
```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%%%%%%%%%          ASSIGNMENT 06          %%%%%%%%%%
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
clc
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%%%%%%%%%%%%% PROBLEM 01 %%%%%%%%%%%%%%
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
fprintf('\n\n%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n')
```

```
fprintf('\nOutput for problem 01:\n')
```

```
fprintf('%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n\n')
```

```
disp(' ')
```

```
m=4;n=5;A=[-2 0 0 5 3; 3 2 1 2 2;-4 -3 0 -2 6; 5 3 -4 2 6]
```

```
Minimax=-2000;Maximin=2000;
```

```
for i=1:m
```

```
    if(Minimax<min(A(i,:)))
```

```
        Minimax=min(A(i,:));
```

```
    end
```

```
end
```

```
for i=1:n
```

```
    if(Maximin>max(A(:,i)))
```

```
        Maximin=max(A(:,i));
```

```
    end
```

```
end
```

```
if(Minimax==Maximin)
```

```
    fprintf('The game value using manual coding is=%d\n\n',Minimax)
```

```
else
```

```
    fprintf('There is no saddle point\n\n')
```

```
end
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%%%%%%%%%%%%% Another Way ShortCut %%%%%%%%%%%%%%
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
Minimax=min(max(A))
```

```
Maximin=max(min(A'))
```

```
if(Minimax==Maximin)
```

```
    fprintf('The game value using MATLAB command is= %d\n\n',Minimax)
```

```
end
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
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```
%%%%%%%%%%%%% PROBLEM 02(A) %%%%%%%%%%%%%%
```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

fprintf('\n\n%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n')
fprintf('\nOutput for problem 02(A):\n')
fprintf('%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n\n')
disp(' ')

clear
m=3;n=4;
a=[2 4 4 1; 10 3 7 7; 6 7 20 5];d=[50 100 150 200];s=[150;200;150];
b=zeros(m,n);
for i=1:m%%%%%%%%Finding the matrix:
    for j=1:n
        if(s(i)&& d(j)>0)
            b(i,j)=min(s(i),d(j));
            s(i)=s(i)-b(i,j);d(j)=d(j)-b(i,j);%Subtract
        end
    end
end
fprintf('The cost matrix with northwest rule is,');b
TotalCost=sum(sum(b.*a))

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%% PROBLEM 02(B) %%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

```

fprintf('\n\n%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n')
fprintf('\nOutput for problem 02(B):\n')
fprintf('%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n\n')
disp(' ')

clear
Cost=[2 4 4 1; 10 3 7 7; 6 7 20 5];d=[50 100 150 200];s=[150;200;150];
%Cost=[5 4 3; 8 4 3; 9 7 5];d=[300 200 200];s=[100;300;300];
[m n]=size(Cost);a=Cost;b=zeros(m,n);
while((sum(d)+sum(s)>0))
    % k=k+1; fprintf("Round: %d\n",k);b %%%%For Printing the
    Round
    mm=min(min(a));
    [p,q] = find(a==mm,1);
    b(p,q)=min(s(p),d(q));
    s(p)=s(p)-b(p,q);d(q)=d(q)-b(p,q);
    if(s(p)==0)
        a(p,:)=intmax;
    else
        a(:,q)=intmax;
    end
end
fprintf("\n\nUsing LCM:\n\nCost= %d\nCost
Matrix,",sum(sum(Cost.*b)));b

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%% PROBLEM 03 %%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

fprintf('\n\n%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n')
fprintf('\nOutput for problem 03:\n')
fprintf('%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%\n\n\n')
disp(' ')

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Problem 03 %%%%%%%%%

clc
clear
a=[2 4 4 1; 10 3 7 7; 6 7 20 5];d=[50 100 150
200];s=[150;200;150];m=3;n=4;
Given_Problem=[a s;d sum(d)]
fprintf("The initial Matrix,") %%%%% Initial function created %%
[b,Initial_LCM_Cost]=LCM(a,d,s,m,n)%Initial_Solution=[b s;d sum(d)]

fprintf("\n\n\nRoundwise Cij-Ui-Vj Matrix,")
c=optCheck(a,b,m,n) %%%%%%%%% Optimality %%%%%%%%%
while(sum(sum(c<0))~=0)%%%%%%%% Subtraction Logic without DFS
    %%%%%%%%%
    [p,q]=find(min(min(c))==c,1);
    T=0;
    for i=1:m
        for j=1:n
            if(b(i,j)~=0 && (i==p||j==q))
                if(i==p)
                    for k=1:m
                        if(b(k,q)~=0 && b(k,j)~=0)
                            T=-5;
                            dsub=min(b(k,q),b(i,j));
                            b(p,q)=b(p,q)+dsub;
                            b(k,q)=b(k,q)-dsub;
                            b(k,j)=b(k,j)+dsub;
                            b(i,j)=b(i,j)-dsub;
                            break
                        end
                    end
                else
                    for k=1:n
                        if(b(k,q)~=0 && b(k,j)~=0)
                            T=-5;
                            dsub=min(b(i,j),b(p,k));
                            b(p,q)=b(p,q)-dsub;
                            b(i,j)=b(i,j)-dsub;
                            b(i,k)=b(i,k)-dsub;
                            b(p,k)=b(p,k)-dsub;

```

```

                                break
                            end
                        end
                    end
                end
            end
        end
    end
    if(T==5)
        break
    end
end
end
fprintf("\n\nRoundwise Cij-Ui-Vj Matrix,")
c=optCheck(a,b,m,n) %%%%%%%%%% Optimality %%%%%%%%%%
fprintf("Solution Matrix,")
b
end
fprintf("The optimality condition satisfied and hence the cost is: %d
\n\n",sum(sum(b.*a)))

```

```

%%%%%%%%%%%%
%%%%%%%%%% PROBLEM 04 %%%%%%%%%%
%%%%%%%%%%%%

```

```

fprintf('\n\n%%%%%%%%%%%%\n\n')
fprintf('\nOutput for problem 04:\n')
fprintf('%%%%%%%%%%%%\n\n\n')
disp(' ')

```

```

clear
a=[20 28 19 13; 15 30 31 28; 40 21 20 17; 21 28 26 12];n=length(a);
fprintf('Row and Column Reduction:')
a=(a'-min(a'))'
a=a-min(a)
[c,ic,sol]=optCheck4(a);
while(ic~=n)
mm=min(min(a+c));
for i=1:n
    for j=1:n
        if(sum(c(i,:)==intmax)+sum(c(:,j)==intmax)==2*n)
            a(i,j)=a(i,j)+mm;
        end
        if(c(i,j)~=intmax)
            a(i,j)=a(i,j)-mm;
        end
    end
end
end

```

```

end
[c,ic,sol]=optCheck4(a);
end
Final_Reduced_Matrix=a
Final_Result=sol'

function [c,ic,sol] = optCheck4(c)
ic=0;n=length(c);
for i1=1:2
p=sum(c'==0)';
for i=1:n          %Row Checking
    if(p(i)==1)
        f=find(0==c(i,:));
        c(:,f)=intmax;
        if(f)
            ic=ic+1;sol(i)=f;
        end
    end
end
p=sum(c==0);
for i=1:n          %Column Checking
    if(p(i)==1)
        f=find(0==c(:,i));
        c(f,:)=intmax;
        if(f)
            ic=ic+1;sol(f)=i;
        end
    end
end
end
end
for i=1:n %Making other elements exactly zero to calculate easily
    for j=1:n
        if(c(i,j)~=intmax)
            c(i,j)=0;
        end
    end
end
end
end

```

```

function[c]=optCheck(a,b,m,n)
c=zeros(m,n);
[p q]=find(0~=b);
u(1:m)=intmax;
v(1:n)=intmax;
u(p(1))=0;%%% Initialisationfor u v
while(sum(intmax==u)+sum(intmax==v)~=0)
    [u v]=solv(u,v,p,q,a); %Solve with a simple function
end
for i=1:m %%%% Optimality Checking at empty cell

```

```

        for j=1:n
            if(b(i,j)==0)
                c(i,j)=a(i,j)-u(i)-v(j);
            end
        end
    end
end
end

function[u v]=solv(u,v,p,q,a)
k=length(p);
for i=1:k
    if(u(p(i))~=intmax)
        v(q(i))=a(p(i),q(i))-u(p(i));
    end
end
% end
% for i=1:k
    if(v(q(i))~=intmax)
        u(p(i))=a(p(i),q(i))-v(q(i));
    end
end
end
end

function [outputArg2,outputArg1] = LCM(Cost,d,s,m,n)
a=Cost;
b=zeros(m,n);
while((sum(d)+sum(s)>0))
    mm=min(min(a));
    [p,q] = find(a==mm,1);
    b(p,q)=min(s(p),d(q));
    s(p)=s(p)-b(p,q);d(q)=d(q)-b(p,q);
    if(s(p)==0)
        a(p,:)=intmax;
    else
        a(:,q)=intmax;
    end
end
sm=sum(sum(Cost.*b));
outputArg1 = sm;
outputArg2 = b;
end

```

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
Output for problem 01:
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

A =

-2	0	0	5	3
3	2	1	2	2
-4	-3	0	-2	6
5	3	-4	2	6

The game value using manual coding is=1

Minimax =

1

Maximin =

1

The game value using MATLAB command is= 1

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
Output for problem 02(A):
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
The cost matrix with northwest rule is,
b =
```

50	100	0	0
0	0	150	50
0	0	0	150

TotalCost =

2650

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
Output for problem 02(B):
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

Using LCM:

Cost= 2700
Cost Matrix,
b =

0	0	0	150
0	100	100	0
50	0	50	50

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
Output for problem 03:
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

Given_Problem =

2	4	4	1	150
10	3	7	7	200
6	7	20	5	150
50	100	150	200	500

*The initial Matrix,
b =*

0	0	0	150
0	100	100	0
50	0	50	50

Initial_LCM_Cost =

2700

*Roundwise Cij-Ui-Vj Matrix,
c =*

0	-8	-12	0
17	0	0	15
0	-9	0	0

*ROundwise Cij-Ui-Vj Matrix,
c =*

0	4	0	0
5	0	0	3
0	3	12	0

*Solution Matrix,
b =*

0	0	50	100
0	100	100	0
50	0	0	100

The optimality condition satisfied and hence the cost is: 2100

%%
Output for problem 04:
%%
Row and Column Reduction:

a =

7	15	6	0
0	15	16	13
23	4	3	0
9	16	14	0

a =

7	11	3	0
0	11	13	13
23	0	0	0
9	12	11	0

Final_Reduced_Matrix =

7	8	0	0
0	8	10	13
26	0	0	3
9	9	8	0

Final_Result =

3
1
2
4

The cost matrix with northwest rule is,
b =

50	100	0	0
0	0	150	50
0	0	0	150

TotalCost =

2650

Using LCM:

Cost= 2700

Cost Matrix,

b =

0	0	0	150
0	100	100	0
50	0	50	50

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