

Risk Analytics: Risk and regulation tutorial sheet

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November 3, 2017

1 Copulas

1. Show by example (in \mathbb{R} or otherwise) that a two-party default model with 2-d t-copula with a given correlation parameter (e.g. $\rho = 0.5$) and degree of freedom approaching infinity converges to default model with a 2-d Gaussian copula with the same correlation coefficient ρ as in the lecture.
2. *Model risk* is the risk of losing money (directly or indirectly through e.g. reputational damage) via inappropriate use of models. Included under this heading are:
 - Failure of key model assumptions
 - Overfitting

The second item refers to the tension in statistical learning theory between *learning* error and *estimation* error.

Discuss the model risk of modeling dependency with a Gaussian vs t-copula.

3. **¹ Let $\mathbf{X} = (X_1, \dots, X_k)$ be a random variable on \mathbb{R}^k (i.e. $\mathbf{X}: \Omega \rightarrow \mathbb{R}^k$, where Ω is universe of events), and let F_1, \dots, F_k be the marginal CDFs of \mathbf{X} . By Sklar's Theorem, there exists a unique copula C such that $F(\mathbf{X}) = C(F_1(x_1), \dots, F_k(x_k))$.
Let $\alpha_1, \dots, \alpha_k$ be strictly increasing functions $\alpha_i: \mathbb{R} \rightarrow \mathbb{R}$. Show that $(\alpha_1(X_1), \dots, \alpha_k(X_k))$ also has copula C . (Hint: First try to prove this for a 2-d copula.)

2 Capital Ratios

1. How would a loan and a (long) CDS protecting against that loan go into a bank's balance sheet?
2. What can go wrong with the balance sheet view of a CDS?
3. * Same as above for a CDO.

¹The asterisk indicates a more challenging problem