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%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Problem 03 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

clc
clear
a=[2 4 4 1; 10 3 7 7; 6 7 20 5];d=[50 100 150
  200];s=[150;200;150];m=3;n=4;
Given_Problem=[a s;d sum(d)]
fprintf("The initial Matrix,") %%%%% Initial function created %%
[b,Initial_LCM_Cost]=LCM(a,d,s,m,n)%Initial_Solution=[b s;d sum(d)]

fprintf("\n\nRoundwise Cij-Ui-Vj Matrix,")
c=optCheck(a,b,m,n) %%%%%%%%% Optimality %%%%%%%%%
while(sum(sum(c<0))~=0)%%%%%%%% Subtraction Logic without DFS
    %%%%%%%%%
    [p,q]=find(min(min(c))==c,1);
    T=0;
    for i=1:m
        for j=1:n
            if(b(i,j)~=0 && (i==p||j==q))
                if(i==p)
                    for k=1:m
                        if(b(k,q)~=0 && b(k,j)~=0)
                            T=-5;
                            dsub=min(b(k,q),b(i,j));
                            b(p,q)=b(p,q)+dsub;
                            b(k,q)=b(k,q)-dsub;
                            b(k,j)=b(k,j)+dsub;
                            b(i,j)=b(i,j)-dsub;
                            break
                        end
                    end
                else
                    for k=1:n
                        if(b(k,q)~=0 && b(k,j)~=0)
                            T=-5;
                            dsub=min(b(i,j),b(p,k));
                            b(p,q)=b(p,q)-dsub;
                            b(i,j)=b(i,j)-dsub;
                            b(i,k)=b(i,k)-dsub;
                            b(p,k)=b(p,k)-dsub;
                            break
                        end
                    end
                end
            end
        end
    end
    if(T==5)
        break
    end
end
end

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fprintf("\n\nRoundwise Cij-Ui-Vj Matrix,")
c=optCheck(a,b,m,n) %%%%%%%%%% Optimality %%%%%%%%%%
fprintf("Solution Matrix,")
b
end
fprintf("The optimality condition satisfied and hence the cost is: %d\n\n",sum(sum(b.*a)))

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function[c]=optCheck(a,b,m,n)
c=zeros(m,n);
[p q]=find(0~=b);
u(1:m)=intmax;
v(1:n)=intmax;
u(p(1))=0;%%% Initialisationfor u v
while(sum(intmax==u)+sum(intmax==v)~=0)
    [u v]=solv(u,v,p,q,a); %Solve with a simple function
end
for i=1:m %%%% Optimality Checking at empty cell
    for j=1:n
        if(b(i,j)==0)
            c(i,j)=a(i,j)-u(i)-v(j);
        end
    end
end
end
end

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function[u v]=solv(u,v,p,q,a)
k=length(p);
for i=1:k
    if(u(p(i))~=intmax)
        v(q(i))=a(p(i),q(i))-u(p(i));
    end
% end
% for i=1:k
    if(v(q(i))~=intmax)
        u(p(i))=a(p(i),q(i))-v(q(i));
    end
end
end
end

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function [outputArg2,outputArg1] = LCM(Cost,d,s,m,n)
a=Cost;
b=zeros(m,n);
while((sum(d)+sum(s)>0))
    mm=min(min(a));
    [p,q] = find(a==mm,1);
    b(p,q)=min(s(p),d(q));
    s(p)=s(p)-b(p,q);d(q)=d(q)-b(p,q);
    if(s(p)==0)
        a(p,:)=intmax;
    else
        a(:,q)=intmax;
    end
end

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end
end
sm=sum(sum(Cost.*b));
outputArg1 = sm;
outputArg2 = b;
end

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*Given\_Problem =*

2	4	4	1	150
10	3	7	7	200
6	7	20	5	150
50	100	150	200	500

*The initial Matrix,  
b =*

0	0	0	150
0	100	100	0
50	0	50	50

*Initial\_LCM\_Cost =*

2700

*Roundwise Cij-Ui-Vj Matrix,  
c =*

0	-8	-12	0
17	0	0	15
0	-9	0	0

*ROundwise Cij-Ui-Vj Matrix,  
c =*

0	4	0	0
5	0	0	3
0	3	12	0

*Solution Matrix,  
b =*

0	0	50	100
0	100	100	0
50	0	0	100

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*The optimality condition satisfied and hence the cost is: 2100*

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