

Multiple Choice Questions

[MHT-CET 2022] (online - shift)

1. Following is the probability distribution of smart phones sold in shop per day :

No. of smart phones	0	1	2	3	4	5
Probability	K	0.3	0.15	0.15	0.1	2K

then $E(x) =$

- a) 2.45 b) 0.75 c) 0.55 d) 2.55
2. A random variable x assumes values $1, 2, 3, \dots, n$ with equal probabilities. If the ratio of variance of x to expected value of x is equal to 4, then the value of n is
- a) 50 b) 30 c) 25 d) 35
3. Two numbers are selected at random from the first six positive integers. If x denotes the larger of two numbers, then $\text{Var}(x) =$

- a) $\frac{1}{3}$ b) $\frac{70}{3}$ c) $\frac{14}{9}$ d) $\frac{14}{3}$

4. A random variable x has following probability distribution

x	0	1	2	3	4	5	6
$P(x)$	K	3K	5K	7K	9K	11K	13K

then $P(x \geq 2)$

- a) $\frac{1}{49}$ b) $\frac{45}{49}$ c) $\frac{40}{49}$ d) $\frac{15}{49}$
5. A player tosses 2 fair coins. He wins ₹ 5 if 2 heads appear, ₹ 2 if 1 head appears and ₹ 1 if no heads appear, then the variance of his winning amount is
- a) $\frac{17}{2}$ b) $\frac{9}{4}$ c) 6 d) $\frac{5}{2}$

6. If the function $P[x=x] = \begin{cases} \frac{K \cdot 2^x}{x!}, & x=0,1,2,3,\dots \\ 0 & \text{otherwise} \end{cases}$ forms p.m.f. then value of K is

- a) $\frac{1}{19}$ b) $\frac{3}{19}$ c) $\frac{2}{19}$ d) $\frac{5}{19}$

7. In pizzahut, the following distribution is found for daily demand

No. of pizzas	5	6	7	8	9	10
Probability	0.07	0.2	0.3	0.3	0.07	0.06

Then expected daily demand and variance are respectively.

- a) 7.28 and 1.52 b) 1.52 and 7.28 c) 7.28 and 54.52 d) 7.28 and 53
8. A random variable x has following probability distribution

x	8	12	16	20	2K
$P(x)$	K	$\frac{1}{6}$	$\frac{3}{8}$	2K	$\frac{1}{12}$

Then the value of K is

- a) $\frac{1}{8}$ b) $\frac{3}{2}$ c) $\frac{1}{2}$ d) $\frac{1}{4}$

Probability Distribution

15. In a meeting 60 % of the members favour and 40 % oppose a certain proposal. A member is selected at random and we take $X = 0$ if he opposed and $X = 1$, if he is in favour, then $\text{Var } X = \dots$

a) 0.36 b) 0.24 c) 0.6 d) 0.06

16. If X is a random variable with p.m.f. as follows

$$\begin{aligned} P(X=x) &= \frac{5}{16} & x &= 0, 1 \\ &= \frac{kx}{48} & x &= 2 \\ &= \frac{1}{4} & x &= 3 \end{aligned}$$

then $E(x) = \dots$

a) 1.1875 b) 1.3125 c) 1.5625 d) 0.5625

17. A bakerman sells 5 types of cakes. Profit due to sale of each type of cake is respectively ₹ 2, ₹ 2.5, ₹ 3, ₹ 1.5, and ₹ 1. The demands of these cakes are 20%, 5%, 10%, 50% and 15% respectively, then the expected profit per cake is

a) ₹ 1.725 b) ₹ 0.01725 c) ₹ 0.1725 d) ₹ 17.25

18. A random variable X has following distribution.

$x = x$	1	2	3	4	5	6
$P[x = x]$	K	3K	5K	7K	8K	K

Then $P(2 \leq x < 5)$

a) $\frac{7}{25}$ b) $\frac{3}{5}$ c) $\frac{24}{25}$ d) $\frac{23}{25}$

19. A coin is tossed three times. If x denotes the absolute difference between the number of heads and the number of tails, then $P(x = 1) = \dots$

a) $\frac{1}{6}$ b) $\frac{1}{2}$ c) $\frac{2}{3}$ d) $\frac{3}{4}$

20. The distribution function $F(x)$ of d.r.v. x is given by

x	1	2	3	4	5	6
$F[x = x]$	0.2	0.37	0.48	0.62	0.85	1

Then $P[x = 4] + P[x = 5] =$

a) 0.14 b) 0.85 c) 0.37 d) 0.23

[MHT-CET 2020]

21. A random variable x takes the values 0, 1, 2. Its mean is 1.2. If $P(x = 0) = 0.3$ then $P(x = 1) =$

a) 0.5 b) 0.2 c) 0.1

22. The c.d.f. $f(x)$ of d.r.v. x is given by

x	-3	-1	0	1	3	5	7	9
$F(x)$	0.1	0.3	0.5	0.65	0.75	0.85	0.90	1

Then $P\{x = 3\} = \dots$

- a) 0.75 b) 0.10 c) 0.85 d) 0.65
23. The c.d.f $F(x)$ associated with p.d.f $f(x) = \begin{cases} 3(1 - 2x^2) & \text{if } 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$

is $K \left(x - \frac{2x^3}{K} \right)$, then value of K is

- a) $\frac{1}{3}$ b) $\frac{1}{6}$ c) 1 d) 3

24. If the probability density function of a continuous random variable is

$$f(x) = \begin{cases} \frac{x^3}{3} & \text{if } -1 < x < 2 \\ 0 & \text{otherwise} \end{cases}$$

Then the cumulative distribution function of x is

- a) $\frac{1}{14} (x^4 - 1)$ b) $\frac{1}{16} [x^4 - 1]$ c) $\frac{1}{12} [x^4 - 1]$ d) $\frac{1}{10} [x^4 - 1]$

25. The p.d.f. of random variable x is given by $f(x) = \begin{cases} \frac{K}{\sqrt{x}} & \text{if } 0 \leq x \leq 4 \\ 0 & \text{otherwise} \end{cases}$

Then $P(1 < x < 4) = \dots$

- a) $\frac{3}{4}$ b) $\frac{1}{5}$ c) $\frac{1}{2}$ d) $\frac{1}{3}$

26. The cumulative distribution function of a continuous random variable x is given by

$$F(x) = \frac{\sqrt{x}}{2}, \text{ then } P[x > 1] \text{ is}$$

- a) $\frac{1}{2}$ b) $\frac{1}{\sqrt{2}}$ c) $\frac{1}{4}$ d) $\frac{1}{3}$

27. If the error involved in making a certain measurement is continuous random variable x with probability density function

$$f(x) = \begin{cases} K(4 - x^2) & \text{if } -2 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

then $P[-1 < x < 1] =$

- a) $\frac{1}{3}$ b) $\frac{13}{16}$ c) $\frac{11}{16}$ d) $\frac{1}{2}$

28. If $F(x) = \frac{x+2}{18}$, where $-2 < x < 4$ is the p.d.f. of r.v. x , then the value of $P(|x| < 2)$ is

- a) $\frac{5}{9}$ b) $\frac{1}{9}$ c) $\frac{2}{9}$ d) $\frac{4}{9}$

64. The p.d.f. of a continuous r.v. X is $f(x) = \begin{cases} 3-6x^2, & 0 < x < 1 \\ 0, & \text{otherwise} \end{cases}$, then $P\left(\frac{1}{4} < x < \frac{1}{3}\right) =$

- a) $\frac{23}{96}$ b) $\frac{52}{243}$ c) $\frac{75}{243}$ d) $\frac{179}{864}$

[MHT - CET 2024]

65. Three balanced coins are tossed simultaneously. If X denotes the number of heads, then the probability distribution of X is

a)

X	0	1	2	3
$P(X)$	1/8	3/8	3/8	1/8

b)

X	0	1	2	3
$P(X)$	3/8	1/8	1/8	3/8

c)

X	0	1	2	3
$P(X)$	3/8	1/8	3/8	1/8

d)

X	0	1	2	3
$P(X)$	1/8	3/8	1/8	3/8

66. Two cards are drawn successively with replacement from a well shuffled pack of 52 cards. Let X denote the random variable of number of jacks obtained in the two drawn cards. Then $P(X=1) + P(X=2)$ equals

- a) $\frac{24}{169}$ b) $\frac{25}{169}$ c) $\frac{49}{169}$ d) $\frac{52}{169}$

67. A bag contains 4 red and 3 black balls. One ball is drawn and then replaced in the bag and the process is repeated. Let X denote the number of times black ball is drawn in 3 draws. Assuming that at each draw, each ball is equally likely to be selected, then the probability distribution of X is given by

a)

X	0	1	2	3
$P(X)$	1/7	3/7	12/7	1/7

b)

X	0	1	2	3
$P(X)$	4/7	3/7	12/7	4/7

c)

X	0	1	2	3
$P(X)$	$(4/7)^2$	$(3/7)^2$	$(12/7)^2$	$(4/7)^2$

d)

X	0	1	2	3
$P(X)$	$(4/7)^3$	$(9/7)(4/7)^2$	$(12/7)(3/7)^2$	$(3/7)^3$

68. A random variable has following probability distribution. Then the value of k is

$X=x$	0	1	2	3	4	5	6	7
$P(X)$	0	$2k$	$2k$	$3k$	k^2	$2k^2$	$7k^2$	$2k$

- a) $\frac{1}{10}$ b) $\frac{3}{20}$ c) $\frac{1}{30}$ d) $\frac{1}{100}$

69. For p.m.f., if $P(X=x) = \begin{cases} \frac{k \cdot 2^x}{x!}, & x=0,1,2,3; k>0 \\ 0, & \text{otherwise} \end{cases}$, then $k =$

- a) $\frac{1}{19}$ b) $\frac{2}{19}$ c) $\frac{3}{19}$ d) $\frac{5}{19}$

70. The p.m.f. of a r.v. is

$$P(X=x) = \begin{cases} \frac{1}{2^5} {}^5C_x, & x=0,1,\dots,5 \\ 0, & \text{otherwise} \end{cases}$$

Then which of the following is not correct?

- a) $P(X=0) = P(X=5)$ b) $P(X \leq 1) = P(X \geq 4)$
 c) $P(X \leq 2) = P(X \geq 3)$ d) $P(X \leq 2) > P(X \geq 3)$