

## Lesson 2 Naive Bayes

### Supervised Classification

- learning from labeled data. After understanding the data, the algorithm determines which label should be given to new data by associating patterns to the unlabeled new data.
- Examples
  - Identifying someone from a set of pictures
  - Song recommendation based on previous liked songs

### Features and Labels

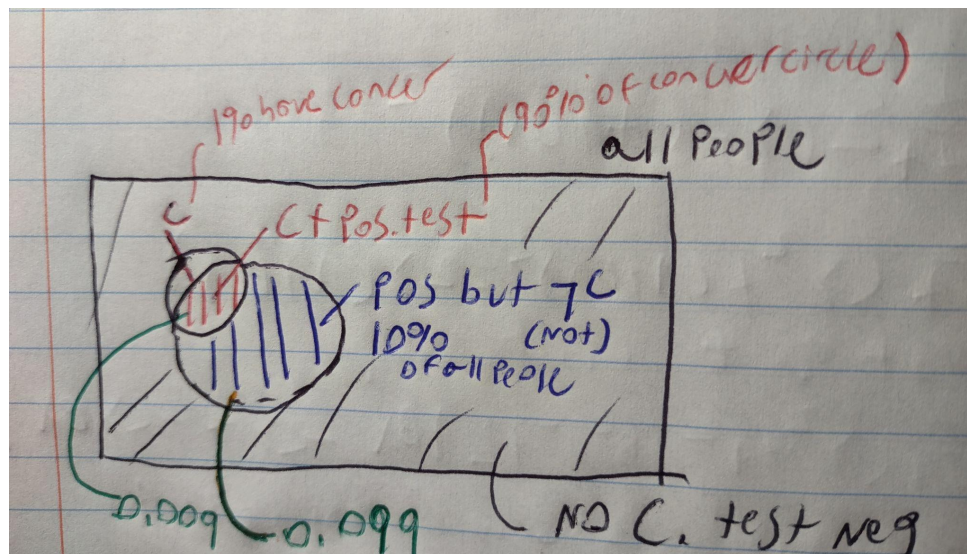
- Song example
- Features
  - Intensity, Temp, Genre, Voice gender
- Labels
  - Like, Dislike

### Naive Bayes

$p(c) = 0.01$ ,  $c = \text{Cancer}$

Test: 90% it is positive if you have C (Sensitivity)  
90% it is negative if you don't have C (Specificity)

Question: Test = Positive



What is the Probability of Having cancer?  
about 8%, see diagram in written notes

- **Sensitivity** (True Positive Rate) refers to the proportion of those who received a positive result on this test out of those who actually have the condition (when judged by the 'Gold Standard').
- **Specificity** (True Negative Rate) refers to the proportion of those who received a negative result on this test out of those who do not actually have the condition (when judged by the 'Gold Standard').

## Bayes Rule

Prior probability \* test evidence → posterior probability

Prior:  $p(c) = 0.01 = 1\%$                        $p(\text{not } c) = 0.99 = 99\%$   
 $p(\text{pos} | c) = .9 = 90\%$   
 $p(\text{neg} | \text{not } c) = 0.9$                        $p(\text{pos} | \text{not } c) = 0.1$

Posterior (joint probability):

$$p(c, \text{pos.}) = p(c) * p(\text{pos} | c) = 0.01 * .9 = 0.009$$

$$p(\text{not } c, \text{pos}) = p(\text{not } c) * p(\text{pos} | \text{not } c) = .99 * 0.1 = 0.099$$

Normalizer

$$p(c, \text{pos.}) + p(\text{not } c, \text{pos}) = 0.009 + 0.099 = 0.108$$

Posterior (actual):

$$p(c | \text{pos}) = \frac{0.009}{0.108} = 0.0833$$

$$p(\text{not } c | \text{pos}) = \frac{0.099}{0.108} = 0.9167$$

$$p(c | \text{pos}) + p(\text{not } c | \text{pos}) = 0.0833 + 0.9167 = 1$$

## Bayes Rule Diagram

