

İktisat- İstatistik 2 Vize Soru Çözümleri

1)

a)

$$P\left(Z > \frac{78 - \mu}{10}\right) = 0,05$$

$$Z_{\alpha/2} = 1,65$$

$$\frac{78 - \mu}{10} = 1,65$$

$$\mu = 61,5$$

b)

$$P\left(Z < \frac{55 - 61,5}{10}\right) = P(Z < -0,65) = 0,5 - 0,2422 = 0,2578$$

2)

$$\bar{x} = \frac{16 + 15 + 18 + 19 + \dots + 14 + 22}{11} = 18$$

$X_i - \bar{X}$	$(X_i - \bar{X})^2$
16-18=-2	4
15-18=-3	9
18-18=0	0
19-18=1	1
17-18=-1	1
21-18=3	9
23-18=5	25
16-18=-2	4
17-18=-1	1
14-18=-4	16
22-18=4	16
$\sum (X_i - \bar{X}) = 0$	$\sum (X_i - \bar{X})^2 = 86$

$$s = \sqrt{\frac{\sum (X_i - \bar{X})^2}{n - 1}} = \sqrt{\frac{86}{11 - 1}} = 2,933$$

$$t_{0,025;11-1} = 2,228$$

$$18 - 2,228 \times \frac{2,933}{\sqrt{11}} \leq \mu \leq 18 + 2,228 \times \frac{2,933}{\sqrt{11}}$$

$$16,03 < \mu < 19,97$$

$$\text{b) Hata büyüklüğü} = 2,228 \times \frac{2,933}{\sqrt{11}} = 1,97$$

c)

$$n = \left( \frac{Z_{\frac{\alpha}{2}} s}{e} \right)^2$$

$$Z_{\alpha/2} = 1,96$$

$$n = \left( \frac{1,96 \times 2,933}{0,2} \right)^2 \cong 826$$

Ya da

$$n = \left( \frac{2.228 \times 2,933}{0,2} \right)^2 \cong 1067$$

3)

$$\hat{p}_1 = \frac{36}{72} = 0,5$$

$$\hat{p}_2 = \frac{31}{50} = 0,62$$

$$(\hat{p}_1 - \hat{p}_2) - Z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}} \leq p_1 - p_2 \leq (\hat{p}_1 - \hat{p}_2) + Z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}}$$

$$(0,50 - 0,62) - 1,96 \times \sqrt{\frac{0,50 \times 0,50}{72} + \frac{0,62 \times 0,38}{50}} \leq p_1 - p_2 \leq (0,50 - 0,62) + 1,96 \times \sqrt{\frac{0,50 \times 0,50}{72} + \frac{0,62 \times 0,38}{50}}$$

$$-0,2973 \leq p_1 - p_2 \leq 0,0573$$

Güven aralığı sıfır değerini içerdüğinden dolayı iki grup arasında anlamlı bir fark olmadığı sonucuna ulaşılır.