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Lab 2

3-Input Priority Encoder

Prepared for:

ELG 4137 - Principles & Application of VLSI Design

February 25, 2022

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Prelab: K-map logical expression and verilog 1-bit comparator

K-map and logical expression

→ 3-bit Priority encoder truth table.

E2	E1	E0	P1	P0
1	X	X	0	1
0	1	X	1	0
0	0	1	1	1
0	0	0	0	0

→ K-map of truth table

P1

	E1 \ E0	00	01	10	11
E2	0	0	1	1	1
	1	0	0	0	0

P0

	E1 \ E0	00	01	10	11
E2	0	0	1	0	0
	1	1	1	1	1

→ Logical expressions from K-map

$$P1 = E2'EO + E2'E1 = E2'(E1 + E0)$$

$$P0 = E'E0 + E2$$

Part II

→ 1-bit comparator truth table

A	B	A < B	A > B	A = B
0	0	0	0	1
0	1	1	0	0
1	0	0	1	0
1	1	0	0	1

→ K-map from truth table

A < B

	A \ B	0	1
B	0	0	1
	1	0	0

A > B

	A \ B	0	1
B	0	1	0
	1	0	1

A = B

	A \ B	0	1
B	0	1	0
	1	0	1

$$A < B = A'B$$

$$A > B = AB'$$

$$A = B = A'B' + AB$$

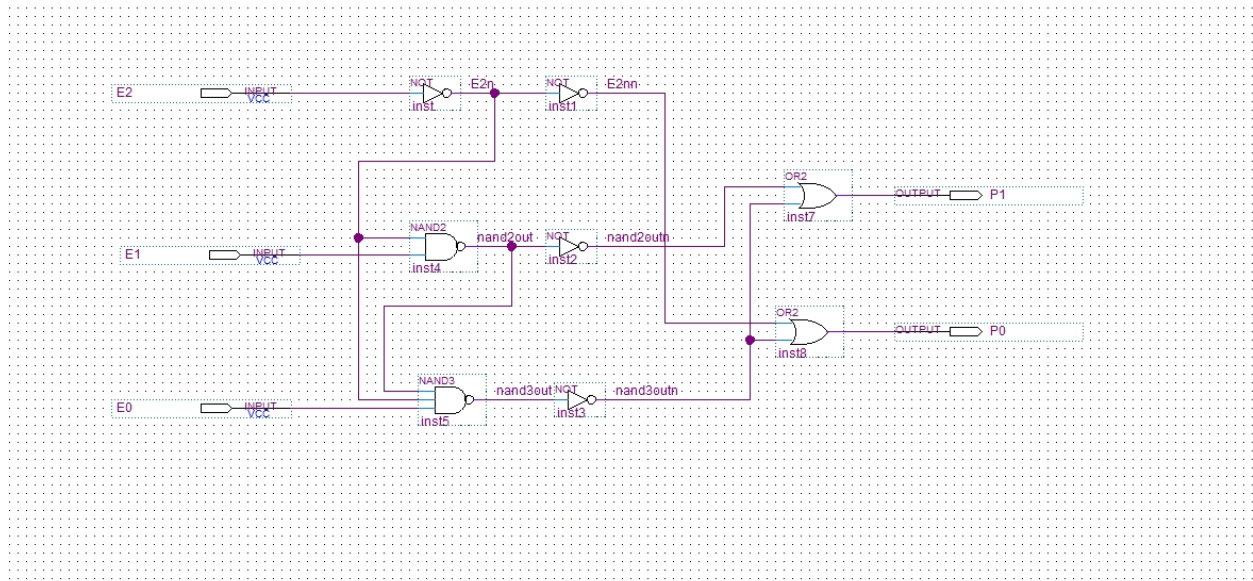
1-Bit Comparator Verilog Code

```
1 module comp_ab (a, b, L, E, G);
2   input a, b; output L, E, G;
3   wire s1, s2;
4   not X1(s1, a);
5   not X2(s2, b);
6   and X3 (L, s1, b);
7   and X4 (G, s2, a);
8   xnor X5 (E, a, b);|
9 endmodule
```

Part 1: Design of Priority Encoder

A priority encoder converts the 3-bit input into a binary (2-bit) representation. The output of the encoder takes the most significant active input and all other lower inputs are ignored.

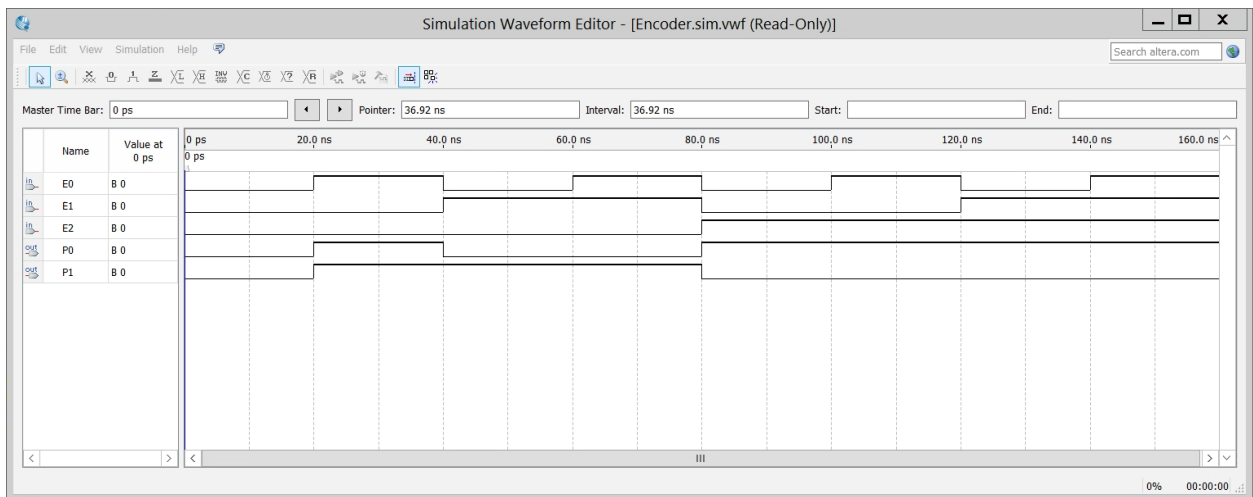
3-Bit Priority Encoder Model



3-Bit Priority Encoder Verilog Program

```
Encoder_Verilog_1.v          Compilation Report - Encoder_verilog_1
1  module Encoder(P0,P1,E0,E1,E2);
2
3      input  E2,E1,E0;
4      output P1,P0;
5      wire  E2n,E2nn,nand2out,nand2outn,nand3out,nand3outn;
6      not(E2n,E2);
7      not(E2nn,E2n);
8      nand(nand2out,E2n,E1);
9      not(nand2outn,nand2out);
10     nand(nand3out,nand2out,E2n,E0);
11     not(nand3outn,nand3out);
12     or(P1,nand2outn,nand3outn);
13     or(P0,E2nn,nand3outn);
14
15
16 endmodule
```

3-Bit Priority Encoder Waveform

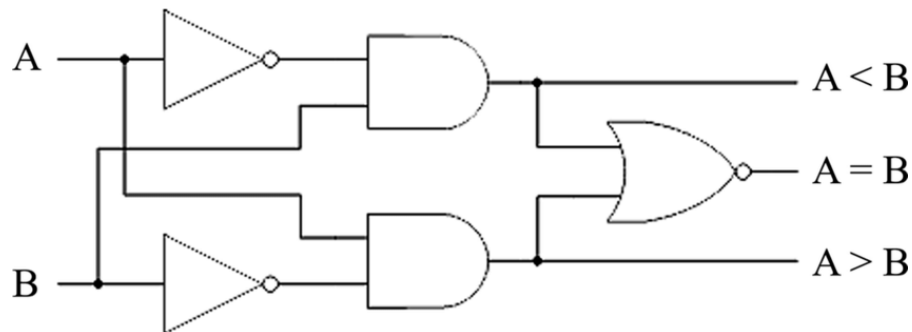


After simulation of the 3-bit priority encoder all results were accurate with what was expected. Looking at the waveform above, depending on whether E2, E1 and E0 are high or low, P0 and P1 change accordingly. When E0 is high, P1P0 is equal to 11, when E1 is high P1P0 is equal to 10 and when E2 is high, P1P0 is 01.

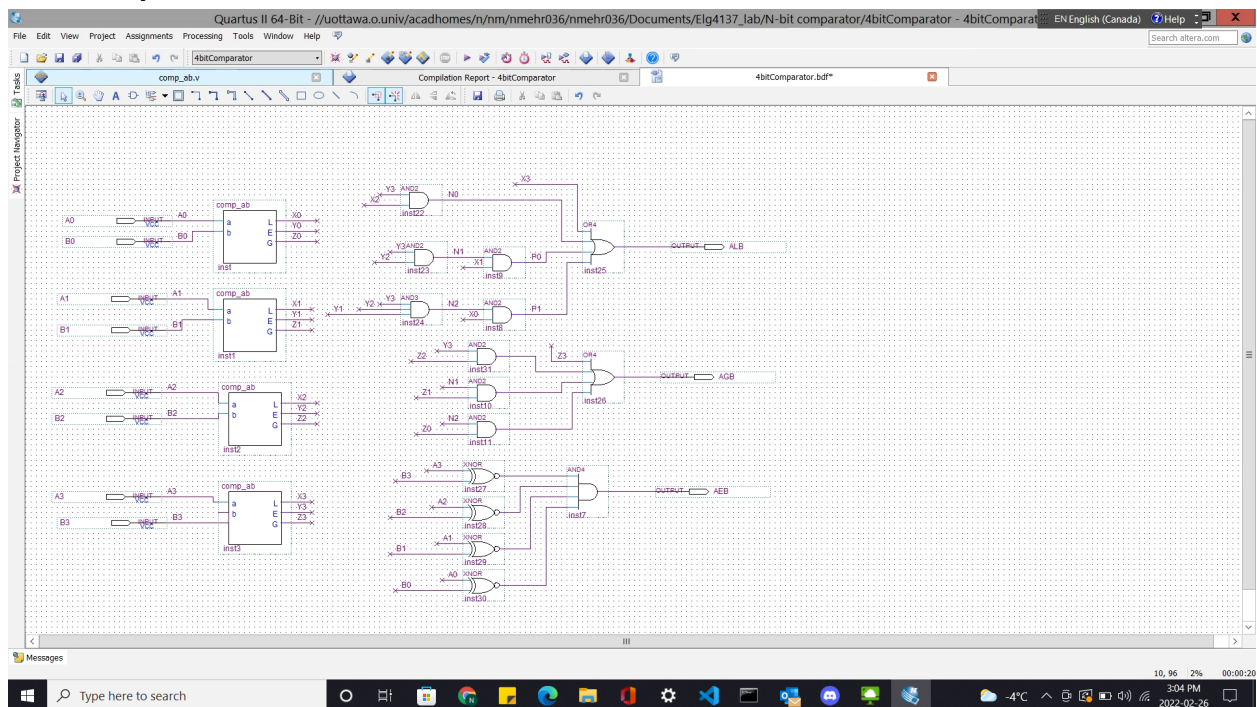
Part 2: Design of an N-bit Comparator

A N-bit comparator compares two N-bit numbers and evaluates whether the numbers are equal to one another or if one is larger than the other.

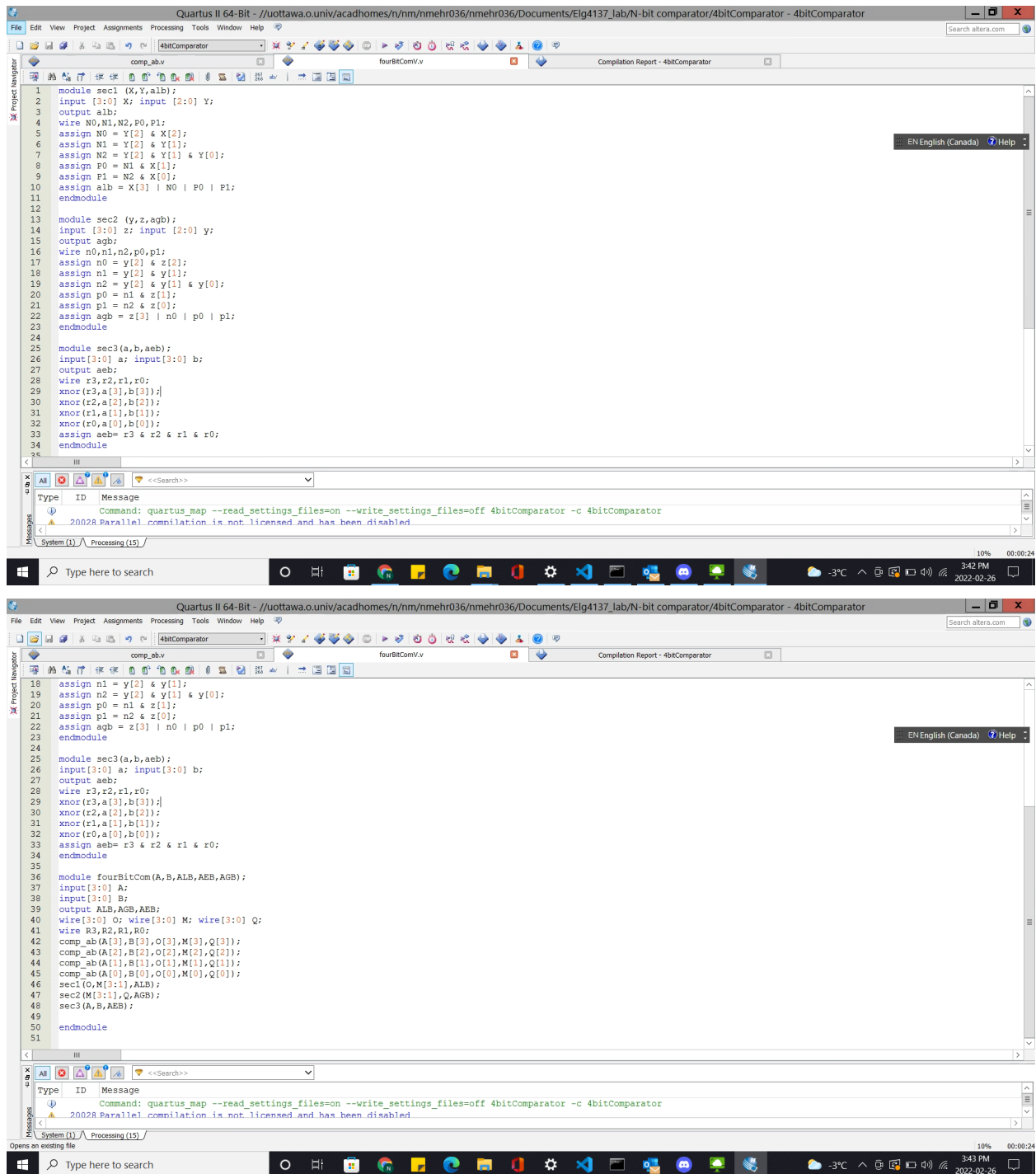
To develop a 4-bit comparator, a 1-bit comparator is designed first and then converted into a block representation. Combining four of these logic circuits to produce the 4-bit comparator.



4-bit Comparator Model



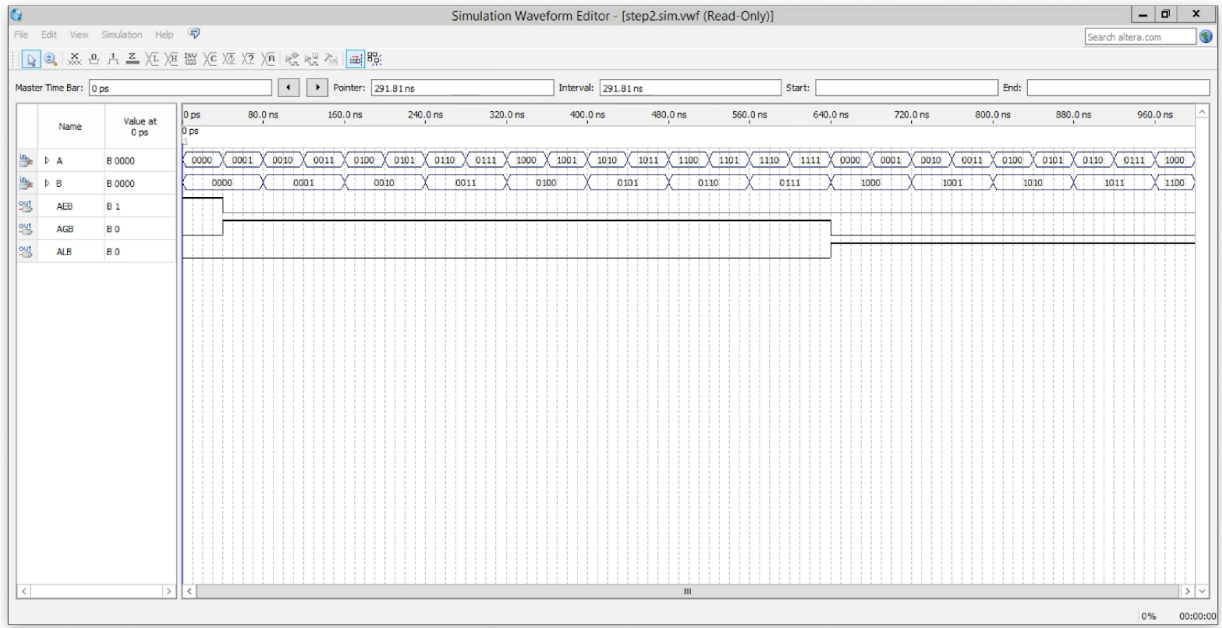
4-bit Comparator Verilog Program



```
1 module sec1 (X,Y,alb);
2   input [3:0] X; input [2:0] Y;
3   output alb;
4   wire n0,n1,n2,p0,p1;
5   assign n0 = Y[2] & X[2];
6   assign n1 = Y[2] & Y[1];
7   assign n2 = Y[2] & Y[1] & Y[0];
8   assign p0 = n1 & X[1];
9   assign p1 = n2 & X[0];
10  assign alb = X[3] | n0 | p0 | p1;
11 endmodule
12
13 module sec2 (y,z,agb);
14   input [3:0] z; input [2:0] y;
15   output agb;
16   wire n0,n1,n2,p0,p1;
17   assign n0 = y[2] & z[2];
18   assign n1 = y[2] & y[1];
19   assign n2 = y[2] & y[1] & y[0];
20   assign p0 = n1 & z[1];
21   assign p1 = n2 & z[0];
22   assign agb = z[3] | n0 | p0 | p1;
23 endmodule
24
25 module sec3(a,b,aeb);
26   input [3:0] a; input [3:0] b;
27   output aeb;
28   wire r3,r2,r1,r0;
29   xnor(r3,a[3],b[3]);
30   xnor(r2,a[2],b[2]);
31   xnor(r1,a[1],b[1]);
32   xnor(r0,a[0],b[0]);
33   assign aeb= r3 & r2 & r1 & r0;
34 endmodule
35
36 module fourBitCom (A,B,ALB,AEB,AGB);
37   input [3:0] A;
38   input [3:0] B;
39   output ALB,AGB,AEB;
40   wire [3:0] Q; wire [3:0] M; wire [3:0] Q;
41   wire R3,R2,R1,R0;
42   comp_ab(A[3],B[3],Q[3],M[3],Q[3]);
43   comp_ab(A[2],B[2],Q[2],M[2],Q[2]);
44   comp_ab(A[1],B[1],Q[1],M[1],Q[1]);
45   comp_ab(A[0],B[0],Q[0],M[0],Q[0]);
46   sec1(Q,M[3:1],ALB);
47   sec2(M[3:1],Q,AGB);
48   sec3(A,B,AEB);
49 endmodule
50
51
```

Command: quartus_map --read_settings_files=on --write_settings_files=off 4bitComparator -c 4bitComparator
20028 Parallel compilation is not licensed and has been disabled

4-bit Comparator Waveform



After simulation of the 4-bit comparator all results were accurate with what was expected. Looking at the waveform diagram above it is clear when A is greater than B, AGB is active. When A is less than B, ALB is active and when A is equal to B, AEB is active.