

RAY OPTICS

Plane mirror

- (i) Angle of deviation
 $\delta = 180 - 2\alpha$
- (ii) length of mirror to see a body of height 'H'
 $n = \frac{H}{2}$
- (iii) length of mirror so that boy can see complete wall.
 $n = \frac{1}{3}$ → length of wall.
- (iv) No. of images
 $n = \frac{360}{\theta}$
 (n-1) even → odd
 symm (n-1) unsym (n)
- (v) velocity of image
 • If obj perpendicular
 $\vec{V}_m = \vec{V}_o + \vec{V}_I$
 $\vec{V}_m = \frac{\vec{V}_o + \vec{V}_I}{2}$
- If vel of obj || to mirror
 $V_o = V_I$

Spherical surfaces

converging → concave
 diverging → convex.

(i) focus :- $\frac{R}{2}$
 actual, for marginal ray

$$F = \frac{R-R}{2 \cos i}$$

(ii) mirror formula :-

$$\frac{1}{F} = \frac{1}{v} + \frac{1}{u}$$

$$v = \frac{fu}{u-f}$$

(iii) magnification :-
 transverse / lateral →

$$mt = \frac{h_i}{h_o} = -\frac{v}{u}$$

$$mt = \frac{f}{f-u}$$

(iv) transverse longitudinal magnification :-

$$M_L = \frac{L_i}{L_o} = \frac{|v_2 - v_1|}{|u_1 - u_2|}$$

$$M_L = \frac{L_i}{L_o} = \frac{v^2}{u^2} = m^2 \quad \text{only magnitude}$$

(v) Newton's formula :-

$$f = \sqrt{x_1 x_2}$$

(vi) Velocity of spherical mirror :-

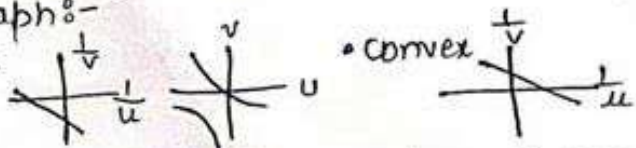
• Obj is moving along principle axis :-

$$\vec{V}_I - \vec{V}_m = -mt^2 (\vec{V}_o - \vec{V}_m)$$

• Obj is ⊥ to principle axis :-

$$\vec{V}_I - \vec{V}_m = -mt (\vec{V}_o - \vec{V}_m)$$

(vii) graph :-
 • concave



Refraction

$$\mu = \frac{c}{v} \rightarrow \text{vacuum} \rightarrow \text{medium}$$

$$\mu_{air} = 1$$

$$\mu_{\text{water}} = \frac{4}{3}$$

$$\mu_{\text{glass}} = \frac{3}{2}$$

$$c = \frac{1}{\sqrt{\mu_o \epsilon_o}} \quad v_m = \frac{1}{\sqrt{\mu_m \epsilon_m}}$$

$$\epsilon_m = \frac{\epsilon_m}{\epsilon_o} \quad \mu_m = \frac{\mu_m}{\mu_o}$$

$$n = \sqrt{\frac{\mu_m}{\mu_o} \times \frac{\epsilon_m}{\epsilon_o}}$$

$$\mu = \sqrt{\mu_m \epsilon_m}$$

for medium :-

$$\frac{c}{v} = \mu \quad v = \frac{c}{\mu} = \frac{c}{\sqrt{\mu_m \epsilon_m}}$$

(i) rarer to denser
 $\angle i > \angle r$

$$\delta = \angle i - \angle r$$

(ii) denser to rarer
 $\angle r > \angle i$

$$\delta = \angle r - \angle i$$

(iii) Cauchy's formula :-

$$\lambda \propto \frac{1}{\mu}$$

$$(iv) \frac{\mu_1}{\mu_2} = \frac{v_2}{v_1} = \frac{\lambda_2}{\lambda_1}$$

(v) Snell's Law :-

$$\mu_1 \sin i = \mu_2 \sin r$$

$$i = \tan^{-1} \mu$$

$$\angle i = \angle e \text{ (emergent)}$$

$$\sin i = \mu \sin r$$

$$\mu \sin r = \sin i$$

$$(vi) \tan i = \frac{\mu_2}{\mu_1}$$

(vii) Real & Apparent Depth

for large angles :-

$$\frac{\tan i}{\tan r} = \frac{h(\text{app})}{H(\text{Real})}$$

for small angles :-

$$\frac{\sin i}{\sin r} = \frac{h}{H}$$

$$\frac{\mu_1}{\mu_2} = \frac{H}{h} \rightarrow \text{from where rays are coming} \rightarrow \text{to where rays are going}$$

$$h(\text{apparent depth}) = \frac{\mu_2}{\mu_1} \times H(\text{Real depth})$$

(viii) Velocity in case of refraction.
 surface → reference

$$\vec{V}_I = \frac{\mu_2}{\mu_1} \vec{V}_o$$

$$\vec{V}_I - \vec{V}_s = \frac{\mu_2}{\mu_1} (\vec{V}_o - \vec{V}_s)$$

(ix) optical path
 $O-P = \mu d$

d = dist travelled by light in medium

$$\mu_1 \sin i = \mu_2 \sin r$$

$$\mu_1 \times \frac{\pi}{H} = \mu_2 \times \frac{\pi}{h}$$