

UNIT VI

GRAVITATION

Kepler's law of Planetary motion

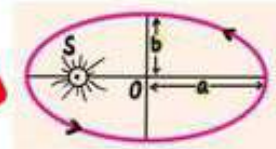
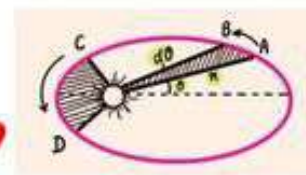
First law : Law of orbits \Rightarrow Planets move in elliptical orbits.

Second law : Law of Areal Velocity \Rightarrow

$$\frac{dA}{dt} = \frac{L}{2m}$$

Third law : Law of Periods \Rightarrow

$$T^2 \propto a^3$$

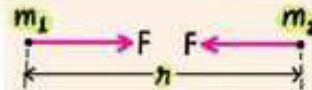


Gravitational force

$$F = G \frac{m_1 m_2}{r^2}$$

Intensity of Gravitational field

$$I = \frac{F}{m}$$



Relation between acceleration due to Earth's gravity g and Gravitational constant G

$$g = \frac{GM_E}{R_E^2}$$

Computation of mass of Earth

$$M_E = \frac{g R_E^2}{G}$$

Density of Earth

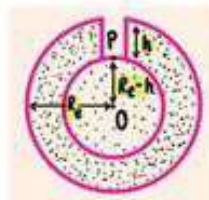
$$\rho = \frac{3g}{4\pi R_E G}$$

Variation in acceleration due to gravity g in going above the surface of the Earth

$$g' = \frac{g}{\left[1 + \frac{h}{R_E}\right]^2}$$

Variation in acceleration due to gravity g in going below the surface of the Earth

$$g' = g \left[1 - \frac{h}{R_E}\right]$$



Expression for variation of g with Latitude

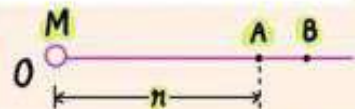
$$g' = g - R_E \omega^2 \cos^2 \lambda$$

Gravitational Potential

$$V = \frac{-W}{m}$$

Gravitational Potential due to a Point - Mass

$$V = -\frac{GM}{r}$$



Gravitational Potential Energy

$$U = -\frac{GMm}{r}$$

Gravitational Potential Energy of a body on Earth's surface

$$U = -\frac{GM_E m}{R_E}$$

$$\text{and } U = -\frac{GM_E m}{r} \therefore GM_E = g R_E^2$$

Orbital speed of Satellite

$$v_o = \sqrt{\frac{GM_E}{R_E + h}}$$

$$v_o = R_E \sqrt{\frac{g}{R_E + h}}$$

