

ZBIERKA ÚLOH Z MATEMATIKY

LINEÁRNE ROVNICE

JAKUB MEDVEC

9.A

Prvý stupeň obt'aznosti

$$5x+2=1+3x$$

$$L'=5x+2=5 \cdot (-0.5)+2=-0.5$$

$$5x-3x=-2+1$$

$$P=1+3x=1+3 \cdot (-0.5)=-0.5$$

$$2x=-1$$

$$x=-1:2$$

$$x=-0.5$$

$$3+4x-2=5x+8+1x$$

$$L'=3+4x-2=3+4 \cdot (-3.5)-2=-13$$

$$4x-5x-1x=-3+2+8$$

$$P=5x+8+1x=5 \cdot (-3.5)+8+1 \cdot (-3.5)=-13$$

$$-2x=7$$

$$x=7:(-2)$$

$$x=-3.5$$

$$2x+2=x+4$$

$$L'=2x+2=2 \cdot 2+2=6$$

$$2x-x=-2+4$$

$$P=x+4=2+4=6$$

$$1x=2$$

$$x=2:1$$

$$x=2$$

$$3+x-1=8+2x$$

$$L'=3+x-1=3+(-6)-1=-4$$

$$1x-2x=-3+1+8$$

$$P=8+2x=8+2 \cdot (-6)=-4$$

$$-1=6$$

$$x=6(-1)$$

$$x=-6$$

$$4x+1=8+2x$$

$$l'=4x+1=4.3,5+1=15$$

$$4x-2x=-1+8$$

$$P=8+2x=8+2.3,5=15$$

$$2x=7$$

$$x=7:2$$

$$x=3,5$$

$$8+2x-3=1x+3$$

$$l'=8+2x-3=8+2.(-2)-3=1$$

$$2x-1x=-8+3+3$$

$$P=1x+3=1.(-2)+3=1$$

$$1=-2$$

$$x=-2:1$$

$$x=-2$$

$$7+2+x=3x$$

$$l'=7+2+x=7+2+4,5=13,5$$

$$x-3x=-7-2$$

$$P=3x=3.4,5=13,5$$

$$-2x=-9$$

$$x=-9:(-2)$$

$$x=4,5$$

$$11+x=x+4x$$

$$l'=11+x=11+2,75=13,75$$

$$x-x-4x=-11$$

$$P=x+4x=2,75+4.2,75=13,75$$

$$-4x=-11$$

$$x=-11:(-4)$$

$$x=2,75$$

$$2+3=4x-2x$$

$$l'=2+3=5$$

$$-4x+2x=-2-3$$

$$P=4x-2x=4 \cdot 2,5-2 \cdot 2,5=5$$

$$-2x=-5$$

$$x=-5: (-2)$$

$$x=2,5$$

$$1x+2=5x+1$$

$$l'=1x+2=1 \cdot 0,25+2=2,25$$

$$1x-5x=-2+1$$

$$P=5x+1=5 \cdot 0,25+1=2,25$$

$$-4x=-1$$

$$x=-1: (-4)$$

$$x=0,25$$

$$1+5x=16+2x$$

$$l'=1+5x=1+5 \cdot 5=26$$

$$5x-2x=-1+16$$

$$P=16+2x=16+2 \cdot 5=26$$

$$3x=15$$

$$x=15:3$$

$$x=5$$

$$2x+2=x+4$$

$$l'=2x+2=2 \cdot 2+2=6$$

$$2x-x=-2+4$$

$$P=x+4=6$$

$$1x=2$$

$$x=2:1$$

$$x=2$$

$$x+5=-10$$

$$l'=-15+5=-10$$

$$x=-5-10$$

$$P=-10$$

$$1x=-15$$

$$x=-15:1$$

$$x=-15$$

$$2x-8=20$$

$$l'=2x-8=2 \cdot 14-8=20$$

$$2x=8+20$$

$$P=20$$

$$2x=28$$

$$x=28:2$$

$$x=14$$

$$x+6=10$$

$$l'=4+6=10$$

$$x=-6+10$$

$$P=10$$

$$1x=4$$

$$x=4:1$$

$$x=4$$

Druhý stupeň obt'ažnosti

$$15(x+2)=6(2x+7)$$

$$l'=15(x+2)=15(4+2)=90$$

$$15x+30=12x+42$$

$$P=6(2x+7)=6(2.4+7)=90$$

$$15x-12x=-30+42$$

$$-3x=12$$

$$x=12: (-3)$$

$$x=4$$

$$8(9+2x)=5(2-3x)$$

$$l'=8(9+2x)=8(9+2.(-2))=40$$

$$72+16x=10-15x$$

$$P=5(2-3x)=5(2-3.(-2))=40$$

$$16x+15x=-72+10$$

$$31x=-62$$

$$x=-62:31$$

$$x=-2$$

$$0,5(x+8)=0,25(20-2x)$$

$$l'=0,5(x+8)=0,5(1+8)=4,5$$

$$0,5x+4=5-0,5x$$

$$P=0,25(20-2x)=0,25(20-2.1)=4,5$$

$$0,5x+0,5x=-4+5$$

$$1x=1$$

$$x=1:1$$

$$x=1$$

$$2(x-1)+4(x-3)=2(x+5)+3(x-2)$$

$$l'=2(x-1)+4(x-3)=2(18-1)+4(18-3)=94$$

$$2x-2+4x-12=2x+10+3x-6$$

$$P=2(x+5)+3(x-2)=2(18+5)+3(18-2)=94$$

$$2x+4x-2x-3x=2+12+10-6$$

$$1x=18$$

$$x=18:1$$

$$x=18$$

$$2(x-1)-5=3(3+x)+x$$

$$l'=2(x-1)-5=2(-8-1)-5=-23$$

$$2x-2-5=9+3x+x$$

$$P=3(3+x)+x=3(3+(-8))+(-8)=-23$$

$$2x-3x-x=2+5+9$$

$$-2x=16$$

$$x=16: (-2)$$

$$x=-8$$

$$4(x-1)-x=3(1+x)-7$$

$$4x-4-x=3+3x-7$$

$$4x-x-3x=4+3-7$$

$$0x=0$$

má nekonečno veľa riešení

$$7x-(x+3)=3(2x+1)$$

$$7x-x-3=6x+3$$

$$7x-x-6x=3+$$

$$0x=6$$

nemá riešenie

$$4(3x+2)=5(2x-7)+x$$

$$l'=4(3x+2)=4(3 \cdot (-43)+2)=-508$$

$$12x+8=10x-35+x$$

$$P=5(2x-7)+x=5(2 \cdot (-43)-7)+(-43)=-508$$

$$12x-10x-x=-8-35$$

$$1x=-43$$

$$x=-43:1$$

$$x=-43$$

$$13(x-0,1)=6(2x+0,1)$$

$$l'=13(x-0,1)=13(1,9-0,1)=23,4$$

$$13x-1,3=12x+0,6$$

$$P=6(2x+0,1)=6(2 \cdot 1,9+0,1)=23,4$$

$$13x-12x=1,3+0,6$$

$$1x=1,9$$

$$x=1,9:1$$

$$x=1,9$$

$$4x-(x+1)=5$$

$$l'=4x-(x+1)=4 \cdot 2-(2+1)=5$$

$$4x-x-1=5$$

$$P=5$$

$$4x-x=1+5$$

$$3x=6$$

$$x=6:3$$

$$x=2$$

$$x+3x-(x+4)=11$$

$$l'=x+3x-(x+4)=5+3\cdot 5-(5+4)=11$$

$$x+3x-x-4=11$$

$$P=11$$

$$x+3x-x=4+11$$

$$3x=15$$

$$x=15:3$$

$$x=5$$

$$(5x+6)-2(x-2)=x-2-(x-3)$$

$$l'=(5x+6)-2(x-2)=(5\cdot (-3)+6)-2(-3-2)=1$$

$$5x+6-2x+4=x-2-x+3$$

$$P=x-2-(x-3)=-3-2-(-3-3)=1$$

$$5x-2x-x+x=-6-4+3-2$$

$$3x=-9$$

$$x=-9:3$$

$$x=-3$$

$$2(x-5)+15=3(x-4)+10$$

$$l'=2(x-5)+15=2(7-5)+15=19$$

$$2x-10+15=3x-12+10$$

$$P=3(x-4)+10=3(7-4)+10=19$$

$$2x-3x=10-15-12+10$$

$$-1x=-7$$

$$x=-7: (-1)$$

$$x=7$$

$$-0,5(x-2)+1,5x=2x+5$$

$$-0,5+1+1,5x=2x+5$$

$$-0,5x+1,5x-2x=-1+5$$

$$-1x=4$$

$$x=4: (-1)$$

$$x=-4$$

$$L'=-0,5(x-2)+1,5x=-0,5(-4-2)+1,5(-4)=-3$$

$$P=2x+5=2(-4)+5=-3$$

$$4(x-1)-x=3(1+x)-7$$

$$4x-4-x=3+3x-7$$

$$4x-x-3x=4+3-7$$

$$-1x=0$$

$$x=0: (-1)$$

$$x=0$$

$$L'=4(x-1)-x=4(0-1)-0=-4$$

$$P=3(1+x)-7=3(1+0)-7=-4$$

Tretí stupeň obt'ážnosti

$$\frac{x}{3} + \frac{1}{2} = \frac{x}{2} \quad /.6$$

$$L = \frac{x}{3} + \frac{1}{2} = \frac{3}{3} + \frac{1}{2} = \frac{6+3}{6} = \frac{9}{6} = \frac{3}{2}$$

$$6 \cdot \frac{x}{3} + 6 \cdot \frac{1}{2} = 6 \cdot \frac{x}{2}$$

$$2x + 3 = 3$$

$$P = \frac{3}{2}$$

$$2x - 3x = -3$$

$$-1x = -3$$

$$x = -3 : (-1)$$

$$x = 3$$

$$\frac{x}{3} + 7 = 8 + \frac{x}{4} \quad /.12 \quad L = \frac{x}{3} + 7 = \frac{12}{3} + \frac{7}{1} = \frac{12+21}{3} = \frac{33}{3} = \frac{11}{1}$$

$$12 \cdot \frac{x}{3} + 12 \cdot 7 = 12 \cdot 8 + 3 \cdot \frac{x}{4}$$

$$4x + 84 = 96 + 3x$$

$$P = 8 + \frac{x}{4} = 8 + \frac{12}{4} = \frac{8}{1} + \frac{12}{4} = \frac{32+12}{4} = \frac{44}{4} = \frac{11}{1}$$

$$4x - 3x = -84 + 96$$

$$1x = 12$$

$$x = 12 : 1$$

$$x = 12$$

$$\frac{3x}{6} - \frac{x}{3} = \frac{5-x}{9} \quad /.18$$

$$L = \frac{3x}{6} - \frac{x}{3} = \frac{3.2}{6} - \frac{2}{3} = \frac{6}{6} - \frac{2}{3} = \frac{6-4}{6} = \frac{2}{6} = \frac{1}{3}$$

$$18 \cdot \frac{3x}{6} - 18 \cdot \frac{x}{3} = 18 \cdot \frac{5-x}{9}$$

$$9x - 6x = 10 - 2x$$

$$P = \frac{5-x}{9} = \frac{5-2}{9} = \frac{3}{9} = \frac{1}{3}$$

$$9x + 2x - 6x = 10$$

$$5x = 10$$

$$x = 10:5$$

$$x = 2$$

$$\frac{6x+1}{8} = 0 \quad /.8$$

$$L = \frac{6x+1}{8} = \frac{6 \cdot \left(-\frac{1}{6}\right) + 1}{8} = \frac{\frac{6}{1} \cdot \left(-\frac{1}{6}\right)}{8} = \frac{1}{8} = \frac{0}{8}$$

$$6x + 1 = 0$$

$$6x = -1$$

$$P = 0$$

$$x = -1:6$$

$$x = -\frac{1}{6}$$

$$\frac{x+8}{3} = 4 \quad /.3$$

$$L = \frac{x+8}{3} = \frac{4+8}{3} = \frac{12}{3} = \frac{4}{1}$$

$$x + 8 = 12$$

$$1x = -8 + 12$$

$$P = \frac{4}{1}$$

$$1x = 4$$

$$x = 4:1$$

$$x = 4$$

$$\frac{1-5x}{4} = \frac{3}{2} \quad / \cdot 4$$

$$L = \frac{1-5x}{4} = \frac{1-5 \cdot (-1)}{4} = \frac{6}{4} = \frac{3}{2}$$

$$4 \cdot \frac{1-5x}{4} = 2 \cdot \frac{3}{2}$$

$$1-5x=6$$

$$P = \frac{3}{2}$$

$$-5x = -1 + 5$$

$$-5x = 5$$

$$x = 5 : (-5)$$

$$x = -1$$

$$x + \frac{5}{3} = 2 \quad / \cdot 3$$

$$L = x + \frac{5}{3} = \frac{1}{3} + \frac{5}{3} = \frac{6}{3} = \frac{2}{1}$$

$$3x + 3 \cdot \frac{5}{3} = 3 \cdot 2$$

$$3x + 5 = 6$$

$$P = \frac{2}{1}$$

$$3x = -5 + 6$$

$$3x = 1$$

$$x = 1 : 3$$

$$x = \frac{1}{3}$$

$$\frac{x-7}{5} = 3 \quad / \cdot 5$$

$$L = \frac{x-7}{5} = \frac{22-7}{5} = \frac{15}{5} = \frac{3}{1}$$

$$5 \cdot \frac{x-7}{5} = 5 \cdot 3$$

$$x-7=15$$

$$P = \frac{3}{1}$$

$$1x = 7 + 15$$

$$1x = 22$$

$$x = 22 : 1$$

$$x = 22$$

$$\frac{x-2}{3} = \frac{x+4}{5} \quad /.15$$

$$L' = \frac{x-2}{3} = \frac{11-2}{3} = \frac{9}{3} = \frac{3}{1}$$

$$15 \cdot \frac{x-2}{3} = 15 \cdot \frac{x+4}{5}$$

$$5x-10=3x+12$$

$$P = \frac{x+4}{5} = \frac{11+4}{5} = \frac{15}{5} = \frac{3}{1}$$

$$5x-3x=10+12$$

$$2x=22$$

$$x=22:2$$

$$x=11$$

$$\frac{13+9x}{8} = \frac{1}{2} \quad /.8$$

$$L' = \frac{13+9x}{8} = \frac{13+9 \cdot (-1)}{8} = \frac{4}{8} = \frac{1}{2}$$

$$8 \cdot \frac{13+9x}{8} = 4 \cdot \frac{1}{2}$$

$$13+9x=4$$

$$P = \frac{1}{2}$$

$$9x=-13+4$$

$$9x=-9$$

$$x=-9:9$$

$$x=-1$$