

Analog Assignment 4

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1) A RC phase shift oscillator (3 stage) for 50 kHz sin wave signal output.

ANSWER :

Handwritten solution for a 3-stage RC phase shift oscillator.

Circuit Diagrams:

- Op-Amp Buffer:** A non-inverting op-amp configuration with a feedback resistor R_f and a resistor R_1 from the inverting input to ground. The gain is $A = 29$. The input is V_{in} and the output is V_{out} .
- Three-Stage RC Network:** A cascade of three RC stages. Each stage consists of a capacitor C in series and a resistor R in shunt to ground. The input is V_{in} , and the output of the third stage is V_{out} . The attenuation of the network is $\beta = 1/29$.

Frequency Formulas:

$$f = \frac{1}{2\pi RC\sqrt{6}}$$

$$f = \frac{1}{2\pi RC\sqrt{2N}} \text{ for } N \text{ stages.}$$

Node Analysis:

At Node V_2 :

$$I_2 = \frac{V_2 - V_o}{jX_c} \quad \text{and} \quad V_o = I_3 \times R$$

$$\frac{V_o}{V_{in}} = \frac{-1}{29}$$

$$\Rightarrow V_o \left[\frac{1}{R} + \frac{1}{-jX_c} \right] = \frac{V_2}{-jX_c}$$

$$V_o \left[\frac{R + jX_c}{-jRX_c} \right] = \frac{V_2 \omega C}{-j}$$

$$V_o \left[\omega CR + j \right] = V_2 \omega C$$

$$\Rightarrow V_o + \frac{jV_o}{\omega CR} = V_2$$

$$\text{or } V_2 = V_o + \frac{jV_o}{\omega CR} = V_o \left[1 + \frac{j}{\omega CR} \right] \quad \text{--- (1)}$$

$$V_1 = V_2 + I_2 \times R = V_o \left[1 + \frac{j}{\omega CR} \right] + \frac{V_o}{R} \left[2 + \frac{j}{\omega CR} \right] \left[\frac{1}{j\omega C} \right]$$

$$V_1 = V_o \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] \quad \text{--- (2)}$$

$$I_1 = \frac{V_1}{R} + I_2 \Rightarrow I_1 = \frac{V_0}{R} \left[\frac{3}{j\omega RC} + \frac{4}{j\omega RC} - \frac{1}{\omega^2 C^2 R^2} \right]$$

$$V_{in} = V_1 + \frac{I_1}{j\omega C} = V_0 \left[1 + \frac{3}{j\omega RC} - \frac{1}{\omega^2 C^2 R^2} \right] + \frac{V_0}{R} \left[\frac{1}{j\omega C} \right] \left[\frac{3}{j\omega RC} + \frac{4}{j\omega RC} - \frac{1}{\omega^2 C^2 R^2} \right]$$

$$V_{in} = V_0 \left[1 + \frac{6}{j\omega RC} - \frac{5}{\omega^2 C^2 R^2} - \frac{1}{j\omega^3 C^3 R^3} \right]$$

$$\frac{6}{j\omega RC} - \frac{1}{\omega^3 C^3 R^3} = 0$$

$$\Rightarrow \omega = \frac{1}{\sqrt{6} RC} \rightarrow V_{in} = V_0 \left[1 - \frac{5}{\omega^2 C^2 R^2} \right]$$

$$V_{in} = V_0 \left[1 - \frac{5}{\frac{1}{6R^2C^2} \times R^2 C^2} \right]$$

The value of R is
assumed fixed
and only C is
changed.

$$\frac{V_{in}}{V_0} = \frac{1}{2} - 29$$

From the basics of an RC phase shift oscillator, we have to make a sine wave of frequency 50KHz

$$f = \frac{1}{2\pi RC\sqrt{6}}$$

Assume a reasonable value for R (i.e., $R_4/R_5/R_2$), let's take 1K. Therefore,

$$C = \frac{1}{2\pi \times 1 \times 10^3 \times \sqrt{6}}$$

$$C = 1.3nF$$

Now for getting a gain $A = 29$

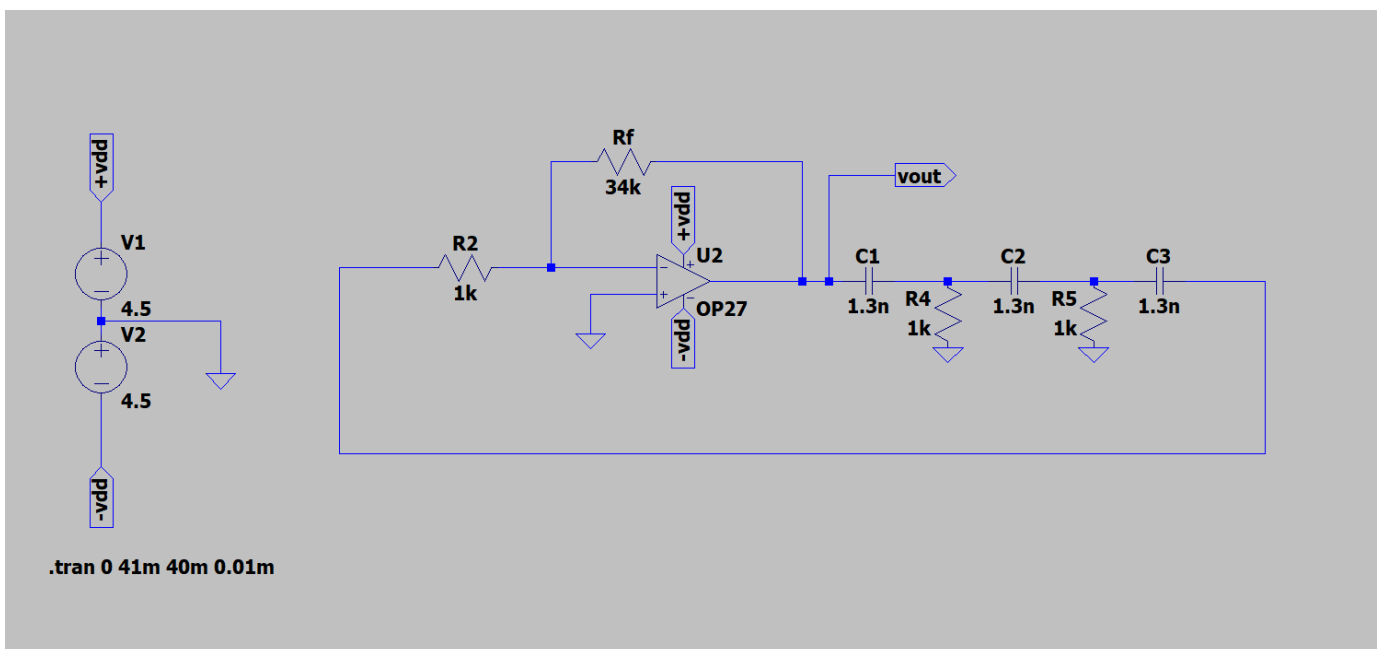
$$\frac{R_f}{R_2} = 29$$

$$R_f = 29k$$

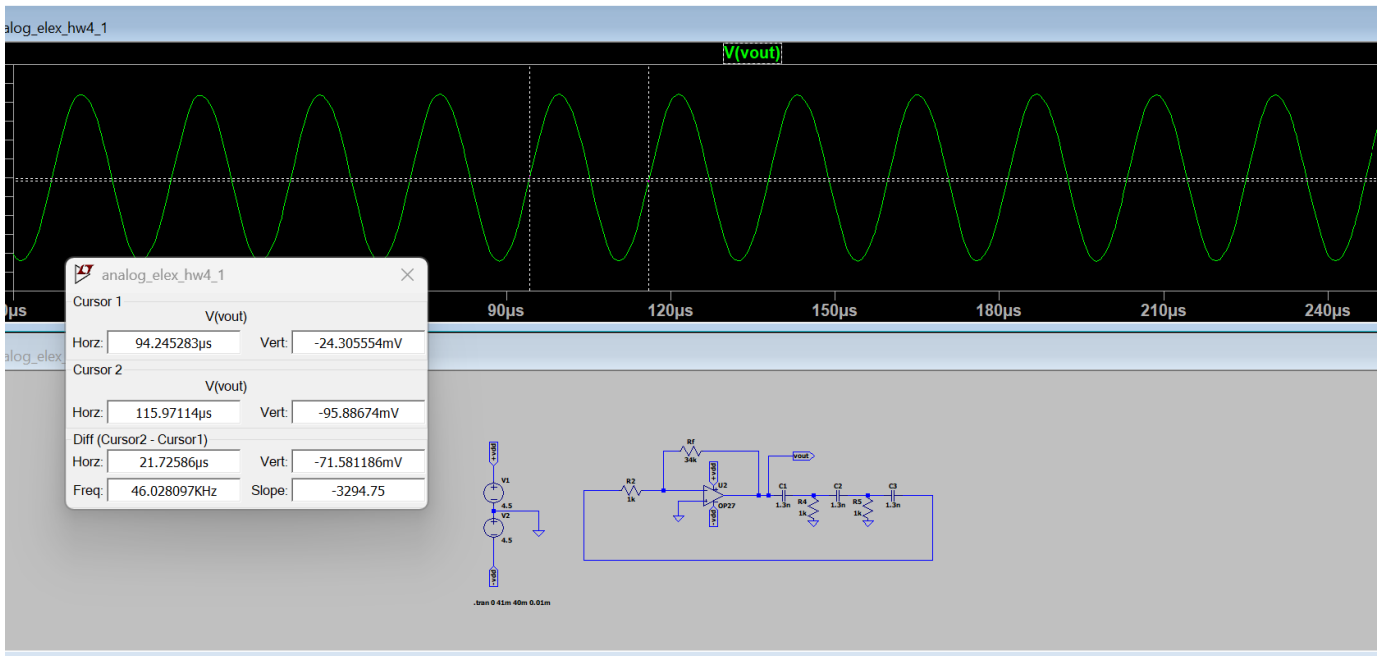
But instead, we take a value slightly higher than 29K so that we can reduce the noise components.

Circuit diagram:

From the output plot we can see that T (time period) = $21\mu s \Rightarrow f = 47KHz$.

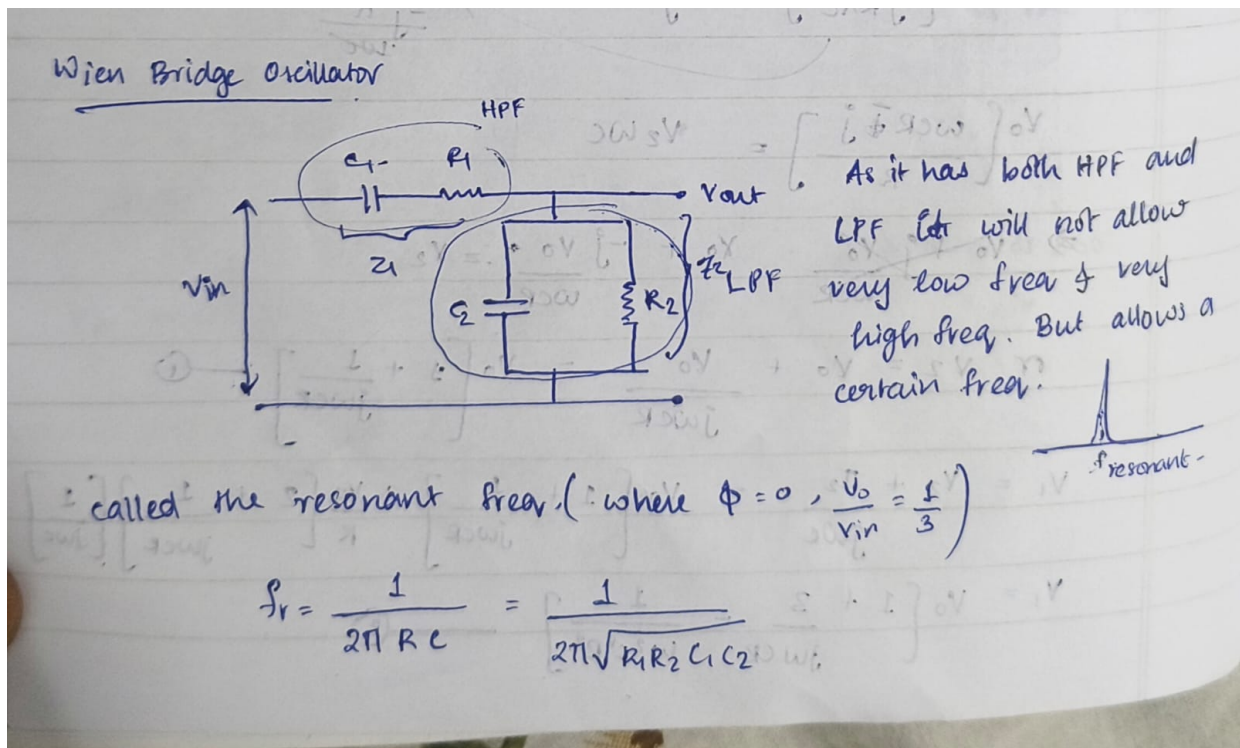


Plot of Vout:



2) A Wien bridge oscillator for 50 kHz sin wave signal output.

ANSWER :



Taking

$$f = \frac{1}{2\pi \sqrt{R_3 R_4 C_1 C_2}}$$

Taking $R_3 = R_4 = 1k$ and $C_1 = C_2$,

$$C = \frac{1}{2\pi \times 1 \times 10^3 \times 50 \times 10^3}$$

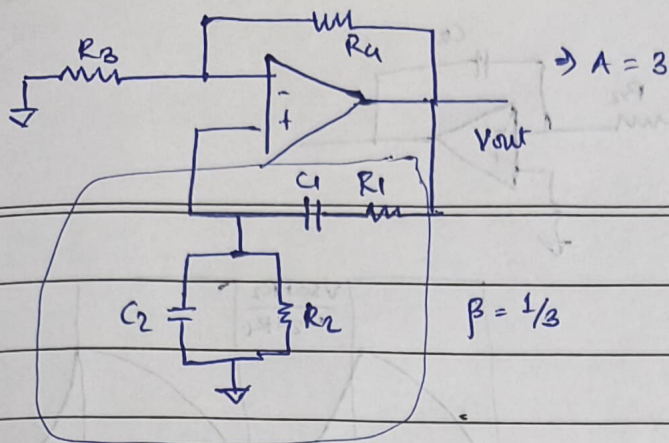
$$C = 3.18nF$$

Now to obtain a gain $A = 3$

$$1 + \frac{R_f}{R_2} = 3$$

$$R_f = 2k$$

But instead we take a value slightly higher than 2K so that we can reduce the noise components.



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$$\text{where } A = 1 + \frac{R_4}{R_3}$$

$$\frac{R_4}{R_3} = 2$$

$$\beta = 1/3$$

for a wanted freq. fr take $R_1 = R_2$ & $C_1 = C_2$.

$$\frac{V_o}{V_{in}} = \frac{Z_2}{Z_1 + Z_2}$$

$$Z_1 = \frac{R_1 + \frac{1}{j\omega C_1}}{j\omega C_1}$$

$$\frac{V_o}{V_{in}} = \frac{\frac{R_2}{1 + j\omega R_2 C_2}}{\frac{R_1 + \frac{1}{j\omega C_1}}{j\omega C_1} + \frac{R_2}{1 + j\omega R_2 C_2}}$$

$$= \frac{R_2(j\omega C_1)}{R_1(j\omega C_1)(1 + j\omega R_2 C_2) + 1 + j\omega R_2 C_2}$$

$$\frac{V_o}{V_{in}} = \frac{j\omega R_2 C_1}{1 - \omega^2 R_1 R_2 C_1 C_2 + j\omega(R_1 C_1 + R_2 C_2 + R_2 C_1)}$$

0 as phase shift = 0

$$\omega^2 R_1 R_2 C_1 C_2 = 0$$

$$\omega = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}$$

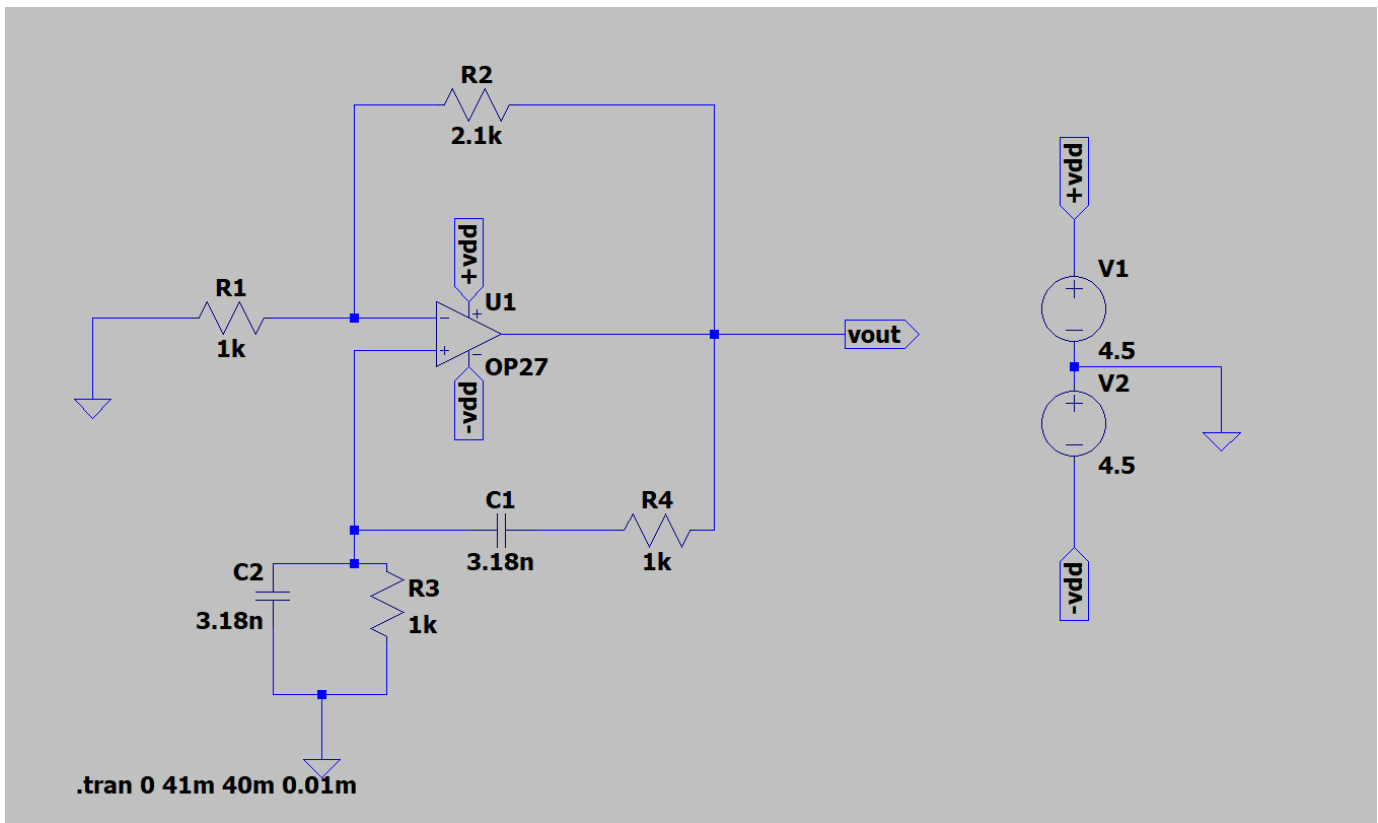
$$\Rightarrow \frac{V_o}{V_{in}} = \frac{R_2 C_1}{R_1 C_1 + R_2 C_2 + R_2 C_1} \quad \text{for } R_1 = R_2, C_1 = C_2$$

$$\frac{V_o}{V_{in}} = \left| \frac{1}{3} \right| = \beta$$

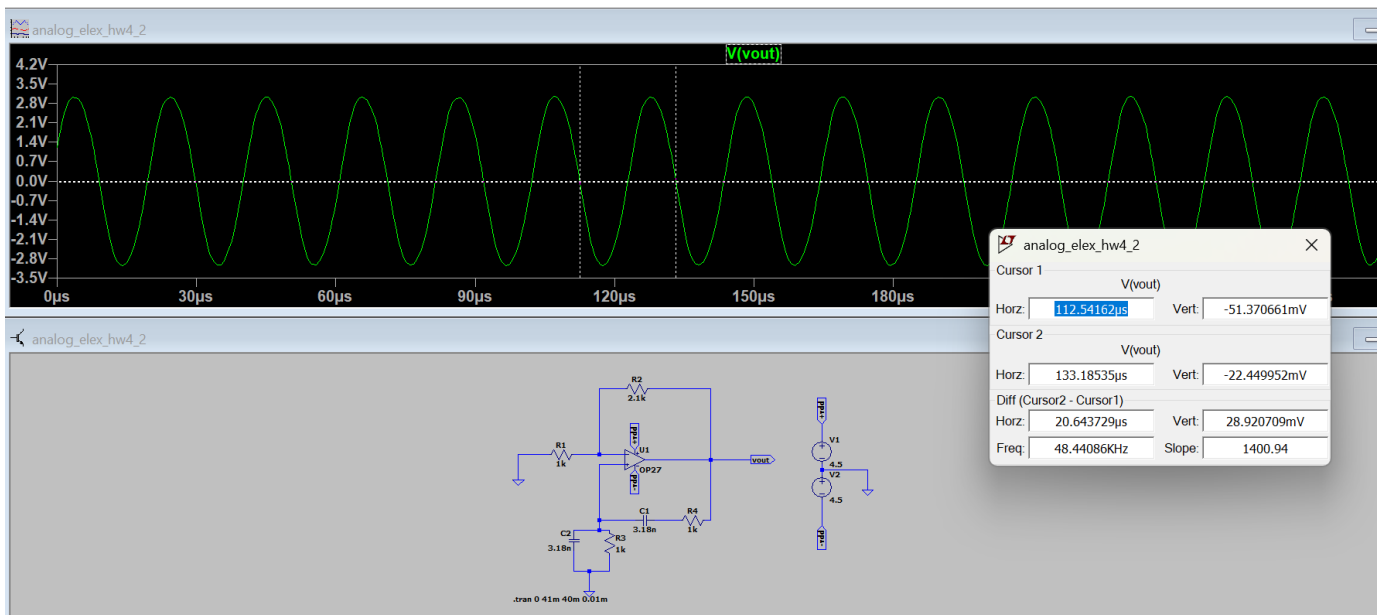
$$A\beta = 1 \Rightarrow A = 3$$

$$RC = \frac{1}{2\pi \cdot 5000}$$

$$C = \frac{1}{2\pi \cdot 5000 \times 10^5} = 3.18 \text{ nF}$$



Plot of vout:



3) A Square wave generator for a fundamental frequency of 10 kHz signal output. Use an integrator and convert the square wave signal into a triangular wave.

ANSWER :

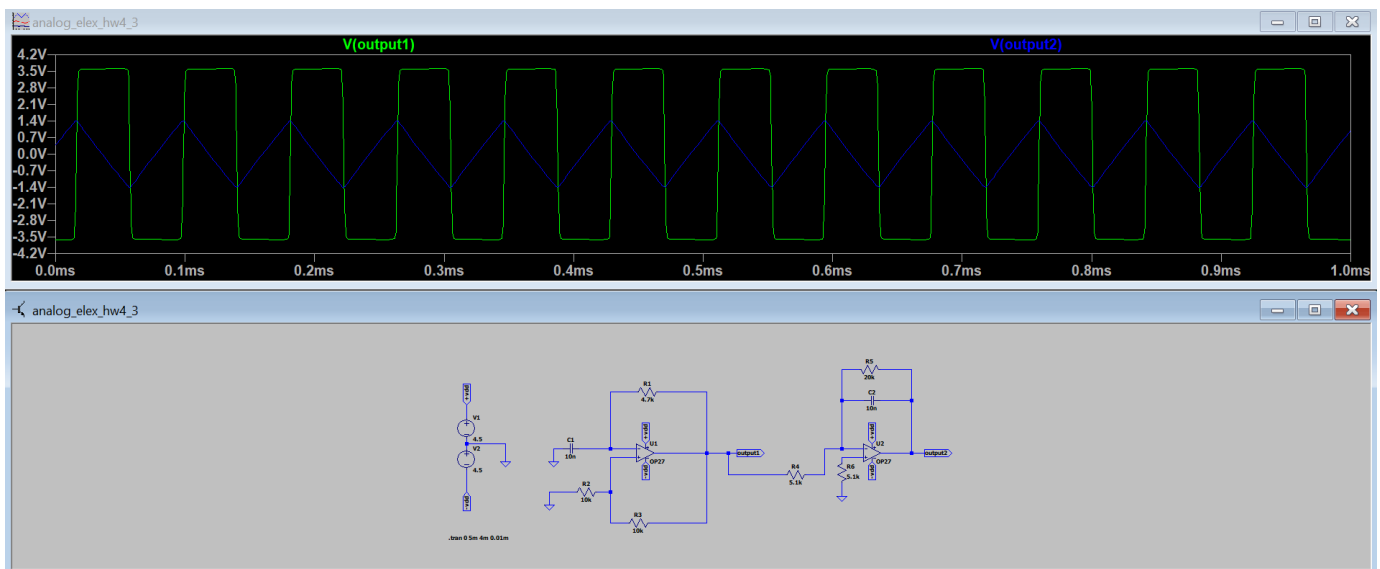
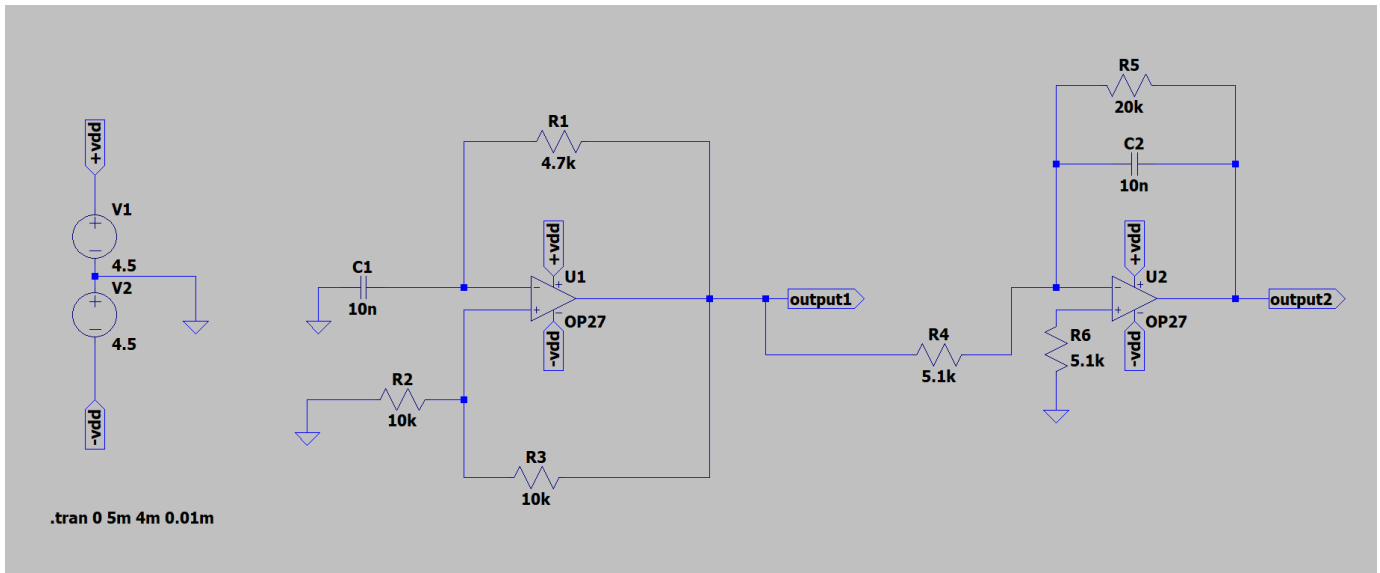
It uses the concepts of the Schmitt trigger. Calculating the time period,

$$T = 2R_1C_1 \ln\left(\frac{2R_2 + R_3}{R_3}\right)$$

take $R_2 = R_3 = 1k$ and C_1 as $10nF$,

$$0.1m = 2R_1 \times 10 \times 10^{-9} \log(3)$$

$$R_1 = 4.7k$$



4)A Square wave generator for a fundamental frequency of 10 kHz signal output. Use an integrator and convert the square wave signal a sawtooth wave with rise time = 1/2 fall time.

ANSWER :

at tripping point

$$V_{sat}R_2 = -V_oR_3$$

—(1)

applying KCL at the node where R1 is situated,

$$\frac{V_{sat} - V_{in}}{R_1} = -\frac{C_1 d(V_o - V_{in})}{dt}$$

$$V_o = -\frac{V_{sat} - V_{in}}{CR_1}$$

substituting (1)

$$t = \frac{V_{sat} \times R_1 R_2 C_1}{R_3 (V_{sat} - V_{in})}$$

for $V_{sat} = +V_{sat}$ the time is rising and when $V_{sat} = -V_{sat}$ time was falling

$$\Rightarrow t_{rise} = 2 \frac{V_{sat} \times R_1 R_2 C_1}{R_3 (V_{sat} + V_{in})}$$

$$\Rightarrow t_{fall} = 2 \frac{V_{sat} \times R_1 R_2 C_1}{R_3 (V_{sat} - V_{in})}$$

Given rise = 1/2 fall

$$V_{in} = \frac{V_{sat}}{3}$$

V_{sat} is 4.5V $\Rightarrow V_{in} = 1.5V$.

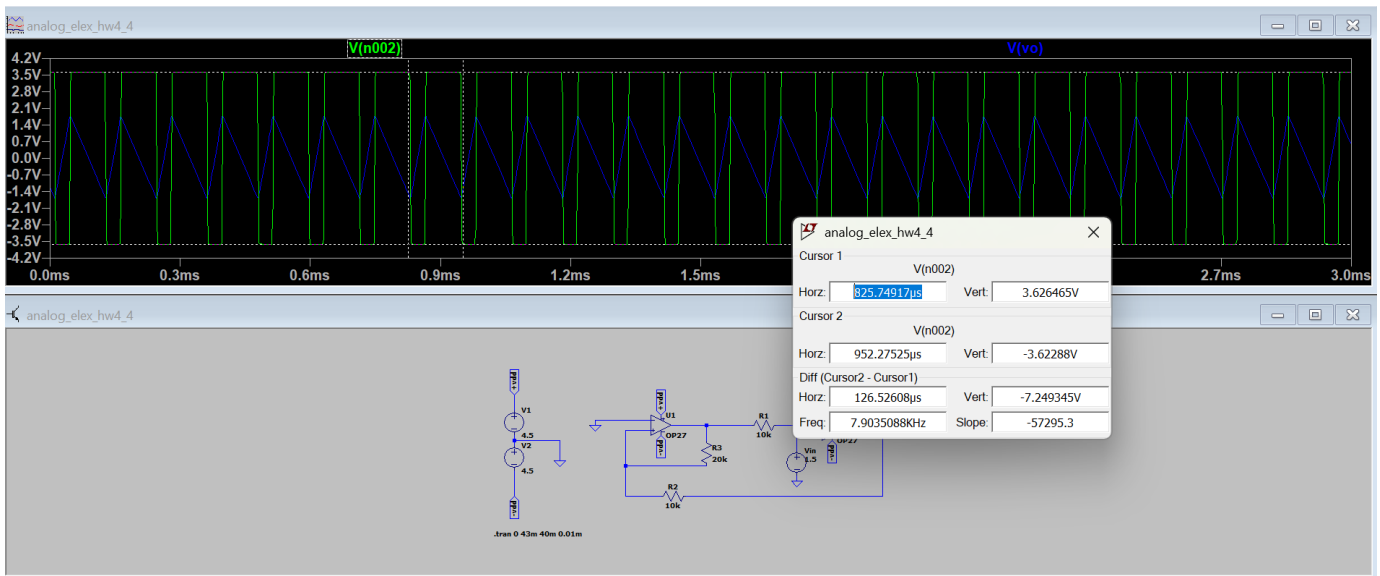
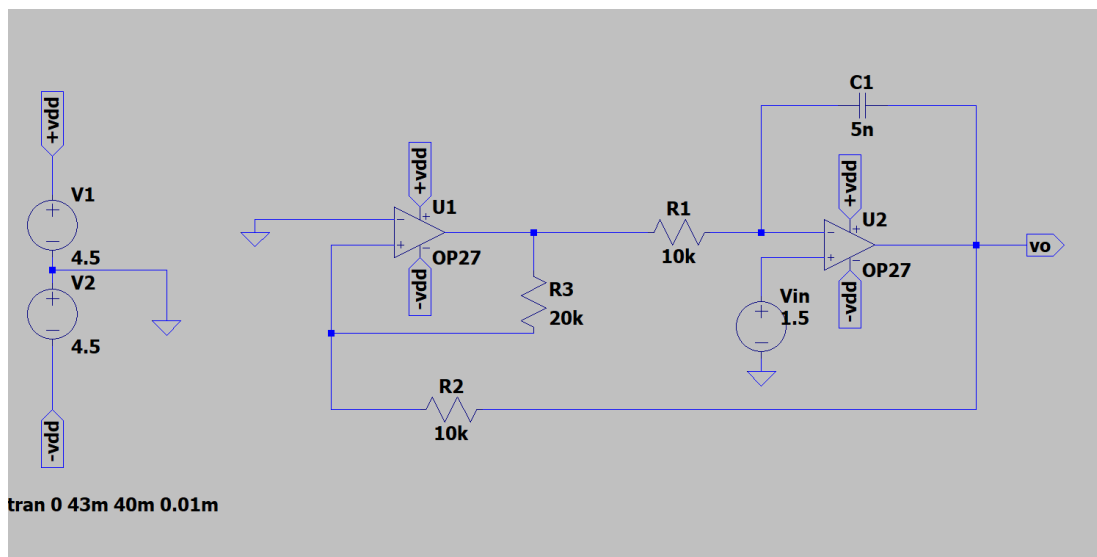
also, the total time period

$$T = \frac{4R_1 R_2 C_1}{R_3}$$

$R_2 = R_1 = 10k$, $R_3 = 20k$

$$10^{-4} = \frac{4 \times 10k \times 10k \times C_1}{20k}$$

$$C_1 = 5n$$



5) Design a schmitt trigger circuit and show the hesteresis curve with V_{th} (+ and -ve) = +- 200mV.

ANSWER :

Calculations for R1 and R2,

$$V_{th} = \frac{V_{Sat} \times R1}{R1 + R2}$$

Lets take R1 =1k

$$200mV = \frac{15 \times 1K}{1K + R2}$$

$$R2 = 62K$$

