Tretia mocnina dvojčlena, rozklad dvojčlenov

(riešené príklady)

Vzorce na tretiu mocninu dvojčlena (nie je potrebné vedieť naspamäť):

•
$$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$$

•
$$(a-b)^3 = a^3 - 3a^2b + 3ab^2 - b^3$$

Vzorce na rozdiel dvojčlenov (nie je potrebné vedieť naspamäť):

•
$$a^3+b^3 = (a+b).(a^2-ab+b^2)$$

•
$$a^3-b^3 = (a-b).(a^2+ab+b^2)$$

1. Umocnite dané výrazy

a.)
$$(a + 4)^3 = a^3 + 3a^2 \cdot 4 + 3a \cdot 4^2 + 4^3 = a^3 + 12a^2 + 48a + 64$$

b.)
$$(3-2x)^3 = 3^3 - 3$$
. $3^2 \cdot 2x + 3 \cdot 3 \cdot (2x)^2 + (2x)^3 = 27 - 54x + 36x^2 + 8x^3$

$$\mathbf{c.)} \begin{pmatrix} x - \frac{1}{3}y \end{pmatrix}^3 = x^3 - 3x^2 \cdot \frac{1}{3}y + 3x \left(\frac{1}{3}y\right)^2 + \left(\frac{1}{3}y\right)^3 = x^3 - x^2y + 3x \left(\frac{1}{9}y^2\right) + \left(\frac{1}{27}y^3\right) = x^3 - x^2y + 3x \left(\frac{1}{9}y^2\right) + \left(\frac{1}{27}y^3\right) = x^3 - x^2y + \frac{1}{3}xy^2 + \frac{1}{27}y^3$$

d.)
$$(5x - 4)^3 = 125x^3 - 3.25.x^2.4 + 3.5x.4^2 - 4^3 = 125x^3 - 300.x^2 + 240.x - 64$$

e.)
$$(a^2 - 2b)^3 = a^6 - 3a^4 \cdot 2b + 3a^2 \cdot 4b^2 - 8b^3 = a^6 - 6a^4 \cdot b + 12 \cdot a^2 \cdot b^2 - 8b^3$$

f.)
$$(x + 2)^3$$

g.)
$$(0.2a - 0.1b)^3$$

h.)
$$(2a + 3b)^3 = (2a)^3 + 3 \cdot (2a)^2 \cdot 3b + 3 \cdot 2a \cdot (3b)^2 + (3b)^3 = 8a^3 + 36a^2b + 54ab^2 + 27b^3$$

i.)
$$\left(x + \frac{2}{3}\right)^3$$

k.)
$$(x^2-3)^3$$

1.)
$$(x^2 + b)^3$$

2. Rozložte na súčin.

a)
$$x^3 - y^3 = (x-y).(x^2 + xy + y^2)$$

 $a^3 - b^3 = (a-b).(a^2 + ab + b^2)$

b)
$$x^3 + 8 = x^3 + 2^3 = (x+2).(x^2 - x^2 + 2^2) = (x+2).(x^2 - 2x + 4)$$

 $a^3 + b^3 = (a+b).(a^2 - ab + b^2)$

c)
$$64y^6 - 8x^3 = (4y^2)^3 - (2x)^3 = (4y^2 - 2x).(4^2y^4 + 4y^2.2x + 2^2x^2) = (4y^2 - 2x).(16y^4 + 8y^2x + 4x^2)$$

d)
$$27x^3 - 8 = (3x)^3 - 2^3 = (3x-2)(9x^2+3x.2+2^2) = (3x-2)(9x^2+6x+4)$$

e)
$$8x^6 + y^3 = (2x^2)^3 + y^3 = (2x^2+y)(4x^4-2x^2.y+y^2)$$

f)
$$0.001a^3 - 64b^3$$

g)
$$\frac{1}{27}x^3 + y^3 = (\frac{1}{3}x)^3 + y^3 = (\frac{1}{3}x + y)(\frac{1}{9}x^2 - \frac{1}{3}x \cdot y + y^2)$$

h)
$$a^3 - \frac{1}{125}$$

i)
$$0.125a^9 + 0.008b^3 = (0.5a^3)^3 + (0.2.b)^3 = (0.5.a^3 + 0.2b) \cdot (0.25a^6 - 0.5.a^3 + 0.2b + 0.04b^2)$$