

M1 – Odmocniny

SKUPINA A:

Blahovský, Kolesárová,
Brettschneider, Macko,

SKUPINA B:

Dravecká, Rejdovjanová, Fedor,
Starinský, Hudáková

SKUPINA C:

Body, Konečná, Brutovský, Falatko,

SKUPINA D:

Schmidt, Hudák, Varga, Jenčík,
Vojtková

1./ Usmerni zlomok (odstráň odmocninu z menovateľa):

$$\text{a/} \quad \frac{3}{1+\sqrt{6}} \cdot \frac{1-\sqrt{6}}{1-\sqrt{6}} = \frac{3(1-\sqrt{6})}{1-6} = -\frac{3-3\sqrt{6}}{5}$$

$$\text{b/} \quad \frac{6}{1-\sqrt{3}} \cdot \frac{1+\sqrt{3}}{1+\sqrt{3}} = \frac{6(1+\sqrt{3})}{1-3} = -3(1+\sqrt{3})$$

$$\text{c/} \quad \frac{5}{\sqrt{2}+1} \cdot \frac{\sqrt{2}-1}{\sqrt{2}-1} = \frac{5(\sqrt{2}-1)}{2-1} = 5(\sqrt{2}-1)$$

$$\text{d/} \quad \frac{6}{\sqrt{3}-1} \cdot \frac{\sqrt{3}+1}{\sqrt{3}+1} = \frac{6(\sqrt{3}+1)}{3-1} = 3(\sqrt{3}+1)$$

2./ Uprav tak, aby vo výsledku bola len jedna odmocnina (za predpokladu, že $x > 0$):

$$\text{a/} \quad \frac{\sqrt{x^3} \cdot \sqrt{x}}{\sqrt{x^2}} = \sqrt{\frac{x^4}{x^2}} = \sqrt{x^2} = x$$

$$\text{b/} \quad \frac{\sqrt[4]{x^7}}{\sqrt[4]{x^3} \cdot \sqrt[4]{x}} = \sqrt[4]{\frac{x^7}{x^4}} = \sqrt[4]{x^3}$$

$$\text{c/} \quad \sqrt[7]{x^5} \cdot \sqrt[7]{x^3} : \sqrt[7]{x^2} = \sqrt[7]{x^{5+3-2}} = \sqrt[7]{x^6}$$

$$\text{d/} \quad \sqrt[3]{x^8} \cdot \sqrt[3]{x^2} : \sqrt[3]{x^4} = \sqrt[3]{x^{8+2-4}} = \sqrt[3]{x^6} = x^2$$

3./ Uprav tak, aby vo výsledku bola len jedna odmocnina (za predpokladu, že $x \geq 0$):

$$\text{a/} \quad x^{\frac{1}{3}} \cdot \sqrt[6]{x} = x^{\frac{1}{3}} \cdot x^{\frac{1}{6}} = x^{\frac{2+1}{6}} = x^{\frac{3}{6}} = x^{\frac{1}{2}} = \sqrt{x}$$

$$\text{b/} \quad \sqrt[3]{x^2} \cdot x^{\frac{1}{4}} = x^{\frac{2}{3}} \cdot x^{\frac{1}{4}} = x^{\frac{8+3}{12}} = x^{\frac{11}{12}} = \sqrt[12]{x^{11}}$$

$$\text{c/} \quad x^{\frac{1}{4}} \cdot \sqrt[5]{x^2} = x^{\frac{1}{4}} \cdot x^{\frac{2}{5}} = x^{\frac{5+8}{20}} = x^{\frac{13}{20}} = \sqrt[20]{x^{13}}$$

$$\text{d/} \quad \sqrt[7]{x^5} \cdot x^{\frac{1}{4}} = x^{\frac{5}{7}} \cdot x^{\frac{1}{4}} = x^{\frac{20+7}{28}} = x^{\frac{27}{28}} = \sqrt[28]{x^{27}}$$

4./ Uprav tak, aby vo výsledku bola len jedna odmocnina a zapíš podmienky:

$$\text{a/} \quad \frac{\sqrt[6]{x^4}}{\sqrt[3]{x^2}} = \frac{x^{\frac{4}{6}}}{x^{\frac{2}{3}}} = \frac{x^{\frac{2}{3}}}{x^{\frac{2}{3}}} = 1$$

$P.: x > 0$

$$\text{b/} \quad \frac{\sqrt[8]{x^2}}{\sqrt[3]{x^4}} = \frac{x^{\frac{2}{8}}}{x^{\frac{4}{3}}} = x^{\frac{1}{4} - \frac{4}{3}} = x^{\frac{3-16}{12}} = x^{-\frac{13}{12}}$$

$$= x^{-\frac{13}{12}} = \sqrt[12]{x^{-13}} = \sqrt[12]{\frac{1}{x^{13}}} \quad P.: x > 0$$

$$\text{c/} \quad \frac{\sqrt[5]{x^3}}{\sqrt[6]{x^2}} = \frac{x^{\frac{3}{5}}}{x^{\frac{2}{6}}} = x^{\frac{3}{5} - \frac{1}{3}} = x^{\frac{9-5}{15}} = x^{\frac{4}{15}} = \sqrt[15]{x^4}$$

$P.: x > 0$

$$\text{d/} \quad \frac{\sqrt[6]{x}}{\sqrt[9]{x^3}} = \frac{x^{\frac{1}{6}}}{x^{\frac{3}{9}}} = x^{\frac{1}{6} - \frac{1}{3}} = x^{\frac{1-2}{6}} = x^{-\frac{1}{6}} = \sqrt[6]{x^{-1}} = \sqrt[6]{\frac{1}{x}}$$

$P.: x > 0$