

Document

Parallelizing Wave Diffusion with MPI and Open MP is hybrid implementation.

Given: Water surface in a two-dimensional square bucket. The water surface can go up and down between 20.0 and -20.0 through the wave dissemination. No wave at time t means $Z_{t,i,j} = 0.0$.

To simulate wave dissemination over this water surface, I will calculate $t=0$, $t=1$ and $t=2$. Then rotate the matrix for further calculations in fashion $t=0 \leftarrow t=1$ and $t=1 \leftarrow t=2$. I have used static scheduling to parallelize with Open MP.

While parallelizing using MPI, I calculated *stripe* sizes to send to each of the rank for calculation at respective ranks. And received by boundary sharing ranks where Rank0 and Rank=MPI_size-1 will only share single boundary data.

- To calculate stripe size, I have used mathematical logic to divide work as much as possible evenly.
Calculated Remainder and divided remaining rows to ranks $<$ Remainder.
Example: for Size=103, 4 Ranks will divide work amongst them
Rank0 = 25, Rank1= 25, Rank2 = 25, Rank3 = 25
Remainder = $103/4 = 3$
After implementing logic, ranks will get:
Rank0 = $25+1=26$
Rank1= $25+1=26$
Rank2 = $25+1=26$
Rank3 = $25+0=25$
- Calculate First and Last of the stripe
First is calculated inclusive of the num of row
Last is calculated exclusive of the num of row
- Using the wave formula given, calculated for $t=1$ and $t=2$
- At $t=2$ to $\text{max_time} - 1$, I am sending and receiving data to respective ranks for calculations.
- Rotating matrix to store upcoming data in $Z[0]$ and $Z[1]$
- Finally, sending calculate data from all other ranks and receiving at Rank0.

Performance Improvement:

(1) The performance improvement with four machines (i.e., four ranks)

```
[nirali09@cssmpi1h prog2]$ mpirun -np 1 ./Wave2D_mpi 588 500 0 1 >out11.txt
```

Rank[0]'s range = 0 ~ 587

Elapsed time = 7410865

```
[nirali09@cssmpi1h prog2]$ mpirun -np 6 ./Wave2D_mpi 588 500 0 1 > out61.txt
```

Rank[0]'s range = 0 ~ 97

Rank[2]'s range = 196 ~ 293

Rank[1]'s range = 98 ~ 195

Rank[5]'s range = 490 ~ 587

Rank[3]'s range = 294 ~ 391

Rank[4]'s range = 392 ~ 489

Elapsed time = 3353541
 $7410865 / 3353541 = 2.209$ times

(2) The performance improvement with four machines (i.e., four ranks) with multithreading

[nirali09@cssmpi1h prog2]\$ mpirun -np 6 ./Wave2D_mpi 588 500 0 4 > out64.txt

Rank[1]'s range = 98 ~ 195

Rank[0]'s range = 0 ~ 97

Rank[2]'s range = 196 ~ 293

Rank[5]'s range = 490 ~ 587

Rank[4]'s range = 392 ~ 489

Rank[3]'s range = 294 ~ 391

Elapsed time = 2990132

$7410865 / 2990132 = 2.47$ times