

# Section 7.1

## Empirical Rule

- 1 standard deviation on both sides of the mean is about \_\_\_\_\_ of the area under the curve.
- 2 standard deviations on both sides of the mean is about \_\_\_\_\_ of the area under the curve.
- 3 standard deviations on both sides of the mean is about \_\_\_\_\_ of the area under the curve.

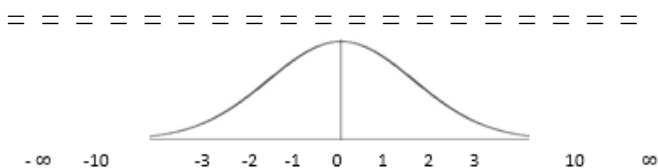
## If the total area under the curve is 1, then

- 1 SD on both sides has an area of about \_\_\_\_\_
- 2 SD on both sides has an area of about \_\_\_\_\_
- 3 SD on both sides has an area of about \_\_\_\_\_

## Area for other than memorized z-values

\_\_\_\_\_ finds the area  
between a & b

For \_\_\_\_\_ we use -10 and for \_\_\_\_\_ we use 10



Find the 4-decimal area between the values

.46 & 2

$-\infty$  & .35

3 &  $\infty$

-2.3 & 1.1

Right of -1.1

Left of 2.6

Find the area to the left of  $z = -1.47$



=====

Find the area to the right of  $z = 1.86$



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Find the area between the z-scores 0 and 1



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**To find the z-value if you have an area**

\_\_\_\_\_ finds z

Find z for each left area (always \_\_\_\_-decimals)

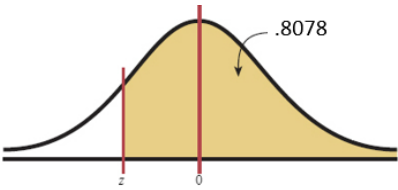
Area left of z is .0032

Area left of z is .1515

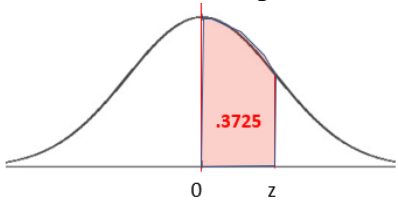
Area left of z is .7422

Area left of z is .9959

What z-value corresponds to the shaded area?



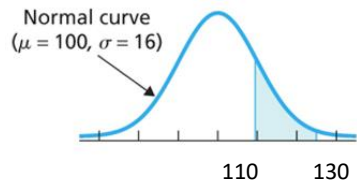
=====  
What z-value corresponds to the shaded area?



=====  
**Finding a Percentage or Probability  
for a normally distributed variable**

- 1. Sketch the normal curve and \_\_\_\_\_ region you are interested in.
- 2. Use \_\_\_\_\_ to find the area
- 3. \_\_\_\_\_ the area to a percent or probability.

=====  
Find the 2-decimal percentage of people that have an IQ between 110 and 130

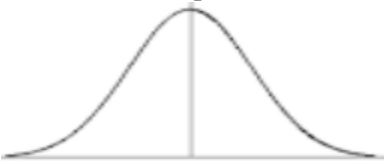


\_\_\_\_\_ % of the people have an IQ between 110 and 130

If the mean of a normally distributed variable is 12 & the SD = 3, what are the quartiles?



What is the 70<sup>th</sup> percentile?



What number represents negative infinity?

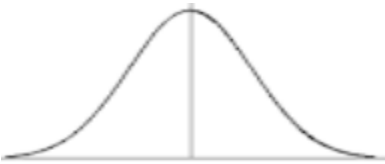
What number represents positive infinity?

=====

If the mean of a normally distributed variable is 12 and the SD = 3, what 2-decimal values divide the region into a symmetric middle area of 92%?



A study found that an animal’s distance to water is normally distributed with a mean of 5.33 and SD = .85.  
Find  $P(Y > 6)$  as a percentage



Find  $P(3 < Y < 7)$  as a percentage

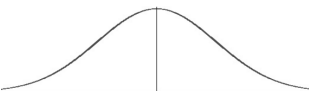


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### Ch 6.3 & 7.1 Review

A normally distributed variable has a mean of 13 and SD=2

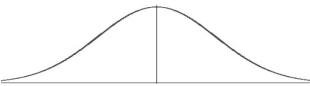
Find the area between 12 & 15.



Find the number that represents negative infinity.

Find the number that represents infinity.

Find the value of the 80<sup>th</sup> percentile.



===== A multiple-choice test has 9 questions with  $P(s)=.53$ , find each 2-decimal answer

$P(f) =$

Probability of getting at most 4 correct.

Probability of getting exactly 5 correct.

The mean.

The Variance

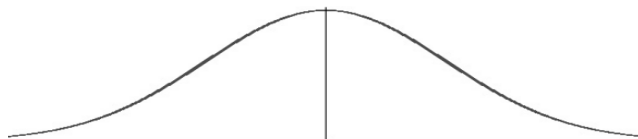
The Standard Deviation

# Section 7.2

## Recap of Area and Values

To find Area, Probability, Percentage's use

To find z-values or other numbers use



The average income for teachers in Texas is \$49,560 with a standard deviation of \$4750. If income is normally distributed, find

$$P(\$41,500 \leq x \leq \$51,270)$$



## Applications

To qualify for the police academy, there is a fitness test. Scores are normally distributed with a mean of 58 and SD of 12. What is the cutoff score if only the top 22% of the applicants are selected?



The national average on the ACT test is 20.8. Assuming it is normally distributed with a standard deviation of 9.4, find the 91<sup>st</sup> percentile score.



Find  $P(x > 28)$



Find  $P(x < 18)$



The average out-of-pocket payment at a clinic is \$456 and the payments are normally distributed with a standard deviation of \$87. What are the limits of the middle 52% of the payments? (2-decimal places)



### Review

A town finds the average number of homes in new subdivisions is 432 with SD = 22. Find  $P(x > 400)$



The average time spent by construction workers on weekends is 7.93 hours. Assume normally distributed with a standard deviation of 0.8 hour.

Probability an individual works fewer than 8 hours



Probability that the mean of a sample of 40 workers  $< 8$



## Section 7.3

### Central Limit Theorem

A teacher gives a class of 4 students a test & the grades are 6, 4, 8, 2

What is the population mean:  $\bar{x} =$  \_\_\_\_\_

Population Standard Deviation:  $\sigma_x =$  \_\_\_\_\_

### z-formulas

If you have a normally distributed population and want information about a \_\_\_\_\_ member use:

If you have a sample of size \_\_\_\_\_ and want information about the sample mean \_\_\_\_\_ use:

The average age of SHSU faculty is 44.2 with a SD of 5.6. Assume normally distributed, for an individual find  $P(39 < x < 46)$ .

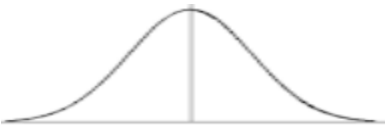


Probability that the mean of a sample of 35 workers is greater than 46



A study found that American families generate an average of 37.4 lbs of plastic garbage per year. If the standard deviation is 6.1 lbs, find each

Probability an individual generates < 29.8 lb



Probability the mean of a sample of 33 is between 35 & 38



=====

### Ch 6&7 Test Review Questions

Find each area:

Left of  $z = 2.58$

Right of  $z = -2.34$

Between  $z = 1.34$  and  $-2.11$

=====

Students at a school have an average weight of 113 lb with a standard deviation of 5.7 lb.

What value represents  $-\infty$

What value represents  $\infty$

The average height of students in a school is 87” with  $SD = 4.8$ ”

What is the z-value for a height of 82”

What is the z-value for a height of 102”

What height gives a z-value of -2.57

=====

A team plays 17 games with  $P(s) = .43$

Write each answer as a 2-decimal percent

What is the probability of exactly 7 wins?

What is the probability of at most 4 wins?

=====

Find each z-value for the given information

z	x	Mean	SD	n
	18	22	3.4	31
	20	17	1.6	42
	64	72	4.5	140