

M1 - Systavy rovníc s dvomi neznámymi

Skupina A

(Blahovský, Brutovský, Dravecká,
Hudáková, Macko, Starinský,)

1/ Riešte sústavu rovníc, urobte skúšku
a zapíšte množinu koreňov:

$$\begin{array}{rcl} 3x + y = 9 & / \cdot (-2) \\ \underline{x + 2y = -2} & \\ -6x - 2y = -18 &] (+) \\ \underline{x + 2y = -2} & \\ -5x = -20 & / : (-5) \\ \underline{x = 4} & \end{array}$$

$$\begin{array}{rcl} 3 \cdot 4 + y = 9 & / -12 \\ \underline{y = -3} & \end{array}$$

sk.: $L_1 = 3 \cdot 4 - 3 = 12 - 3 = 9$

$$P_1 = 9$$

$$L_1 = P_1$$

$$L_2 = 4 + 2 \cdot (-3) = 4 - 6 = -2$$

$$P_2 = -2$$

$$L_2 = P_2 \quad \underline{K = \{[4; -3]\}}$$

2/ Riešte sústavu rovníc a zapíšte množinu
koreňov:

$$\frac{3x-2y}{5} + \frac{2x-3y}{3} = 1 \quad / \cdot 15$$

$$\frac{2x-6y}{3} + \frac{4x-3y}{2} = 1 \quad / \cdot 6$$

$$\begin{array}{rcl} 3(3x-2y) + 5(2x-3y) & = & 15 \\ \underline{2(2x-6y) + 3(4x-3y) = 6} & & \\ 9x-6y + 10x-15y & = & 15 \\ \underline{4x-12y + 12x-9y = 6} & & \\ 19x - 21y & = & 15 \quad] (-) \\ \underline{16x - 21y = 6} & & \\ 3x & = & 9 \quad / : 3 \\ \underline{x = 3} & & \end{array}$$

$$\begin{array}{rcl} 19 \cdot 3 - 21y & = & 15 \quad / -57 \\ -21y & = & -42 \quad / : (-21) \\ \underline{y = 2} & & \end{array}$$

$$\underline{K = \{[3; 2]\}}$$

Skupina B

(Body, Falatko, Hudák,
Jenčík, Konečná, Varga)

1/ Riešte sústavu rovníc, urobte skúšku
a zapíšte množinu koreňov:

$$\begin{array}{rcl} 3x - y = 6 & / \cdot 2 \\ \underline{x + 2y = -5} & \\ 6x - 2y = 12 &] (+) \\ \underline{x + 2y = -5} & \\ 7x = 7 & / : 7 \\ \underline{x = 1} & \end{array}$$

$$\begin{array}{rcl} 3 \cdot 1 - y = 6 & / -3 \\ -y = 3 & / : (-1) \\ \underline{y = -3} & \end{array}$$

sk.: $L_1 = 3 \cdot 1 - (-3) = 3 + 3 = 6$

$$P_1 = 6$$

$$L_1 = P_1$$

$$L_2 = 1 + 2 \cdot (-3) = 1 - 6 = -5$$

$$P_2 = -5$$

$$L_2 = P_2 \quad \underline{K = \{[1; -3]\}}$$

2/ **Riešte sústavu rovníc a zapíšte množinu koreňov:**

$$\frac{2x-1}{5} + \frac{3y-2}{4} = 2 \quad /.20$$

$$\frac{3x+1}{5} - \frac{3y+2}{4} = 0 \quad /.20$$

$$\begin{array}{r} 4(2x-1) + 5(3y-2) = 40 \\ 4(3x+1) - 5(3y+2) = 0 \\ \hline 8x - 4 + 15y - 10 = 40 \quad /+14 \\ 12x + 4 - 15y - 10 = 0 \quad /+6 \\ \hline 8x + 15y = 54 \quad](+) \\ 12x - 15y = 6 \\ \hline 20x = 60 \quad /:20 \\ \underline{x = 3} \end{array}$$

$$\begin{array}{r} 8.3 + 15y = 54 \quad /-24 \\ 15y = 30 \quad /:15 \\ \underline{y = 2} \end{array}$$

$$\underline{K = \{[3; 2]\}}$$

Bodovanie:

- 1.úloha – 8 bodov
- 2.úloha – 10 bodov

Skupina C

(Brettschneider, Fedor, Kolesárová,
Rejdovjanová, Schmidt, Vojtková)

1/ **Riešte sústavu rovníc, urobte skúšku a zapíšte množinu koreňov:**

$$\begin{array}{r} 5x - y = 1 \quad /.6 \\ 3x + 6y = -6 \\ 30x - 6y = 6 \quad](+) \\ \hline 3x + 6y = -6 \\ 33x = 0 \quad /:33 \\ \underline{x = 0} \end{array}$$

$$\begin{array}{r} 5.0 - y = 1 \quad /:(-1) \\ \underline{y = -1} \end{array}$$

$$\begin{array}{l} \text{sk.: } L_1 = 5.0 - (-1) = 0 + 1 = 1 \\ P_1 = 1 \\ L_1 = P_1 \end{array}$$

$$\begin{array}{l} L_2 = 3.0 + 6 \cdot (-1) = 0 - 6 = -6 \\ P_2 = -6 \\ L_2 = P_2 \end{array}$$

$$\underline{K = \{[0; -1]\}}$$

Stupnica:

- 18,0-16,0 výborný
- 15,5-13,5 chválitebný
- 13,0-09,0 dobrý
- 08,5-06,5 dostatočný

2/ **Riešte sústavu rovníc a zapíšte množinu koreňov:**

$$\frac{x+1}{2} = \frac{y-2}{3} + 1 \quad /.6$$

$$\frac{x+2}{5} + 2y = 11 \quad /.5$$

$$\begin{array}{r} 3(x+1) = 2(y-2) + 6 \quad /-3 \quad /-2y \\ x+2 + 10y = 55 \quad /-2 \\ \hline 3x - 2y = -1 \quad /.5 \\ \underline{x + 10y = 53} \\ 15x - 10y = -5 \quad](+) \\ \hline x + 10y = 53 \\ 16x = 48 \quad /:16 \\ \underline{x = 3} \end{array}$$

$$\begin{array}{r} 3 + 10y = 53 \quad /-3 \\ 10y = 50 \quad /:10 \\ \underline{y = 5} \end{array}$$

$$\underline{K = \{[3; 5]\}}$$

