

1. K nasledujúcim lineárnym funkciám nakreslite graf a určte:

- definičný obor,
- obor hodnôt,
- hodnotu funkcie pre $x = -2$ a $x = 8$,
- priesečník s osou o_y ,
- priesečník s osou o_x ,
- či je rastúca, či klesajúca

a) $y = 4x$

b) $y = -2x+5$

c) $y = 5x-9$

d) $y = 4x+1$

e) $y = -3x-6$

2. K nasledujúcim funkciám nakreslite graf a určte:

- definičný obor,
- obor hodnôt,
- hodnotu funkcie pre $x = 5$,
- priesečník s osou o_y ,
- priesečníky s osou o_x ,
- minimum funkcie,
- maximum funkcie
- kde klesá a kde rastie

a) $y = |x - 1| + 5$

b) $y = 4|x + 1| - 3$

c) $y = -|2x + 4| - 3$

d) $y = |x + 4| - 2x$

e) $y = -3|x - 1| + 4x$

3. Pre kvadratické funkcie dané predpisom nakreslite graf a určte:

- priesečníky s osou o_x ,
- vrchol grafu funkcie,
- priesečník s osou o_y ,
- definičný obor,
- obor hodnôt $H(f)$,
- interval, na ktorom je funkcia rastúca a na ktorom je klesajúca.

a) $f: y = 2x^2 - 4x - 6$

b) $f: y = -2x^2 - 16x - 30$

c) $f: y = x^2 + 2x - 3$

d) $f: y = x^2 - 7x + 6$

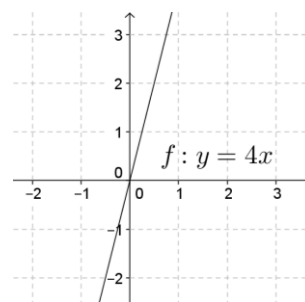
e) $f: y = -4x^2 + 16x - 12$

Výsledky:

1.

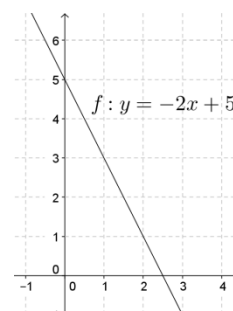
a)

- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(-2) = -8, f(8) = 32$
- $[0,0]$
- $[0,0]$
- je rostúca



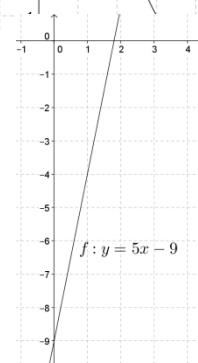
b)

- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(-2) = 9, f(8) = -11$
- $[5/2, 0]$
- $[0, 5]$
- je klesajúca



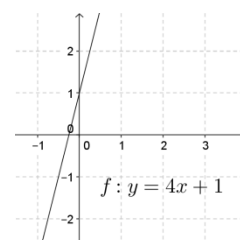
c)

- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(-2) = -19, f(8) = 31$
- $[5/9, 0]$
- $[0, -9]$
- je rostúca



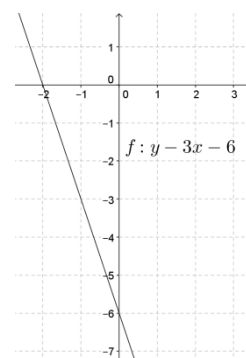
d)

- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(-2) = -7, f(8) = 33$
- $[-1/4, 0]$
- $[0, 1]$
- je rostúca



e)

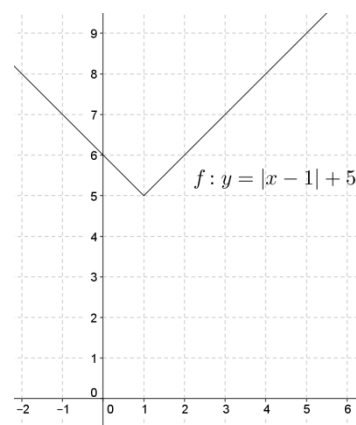
- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(-2) = 0, f(8) = -30$
- $[-2, 0]$
- $[0, -6]$
- je klesajúca



2.

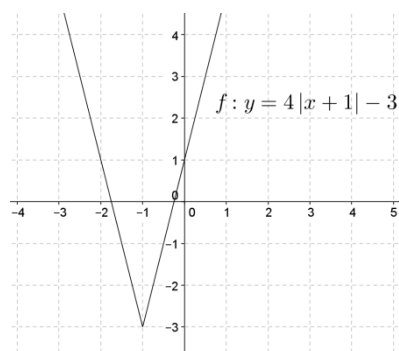
a)

- $D(f) = \mathbb{R}$
- $H(f) = \langle 5, \infty \rangle$
- $f(5) = 9$
- nemá
- $[0, 6]$
- minimum nadobúda pre $x = 1$
- maximum nemá
- klesá na $(-\infty, 1)$; rastie na $\langle 1, \infty \rangle$



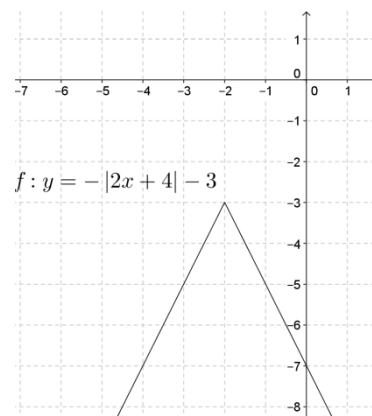
b)

- $D(f) = \mathbb{R}$
- $H(f) = \langle -3, \infty \rangle$
- $f(5) = 21$
- $[-7/4, 0], [-1/4, 0]$
- $[0, 1]$
- minimum nadobúda pre $x = -1$
- maximum nemá



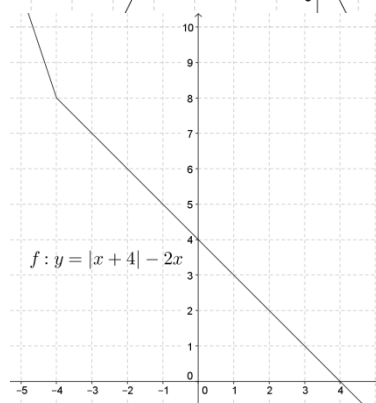
c)

- klesá na $(-\infty, -1)$; rastie na $\langle -1, \infty \rangle$
- $D(f) = \mathbb{R}$
- $H(f) = (-\infty, -3)$
- $f(5) = -17$
- nemá
- $[0, -7]$
- minimum nemá
- maximum nadobúda pre $x = -2$
- klesá na $\langle -2, \infty \rangle$; rastie na $(-\infty, -2)$



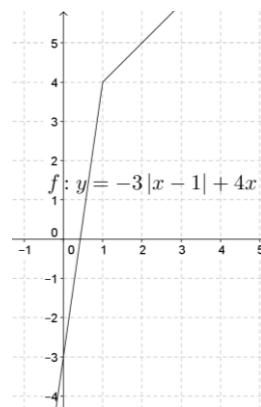
d)

- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(5) = -1$
- $[4, 0]$
- $[0, 4]$
- minimum nemá
- maximum nemá
- klesá na $(-\infty, \infty)$; rastie nikde



e)

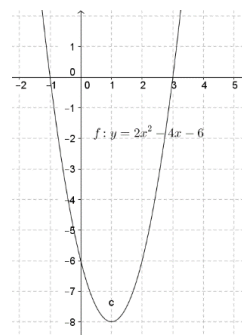
- $D(f) = \mathbb{R}$
- $H(f) = \mathbb{R}$
- $f(5) = 8$
- $[3/7, 0]$
- $[0, -3]$
- minimum nemá
- maximum nemá
- klesá nikde; rastie na $(-\infty, \infty)$



3.

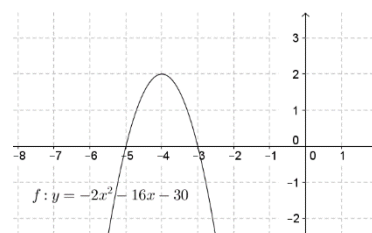
a)

- $[-1, 0], [3, 0]$
- $[1, -8]$
- $[0, -6]$
- $D(f) = \mathbb{R}$
- $H(f) = \langle -8, \infty \rangle$
- klesá na $(-\infty, 1)$, rastie na $\langle 1, \infty \rangle$



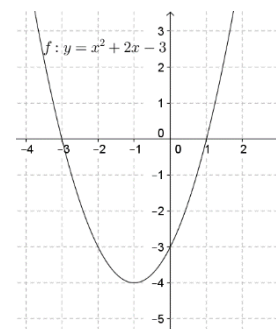
b)

- $[-5, 0], [-3, 0]$
- $[-4, 2]$
- $[0, -30]$
- $D(f) = \mathbb{R}$
- $H(f) = (-\infty, 2)$
- klesá na $\langle -4, \infty \rangle$, rastie na $(-\infty, -4)$



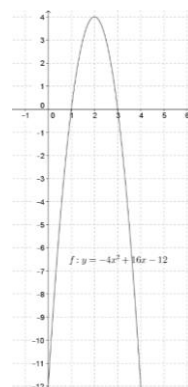
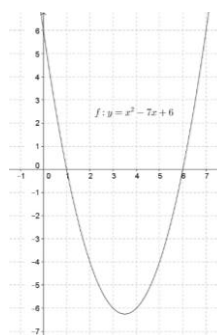
c)

- $[-3, 0], [1, 0]$
- $[-1, 4]$
- $[0, -3]$
- $D(f) = \mathbb{R}$
- $H(f) = \langle -4, \infty \rangle$
- klesá na $(-\infty, -1)$, rastie na $\langle -1, \infty \rangle$.



d)

- $[1, 0], [6, 0]$
- $[-25/4, 7/2]$
- $[0, 6]$
- $D(f) = \mathbb{R}$
- $H(f) = \langle -25/4, \infty \rangle$
- klesá na $(-\infty, 7/2)$, rastie na $\langle 7/2, \infty \rangle$



e)

- $[1, 0], [3, 0]$
- $[2, 4]$
- $[0, -12]$
- $D(f) = \mathbb{R}$

- $H(f) = (-\infty, 4)$
- klesá na $\langle 2, \infty)$, rastie na $(-\infty, 2)$.