

$$N_A = 6.022 \times 10^{23}$$

# KINETIC THEORY OF GASES : $1 \text{ gm} \rightarrow 10^{-3} \text{ kg}$

## \* Ideal gas Equation:

$$[PV = nRT]$$

$P$  = Pressure,  $V$  = volume  
 $n$  = moles,  $R$  = universal gas constant

$$R = 8.314 \text{ J/mol K}$$

$T$  = Temperature

## \* Kinetic theory:-

1. gas consists of large number of tiny particles
2. No intermolecular forces.

## \* Different form of Ideal gas equation:-

$$n = \frac{m}{m_w}, PV = \frac{m}{m_w} RT$$

$$P \cdot m_w = \rho RT$$

$$n = \frac{N}{N_A} \cdot RT$$

$$PV = N \left( \frac{R}{N_A} \right) T$$

$$PV = N k_B T$$

$$k_B = 1.38 \times 10^{-23}$$

## \* Mean free path:-

The average distance a molecule can travel without colliding is called the mean free path.

$$\lambda = \frac{RT}{\sqrt{2} \pi d^2 N_A P}$$

$d$  = diameter.

$$\lambda = \frac{1}{\sqrt{2} \pi d^2 n}$$

$n$  = number density

$$n = \frac{N_A P}{RT}$$

## \* Velocity of gas molecule

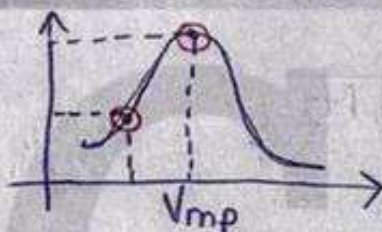
$$V_{rms} = \sqrt{\frac{3RT}{m_w}}$$

$$V_{avg} = \sqrt{\frac{8RT}{\pi m_w}}$$

$$V_{mp} = \sqrt{\frac{2RT}{m_w}}$$

max velocity  $RMS > Avg >$   
 most probable  $\{RAM\}$

## \* Maxwell's Curve:



## \* Pressure equation

$$P = \frac{1}{3} \rho C_{rms}^2$$

$C_{rms} = V_{rms}$  (same)

$$P = \frac{2}{3} \frac{1}{V} (KE)$$

$$KE = \frac{3}{2} P \cdot V$$

$$KE = \frac{3}{2} nRT \quad \text{for } n \text{ moles}$$

$$KE = \frac{3}{2} RT \quad \text{for one mole}$$

$$KE = \frac{3}{2} \frac{RT}{N_A} \quad \text{per molecule}$$

$$KE = \frac{3}{2} k_B T$$

## \* GAS LAWS:-

1. Boyle's law  $PV = \text{const}$

2. Charles's law  $\frac{V}{T} = \text{const}$

3. Gay Lussac law  $\frac{P}{T} = \text{const}$

## \* Degree of freedom:-

$f$  = Vibrational  
 (i) Mono-atomic:-

3 Translation ( $x, y, z$ )  
 0 Rotation  
 0 Vibration  
 $f = 3$

(ii) Diatomic:-

3 Translation ( $x, y, z$ )  
 2 Rotation  
 2 Vibration  
 $f = 5 + 2 = 7$

(iii) Poly-atomic:-

3 Translation ( $x, y, z$ )  
 3 Rotation  
 2 Vibration  
 $f = 6 + 2 = 8$   
 Rigid

## \* $C_p$ and $C_v$ :

Specific heat = amt of heat required to raise the temp of 1 kg substance by  $1^\circ\text{C}$  or  $1^\circ\text{K}$ .

Pressure  $\rightarrow$  const  $\Leftarrow$  Volume  
 $C_p$   $C_v$

$$C_p > C_v$$

$$C_p - C_v = R$$

$C_v = \frac{fR}{2}$   $f$  = degree of freedom

mono  $\Rightarrow C_v = \frac{3R}{2}$   $C_p = \frac{5R}{2}$

dia  $\Rightarrow C_v = \frac{5R}{2}$   $C_p = \frac{7R}{2}$

Poly  $\Rightarrow C_v = \frac{6R}{2}$   $C_p = 4R$

## \* Ratio of specific heats:-

$$\gamma = \frac{C_p}{C_v}; \gamma = 1 + \frac{2}{f}$$