

## ELECTROSTATICS

### LEGEND

$\phi \rightarrow$  Electric flux

$E \rightarrow$  Electrical field

$\varepsilon \rightarrow$  Permittivity

$H \rightarrow$  Magnetic field

$\rho \rightarrow$  electrical resistivity

$Q \rightarrow$  electric charge

$W \rightarrow$  Work done

$V \rightarrow$  Electric potential

$C_s \rightarrow$  Equivalent capacity in series combination

$C_p \rightarrow$  Equivalent capacity in parallel combination

$\lambda \rightarrow$  linear charge density

$C_0 \rightarrow$  Original capacitance

$E_0 \rightarrow$  Original electric field

$E_d \rightarrow$  Electric field with dilectric

## ELECTROSTATICS

1. Charge per unit length (Linear charge density):

$$\lambda = \frac{q}{l}$$

2. Charge per unit surface area (Surface charge density):

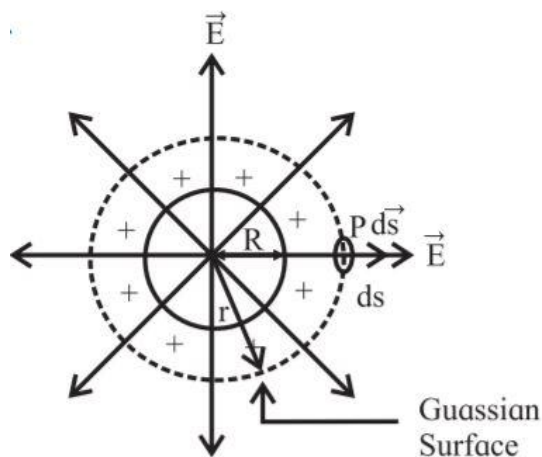
$$\sigma = \frac{q}{a}$$

3. Electric flux:

i.  $\phi = \int \vec{E} \cdot d\vec{s} = Es \cos\theta$

ii.  $\phi = \frac{q}{\epsilon_0}$

iii.  $\phi = \frac{q}{k\epsilon_0}$



4. Dielectric constant of a medium:

$$k = \frac{\epsilon}{\epsilon_0}$$

## ELECTROSTATICS

5. Electric intensity:

$$E = \frac{1}{4\pi k\epsilon_0} \frac{q}{r^2}$$

6. Electric intensity at a point outside a charged spherical conductor:

$$\text{i. } E_{\text{medium}} = \frac{q}{4\pi k\epsilon_0 r^2} = \frac{\sigma R^2}{k\epsilon_0 r^2} \dots (r > R)$$

$$\text{ii. } E_{\text{vacuum}} = \frac{q}{4\pi\epsilon_0 r^2} = \frac{\sigma R^2}{\epsilon_0 r^2} \dots (r > R)$$

$$\text{where, } \sigma = \frac{q}{4\pi R^2}$$

$$\text{iii. } E_{\text{inside}} = 0 \quad \dots (r < R)$$

7. Electric intensity at a point outside a charged cylindrical conductor:

i. Cylinder in any medium,

$$E = \frac{\lambda}{2\pi\epsilon r} = \frac{\lambda}{2\pi k\epsilon_0 r} = \frac{\sigma R}{k\epsilon_0 r} \dots (r > R)$$

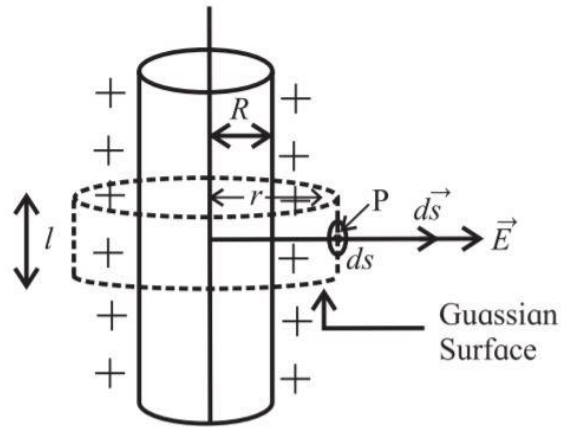
ii. cylinder in free space or vacuum,

$$E = \frac{\lambda}{2\pi\epsilon_0 r} = \frac{1}{4\pi\epsilon_0} \frac{2\lambda}{r} \dots (r > R)$$

iii. Inside the cylinder.

$$E = 0 \quad \dots (r < R)$$

## ELECTROSTATICS



8. Electric intensity at a short distance from a charged conductor of any shape:

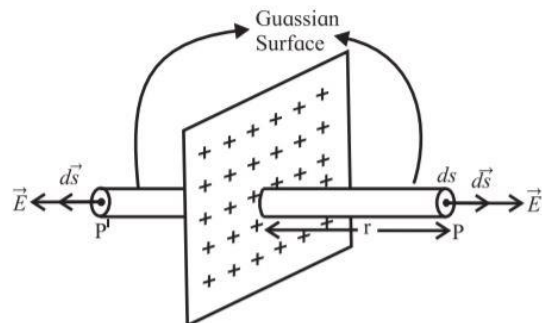
i.  $E = \frac{\sigma}{k\epsilon_0}$

ii. conductor in free space or air or vacuum,

$$E_0 = \frac{\sigma}{\epsilon_0} = KE$$

9. Electric intensity at a point outside a uniformly charged infinite plane sheet:

$$E = \frac{\sigma}{2\epsilon}$$



10. Work done:

i.  $W = qV$

ii.  $W = q (V_b - V_a)$

## ELECTROSTATICS

11. Torque on a dipole:

i.  $\tau = \vec{p} \times \vec{E}$

ii.  $\tau = pE \sin \theta$

iii. for  $\theta = 90^\circ, \tau_{max} = pE$

iv. for  $\theta = 0, \tau_{min} = 0$

12. Work done by the external torque on dipole:

$$W = \int_{\theta_0}^{\theta} \tau_{ext}(\theta) d\theta = \int_{\theta_0}^{\theta} pE \sin \theta d\theta$$

13. Potential energy of electric dipole in external electric field:

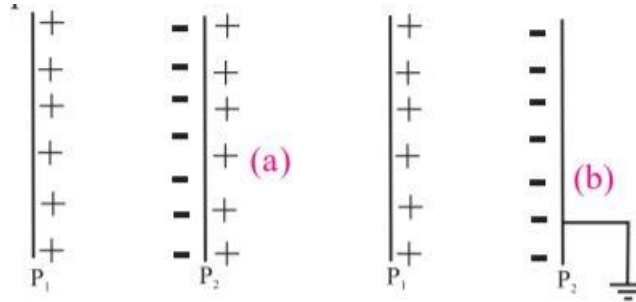
$$U(\theta) - U(\theta_0) = pE (\cos \theta_0 - \cos \theta)$$

14. Capacity of condenser:

$$C = \frac{Q}{V}$$

## ELECTROSTATICS

15. Parallel plate condenser:



i. Intensity between the plates,

$$E = \frac{\sigma}{\epsilon} = \frac{Q}{A\epsilon} = \frac{\sigma}{k\epsilon_0} = \frac{Q}{Ak\epsilon_0}$$

ii. Potential difference between,

$$V = Ed$$

iii. Capacity between the plates,

$$C = \frac{A\epsilon}{d} = kC_0$$

iv. Capacity of vacuum,

$$C_0 = \frac{A\epsilon_0}{d}$$

## ELECTROSTATICS

16. Capacitance of capacitor with dielectric:

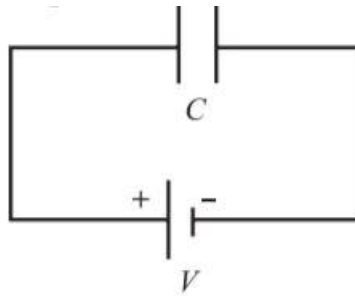
$$C_d = C_0 \frac{E_0}{E_d}$$

Where,  $C_0$  is original capacitance

$E_0$  is original electric field

$E_d$  is electric field with dielectric

17. Energy stored in a charged capacitor:



$$U = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} CV^2 = \frac{1}{2} QV$$

18. Series combination of 'n' condenser:

i.  $V = V_1 + V_2 + V_3 + \dots + V_n$

ii.  $Q = Q_1 = Q_2 = Q_3 = \dots = Q_n$

iii.  $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_n}$

19. Parallel combination of 'n' condenser:

i.  $Q = Q_1 + Q_2 + Q_3 + \dots + Q_n$

ii.  $V = V_1 = V_2 = V_3 = \dots = V_n$

iii.  $C = C_1 + C_2 + C_3 + \dots + C_n$