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Disciplina: BCC 263 – Arquitetura de Computadores

Lista de Exercícios 1

Questão 1.3

Describe the steps that transform a program written in a high-level language such as C into a representation that is directly executed by a computer processor.

Primeiramente, um programador pode usar uma linguagem de alto nível, como C ou Java, para expressar sua linha de raciocínio de forma mais concisa e natural, utilizando palavras e expressões algébricas. Então, um compilador traduzirá este programa em uma linguagem *assembly*, uma outra forma de representar simbolicamente as operações a serem realizadas pela máquina. Por fim, um *assembler* irá traduzir essa linguagem *assembly* em linguagem de máquina, composta por *binary digits*, ou bits, podendo ser estes 0 ou 1. Os bits serão entendidos pelo hardware como sinais elétricos de ligar e desligar, e deste modo, as instruções contidas no programa serão realizadas.

Questão 1.5

Consider three different processors P1, P2, and P3 executing the same instruction set. P1 has a 3 GHz clock rate and a CPI of 1.5. P2 has a 2.5 GHz clock rate and a CPI of 1.0. P3 has a 4.0 GHz clock rate and has a CPI of 2.2.

- Which processor has the highest performance expressed in instructions per second?
- If the processors each execute a program in 10 seconds, find the number of cycles and the number of instructions.
- We are trying to reduce the execution time by 30%, but this leads to an increase of 20% in the CPI. What clock rate should we have to get this time reduction?

1.5.a) Execution Time (P1) = $(I \cdot 1.5) / (3E9) = 0,0000000005 \cdot I$
Execution Time (P2) = $(I \cdot 1) / (2.5E9) = 0,0000000004 \cdot I$
Execution Time (P3) = $(I \cdot 2.2) / (4E9) = 0,00000000055 \cdot I$
P2 é o processador com maior performance.

1.5.b) $10 = \text{CPU Clock Cycles (P1)} / (3E9) \rightarrow \text{CPU Clock Cycles (P1)} = 3E10 \text{ ciclos}$
 $3E10 = I \cdot 1.5 \rightarrow I \text{ (P1)} = 2E10 \text{ instruções}$

$10 = \text{CPU Clock Cycles (P2)} / (2.5E9) \rightarrow \text{CPU Clock Cycles (P2)} = 2.5E10 \text{ ciclos}$
 $2.5E10 = I \cdot 1 \rightarrow I \text{ (P2)} = 2.5E10 \text{ instruções}$

$10 = \text{CPU Clock Cycles (P3)} / (4E9) \rightarrow \text{CPU Clock Cycles (P3)} = 4E10 \text{ ciclos}$
 $4E10 = I \cdot 2.2 \rightarrow I \text{ (P3)} = 1.8E10 \text{ instruções}$

1.5.c) $0,7 \cdot \text{CPU Time (P1)} = (I \cdot 1,8) / \text{Clock Rate (P1)} \rightarrow$
 $0,7 \cdot 0,0000000005 \cdot I = (I \cdot 1,8) / \text{Clock Rate (P1)} \rightarrow$
Clock Rate (P1) = 5.1 GHz

$0,7 \cdot \text{CPU Time (P2)} = (I \cdot 1,2) / \text{Clock Rate (P2)} \rightarrow$
 $0,7 \cdot 0,0000000004 \cdot I = (I \cdot 1,2) / \text{Clock Rate (P2)} \rightarrow$
Clock Rate (P2) = 4.3 GHz

$0,7 \cdot \text{CPU Time (P3)} = (I \cdot 2,64) / \text{Clock Rate (P3)} \rightarrow$

$$0,7 * 0,00000000055 * I = (I * 2,64) / \text{Clock Rate (P3)} \rightarrow$$

$$\text{Clock Rate (P3)} = 6.9 \text{ GHz}$$

Questão 1.6

Consider two different implementations of the same instruction set architecture. The instructions can be divided into four classes according to their CPI (classes A, B, C, and D). P1 with a clock rate of 2.5 GHz and CPIs of 1, 2, 3, and 3, and P2 with a clock rate of 3 GHz and CPIs of 2, 2, 2, and 2. Given a program with a dynamic instruction count of 1.0E6 instructions divided into classes as follows: 10% class A, 20% class B, 50% class C, and 20% class D, which is faster: P1 or P2?

- a. What is the global CPI for each implementation?
- b. Find the clock cycles required in both cases.

$$1.6) \text{ CPU Clock Cycles (P1)} = (0.1 * 1 * 1E6) + (0.2 * 2 * 1E6) + (0.5 * 3 * 1E6) + (0.2 * 3 * 1E6)$$

$$\text{CPU Clock Cycles (P1)} = 2\,600\,000 \text{ ciclos}$$

$$\text{CPU Time (P1)} = 2\,600\,000 / 2.5E9 = 0,00104 \text{ segundos}$$

$$\text{CPU Clock Cycles (P2)} = (0.1 * 2 * 1E6) + (0.2 * 2 * 1E6) + (0.5 * 2 * 1E6) + (0.2 * 2 * 1E6)$$

$$\text{CPU Clock Cycles (P2)} = 2\,000\,000 \text{ ciclos}$$

$$\text{CPU Time (P2)} = 2\,000\,000 / 3E9 = 0,00067 \text{ segundos}$$

P2 é mais rápido.

$$1.6.a) \text{ CPI (P1)} = 2\,600\,000 / 1E6 = 2.6$$

$$\text{CPI (P2)} = 2\,000\,000 / 1E6 = 2$$

$$1.6.b) \text{ CPU Clock Cycles (P1)} = 1E6 * 2.6 = 2\,600\,000 \text{ ciclos}$$

$$\text{CPU Clock Cycles (P2)} = 1E6 * 2 = 2\,000\,000 \text{ ciclos}$$

Questão 1.7

Compilers can have a profound impact on the performance of an application. Assume that for a program, compiler A results in a dynamic instruction count of 1.0E9 and has an execution time of 1.1 s, while compiler B results in a dynamic instruction count of 1.2E9 and an execution time of 1.5 s.

- a. Find the average CPI for each program given that the processor has a clock cycle time of 1 ns.
- b. Assume the compiled programs run on two different processors. If the execution times on the two processors are the same, how much faster is the clock of the processor running compiler A's code versus the clock of the processor running compiler B's code?
- c. A new compiler is developed that uses only 6.0E8 instructions and has an average CPI of 1.1. What is the speedup of using this new compiler versus using compiler A or B on the original processor?

$$1.7.a) 1.1 = \text{CPU Clock Cycles (A)} * 1E-9 \rightarrow \text{CPU Clock Cycles (A)} = 1\,100\,000\,000 \text{ ciclos}$$

$$1\,100\,000\,000 = 1E9 * \text{CPI (A)} \rightarrow \text{CPI (A)} = 1.1$$

$$1.5 = \text{CPU Clock Cycles (B)} * 1E-9 \rightarrow \text{CPU Clock Cycles (B)} = 1\,500\,000\,000 \text{ ciclos}$$

$$1\,500\,000\,000 = 1.2E9 * \text{CPI (B)} \rightarrow \text{CPI (B)} = 1.25$$

$$1.7.b) \text{ Execution Time} = 1\,100\,000\,000 * \text{Clock Cycle Time (A)}$$

$$\text{Execution Time} = 1\,500\,000\,000 * \text{Clock Cycle Time (B)}$$

$$1\,100\,000\,000 * \text{Clock Cycle Time (A)} = 1\,500\,000\,000 * \text{Clock Cycle Time (B)}$$

$$\text{Clock Cycle Time (A)} = (1\,500\,000\,000 * \text{Clock Cycle Time (B)}) / 1\,100\,000\,000$$

$$\text{Clock Cycle Time (A)} = 1.36 * \text{Clock Cycle Time (B)}$$

O clock do processador quando “roda” o código do compilador A é cerca de 1,36 vezes mais rápido do que quando “roda” o código do compilador B.

$$1.7.c) \text{ CPU Clock Cycles (C)} = 6E8 * 1.1 \rightarrow \text{CPU Clock Cycles (C)} = 660\,000\,000 \text{ ciclos}$$

$$\text{Execution Time (C)} = 660\,000\,000 * 1E-9 \rightarrow \text{Execution Time (C)} = 0,66 \text{ segundos}$$

$$\text{CPU Performance (C)} / \text{CPU Performance (A)} =$$

$$\text{CPU Execution Time (A)} / \text{CPU Execution Time (C)} = 1.1/0.66 = 1.67$$

$$\text{CPU Performance (C)} / \text{CPU Performance (B)} =$$

$$\text{CPU Execution Time (B)} / \text{CPU Execution Time (C)} = 1.5/0.66 = 2.27$$

O compilador C é cerca de 1.67 vezes mais rápido que o compilador A e cerca de 2.27 vezes mais rápido que o compilador B, usando o mesmo processador.

Questão 1.9

Assume for arithmetic, load/store, and branch instructions, a processor has CPIs of 1, 12, and 5, respectively. Also assume that on a single processor a program requires the execution of 2.56E9 arithmetic instructions, 1.28E9 load/store instructions, and 256 million branch instructions. Assume that each processor has a 2 GHz clock frequency. Assume that, as the program is parallelized to run over multiple cores, the number of arithmetic and load/store instructions per processor is divided by $0.7 \times p$ (where p is the number of processors) but the number of branch instructions per processor remains the same.

1.9.1. Find the total execution time for this program on 1, 2, 4, and 8 processors, and show the relative speedup of the 2, 4, and 8 processors result relative to the single processor result.

1.9.2. If the CPI of the arithmetic instructions was doubled, what would the impact be on the execution time of the program on 1, 2, 4, or 8 processors?

1.9.3. To what should the CPI of load/store instructions be reduced in order for a single processor to match the performance of four processors using the original CPI values?

1.9.1)

- Para 1 Processador:

$$\text{Clock Cycles} = (1 * 2.56E9) + (12 * 1.28E9) + (5 * 2.56E8) = 1,92E10 \text{ ciclos}$$

$$\text{Execution Time} = 1,92E10/2E9 = 9,6 \text{ segundos}$$

- Para 2 Processadores:

$$\text{Número de instruções aritméticas: } 2.56E9 / (0,7 * 2) = 1,83E9 \text{ instruções}$$

$$\text{Número de instruções load/store: } 1.28E9 / (0,7 * 2) = 9,14E8 \text{ instruções}$$

$$\text{Clock Cycles} = (1 * 1.83E9) + (12 * 9.14E8) + (5 * 2.56E8) = 1,41E10 \text{ ciclos}$$

$$\text{Execution Time} = 1,41E10/2E9 = 7,039 \text{ segundos}$$

$$9,6 / 7,039 = 1,36$$

O programa é 1,36 vezes mais rápido ao utilizar 2 processadores, em relação a utilizar 1 processador.

- Para 4 Processadores:

$$\text{Número de instruções aritméticas: } 2.56E9 / (0,7 * 4) = 9,14E8 \text{ instruções}$$

$$\text{Número de instruções load/store: } 1.28E9 / (0,7 * 4) = 4,57E8 \text{ instruções}$$

$$\text{Clock Cycles} = (1 * 9.14E8) + (12 * 4.57E8) + (5 * 2.56E8) = 7,68E9 \text{ ciclos}$$

$$\text{Execution Time} = 7,68E9/2E9 = 3,839 \text{ segundos}$$

$$9,6 / 3,839 = 2,5$$

O programa é 2,5 vezes mais rápido ao utilizar 4 processadores, em relação a utilizar 1 processador.

- Para 8 Processadores:

Número de instruções aritméticas: $2.56E9 / (0,7 * 8) = 4,57E8$ instruções

Número de instruções load/store: $1.28E9 / (0,7 * 8) = 2,29E8$ instruções

Clock Cycles = $(1 * 4.57E8) + (12 * 2.29E8) + (5 * 2.56E8) = 4,48E9$ ciclos

Execution Time = $4,48E9 / 2E9 = 2,2425$ segundos

$9,6 / 2,2425 = 4,28$

O programa é 4,28 vezes mais rápido ao utilizar 8 processadores, em relação a utilizar 1 processador.

1.9.2)

- Para 1 Processador:

Clock Cycles = $(2 * 2.56E9) + (12 * 1.28E9) + (5 * 2.56E8) = 2,18E10$ ciclos

Execution Time = $2,18E10 / 2E9 = 10,88$ segundos

$10,88 / 9,6 = 1,13$

Ao dobrar o CPI das instruções aritméticas, o programa é executado 1,13 vezes mais lento ao utilizar 1 processador.

- Para 2 Processadores:

Clock Cycles = $(2 * 1.83E9) + (12 * 9.14E8) + (5 * 2.56E8) = 1,59E10$ ciclos

Execution Time = $1,59E10 / 2E9 = 7,954$ segundos

$7,954 / 7,039 = 1,13$

Ao dobrar o CPI das instruções aritméticas, o programa é executado 1,13 vezes mais lento ao utilizar 2 processadores.

- Para 4 Processadores:

Clock Cycles = $(2 * 9.14E8) + (12 * 4.57E8) + (5 * 2.56E8) = 8,59E9$ ciclos

Execution Time = $8,59E9 / 2E9 = 4,296$ segundos

$4,296 / 3,839 = 1,12$

Ao dobrar o CPI das instruções aritméticas, o programa é executado 1,12 vezes mais lento ao utilizar 4 processadores.

- Para 8 Processadores:

Clock Cycles = $(2 * 4.57E8) + (12 * 2.29E8) + (5 * 2.56E8) = 4,94E9$ ciclos

Execution Time = $4,94E9 / 2E9 = 2,471$ segundos

$2,471 / 2,2425 = 1,1$

Ao dobrar o CPI das instruções aritméticas, o programa é executado 1,1 vezes mais lento ao utilizar 8 processadores.

1.9.3) $3,839 = \text{Clock Cycles} / 2E9 \rightarrow \text{Clock Cycles} = 7,69E9$ ciclos

$7,69E9 = (1 * 2.56E9) + (\text{CPI} * 1.28E9) + (5 * 2.56E8)$

$3,84E9 = \text{CPI} * 1.28E9 \rightarrow \text{CPI} = 3$

Para que a performance de 1 processador se equipare a performance de 4 processadores usando os valores de CPI originais, o CPI das instruções de load/store deve ser mudado para 3.

Questão 1.12

Section 1.10 cites as a pitfall the utilization of a subset of the performance equation as a performance metric. To illustrate this, consider the following two processors. P1 has a clock rate of 4 GHz, average CPI of 0.9, and requires the execution of $5.0E9$ instructions. P2 has a clock rate of 3 GHz, an average CPI of 0.75, and requires the execution of $1.0E9$ instructions.

1.12.1. One usual fallacy is to consider the computer with the largest clock rate as having the highest performance. Check if this is true for P1 and P2.

1.12.2. Another fallacy is to consider that the processor executing the largest number of instructions will need a larger CPU time. Considering that processor P1 is executing a sequence of $1.0E9$ instructions and that the CPI of processors P1 and P2 do not change, determine the number of instructions that P2 can execute in the same time that P1 needs to execute $1.0E9$ instructions.

1.12.3. A common fallacy is to use MIPS (millions of instructions per second) to compare the performance of two different processors, and consider that the processor with the largest MIPS has the largest performance. Check if this is true for P1 and P2.

1.12.4. Another common performance figure is MFLOPS (millions of floating-point operations per second), defined as:

$$\text{MFLOPS} = \text{Number of FP Opearitions} / (\text{Execution Time} * 1E6)$$

But this figure has the same problems as MIPS. Assume that 40% of the instructions executed on both P1 and P2 are floating-point instructions. Find the MFLOPS figures for the processors.

1.12.1) $\text{Execution Time (P1)} = (5E9 * 0,9) / 4E9 = 1,125 \text{ segundos}$

$\text{Execution Time (P2)} = (1E9 * 0,75) / 3E9 = 0,25 \text{ segundos}$

Apesar do clock rate de P1 ser maior, P2 possui uma maior performance.

1.12.2) $\text{Execution Time} = (1E9 * 0,9) / 4E9 = 0,225 \text{ segundos}$

$0,225 = (I * 0,75) / 3E9 \rightarrow I * 0,75 = 675\ 000\ 000 \rightarrow I = 900\ 000\ 000 \rightarrow I = 9E8 \text{ Instruções}$

1.12.3) $\text{MIPS (P1)} = 5E9 / (1,125 * 1E6) = 4\ 444$

$\text{MIPS (P2)} = 1E9 / (0,25 * 1E6) = 4000$

Apesar do MIPS de P1 ser maior que o MIPS de P2, já foi comprovado que a performance de P2 é maior que a de P1 através do exercício 1.12.1.

1.12.4) $\text{MFLOPS (P1)} = (0,4 * 5E9) / (1,125 * 1E6) = 1777$

$\text{MFLOPS (P2)} = (0,4 * 1E9) / (0,25 * 1E6) = 1600$

Apesar do MFLOPS de P1 ser maior que o MFLOPS de P2, já foi comprovado que a performance de P2 é maior que a de P1 através do exercício 1.12.1.

Questão 1.14

Assume a program requires the execution of 50×10^6 FP instructions, 110×10^6 INT instructions, 80×10^6 L/S instructions, and 16×10^6 branch instructions. The CPI for each type of instruction is 1, 1, 4, and 2, respectively. Assume that the processor has a 2 GHz clock rate.

1.14.1. By how much must we improve the CPI of FP instructions if we want the program to run two times faster?

1.14.2. By how much must we improve the CPI of L/S instructions if we want the program to run two times faster?

1.14.3. By how much is the execution time of the program improved if the CPI of INT and FP instructions is reduced by 40% and the CPI of L/S and Branch is reduced by 30%?

1.14.1) $\text{Clock Cycles} = (1 * 50E6) + (1 * 110E6) + (4 * 80E6) + (2 * 16E6) = 5,12E8 \text{ ciclos}$

$\text{Execution Time} = 5,12E8 / 2E9 = 0,256 \text{ segundos}$

$\text{Execution Time (FP instructions)} = (1 * 50E6) / 2E9 = 0,025 \text{ segundos}$

$0,128 = 0,025 / n + (0,256 - 0,025) \rightarrow 0,128 - 0,231 = 0,025 / n \rightarrow -0,103 = 0,025 / n$

$n = -0,243$

Como o valor de n é negativo, não há valor de CPI para as instruções FP que faça o programa rodar 2 vezes mais rápido.

1.14.2) $\text{Execution Time (L/S instructions)} = (4 * 80E6) / 2E9 = 0,16 \text{ segundos}$

$$0,128 = 0,16 / n + (0,256 - 0,16) \rightarrow 0,128 - 0,096 = 0,16 / n \rightarrow 0,032 = 0,16 / n \rightarrow n = 5$$

Para que o programa rode 2 vezes mais rápido, é necessário melhorar o CPI das instruções L/S em 5 vezes.

1.14.3) New Clock Cycles = $(0.6 * 50E6) + (0.6 * 110E6) + (2.8 * 80E6) + (1.4 * 16E6) = 3,424E8$ ciclos

New Execution Time = $3,424E8 / 2E9 = 0,1712$ segundos

$$0,256 / 0,1712 = 1,49$$

O tempo de execução é melhorado em cerca de 1,49 vezes ao aplicar as melhorias descritas.