



Oscillations

★ Relation between ν and T
 ν = frequency

$$\nu = \frac{1}{T}$$

★ Time period

$$T = \frac{2\pi}{\omega}$$

★ Displacement Equation of Simple Harmonic Motion (S.H.M.)

$$x(t) = A \cos(\omega t + \phi)$$

$$y(t) = A \sin(\omega t + \phi)$$

★ Velocity in S.H.M.

$$v(t) = -\omega A \sin(\omega t + \phi)$$

$$v(t) = \frac{d}{dt} x(t)$$

★ Acceleration in S.H.M.

$$a = -\omega^2 x(t)$$

★ Time - Displacement curve of S.H.M.

$$y = a \sin\left[2\pi \frac{t}{T}\right]$$

★ Force law in Simple Harmonic motion (Spring)

$$F = -kx$$

$$\omega = \sqrt{\frac{k}{m}}$$

$$T = 2\pi \sqrt{\frac{m}{k}}$$

ω = angular frequency
 T = Time period

★ Potential Energy in S.H.M.

$$U = \frac{1}{2} m \omega^2 y^2$$

$$\text{OR } U = \frac{1}{2} k A^2 \cos^2(\omega t + \phi)$$

★ Kinetic Energy in S.H.M.

$$K = \frac{1}{2} m \omega^2 (a^2 - y^2)$$

$$\text{OR } K = \frac{1}{2} k A^2 \sin^2(\omega t + \phi)$$

★ Total Energy in S.H.M.

$$E = \frac{1}{2} m \omega^2 a^2 = 2\pi^2 m \nu^2 a^2$$

$$\text{OR } E = \frac{1}{2} k A^2$$

★ Time period of S.H.M.

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$\& \omega = \sqrt{\frac{mgL}{I}}$$

★ Motion of body suspended by two springs

$$T = 2\pi \sqrt{\frac{m}{k_1 + k_2}}$$

$$T = 2\pi \sqrt{m \left(\frac{1}{k_1} + \frac{1}{k_2} \right)}$$

★ Time period of Simple Pendulum

$$T = 2\pi \sqrt{\frac{L}{g}}$$

★ Second's Pendulum

$$L = \frac{g}{\pi^2} \approx 1 \text{ m}$$

R_e = Radius of Earth ($6.4 \times 10^6 \text{ m}$)

★ Time period of a Simple pendulum of infinite length

$$T = 2\pi \sqrt{\frac{R_e}{g}}$$

★ Electromagnetic Resonance frequency

$$f = \frac{1}{2\pi \sqrt{LC}}$$