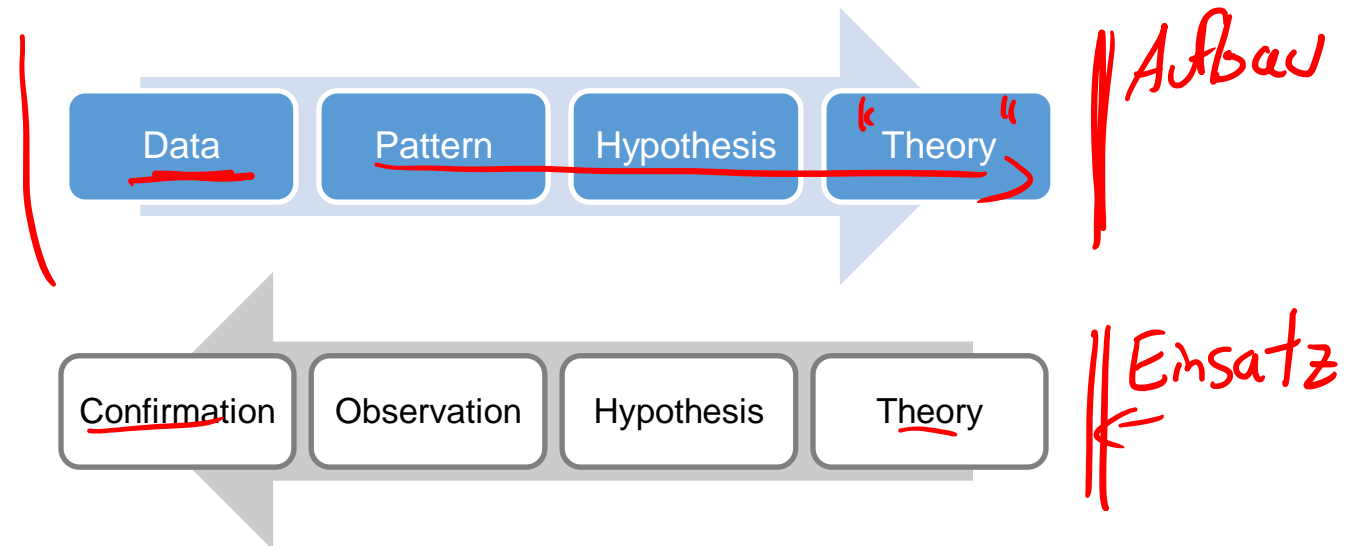
## Induction

Creation of models from data

Refers to generalizing from specific case to general rules

How can we select one or more attributes / features / variables that will best divide the sample w.r.t. our target variable of interest?

Unlike deduction:



# Now: From Data to Decision Trees

→ [??] →

Attributes				Target attribute
Name	Balance	Age	Employed	Write-off
Mike	\$200,000	42	no	yes
Mary	\$35,000	33	yes	no
Claudio	\$115,000	40	no	no
Robert	\$29,000	23	yes	yes
Dora	\$72,000	31	no	no

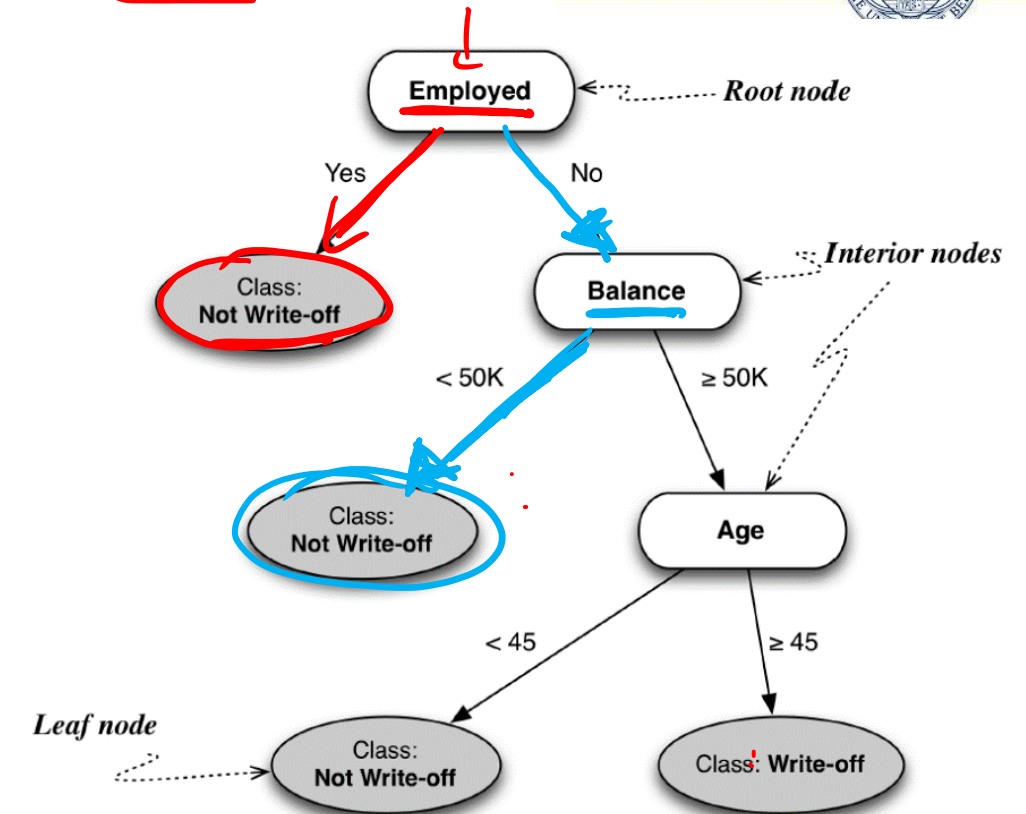
This is one row (example).  
Feature vector is: <Claudio,115000,40,no>  
Class label (value of Target attribute) is no

e.g., [Michi, 40,000, 24, ~~yes~~, Write-off?] → no

If we select multiple attributes each giving some information gain, it's not clear how to put them together

→ **decision trees**

Decision trees are often used as **predictive models**



The tree creates a segmentation of the data

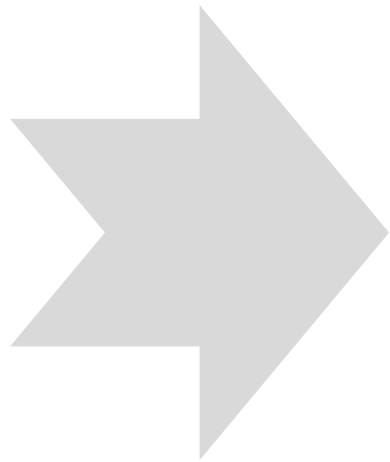
Each *node* in the tree contains a test of an attribute

Each *path* eventually terminates at a *leaf*

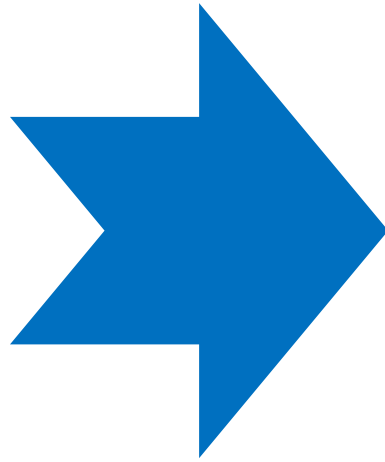
Each leaf corresponds to a *segment*, and the attributes and values along the path give the characteristics

Each leaf contains a value for the target variable

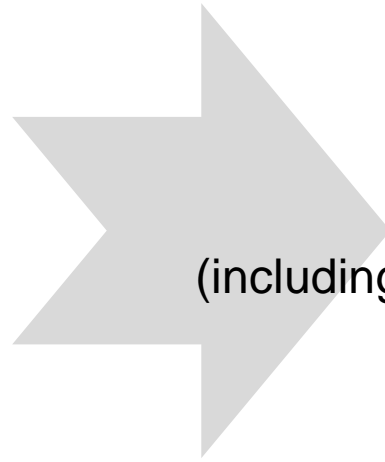




(1) Models and Induction



(2) Attribute Selection



(3a) Decision Trees  
Algorithmic view



Next week  
(including the Python-exercise on Friday)

(3b) Probability Estimation



(3c) Decision Tree Examples

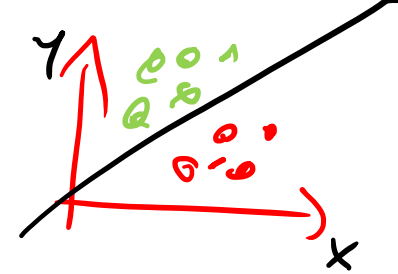
# Supervised segmentation

## Intuitive approach

Segment the population into **subgroups** which have different values for the target variable (*high inter-group discrimination*) and similar values for the target variable within the subgroup (*low intra-group discrimination*)



Ref.



Segmentation may provide a **human-understandable set of segmentation patterns**

(e.g., „Middle-aged professionals who reside in New York City on average have a churn rate of 5%“)

How can we (automatically) judge whether a variable contains important information about the target variable?

What variable gives us the most information about the future churn rate of the population?

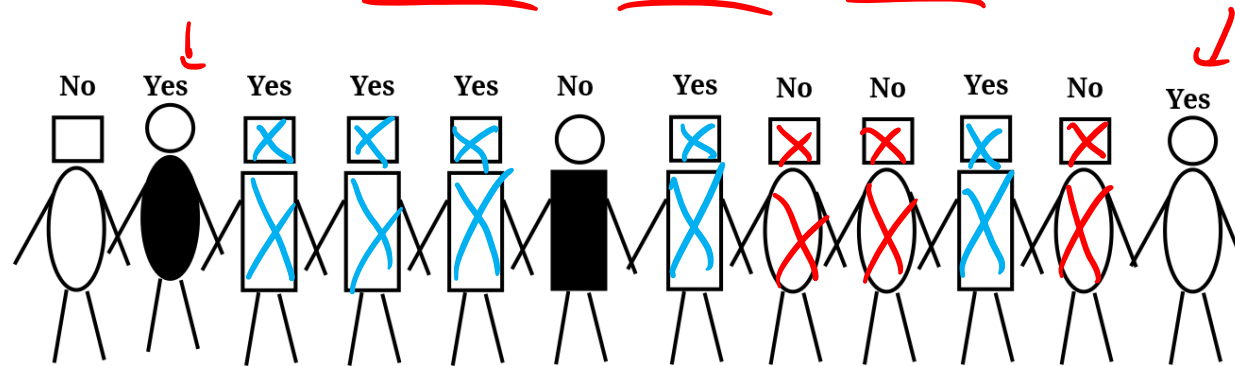
# Supervised Segmentation – Decision Tree Example

How can we (automatically) judge whether a variable contains important information about the target variable?

Consider a binary (two class) classification problem

Binary target variable: {"Yes", "No"}

Attributes: head-shape, body-shape, shirt-color



Yes  
No

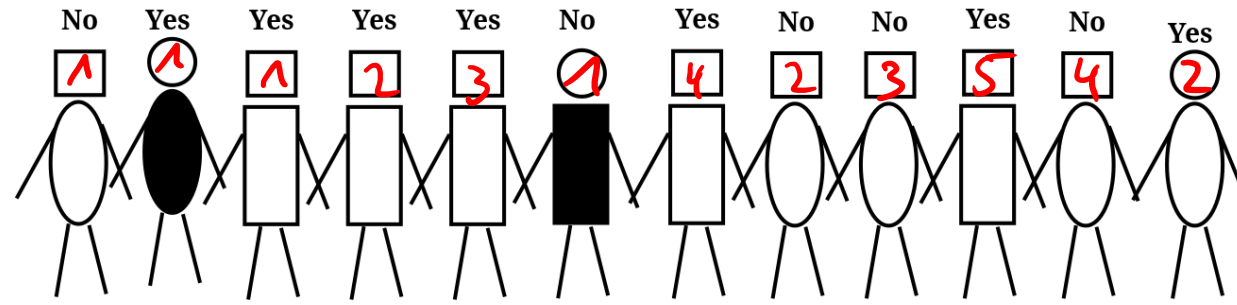
Kopf und Körper  
→ gleiche Form ⇒ Yes  
unterschiedlich ⇒ No

Which of the attributes would be the best to segment these people in groups such that write-offs will be distinguished from non-write-offs?

Resulting groups should be as **pure** as possible!

# Exercise – attribute selection

And a first step to build decision trees



target:

#      yes      no

head-shape:

square

circular

9	5	4
3	2	1

body-shape:

rectangular

oval

6	5	1
6	2	4

shirt-color:

white

black

10	6	4
2	1	1

$\frac{2}{12}$

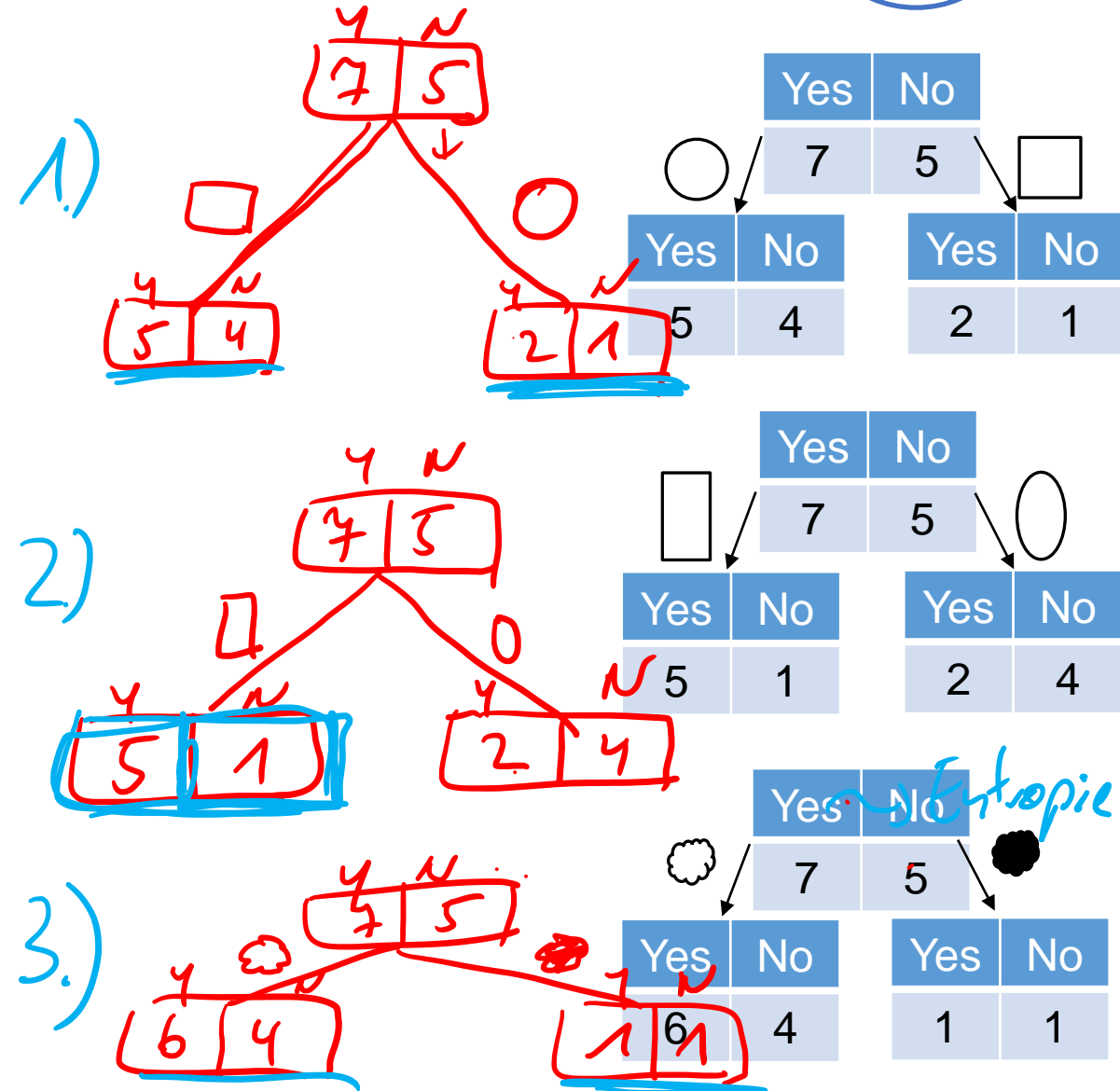
A B C D  
++ --

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5 Min.

erlin

Which attribute should be selected first?



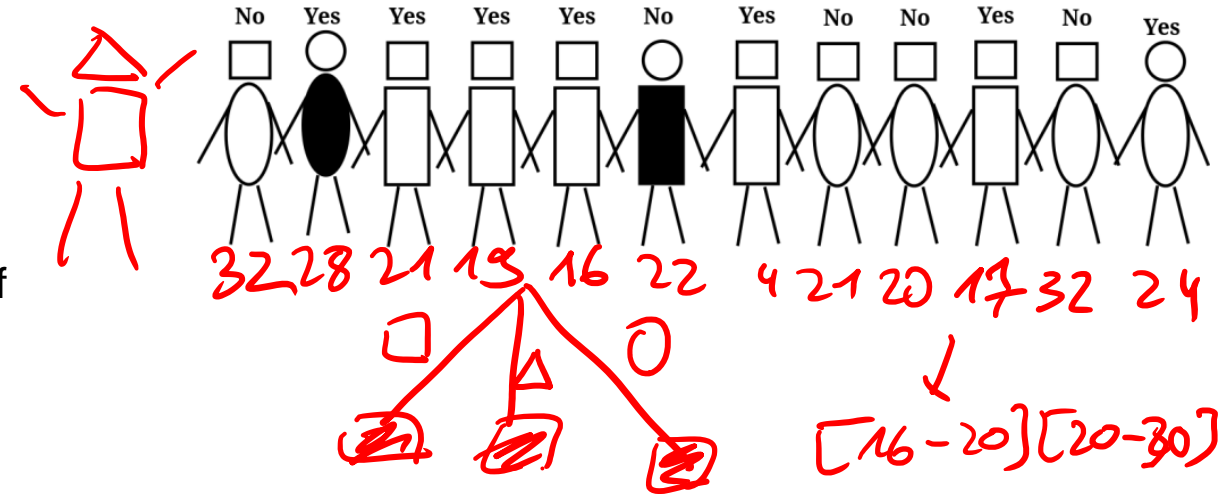
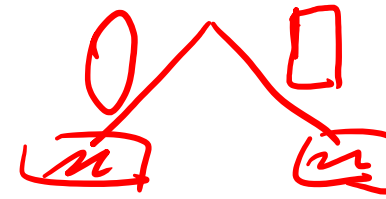
# Reduce impurity



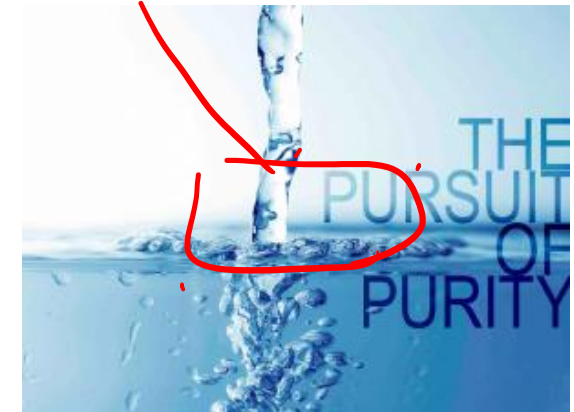
## Attributes rarely split a group perfectly

- Consider if the second person were not there  
– Then, *shirt-color* would create a pure segment where all individuals have (*write-off=no*)
- – Then, the condition *shirt-color=black* would only split off one single data point into the pure subset. Is this better than a split that does not produce any pure subset, but reduces the impurity more broadly?
- Not all attributes are binary. How do we compare the splitting into two groups with **splitting into more groups**?
- Some attributes take on numeric values. How should we think about creating supervised segmentations using numeric attributes?

Purity measure → **information gain** / **entropy**



$\geq [16-20]$



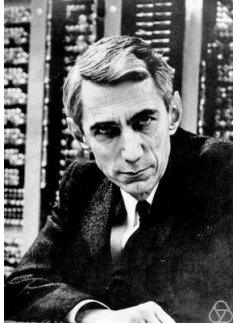


# Entropy

$$-\sum p_i \log_2(p_i)$$

Entropy is a measure of disorder that can be applied to a set

Disorder corresponds to how mixed (impure) a segment is w.r.t. the properties of interest (values of target)



Claude E. Shannon

*entropy*

$$= -p_1 \log_2(p_1) - p_2 \log_2(p_2) - \dots - p_n \log_2(p_n)$$

with  $p_i$  as the relative percentage of property  $i$  within the set, ranging from  $p_i = 0$  to  $p_i = 1$  (all have property  $i$ ).

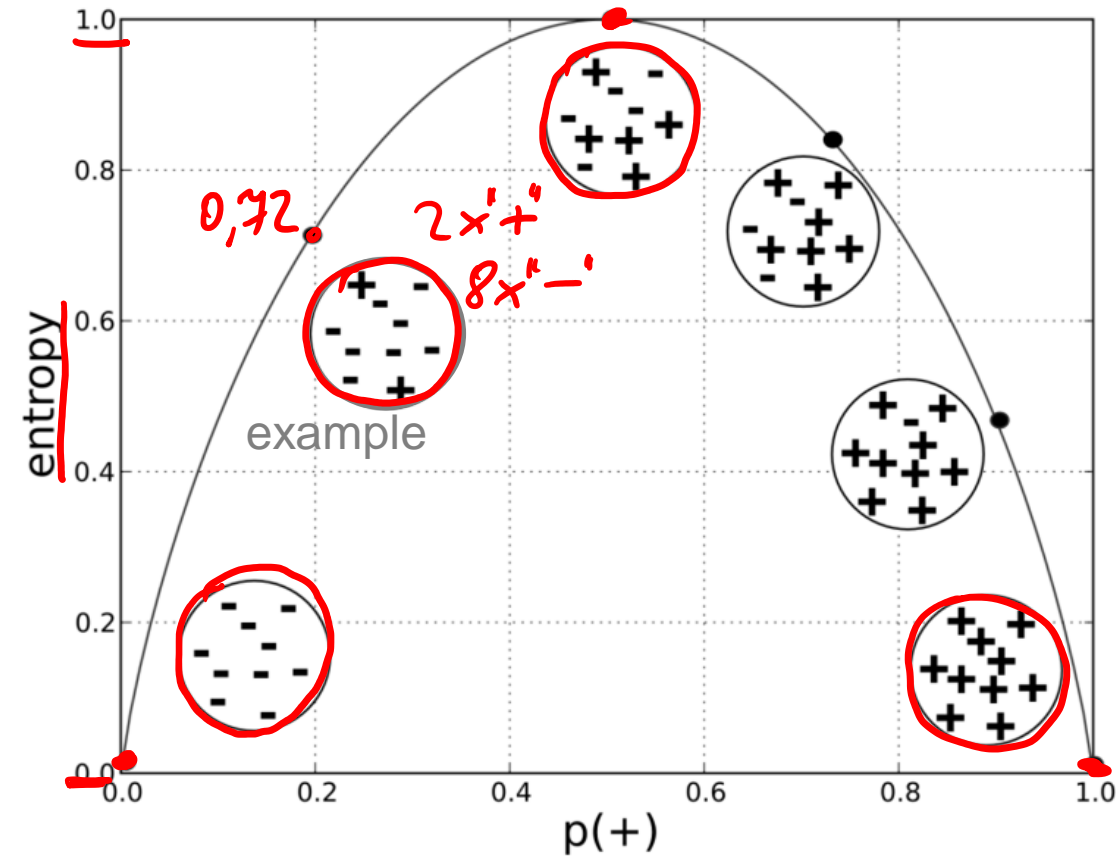
**Entropy measures the general disorder of a set**, ranging from **zero** at minimum disorder (the set has members all with the same, single property) to **one** at maximal disorder (the properties are equally mixed)

Example



```
#Entropy :
import math as m
def entropy(p1,p2):
    return - p1 * m.log2(p1) - p2 * m.log2(p2)

#Excursus (alternatively): gini-coefficient
def gini(p1,p2):
    return 1- (p1*p1 + p2*p2)
```



$$p(-) = 8/10 \quad p(+) = 2/10$$

$$\begin{aligned} \text{entropy}(S) &= -[0.8 \times \log_2(0.8) + 0.2 \times \log_2(0.2)] \\ &= -[0.8 \times (-0.32) + 0.2 \times (-2.32)] \approx 0.72 \end{aligned}$$

Basic idea behind information gain:

Measure how much an attribute improves (**decreases**) entropy over the whole segmentation it creates.

IG measures the change in entropy due to any amount of new information added

How much purer are the **children c** (split set) compared to their **parent** (original set)?

$$\begin{aligned} IG(\text{parent}, \text{children}) \\ = \text{entropy}(\text{parent}) - [p(c_1) \times \text{entropy}(c_1) + \\ p(c_2) \times \text{entropy}(c_2) + \dots] \end{aligned}$$

The entropy for each child  $c_i$  is weighted by **the proportion of instances** belonging to that child

# Information gain

## Example 1

$$-\sum p_i \log_2(p_i)$$

Two-class problem (• and ★)

Entropy parent:

$$\begin{aligned} &= -[p(\bullet) \times \log_2 p(\bullet) + p(\star) \times \log_2 p(\star)] \\ &\approx -[0.53 \times -0.9 + 0.47 \times -1.1] \\ &\approx 0.99 \quad (\text{very impure}) \end{aligned}$$

Entropy left child:

$$\begin{aligned} &= -[p(\bullet) \times \log_2 p(\bullet) + p(\star) \times \log_2 p(\star)] \\ &\approx -[0.92 \times (-0.12) + 0.08 \times (-3.7)] \\ &\approx 0.39 \end{aligned}$$

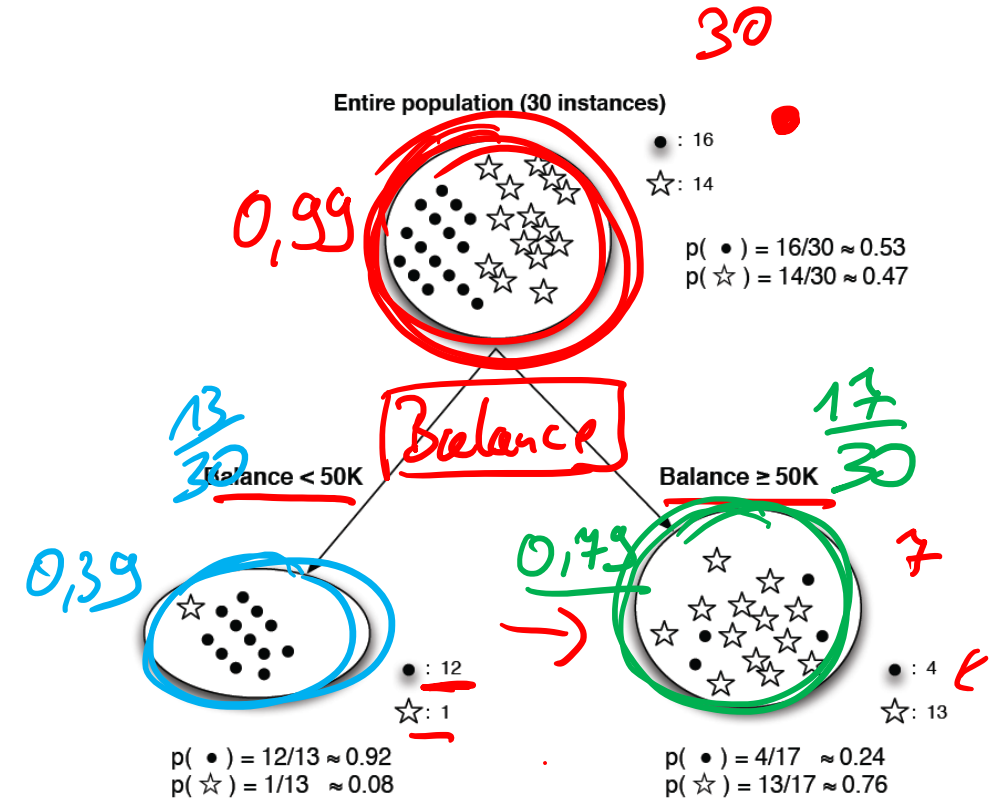
Entropy right child:

$$\begin{aligned} &= -[p(\bullet) \times \log_2 p(\bullet) + p(\star) \times \log_2 p(\star)] \\ &\approx -[0.24 \times (-2.1) + 0.76 \times (-0.39)] \\ &\approx 0.79 \end{aligned}$$

IG:

Information Gain

$$\begin{aligned} &= \text{entropy(parent)} - [p(\text{Balance} < 50K) \times \text{entropy}(\text{Balance} < 50K) \\ &\quad + p(\text{Balance} \geq 50K) \times \text{entropy}(\text{Balance} \geq 50K)] \\ &\approx 0.99 - [0.43 \times 0.39 + 0.57 \times 0.79] \\ &\approx 0.37 \end{aligned}$$





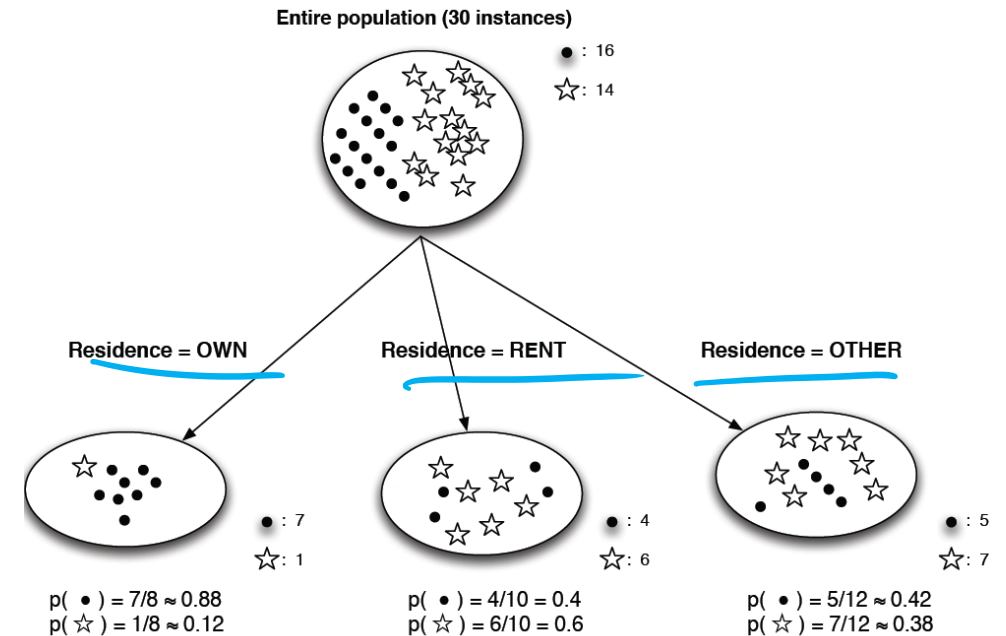
# Information gain

## Example 2

Same example, but different candidate split

attribute here: *residence*

entropy and information gain computations:



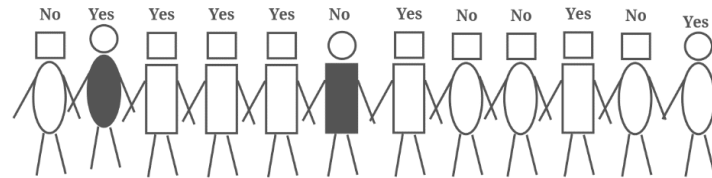
The *residence* variable does have a positive information gain, but it is lower than that of *balance*.

$$\begin{aligned} \text{entropy}(\text{parent}) &\approx 0.99 \\ \text{entropy}(\text{Residence=OWN}) &\approx 0.54 \\ \text{entropy}(\text{Residence=RENT}) &\approx 0.97 \\ \text{entropy}(\text{Residence=OTHER}) &\approx 0.98 \\ \text{IG} &\approx 0.13 \end{aligned}$$

# Exercise – Information gain

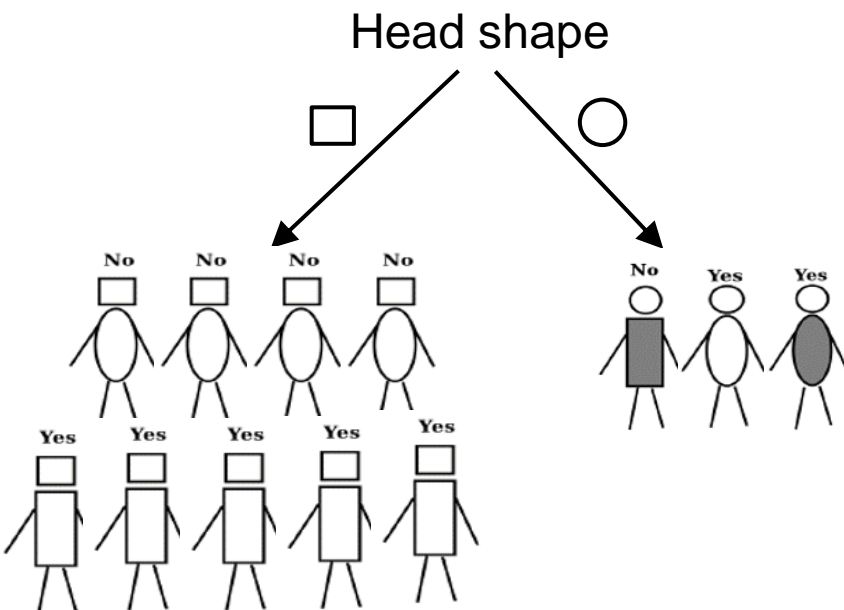
Example 3, 4 and 5

Which attribute to choose?



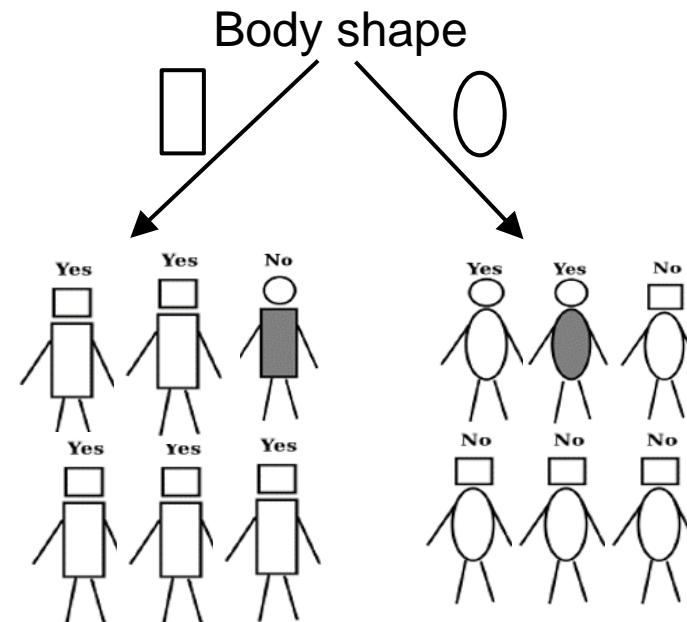
Yes: 7  
No: 5

$entropy(parent) \approx 0,98$



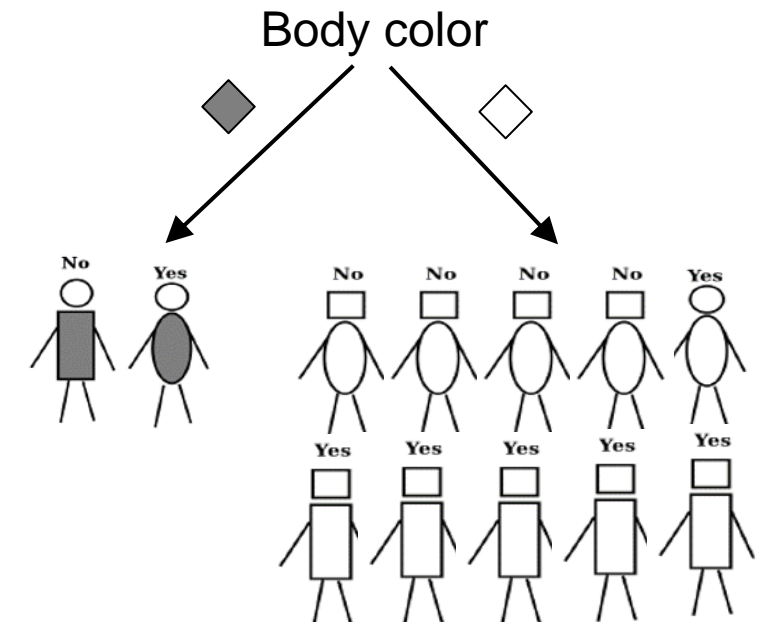
$entropy(\square) \approx 0,99$   $entropy(\bigcirc) \approx 0,92$

IG  $\approx 0,007$



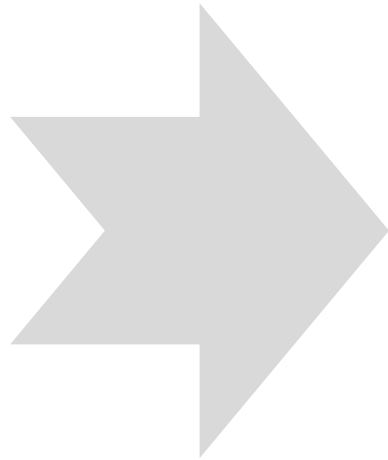
$entropy(\square) \approx 0,65$   $entropy(\bigcirc) \approx 0,92$

IG  $\approx 0,196$

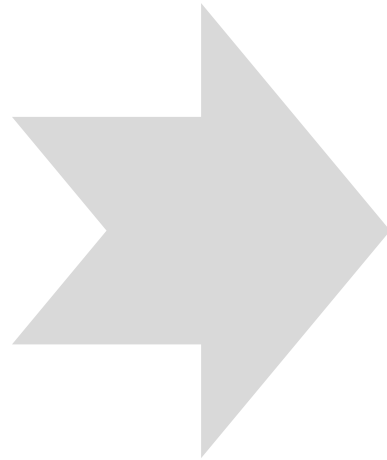


$entropy(\blacklozenge) \approx 1,00$   $entropy(\blacklozenge) \approx 0,97$

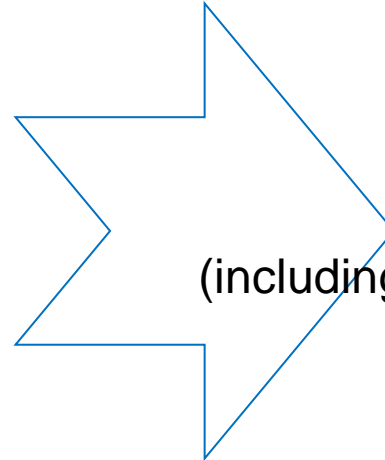
IG  $\approx 0,004$



(1) Models and Induction



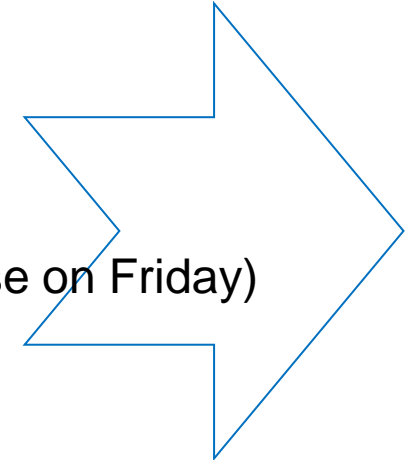
(2) Attribute Selection



(3a) Decision Trees  
Algorithmic view



(3b) Probability Estimation



(3c) Decision Tree Examples

Next week  
(including the Python-exercise on Friday)

# Fragen?

- ✓ Predictive modeling I
  - ✓ Models and induction
  - ✓ Attribute selection
  - ✓ Decision trees - introduction
    - Algorithms for tree induction
    - Probability estimation tree

# Todos for this week

Choose your project and your project group (4 persons per group)

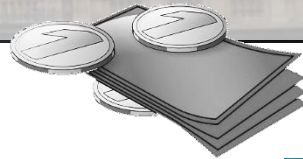
See slides BI-Project ("Folien – Projektaufgabe – ab 7.6.'24" in Blackboard)



## Costa Rican Household Poverty Prediction

Set of household characteristics from a representative sample of households  
Make sure the right people are given enough aid

Goal: Predict the level of need (income level)



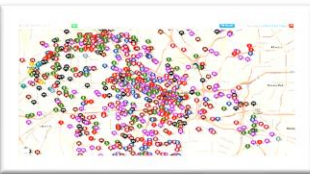
## West Nile Virus Prediction in Chicago

7 years of weather, location, testing, and spraying data

Goal: predict the presence of West Nile virus for a given time, location, and species



>> Crime Mapping



## Crime Classification in Los Angeles

4 years of crime reports from all across Los Angeles

Goal: Predict the category of crime that occurred given a certain time and location

## Crime Classification in San Francisco

12 years of crime reports from all across San Francisco

Goal: Predict the category of crime that occurred given a certain time and location



## Data Preparation

Berthold et al. Chapter 4, 6

Han, J., Kamber, M., Pei, J.: Data Mining: Concepts and Techniques. Morgan Kaufmann, 2011

## Predictive Modeling

Provost, F.,  
Fawcett, T. Data Science for Business  
Chapter 3

Berthold et al. Guide to Intelligent Data Analysis  
Chapter 8.1

Hand, D. Principles of Data Mining  
Chapter 10

Quinlan, J.R. Induction of Decision Trees (in: Machine Learning, 1(1), p. 81-106, 1986)



- J. Bertin (1983) *Semiology of graphics: diagrams, networks, maps*. University of Wisconsin Press. Originally in French: *Semiologie Graphique*, 1967
- Cairo, A. (2012). *The Functional Art: An introduction to information graphics and visualization*. New Riders.
- Mertens, P., & Meier, M. (2009). *Integrierte Informationsverarbeitung*. Wiesbaden: Gabler.
- Woolman, M. (2002). *Digital information graphics*. Watson-Guptill Publications, Inc..