

1. INDEFINITE INTEGRATION

SYNOPSIS:

GENERAL FORMULAE

- $\int K dx = Kx + c$ if $K \in R$
- $\int x^n dx = \frac{x^{n+1}}{n+1} + c$, If $n \neq -1$
- $\int \frac{1}{\sqrt{x}} dx = 2\sqrt{x} + c$
- $\int \frac{1}{x} dx = \log |x| + C$
- $\int e^x \cdot dx = e^x + C$
- $\int a^x dx = \frac{a^x}{\log a} + C$ (for $a > 0, a \neq 1$)
- $\int \sin x dx = -\cos x + C$
- $\int \cos x dx = \sin x + C$
- $\int \tan x dx = \log | \sec x | + C$
 $= -\log |\cos x| + c$
- $\int \cot x dx = \log | \sin x | + C$
- $\int \sec x dx = \log | \sec x + \tan x | + C$
 $= \log \left| \tan \left(\frac{\pi}{4} + \frac{x}{2} \right) \right| + C$
- $\int \operatorname{Co sec} x dx = \log | \operatorname{Co sec} x - \cot x | + C$
 $= \log \left| \tan \frac{x}{2} \right| + C$
 $= -\log | \operatorname{Co sec} x + \cot x | + C$

- $\int \sec x \tan x dx = \sec x + C$
- $\int \operatorname{Co sec} x \cot x dx = -\operatorname{Co sec} x + C$
- $\int \sec^2 x dx = \tan x + C$
- $\int \operatorname{Co sec}^2 x dx = -\cot x + C$
- $\int \sinh x dx = \cosh x + C$
- $\int \cosh x dx = \sinh x + C$
- $\int \tanh x dx = \log | \cosh x | + C$
- $\int \coth x dx = \log | \sinh x | + C$
- $\int \operatorname{Sec} h x dx = 2 \tan^{-1}(e^x) + C$
- $\int \operatorname{Co sec} hx = \log \left| \tan h \frac{x}{2} \right| + C$
- $\int \sec^2 x dx = \tan x + C$
- $\int \operatorname{Co sec} h^2 x dx = -\cot h x + C$
- $\int \sec hx \tan h x dx = -\sec hx + C$
- $\int \operatorname{Co sec} h x \cot h x dx = -\operatorname{Co sec} hx + C$

IMPORTANT RESULTS

- $\int f^1(ax+b)dx = \frac{f(ax+b)}{a} + C$
- $\int \frac{f^1(x)}{f(x)} dx = \log | f(x) | + C$
- $\int \{f(x)\}^n \cdot f^1(x) dx = \frac{\{f(x)\}^{n+1}}{n+1} + C$ ($n \neq -1$)

$$\bullet \int f^1\{g(x)\} \cdot g^1(x) dx = f\{g(x)\} + C$$

$$\bullet \frac{d}{dx} \left(\int f(x) dx \right) = f(x)$$

$$\bullet \int \left[\frac{d}{dx} f(x) \right] dx = f(x) + C$$

$$\bullet \int \frac{dx}{\sqrt{1-x^2}} = \sin^{-1} x + C$$

$$= -\cos^{-1} x + C$$

$$\bullet \int \frac{dx}{1+x^2} = \tan^{-1} x + C$$

$$= -\cot^{-1} x + C$$

$$\bullet \int \frac{dx}{|x|\sqrt{x^2-1}} = \sec^{-1} x + C$$

INTEGRATION OF PARTIAL FRACTIONS

$$\bullet \int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \log \left| \frac{x+a}{x+b} \right| + C,$$

$$\bullet \int \frac{1}{(ax+b)(cx+d)} dx = \frac{1}{ad-bc} \log \left| \frac{ax+b}{cx+d} \right| + K$$

$$\bullet \int \frac{1}{(x^2+a^2)(x^2+b^2)} dx = \frac{1}{b^2-a^2} \left[\frac{1}{a} \tan^{-1} \frac{x}{a} - \frac{1}{b} \tan^{-1} \frac{x}{b} \right] + C$$

$$\bullet \int \frac{x}{(x^2+a^2)(x^2+b^2)} dx = \frac{1}{2(b^2-a^2)} \log \left| \frac{x^2+a^2}{x^2+b^2} \right| + C$$

$$\bullet \int \frac{1}{x(x^n+1)} dx = \frac{1}{n} \log \left| \frac{x^n}{1+x^n} \right| + C$$

$$\bullet \int \frac{1}{x(1-x^n)} dx = \frac{1}{n} \log \left| \frac{x^n}{1-x^n} \right| + C$$

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$$\bullet \int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1} \left(\frac{x}{a} \right) + C$$

$$\bullet \int \frac{1}{\sqrt{x^2-a^2}} dx = \cosh^{-1} \left(\frac{x}{a} \right) + C$$

$$= \log \left| x + \sqrt{x^2-a^2} \right| + C$$

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$$\bullet \int \frac{1}{a^2-x^2} dx = \frac{1}{2a} \log \left| \frac{a+x}{a-x} \right| + C$$

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INTEGRATION OF PARTIAL FRACTIONS

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$$\bullet \int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1} \left(\frac{x}{a} \right) + C$$

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INTEGRATION OF PARTIAL FRACTIONS

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INTEGRATION OF PARTIAL FRACTIONS

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$$\bullet \int \frac{1}{(ax+b)(cx+d)} dx = \frac{1}{ad-bc} \log \left| \frac{ax+b}{cx+d} \right| + K$$

$$\bullet \int \frac{1}{(x^2+a^2)(x^2+b^2)} dx = \frac{1}{b^2-a^2} \left[\frac{1}{a} \tan^{-1} \frac{x}{a} - \frac{1}{b} \tan^{-1} \frac{x}{b} \right] + C$$

$$\bullet \int \frac{x}{(x^2+a^2)(x^2+b^2)} dx = \frac{1}{2(b^2-a^2)} \log \left| \frac{x^2+a^2}{x^2+b^2} \right| + C$$

$$\bullet \int \frac{1}{x(x^n+1)} dx = \frac{1}{n} \log \left| \frac{x^n}{1+x^n} \right| + C$$

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$$\bullet \int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1} \left(\frac{x}{a} \right) + C$$

$$\bullet \int \frac{1}{\sqrt{x^2-a^2}} dx = \cosh^{-1} \left(\frac{x}{a} \right) + C$$

$$= \log \left| x + \sqrt{x^2-a^2} \right| + C$$

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INTEGRATION OF PARTIAL FRACTIONS

$$\bullet \int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \log \left| \frac{x+a}{x+b} \right| + C,$$

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INTEGRATION OF PARTIAL FRACTIONS

$$\bullet \int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \log \left| \frac{x+a}{x+b} \right| + C,$$

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INTEGRATION OF PARTIAL FRACTIONS

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INTEGRATION OF PARTIAL FRACTIONS

$$\bullet \int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \log \left| \frac{x+a}{x+b} \right| + C,$$

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INTEGRATION OF PARTIAL FRACTIONS

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INTEGRATION OF PARTIAL FRACTIONS

$$\bullet \int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \log \left| \frac{x+a}{x+b} \right| + C,$$

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$$\bullet \int \frac{dx}{|x|\sqrt{x^2-1}} = \sec^{-1} x + C$$

INTEGRATION OF PARTIAL FRACTIONS

$$\bullet \int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \log \left| \frac{x+a}{x+b} \right| + C,$$

$$\bullet \int \frac{1}{(ax+b)(cx+d)} dx = \frac{1}{ad-bc} \log \left| \frac{ax+b}{cx+d} \right| + K$$

$$\bullet \int \frac{1}{(x^2+a^2)(x^2+b^2)} dx = \frac{1}{b^2-a^2} \left[\frac{1}{a} \tan^{-1} \frac{x}{a} - \frac{1}{b} \tan^{-1} \frac{x}{b} \right] + C$$

$$\bullet \int \frac{x}{(x^2+a^2)(x^2+b^2)} dx = \frac{1}{2(b^2-a^2)} \log \left| \frac{x^2+a^2}{x^2+b^2} \right| + C$$

$$\bullet \int \frac{1}{x(x^n+1)} dx = \frac{1}{n} \log \left| \frac{x^n}{1+x^n} \right| + C$$

$$\bullet \int \frac{1}{x(1-x^n)} dx = \frac{1}{n} \log \left| \frac{x^n}{1-x^n} \right| + C$$

STANDARD INTEGRALS

$$\bullet \int \frac{1}{\sqrt{a^2-x^2}} dx = \sin^{-1} \left(\frac{x}{a} \right) + C$$

$$\bullet \int \frac{1}{\sqrt{x^2-a^2}} dx = \cosh^{-1} \left(\frac{x}{a} \right) + C$$

$$= \log \left| x + \sqrt{x^2-a^2} \right| + C$$

$$\bullet \int \frac{1}{\sqrt{x^2+a^2}} dx = \sinh^{-1} \left(\frac{x}{a} \right) + C$$

$$= \log \left| x + \sqrt{x^2+a^2} \right| + C$$

$$\bullet \int \frac{1}{x^2+a^2} dx = \frac{1}{a} \tan^{-1} \left(\frac{x}{a} \right) + C$$

$$\bullet \int \frac{1}{a^2-x^2} dx = \frac{1}{2a} \log \left| \frac{a+x}{a-x} \right| + C$$

$$\bullet \int \frac{1}{x^2-a^2} dx = \frac{1}{2a} \log \left| \frac{x-a}{x+a} \right| + C$$

$$\bullet \int \sqrt{a^2-x^2} dx = \frac{x}{2} \sqrt{a^2-x^2} + \frac{a^2}{2} \sin^{-1} \left(\frac{x}{a} \right) + C$$

$$\bullet \int \sqrt{x^2-a^2} dx = \frac{x}{2} \sqrt{x^2-a^2} - \frac{a^2}{2} \cosh^{-1} \left(\frac{x}{a} \right) + C$$

$$= \frac{x}{2} \sqrt{x^2-a^2} - \frac{a^2}{2} \log \left| x + \sqrt{x^2-a^2} \right| + C$$

$$\bullet \int \sqrt{x^2+a^2} dx = \frac{x}{2} \sqrt{x^2+a^2} + \frac{a^2}{2} \sinh^{-1} \left(\frac{x}{a} \right) + C$$

$$= \frac{x}{2} \sqrt{x^2+a^2} + \frac{a^2}{2} \log \left| x + \sqrt{x^2+a^2} \right| + C$$