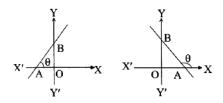
Formulae

1. Slope (Gradient) of a line:

The trigonometrical tangent of the angle that a line makes with the positive direction of the X-axis in anticlockwise sense is called the slope or gradient of the line. The slope of a line is generally denoted by m. Thus, $m = \tan \theta$.



- i. Slope of line parallel to X axis is
- ii. Slope of line parallel to Y axis is $m = \tan 90^0 = \infty$.
- iii. Slope of the line passing through the points

$$(x_1, y_1)$$
 and (x_2, y_2) is $\frac{y_2 - y_1}{x_2 - x_1}$, $x_1 \neq x_2$

- iv. Slope of the line ax + by + c = 0, $b \ne 0$ is a $-\frac{a}{b}$
- v. If m_1 and m_2 be the slopes of two perpendicular lines, then $m_1m_2 = -1$.

2. Equation of straight line in standard forms:

- i. Slope intercept form: The equation of a line with slope 'm' and making an intercept on Y axis is y = mx + c
- ii. Slope point form: The equation of a line which passes through the point (x_1, y_1) and has slope 'm' is $y y_1 = m(x x_1)$
- iii. Two point form: The equation of a line passing through two points (x_1, y_1) and

$$(x_2, y_2)$$
 is $\frac{y - y_1}{y_1 - y_2} = \frac{x - x_1}{x_1 - x_2}$

iv. **Double - intercept form:** The equation of a line which cuts off intercepts a and b from

the X and Y - axis is
$$\frac{x}{a} + \frac{y}{b} = 1$$

- v. Normal form: The equation of a straight line upon which the length of the perpendicular from the origin is p and this perpendicular makes an angle a with $X axis is x cos \alpha + y sin \alpha = p$
- vi. Parametric form: The equation of the straight line passing through (x_1, y_1) and making an angle θ with the positive direction

of X – axis is
$$\frac{x - x_1}{\cos \theta} = \frac{y - y_1}{\sin \theta} = r$$
, where r is the distance of the point (x, y) on the line from the point (x_1, y_1) .

3. General equation of a straight line and its transformation in standard forms:

General form of equation of a line is ax + by + c = 0, its

- i. Slope intercept form: $y = -\frac{a}{b}x \frac{c}{b}$, slope $m = -\frac{a}{b}$ and intercept on Y-axis is $C = -\frac{c}{b}$
- ii. Intercept form: $\frac{x}{-c/a} + \frac{y}{-c/b} = 1$,

x intercept
$$=\left(-\frac{c}{a}\right)$$
 and

y intercept
$$=\left(-\frac{c}{b}\right)$$

iii. Normal form: To change the general form of a line into normal form, first take c to right hand side and make it positive, then divide the whole equation

by
$$\sqrt{a^2 + b^2}$$
 like

$$-\frac{ax}{\sqrt{a^2+b^2}} - \frac{by}{\sqrt{a^2+b^2}} = \frac{c}{\sqrt{a^2+b^2}},$$

where
$$\cos \alpha = -\frac{a}{\sqrt{a^2 + b^2}}$$
,

$$\sin \alpha = -\frac{b}{\sqrt{a^2 + b^2}}, p = \frac{c}{\sqrt{a^2 + b^2}}$$

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Straight Line

it Line

4. Two intersecting lines:

- i. Angle between two intersecting lines:
 - a. If θ is the acute angle between the lines with slopes mi and m₂, then

$$\tan \theta = \left| \frac{\mathbf{m}_1 - \mathbf{m}_2}{1 + \mathbf{m}_1 \mathbf{m}_2} \right|$$

b. If θ is the acute angle between the lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$, then

$$\tan \theta = \left| \frac{a_2 b_1 - a_1 b_2}{a_1 a_2 + b_1 b_2} \right|$$

ii. Point of intersection of two lines:

Point of intersection of two lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$ is

$$(x', y') = \left(\frac{b_1c_2 - b_2c_1}{a_1b_2 - a_2b_1}, \frac{c_1a_2 - c_2a_1}{a_1b_2 - a_2b_1}\right)$$

5. Concurrent lines:

Three or more lines are said to be concurrent if they meet at a point.

- i. If the three lines $a_1x + b_1y + c_1 = 0$, $a_2x + b_2y + c_2 = 0$ and $a_3x + b_3y + c_3 = 0$ are concurrent, then $a_1 (b_2c_3 b_3c_2) b_1 (a_2c_3 a_3c_2) + c_1 (a_2b_3 a_3b_2) = 0$
- 6. Length of perpendicular:
 - i. Distance of a point from a line:

The length p of the perpendicular from the point (x, y) to the line ax + by + c = 0

is given by
$$p = \left| \frac{ax_1 + by_1 + c}{\sqrt{a^2 + b^2}} \right|$$

Length of perpendicular from origin to the

line
$$ax + by + c = 0$$
 is $\left| \frac{c}{\sqrt{a^2 + b^2}} \right|$

ii. Distance between two parallel lines:

The distance between two parallel lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$

is
$$\left| \frac{c_1 - c_2}{\sqrt{a^2 + b^2}} \right|$$

Shortcuts

- Slope of the line equally inclined with the axis is 1 or - 1
- 2. Slope of two parallel lines are equal.
- 3. Equation of a line parallel to ax + by + c = 0 is $ax + by + \lambda = 0$, where λ , is a constant.
- 4. Equation of a line perpendicular to ax + by + c = 0 is $bx ay + \lambda$, = 0, where λ , is a constant.
- 5. If the equation of line be a $\sin \theta + b \cos \theta = c$, then line
 - i. Parallel to it is a $\sin \theta + b \cos \theta = d$
 - ii. Perpendicular to it is a

$$\sin\left(\frac{\pi}{2} + \theta\right) + b \cos\left(\frac{\pi}{2} + \theta\right) = d$$



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MULTIPLE CHOICE QUESTIONS

Classical Thinking

6.1 Slope of a line, Equation of a line in different forms

- Slope of a line which cuts intercepts of equal lengths on the axes is
 - a) 1
- b) 0
- c) 2
- d) $\sqrt{3}$
- The equation of the line whose slope is 3 and which cuts off an intercept 3 from the positive X - axis is
 - A) y = 3x 9
- b) y = 3x + 3
- c) y = 3x + 9
- d) None of these
- If the co-ordinates of A and B are (1, 1) and (5, 7), then the equation of the perpendicular bisector of the line segment AB is
 - a) 2x + 3y = 18
- b) 2x 3y + 18 = 0
- c) 2x + 3y 1 = 0 d) 3x 2y + 1 = 0
- 4. The equation of the line passing through the point (x', y') and perpendicular to the line
 - a) xy' + 2ay + 2ay' x'y' = 0
 - b) xy' + 2ay 2ay' x'y' = 0
 - c) xy' + 2ay + 2ay' + x'y' = 0
 - d) xy' + 2ay 2ay' + x'y' = 0
- 5. The equation of the line bisecting the line segment joining the points (a, b) and (a', b') at right angle, is
 - a) $2(a a')x + 2(b b') v = a^2 + b^2 a'^2 b'^2$
 - b) $(a a') x + (b b') y = a^2 + b^2 a'^2 b'^2$
 - c) $2(a-b) x + 2 (b-b') y = a'^2 + b'^2 a'^2 b'^2$
 - d) None of these
- The equation of a line joining the origin to the point (-4, 5) is
 - a) 5x + 4y = 0
- b) 3x + 4y = 2
- c) 5x 4y = 0
- d) 4x 5y = 0
- 7. The equation of the line which cuts off an intercept 3 units on OX and an intercept – 2 units on OY is

 - a) $\frac{x}{3} \frac{y}{2} = 1$ b) $\frac{x}{3} + \frac{y}{2} = 1$
 - c) $\frac{x}{2} + \frac{y}{3} = 1$ d) $\frac{x}{2} \frac{y}{3} = 1$

- The equation of a line through (3, -4) and perpendicular to the line 3x + 4y = 5 is
 - a) 4x + 3y = 24
- b) y 4 = x + 3
- c) 3y-4x=24 d) $y+4=\frac{4}{2}(x-3)$

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- **9.** Equation of a line passing through (1, 2) and parallel to the line y = 3x - 1 is

 - a) y + 2 = x + 1 b) y + 2 = 3(x + 1)
 - c) y-2=3(x-1) d) -y-2=x-1
- 10. Equation of a line through the origin and perpendicular to the line joining (a, 0) and (-a, 0)is
 - a) y = 0
- b) x = 0
- c) x = -a
- d) y = -a
- 11. The equation of a line which bisects the line joining two points (2, -19) and (6, 1) and perpendicular to the line joining two points (-1, 3) and (5, -1), is
 - a) 3x 2y = 30
- b) 2x y 3 = 0
- c) 2x + 3y = 20
- d) None of these
- 12. The equation of line whose midpoint (x_1, y_1) in between the axes, is

 - a) $\frac{x}{x_1} + \frac{y}{y_1} = 2$ b) $\frac{x}{x_1} + \frac{y}{y_2} = \frac{1}{2}$
 - c) $\frac{x}{x_1} + \frac{y}{y_1} = 1$ d) None of these
- 13. The equation of a line passing through (c, d) and parallel to ax + by + c = 0 is
 - a) a(x + c) + b(y + d) = 0
 - b) a(x + c) b(y + d) = 0
 - c) a(x-c) + b(y-d) = 0
 - d) a(x-c) b(y-d) = 0
- 14. The equation of a line passing through (4, -6)and making an angle 45° with positive X-axis, is

 - a) x y 10 = 0 b) x 2y 16 = 0

 - c) x 3y 22 = 0 d) x 2y 10 = 0
- 15. The equation of a straight line passing through the points (-5, -6) and (3, 10) is
 - a) x 2y = 4
- b) 2x y + 4 = 0
- c) 2x + y = 4 d) x 2y + 4 = 0

- 16. The equation of the line which cuts off intercepts $2a \sec \theta$ and $2a \csc \theta$ on X-axis and Y-axis respectively is
 - a) $x \sin \theta + y \cos \theta 2a = 0$
 - b) $x \cos \theta + y \sin \theta 2a = 0$
 - c) $x \sec \theta + y \csc \theta 2a = 0$
 - d) $x \csc \theta + y \sec \theta 2a = 0$
- 17. A straight line makes an angle of 135° with the X-axis and cuts Y-axis at a distance – 5 from the origin. The equation of the line is
 - a) 2x + y + 5 = 0
- b) x + 2y + 3 = 0
- c) x + y + 5 = 0
- d) x + y + 3 = 0
- 18. The equation of line perpendicular to x + c is
 - a) y = d
- b) x = d
- c) x = 0
- d) None of these
- 19. If the line $\frac{x}{a} + \frac{y}{b} = 1$ passes through the points a
 - (2, -3) and (4, -5), then (a, b) =
 - a) (1, 1)
- b) (-1, 1)
- c) (1,-1)
- d) (-1, -1)
- 20. The equation of a line perpendicular to line ax + by + c = 0 and passing through (a, b) is equal to
 - a) bx ay = 0
- b) bx + ay 2ab = 0
- c) bx + ay = 0
- d) bx ay + 2ab = 0
- **21.** A line passes through (2, 2) and is perpendicular to the line 3x + y = 3. Its y – intercept is
 - a) $\frac{1}{3}$
- c) 1
- 22. The number of straight lines which are equally inclined to both the axes is
 - a) 4
- c) 3
- d) 1
- **23.** Let P(-1, 0), Q(0, 0) and R(3, $3\sqrt{3}$) be three points. Then, the equation of the bisector of the angle PQR is
 - a) $\frac{\sqrt{3}}{2}x + y = 0$ b) $x + \sqrt{3}y = 0$

 - c) $\sqrt{3}x + y = 0$ d) $x + \frac{\sqrt{3}}{2}y = 0$

- **24.** The lines $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$ are perpendicular to each other, if
 - a) $a_1b_2 b_1a_2 = 0$
 - b) $a_1 a_2 + b_1 b_2 = 0$
 - c) $a_1^2b_2 + b_1^2a_2 = 0$
 - d) $a_1b_1 + a_2b_2 = 0$
- **25.** The line passing through (1, 0) and $(-2, \sqrt{3})$ makes an angle of with X-axis.
 - a) 60°
- b) 120°
- c) 150°
- d) 1350

6.2 Two intersecting lines and family of lines

- **26.** The equation of a line through the intersection of lines x - 0 and y = 0 and through the point (2, 2)
 - a) y = x 1
- b) y = -x
- c) y = x
- d) y = -x + 2
- **27.** For the lines 2x + 5y = 1 and 2x 5y = 9, which of the following statement is true?
 - a) Lines are parallel
 - b) Lines are coincident
 - c) Lines are intersecting
 - d) Lines are perpendicular
- 28. The acute angle between the lines y = 3 and $y = \sqrt{3}x + 9$ is
 - a) 30^{0}
- b) 60°
- c) 45°
- d) 90°
- **29.** The angle between the lines $y = (2 \sqrt{3})x + 5$

and
$$y = (2 + \sqrt{3})x - 7$$
 is

- a) 30^{0}
- b) 60°
- c) 45°
- d) 90°
- **30.** Equations of the two straight lines passing through the point (3, 2) and making an angle of 45° with the line x - 2y = 3, are
 - a) 3x + y + 1 = 0 and x + 3y + 9 = 0
 - b) 3x y 7 = 0 and x + 3y 9 = 0
 - c) x + 3y 1 = 0 and x + 3y 9 = 0
 - d) None of these
- 31. The value of k for which the lines 7x 8x + 5 = 0, 3x-4y+5=0 and 4x+5y+k=0 are concurrent is given by
 - a) -45
- b) 44
- c) 54
- d) 54

- **32.** The lines 15x 18y + 1 = 0, 12x + 10y 3 = 0and 6x + 66y - 11 = 0 are
 - a) Parallel
- b) Perpendicular
- c) Concurrent
- d) None of these
- **33.** If $u = a_1x + b_1y + c_1 = 0$, $v = a_2x + b_2y + c_2 = 0$ and $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$, then the curve u + kv = 0 is
 - a) same straight line u
 - b) different straight line
 - c) not a straight line
 - d) None of these
- **34.** The angle between the lines whose intercepts on the axes are (a, -b) and (b, -a) respectively, is

 - a) $\tan^{-1} \frac{a^2 + b^2}{ab}$ b) $\tan^{-1} \frac{b^2 a^2}{2}$
 - c) $\tan^{-1} \frac{b^2 a^2}{2ab}$ d) None of these
- **35.** The angle between the lines $x \cos 30^{0} + y \sin 30^{0} = 3$ and $x \cos 60^{0} + y \sin 60^{0} = 5$
 - a) 90°
- b) 30°
- c) 60°
- **36.** If the lines $y = m_1 x + c_1$, $y = m_2 x + c_2$ and $y = m_3 x + c_3$, are concurrent, then
 - a) $m_1(c_2 c_3) + m_2(c_3 c_1) + m_2(c_1 c_2) = 0$
 - B) $m_1(c_2 c_1) + m_2(c_2 c_2) + m_2(c_1 c_2) = 0$
 - c) $c_1(m_2 m_2) + c_2(m_2 m_1) + c_2(m_1 m_2) = 0$
 - d) $C_1(m_1 m_2) + c_2(m_2 m_3) + C_3(m_3 m_1) = 0$
- 37. The angle between the lines $a_1x + b_1y + c_1 = 0$ and $a_{2}x + b_{2}y + c_{2} = 0$, is
 - a) $\tan^{-1} \frac{a_1b_2 + a_2b_1}{a_1a_2 b_1b_2}$ b) $\cot^{-1} \frac{a_1b_2 + b_1b_2}{a_1b_2 a_2b_1}$
 - c) $\cot^{-1} \frac{a_1b_2 a_2b_2}{a_1a_2 + b_1b_2}$ d) $\tan^{-1} \frac{a_1b_1 a_2b_2}{a_1a_2 + b_1b_2}$

6.3 Distance of a point from a line

- 38. If the length of the perpendicular drawn from the origin to the line whose intercepts on the axes are a and b be p, then

 - a) $a^2 + b^2 = p^2$ b) $a^2 + b^2 = \frac{1}{p^2}$

 - c) $\frac{1}{a^2} + \frac{1}{b^2} = \frac{2}{n^2}$ d) $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{n^2}$

- 39. The length of the perpendicular from the point (b, a) to the line $\frac{x}{a} - \frac{y}{b} = 1$ is

 - a) $\left| \frac{a^2 ab + b^2}{\sqrt{a^2 + b^2}} \right|$ b) $\left| \frac{b^2 ab + a^2}{\sqrt{a^2 + b^2}} \right|$

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- c) $\left| \frac{a^2 + ab b^2}{\sqrt{a^2 + b^2}} \right|$ d) $\left| \frac{a^2 + ab + b^2}{\sqrt{a^2 + b^2}} \right|$
- 40. The length of perpendicular drawn from origin on the line joining (x', y') and (x'', y'') is
 - a) $\left| \frac{x'y'' + x''y'}{\sqrt{(x'' x')^2 + (y'' y')^2}} \right|$
 - b) $\left| \frac{x'y''-x''y'}{\sqrt{(x''-x')^2+(y''-y')^2}} \right|$
 - c) $\left| \frac{x'y'' + y'y''}{\sqrt{(x'' + x')^2 + (y'' + y')^2}} \right|$
 - d) $\left| \frac{x'x'' + y'y''}{\sqrt{(x'' + x')^2 + (y'' y')^2}} \right|$
- 41. The perpendicular distance of the straight line 12x + 5y = 7 from the origin is
 - a) $\frac{7}{13}$ b) $\frac{12}{13}$
- **42.** The length of perpendicular from (3, 1) on line 4x + 3y + 20 = 0, is
 - a) 6
- b) 7
- c) 5
- d) 8
- **43.** The distance of the point (-2, 3) from the line x - y = 5 is
 - a) $5\sqrt{2}$
- b) $2\sqrt{5}$
- c) $3\sqrt{5}$
- d) $5\sqrt{3}$
- **44.** Distance between the lines 5x + 3y 7 = 0 and 15x + 9y + 14 = 0 is
 - a) $\frac{35}{\sqrt{34}}$
- b) $\frac{1}{3\sqrt{34}}$

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Straight Line

- **45.** The position of the point (8, -9) with respect to the lines 2x + 3y - 4 = 6 and 6x + 9y + 8 = 0 is
 - a) Point lies on the same side of the lines
 - b) Point lies on the different sides of the line
 - c) Point lies on one of the line
 - d) None of these
- 46. The length of perpendicular from the point (a $\cos \alpha$, a $\sin \alpha$) upon the straight line $y = x \tan \alpha + c, c > 0$ is
 - a) c cos α
- b) $c sin^2 \alpha$
- c) c $\sec^2 \alpha$
- d) c $\cos^2 \alpha$
- **47.** The equations (b c)x + (c a)y + (a b) = 0and $(b^3 - c^3)x + (c^3 - a^3)y + a^3 - b^3 = 0$ will represent the same line, if
 - a) b = c
- b) c = a
- c) a = b
- d) All the above

Critical Thinking

6.1 Slope of a line, Equation of a line in different forms

- 1. Equation of the hour hand at 4 O' clock is
 - a) $x \sqrt{3}y = 0$ b) $\sqrt{3}x y = 0$
 - c) $x + \sqrt{3}y = 0$ d) $\sqrt{3}x + y = 0$
- 2. A straight line through origin bisects the line passing through the given points (a $\cos \alpha$, a $\sin \alpha$) and (a $\cos\beta$, a $\sin\alpha$), then the lines are
 - a) Perpendicular
 - b) Parallel
 - c) Angle between them is $\frac{\pi}{4}$
 - d) None of these
- A line L is perpendicular to the line 5x y = 1 and the area of the triangle formed by the line L and coordinate axes is 5. The equation of the line L is

 - a) x + 5y = 5 b) $x + 5y = \pm 5\sqrt{2}$

 - c) x 5y = 5 d) $x 5y = 5\sqrt{2}$
- 4. A line passes through the point (3, 4) and cuts off intercepts from the co-ordinates axes such that their sum is 14. The equation of the line is
 - a) 4x 3y = 24
- b) 4x + 3y = 24
- c) 3x 4y = 24
- d) 3x + 4y = 24

- The equation of the line parallel to the line 2x - 3y = 1 and passing through the middle point of the line segment joining the points (1, 3) and (1, -7), is
 - a) 2x 3y + 8 = 0
 - b) 2x 3y = 8
 - c) 2x 3y + 4 = 0
 - d) 2x 3y = 4
- The intercept cut off from Y-axis is twice that from X-axis by the line and line passes through (1, 2), then its equation is
 - a) 2x + y = 4
- b) 2x + y + 4 = 0
- c) 2x y = 4
- d) 2x y + 4 = 0
- The equation of the straight line passing through the point (a $\cos^3 \theta$, a $\sin^3 \theta$) and perpendicular to the line $x \sec \theta + y \csc \theta = a$ is
 - a) $x \cos \theta y \sin 6 = a \cos 2\theta$
 - b) $x \cos \theta + y \sin \theta = a \cos 2\theta$
 - c) $x \sin \theta + y \cos \theta = 3 \cos 2\theta$
 - d) None of these
- Equation of the line passing through the point (-4, 3) and the portion of the line intercepted between the axes which is divided internally in the ratio 5 : 3 by this point, is
 - a) 9x + 20y + 96 = 0
 - b) 20x + 9y + 96 = 0
 - c) 9x 20y + 96 = 0
 - d) None of these
- A straight line through P (1, 2) is such that its intercept between the axes is bisected at P. Its equation is
 - a) x + 2y = 5
 - b) x y + 1 = 0
 - c) x + y 3 = 0
 - d) 2x + y 4 = 0
- 10. The point P(a, b) lies on the straight line 3x + 2y = 13 and the point Q (b, a) lies on the straight line 4x - y = 5, then the equation of line PQ is
 - a) x y = 5
- b) x + y = 5
- c) x + y = -5
- d) x y = -5
- 11. A line AB makes zero intercepts on X axis and Y - axis and it is perpendicular to another line CD, 3x + 4y + 6 = 0. The equation of line AB is
 - a) y = 4
- b) 4x 3y + 8 = 0
- c) 4x 3y = 0
- d) 4x 3y + 6 = 0

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Straight Line

- 12. The line passing through $(-1, \pi/2)$ and perpendicular to $\sqrt{3}\sin\theta + 2\cos\theta = \frac{4}{r}$ is
 - a) $2 = \sqrt{3} r \cos \theta 2r \sin \theta$
 - b) $5 = -2\sqrt{3} r \cos \theta + 4r \sin \theta$
 - c) $2 = \sqrt{3} r \cos \theta + 2r \sin \theta$
 - d) $5 = 2\sqrt{3} \operatorname{rcos} \theta + 4 \operatorname{rsin} \theta$
- 13. The opposite vertices of a square are (1, 2) and (3, 8), then the equation of a diagonal of the square passing through the point (1, 2), is
 - a) 3x y 1 = 0
- b) 3y x 1 = 0
- c) 3x + y + 1 = 0
- d) None of these
- 14. The ends of the base of an isosceles triangle are at (2a, 0) and (0, a). The equation of one side is x = 2a. The equation of the other side is
 - a) x + 2y a = 0
- b) x + 2y = 2a
- c) 3x + 4y 4a = 0 d) 3x 4y + 4a = 0
- 15. The points (1, 3) and (5, 1) are the opposite vertices of a rectangle. The other two vertices lie on the line y = 2x + c, then the value of c will be
 - a) 4
- b) -4
- c) 2
- d) -2
- 16. The equation of the lines on which the perpendiculars from the origin make 30° angle with X-axis and which form a triangle of area

$$\frac{50}{\sqrt{3}}$$
 with axes, are

- a) $x + \sqrt{3}y \pm 10 = 0$ b) $\sqrt{3}x + y \pm 10 = 0$
- c) $x \pm \sqrt{3}y 10 = 0$ d) None of these
- 17. The line joining two points A(2, 0), B(3, 1) is rotated about A in anti-clockwise direction through an angle of 15°. The equation of the line in the new position, is
 - a) $\sqrt{3}x y 2\sqrt{3} = 0$ b) $x 3\sqrt{y} 2 = 0$
 - c) $\sqrt{3}x + y 2\sqrt{3} = 0$ d) $x + \sqrt{3}y 2 = 0$
- **18.** If the lines 2x + 3ay 1 = 0 and 3x + 4y + 1 = 0are mutually perpendicular, then the value of a will be

- a) $\frac{1}{2}$
- b) 2
- d) 2
- 19. The distance of the line 2x 3y = 4 from the point (1, 1) measured parallel to the line
 - a) $\sqrt{2}$
- b) $\frac{5}{\sqrt{2}}$
- c) $\frac{1}{\sqrt{2}}$
- 20. The equation of perpendicular bisectors of the sides AB and AC of a triangle ABC are x - y + 5 = 0 and x + 2y - 0 respectively. If the point A is (1, -2), then the equation of line BC is
 - a) 23x + 14y 40 = 0
 - b) 14x 23y + 40 = 0
 - c) 23x 14y + 40 = 0
 - d) 14x + 23y 40 = 0
- 21. Let PS be the median of the triangle with vertices P(2, 2), Q(6, -1) and R(7, 3). The equation of the line passing through (1,-1) and parallel to PS is
 - a) 2x 9y 7 = 0
 - b) 2x 9y 11 = 0
 - c) 2x + 9y 11 = 0
 - d) 2x + 9y + 7 = 0
- 22. The intercept of a line between the coordinate axes is divided by the point (-5, 4) in the ratio 1:2. The equation of the line will be
 - a) 5x 8y + 60 = 0
 - b) 8x 5y + 60 = 0
 - c) 2x 5y + 30 = 0
 - d) None of these
- 23. The number of lines that are parallel to 2x + 6y + 1 = 0 and have an intercept of length 10 between the coordinate axes is
 - a) 1
- b) 2
- c) 4
- d) Infinitely many
- 24. A straight line moves so that the sum of the reciprocals of its intercepts on two perpendicular lines is constant, then the line passes through
 - a) A fixed point
- b) A variable point
- c) Origin
- d) None of these

- **25.** A line through A(-5, -4) meets the lines x + 3y + 2 = 0, 2x + y + 4 = 0 and x - y - 5 = 0 at B, C and D respectively. If
 - $\left(\frac{15}{AD}\right)^2 + \left(\frac{10}{AC}\right)^2 = \left(\frac{6}{AD}\right)^2$, then the equation

of the line is

- a) 2x + 3y + 22 = 0
- b) 5x 4y + 7 = 0
- x) 3x 2y + 3 = 0
- d) None of these
- **26.** In what direction a line be drawn through the point (1, 2) so that its points of intersection with the

line x + y = 4 is at a distance $\frac{\sqrt{6}}{2}$ from the given

point

- a) 30°
- b) 45°
- c) 60°
- d) 75°
- 27. The sides AB, BC, CD and DA of a quadrilateral are x + 2y = 3, x=1, x - 3y = 4, 5x + y + 12 = 0respectively. The angle between diagonals AC and BD is
 - a) 45°
- b) 60°
- c) 90°
- d) 30°

6.2 Two intersecting lines and family of lines

- 28. The equation of a line passing through the point of intersection of the lines 4x - 3y - 1 = 0 and 5x-2y-3=0 and parallel to the line 2y - 3x + 2 = 0 is
 - a) x 3y = 1
 - b) 3x 2y = 1
 - c) 2x 3y = 1
 - d) 2x y = 1
- 29. The straight line passing through the point of intersection of the straight lines x + 2y - 10 = 0and 2x + y + 5 = 0 is
 - a) 5x 4y = 0
- b) 5x + 4y = 0
- c) 4x 5y = 0
- d) 4x + 5y = 0
- **30.** The equation of the straight line passing through the point of intersection of the lines 5x - 6y - 1 = 0 and 3x + 2y + 5 = 0 and perpendicular to the line 3x - 5y + 11 = 0 is
 - a) 5x + 3y + 8 = 0 b) 3x 5y + 8 = 0
 - c) 5x + 3y + 11 = 0 d) 3x 5y + 11 = 0

- 31. The equation of straight line passing through the intersection of the lines x - 2y = 1 and x + 3y = 2and parallel to 3x + 4y = 0 is
 - a) 3x + 4y + 5 = 0
- b) 3x + 4y 10 = 0

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- c) 3x + 4y 5 = 0 d) 3x + 4y + 6 = 0
- **32.** The point of intersection of the lines

$$\frac{x}{a} + \frac{y}{b} = 1$$
 and $\frac{y}{b} + \frac{y}{a} = 1$ lies on the line

- a) x y = 0
- b) (x + y) (a + b) = 2ab
- c) (lx + my) (a + b) = (l + m) ab
- d) All of these
- 33. If the co-ordinates of the vertices A, B, C of the triangle ABC are (-4, 2), (12, -2) and (8, 6)respectively, then $\angle B =$
 - a) $\tan^{-1}\left(-\frac{6}{7}\right)$ b) $\tan^{-1}\left(\frac{6}{7}\right)$
 - c) $\tan^{-1}\left(-\frac{7}{6}\right)$ d) $\tan^{-1}\left(\frac{7}{6}\right)$
- **34.** If the lines y = 3x + 1 and 2y = x + 3 are equally inclined to the line y = mx + 4, then m =
 - a) $\frac{1+3\sqrt{2}}{7}$ b) $\frac{1-3\sqrt{2}}{7}$
 - c) $\frac{1 \pm 2\sqrt{2}}{7}$ d) $\frac{1 \pm 5\sqrt{2}}{7}$
- **35.** The angle between the lines

 $x \cos \alpha_1 + y \sin \alpha_1 = p_1$ and $x \cos \alpha_2 + y \sin \alpha_2 = p_2$

- a) $0, 1 + \alpha_2$ b) $\alpha_1 \alpha_2$
- c) $2\alpha_1$
- d) $2\alpha_{a}$
- **36.** If the lines $y = (2 + \sqrt{3})x + 4$ and y = kx + 6 are inclined at an angle 60° to each other, then the value of k will be
 - a) 1
- b) 2
- c) 1
- d) 2
- **37.** The lines

$$(p-q)(q-r)y+(r-p)=0$$

$$(q-r)(r-p)y + (p-q) = 0$$

- (r-p) x + (p-q) y + (q-r) = 0 are
- a) parallel
- b) perpendicular
- c) concurrent
- d) none of these

- **38.** Which of the following lines is concurrent with the lines 3x + 4y + 6 = 0 and 6x + 5y + 9 = 0?
 - a) 2x + 3y + 5 = 0
 - b) 3x + 3y + 5 = 0
 - c) 1x + 9y + 3 = 0
 - d) None of these
- **39.** The straight lines x + 2y 9 = 0, 3x + 5y 5 = 0and ax + by - 1 = 0 are concurrent, if the straight line 35x - 22y + 1 = 0 passes through the point
 - a) (a, b)
- b) (b, a)
- c) (-a, -b)
- d) (a, -b)
- **40.** If the lines ax + y + 1 = 0, x + by + 1 = 0 and x + y + c = 0 (a, b, c being distinct and different from 1) are concurrent, then

$$\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} =$$

- a) 0
- b) 1
- c) $\frac{1}{a+b+c}$
- **41.** If the lines ax + 2y + 1 = 0, bx + 3y + 1 = 0 and cx + 4y + 1 = 0 are concurrent, then a, b, c are in
 - a) A. P.
- b) G. P.
- c) H.P.
- d) None of these
- 42. The straight lines 4ax + 3by + c = 0, where a + b + c = 0, will be concurrent, if point is
 - a) (4, 3)
- b) (1/4, 1/3)
- c) (1/2, 1/3)
- d) None of these
- 43. The value of λ , for which the lines 3x + 4y = 5, 5x + 4y = 4 and $\lambda x + 4y = 6$ meet at a point is
 - a) 2
- b) 1
- c) 4
- d) 3
- **44.** The equation of a line passing through the point of intersection of lines 2x + 3y + 1 = 0 and 3x - 5y - 5 = 0 and making an angle of 45° with positive X-axis is
 - a) 2x 19y + 23 = 0
 - b) 19x 23y + 15 = 0
 - c) 19x 19y 23 = 0
 - d) 20x 19y + 23 = 0
- **45.** Which of the following represents the equation of a line passing through point of intersection of lines x + 2y + 5 = 0 and 3x + 4y + 1 = 0 and passing through point (3, 2)?
 - a) 2x + 3y 5 = 0 b) 3x + 2y 13 = 0
 - c) x + 3y + 13 = 0 d) 3x 2y 7 = 0

- **46.** The equation of a line passing through the point of intersection of lines x + 2y + 3 = 0 and 3x + 4y + 7 = 0 and perpendicular to the line x - y + 9 = 0 is
 - a) x + y + 2 = 0
- b) x y 2 = 0
- c) x + y 5 = 0
- d) x + 2y 5 = 0

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- 47. Three sides of a triangle are represented by the equation x + y - 6 = 0, 2x + y - 4 = 0 and x+2y-5=0. The co-ordinate of its orthocentre is
 - a) (10, 11)
- b) (2,3)
- c) (-2, -3)
- d) (-11, -10)
- **48.** The equations of two equal sides of an isosceles triangle are 7x - y + 3 = 0 and x + y - 3 = 0 and the third side passes through the point (1, -10). The equation of the third side is
 - a) 3x y 31 = 0 or x + y + 7 = 0
 - b) 3x y + 7 = 0 or x + 3y 31 = 0
 - c) 3x + y + 7 = 0 or x 3y 31 = 0
 - d) Neither 3x + y + 7 nor x 3y 31 = 0
- 49. For the straight lines given by the equation (2 + k) x + (1 + k)y = 5 + 7k, for different values of k which of the following statements is true
 - a) Lines are parallel
 - b) Lines pass through the point (-2, 9)
 - c) Lines pass through the point (2, -9)
 - d) None of these
- **50.** The diagonals of the parallelogram whose sides are lx + my + n = 0, lx + my + n' = 0, mx + y + n = 0, mx + ly + n' = 0 include an angle
- c) $\tan^{-1} \left(\frac{l^2 m^2}{l^2 + m^2} \right)$ d) $\tan^{-1} \left(\frac{2lm}{l^2 + m^2} \right)$
- **51.** The opposite angular points of a square are (3, 4)and (1, -1). Then the co-ordinates of other two points are
 - a) $D\left(\frac{1}{2}, \frac{9}{2}\right), B\left(-\frac{1}{2}, \frac{5}{2}\right)$
 - b) $D\left(\frac{1}{2}, \frac{9}{2}\right), B\left(\frac{1}{2}, \frac{5}{2}\right)$
 - c) $D\left(\frac{9}{2}, \frac{1}{2}\right), B\left(-\frac{1}{2}, \frac{5}{2}\right)$
 - d) None of these

 $a) a^2$

b) b²

52. If a + b + c = 0 and $p \ne 0$ the lines

ax + (b + c) y = p, bx + (c + a) y = p and cx + (a + b) y = p

- a) do not intersect
- b) intersect
- c) are concurrent
- d) none of these
- **53.** The equation of straight line passing through point of intersection of the straight lines 3x - y + 2 = 0and 5x - 2y + 7 = 0 and having infinite slope is
 - a) x = 2
- b) x + y = 3
- c) x = 3
- d) x = 4
- **54.** If vertices of a parallelogram are respectively (0,0),(1,0),(2,2) and (1,2), then angle between diagonals is
 - a) $\frac{\cdot \cdot}{3}$

6.3 Distance of a point from a line

- 55. The points on the line x + y = 4 which lie at a unit distance from the line 4x + 3y = 10, are
 - a) (3, 1), (-7, 11)
- b) (3, 1), (7, 11)
- c) (-3, 1), (-7, 11) d) (1, 3), (-7, 11)
- **56.** If p and p' be the distances from origin to the lines $x \sec \alpha + y \csc \alpha = k$ and

 $x \cos \alpha - y \sin \alpha = k \cos 2\alpha$, then $4p^2 + p'^2 =$

- a) k
- b) 2k
- $c) k^2$
- d) 2k²
- 57. The distance between two parallel lines 3x + 4y - 8 = 0 and 3x + 4y - 3 = 0 is given by
 - a) 4
- b) 5
- c) 3
- d) 1
- **58.** The vertex of an equilateral triangle is (2, -1) and the equation of its base is x + 2y = 1. The length of its sides is

- 59. The product of the perpendiculars drawn from the points $(\pm \sqrt{a^2 - b^2}, 0)$ on the line

$$\frac{x}{a}\cos\theta + \frac{y}{b}\sin\theta = 1$$
, is

- c) $a^2 + b^2$
- d) $a^2 b^2$
- **60.** The ratio in which the line 3x + 4y + 2 = 0 divides the distance between 3x + 4y + 5 = 0 and 3x + 4y - 5 = 0, is
 - a) 5:3
- b) 3:7
- c) 2:3
- d) None of these

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61. If 2p is the length of perpendicular from the origin

to the lines $\frac{x}{a} + \frac{y}{b} = 1$, then a^2 , $8p^2$, b^2 are in

- a) A. P.
- b) G.P.
- c) H.P.
- d) None of these
- **62.** A point equidistant from the lines

4x + 3y + 10 = 0, 5x - 12y + 26 = 0 and 7x + 24y - 50 = 0 is

- a) (1, -1)
- b) (1, 1)
- (0,0)
- d) (0, 1)
- 63. Which pair of points lie on the same side of 3x - 8y - 7 = 0?
 - a) (0, -1) and (0, 0)
 - b) (4, -3) and (0, 1)
 - c) (-3, -4) and (1, 2)
 - d) (-1, -1) and (3, 7)
- **64.** To which of the following types the straight lines represented by 2x + 3y - 1 = 0 and 2x + 3y - 5 = 0belong
 - a) Parallel to each other
 - b) Perpendicular to each other
 - c) Inclined at 45° to each other
 - d) Coincident pair of straight lines
- **65.** The equations of two lines through (0, a) which are at distance 'a' from the point (2a, 2a) are
 - a) y a = 0 and 4x 3y 3a = 0
 - b) y a = 0 and 3x 4y + 3a = 0
 - c) y a = 0 and 4x 3y + 3a = 0
 - d) None of these
- **66.** If the equation y = mx + c and $x \cos \alpha + y \sin \alpha = p$ represents the same straight line, then
 - a) $p = c\sqrt{1 + m^2}$
 - b) $c = p\sqrt{1 + m^2}$
 - c) $cp = \sqrt{1 + m^2}$

d) $p^2 + c^2 + m^2 = 1$

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Straight Line

67. The equations of the lines through the point of intersection of the lines x - y + 1 = 0 and 2x - 3y + 5 = 0 and whose distance from the

point
$$(3, 2)$$
 is $\frac{7}{5}$, is

- a) 3x 4y 6 = 0 and 4x + 3y + 1 = 0
- b) 3x 4y + 6 = 0 and 4x 3y 1 = 0
- c) 3x 4y + 6 = 0 and 4x 3y + 1 = 0
- d) None of these
- **68.** Equation of a straight line on which length of perpendicular from the origin is four units and the line makes an angle of 120° with the X-axis,
 - a) $x\sqrt{3} + y + 8 = 0$ b) $x\sqrt{3} y = -8$

 - c) $x\sqrt{3} y = 8$ d) $x \sqrt{3}y + 8 = 0$
- **69.** In the equation $y y_1 = m(x x_1)$ if m and x_1 are fixed and different lines are drawn for different values of y₁, then
 - a) The lines will pass through a single point
 - b) There will be a set of parallel lines
 - c) There will be one line only
 - d) None of these
- 70. The equations of the lines passing through the point (1, 0) and at a distance $\frac{\sqrt{3}}{2}$ from the origin,

are

a)
$$\sqrt{3}x + y - \sqrt{3} = 0$$
, $\sqrt{3}x - y - \sqrt{3} = 0$

b)
$$\sqrt{3}x + y + \sqrt{3} = 0$$
, $\sqrt{3}x - y + \sqrt{3} = 0$

c)
$$x + \sqrt{3}y - \sqrt{3} = 0$$
, $x - \sqrt{3}x - \sqrt{3} = 0$

- d) None of these
- 71. $(\sin \theta, \cos \theta)$ and (3, 2) lies on the same side of the line x + y = 1, then θ lies between
 - a) $(0, \pi/2)$
- b) $(0, \pi)$
- c) $(\pi/4, \pi/2)$
- d) $(0, \pi/4)$
- 72. If we reduce 3x + 3y + 7 = 0 to the form $x \cos \alpha + y \sin \alpha = p$, then the value of p is
 - a) $\frac{7}{2\sqrt{3}}$
- c) $\frac{3\sqrt{7}}{2}$

Competitive Thinking

6.1 Slope of a line, Equation of a line in different forms

- The gradient of the line joining the points on the curve $y = x^2 + 2x$ whose abscissa are 1 and 3, is
 - a) 6
- b) 5
- c) 4
- d) 3
- The line passing through the points (3, -4) and 2. (-2, 6) and a line passing through (-3, 6) and (9, -18)
 - a) are perpendicular
 - b) are parallel
 - c) make an angle 60° with each other
 - d) none of these
- The lines y = 2x and x = -2y are
 - a) parallel
 - b) perpendicular
 - c) equally inclined to axes
 - d coincident
- If the line passing through (4, 3) and (2, k) is perpendicular to y = 2x + 3, then k =
 - a) 1
- b) 1
- c) 4
- d) 4
- The equation of a straight line passing through the point (3, 2) and perpendicular to the line y = xis
 - a) x y = 5
- b) x + y = 5
- c) x + y = 1
- d) x y = 1
- The equation of the line perpendicular to the line
 - $\frac{x}{a} \frac{y}{b} = 1$ and passing through the point at which

it cuts X-axis, is

- a) $\frac{x}{a} + \frac{y}{b} + \frac{a}{b} = 0$ b) $\frac{x}{b} + \frac{y}{a} + \frac{b}{a}$
- c) $\frac{x}{h} + \frac{y}{a} = 0$ d) $\frac{x}{h} + \frac{y}{a} = \frac{a}{h}$
- The equation of a line passing through the point (1, 2) and perpendicular to the line x + y + 1 = 0

 - a) y-x+1=0b) y-x-1=0c) y-x+2=0d) y-x-2=0

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Straight Line

- The equation of a straight line passing through (-3, 2) and cutting an intercept equal in magnitude but opposite in sign from the axes is given by
 - a) x y + 5 = 0
- b) x + y 5 = 0
- c) x y 5 = 0
- d) x + y + 5 = 0
- **9.** Equation of the line passing through (-1, 1) and perpendicular to the line 2x + 3y + 4 = 0 is
 - a) 2(y-1) = 3(x+1) b) 3(y-1) = -2(x+1)

 - c) y-1=2(x+1) d) 3(y-1)=x+1
- 10. The points A(1, 3) and C(5, 1) are the opposite vertices of rectangle. The equation of line passing through other two vertices and of gradient 2, is
 - a) 2x + y 8 = 0
- b) 2x y 4 = 0
- c) 2x y + 4 = 0
- d) 2x + y + 7 = 0
- 11. A line is such that its segment between the straight lines 5x-y-4=0 and 3x+4y-4=0 is bisected at the point (1,5), then its equation is
 - a) 83x 35y + 92 = 0
 - b) 35x 83y + 92 = 0
 - c) 35x + 35y + 92 = 0
 - d) None of these
- 12. The equation of a line bisecting perpendicularly the segment joining the points (-4, 6) and (8, 8) is
 - a) 6x + y 19 = 0
- b) y = 7
- c) 6x + 2y 19 = 0 d) x + 2y 7 = 0
- 13. A (-1, 1), B(5, 3) are opposite vertices of a square in jry-plane. The equation of the other diagonal not passing through (A, B) of the square is given
 - a) x 3y + 4 = 0 b) 2x y + 3 = 0
 - c) y + 3x 8 = 0
- d) x + 2y 10
- 14. Equations of diagonals of square formed by lines x = 0, y = 0, x = 1 and y = 1 are

 - a) y = x, y + x = 1 b) y = x, x + y = 2
 - c) 2y = x, $y + x = \frac{1}{2}$ d) y = 2x, y + 2x = 1
- 15. The diagonal passing through origin of a quadrilateral formed by x = 0, y = 0, x + y = 1 and 6x + y = 3 is
 - a) 3x 2y = 0
- b) 2x 3y = 0
- c) 3x + 2y = 0
- d) None of these
- 16. Equation of the straight line making equal intercepts on the axes and passing through the point (2,4) is
 - a) 4x y 4 = 0 b) 2x + y 8 = 0
 - c) x + y 6 = 0
- d) x + 2y 10 = 0

17. The equations of the straight line passing through the point (4, 3) and making intercepts on the co-ordinate axes whose sum is -1, is

a)
$$\frac{x}{2} - \frac{y}{3} = 1$$
 and $\frac{x}{-2} + \frac{y}{1} = 1$

b)
$$\frac{x}{2} - \frac{y}{3} = -1$$
 and $\frac{x}{-2} + \frac{y}{1} = -1$

c)
$$\frac{x}{2} - \frac{y}{3} = 1$$
 and $\frac{x}{2} + \frac{y}{1} = 1$

d)
$$\frac{x}{2} + \frac{y}{1} = 1$$
 and $\frac{x}{-2} + \frac{y}{1} = -1$

- **18.** The equation to the line bisecting the join of (3, -4) and (5, 2) and having its intercepts on the X-axis and the Y-axis in the ratio 2:1 is
 - a) x + y 3 = 0
- b) 2x y = 9
- c) x + 2y = 2
- d) 2x + y = 7
- 19. If the straight line ax + by + c = 0 always passes through (1, -2), then a, b, c are in
 - a) A.P.
- b) H.P.
- c) G.P.
- d) None of these
- 20. The inclination of the straight line passing through the point (-3, 6) and the midpoint of the line joining the points (4, -5) and (-2, 9) is

- 21. For what values of a and b, the intercepts cut off on the coordinate axes by the line ax + by + 8 = 0are equal in length but opposite in sign to those cut off by the line 2x - 3y + 6 = 0 on the axes?

 - a) $a = \frac{8}{3}$, b = -4 b) $a = -\frac{8}{3}$, b = -4

 - c) $a = \frac{8}{2}$, b = 4 d) $a = -\frac{8}{2}$, b = 4
- 22. The medians AD and BE of a triangle with vertices A(0, b), B(0, 0) and C(a, 0) are perpendicular to each other, if
 - a) $a = \sqrt{2}b$
- b) $a = -\sqrt{2}b$
- c) Both (a) and (b) d) None of these

23. If $\left(\frac{3}{2}, \frac{5}{2}\right)$ is the midpoint of line segment

intercepted by a line between axes, the equation of the line is

a)
$$5x + 3y + 15 = 0$$
 b) $3x + 5y + 15 = 0$

a)
$$5x + 5y + 15 = 0$$
 b) $5x + 5y + 15 = 0$

c)
$$5x + 3y - 15 = 0$$
 d) $3x + 5y - 15 = 0$

24. The slope of a line that makes an angle of measure 30° with Y-axis is

a)
$$\sqrt{3}$$

b)
$$-\sqrt{3}$$

c)
$$\pm\sqrt{3}$$

d)
$$\pm \frac{1}{\sqrt{3}}$$

- **25.** If *l*, m, n are in arithmetic progression, then the straight line lx + my + n = 0 will pass through the point
 - a) (-1, 2)
- b) (1, -2)
- (1,2)
- d) (2, 1)
- **26.** A straight line through the point A(3, 4) is such that its intercept between the axes is bisected at A. Its equation is
 - a) x + y = 7
 - b) 3x 4y + 7 = 0
 - c) 4x + 3y = 24
 - d) 3x + 4y = 25
- 27. If a straight line passes through the points

$$\left(\frac{-1}{2},1\right)$$
 and (1,2), then its x-intercept is

- a) -2
- b) -1
- c) 2
- d) 1
- 28. The equation of the perpendicular bisector of the line segment joining A(-2, 3) and B(6, -5) is
 - a) x y = -1
- b) x y = 3
- c) x + y = 3
- d) x + y = 1
- 29. The slope of the straight line which does not intersect X-axis is equal to
 - a) $\frac{1}{2}$
- c) $\sqrt{3}$
- d) 0
- **30.** If the three points A(1, 6), B(3, -4) and C(x,y) are collinear, then the equation satisfying by x and y is
 - a) 5x + y 11 = 0
- b) 5x + 13y + 5 = 0
 - c) 5x 13y + 5 = 0 d) 13x y + 5 = 0

- **31.** If the line px qy = r intersects the co-ordinate axes at (a, 0) and (0, b), then the value of a + b is equal to

 - a) $r\left(\frac{q+p}{pq}\right)$ b) $r\left(\frac{q-p}{pq}\right)$

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- c) $r\left(\frac{p-q}{pq}\right)$ d) $r\left(\frac{p+q}{p-q}\right)$
- **32.** Equation of the line through (α, β) which is the midpoint of the line intercepted between the coordinate axes is
 - a) $\frac{x}{\alpha} + \frac{y}{\beta} = 1$ b) $\frac{x}{\alpha} + \frac{y}{\beta} = 2$

 - c) $\frac{x}{\alpha} \frac{y}{\beta} = -1$ d) $\frac{x}{\alpha} \frac{y}{\beta} = -2$
- **33.** The equation of the line which is such that the portion of line segment between the coordinate axes is bisected at (4, -3) is
 - a) 3x + 4y = 24
- b) 3x 4y = 12
- c) 3x 4y = 24
- d) 4x 3y = 24
- **34.** Two lines represented by equations x + y = 1 and x + ky = 0 are mutually orthogonal if k is
 - a) 1
- b) -1
- c) 0
- d) None of these

6.2 Two intersecting lines and family of lines

35. The equation of a line passing through the point of intersection of the lines x+5y+7=0, 3x+2y-5=0and perpendicular to the line 7x + 2y - 5 = 0, is

a)
$$2x - 7y - 20 = 0$$

- b) 2x + 7y 20 = 0
- c) -2x + 7y 20 = 0
- d) 2x + 7y + 20 = 0
- **36.** A line passing through the point of intersection of 2x + y = 5 and x + 3y + 8 = 0 and parallel to the line 3x + 4y = 1 is
 - a) 3x + 4y + 3 = 0 b) 3x + 4y = 0
 - c) 4x 3y + 3 = 0 d) 4x 3y = 3
- **37.** Equations of lines which passes through the points of intersection of the lines 4x - 3y - 1 = 0 and 2x - 5y + 3 = 0 and are equally inclined to the axes are
 - a) $y \pm x = 0$
- b) $y-1=\pm 1 (x-1)$
- c) $x-1=\pm 2 (y-1)$ d) $y \pm x = 2$

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Straight Line

- **38.** Angle between the lines $\frac{x}{a} + \frac{y}{b} = 1$ and
 - $\frac{x}{a} \frac{y}{b} = 1$ is

 - a) $2 \tan^{-1} \frac{b}{a}$ b) $\tan^{-1} \frac{2ab}{a^2 + b^2}$
 - c) $\tan^{-1} \frac{a^2 b^2}{a^2 + b^2}$ d) None of thes
- **39.** The angle between the two lines y 2x = 9 and x + 2y = -1, is
 - a) 60°
- b) 30°
- c) 90°
- d) 45°
- **40.** If $\frac{1}{ab'} + \frac{1}{ba'} = 0$, then lines $\frac{x}{a} + \frac{y}{b} = 1$ and
 - $\frac{x}{b'} + \frac{y}{a'} = 1$ are
 - a) Parallel
 - b) Inclined at 60° to each other
 - c) Perpendicular to each other
 - d) Inclined at 30° to each other
- **41.** Angle between x = 2 and x 3y = 6 is
 - a) ∞
- b) tan^{-1} (3)
- c) $\tan^{-1}\left(\frac{1}{2}\right)$ d) None of these
- **42.** The angle between the lines 2x y + 3 = 0 and x + 2y + 3 = 0 is
 - a) 90°
- b) 60°
- c) 45°
- d) 30°
- **43.** If the lines ax + by + c = 0, bx + cy + a = 0 and cx + ay + b = 0 be concurrent, then
 - a) $a^3 + b^3 + c^3 + 3abc = 0$
 - b) $a^3 + b^3 + c^3 abc = 0$
 - c) $a^3 + b^3 + c^3 3abc = 0$
 - d) None of these
- **44.** For what value of 'a' the lines x = 3,y = 4 and 4x - 3y + a = 0 are concurrent
 - a) 0
- b) -1
- c) 2
- d) 3
- **45.** The lines 2x + y 1 = 0, ax + 3y 3 = 0 and 3x + 2y - 2 = 0 are concurrent for
 - a) All a
- b) a = 4 only
- c) $-1 \le a \le 3$
- d) a > 0 only

- **46.** If the lines 4x + 3y = 1, x y = -5 and 5y + bx = 3 are concurrent, then b equals
 - a) 1
- b) 3
- c) 6
- d) 0
- 47. If a and b are two arbitrary constants, then the straight line (a - 2b)x + (a + 3b)y + 3a + 4b = 0will pass through
 - a) (-1, -2)
- b) (1, 2)
- c) (-2, -3)
- d) (2,3)
- 48. If a, b, c are in harmonic progression, then straight

line $\frac{x}{a} + \frac{y}{b} + \frac{1}{c} = 0$ always passes through a fixed

- point, that point is
- b) (-1, 2)
- c) (1, -2)

a) (-1-2)

- d) (1, -1/2)
- 49. The equation to the sides of a triangle are x - 3y = 0, 4x + 3y = 5, and 3x + y = 0. The line 3x - 4y = 0 passes through
 - a) The incentre
 - b) The centroid
 - c) The circumcentre
 - d) The orthocentre of the triangle
- 50. Two consecutive sides of a parallelogram are 4x + 5y = 0 and 7x + 2y = 0. If the equation to one diagonal is 11x + 7y = 9, then the equation of the other diagonal is
 - a) x + 2y = 0
- b) 2x + y = 0
- c) x y = 0
- d) None of these
- **51.** The triangle formed by the lines x + y 4 = 0, 3x + y = 4, x + 3y = 4 is
 - a) isosceles
- b) equilateral
- c) right-angled
- d) none of these
- **52.** The lines ax + by + c = 0, where 3a + 2b + 4c = 0are concurrent at the point
 - a) (1/2,3/4)
- b) (1,3)
- c) (3,1)
- d) (3/4,1/2)
- 53. The parallelism condition for two straight lines one of which is specified by the equation ax + by + c = 0, the other being represented parametrically by $x = \alpha t + \beta$, $y = \gamma t + \delta$ is given
 - a) $\alpha\delta b\alpha = 0$, $\beta = \delta = c = 0$
 - b) $a\alpha b\gamma = 0$, $\beta = \delta = 0$
 - c) $a\alpha + b\gamma = 0$
 - d) $ay = b\alpha = 0$

54. The equation of the line which passes through the point (3, -2) and are inclined at 60° to the line $\sqrt{3}x + y = 1$, is

a)
$$y + 2 = 0, \sqrt{3}x - y - 2 - 3\sqrt{3} = 0$$

b)
$$x-2=0, \sqrt{3}x-y+2+3\sqrt{3}=0$$

c)
$$\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$$

d)
$$x - \sqrt{3}y + 2 + 3\sqrt{3} = 0$$

55. The point (-4, 5) is the vertex of a square and one of its diagonals is 7x - y + 8 = 0. The equation of the other diagonal is

a)
$$7x - y + 23 = 0$$

b)
$$7y + x = 30$$

c)
$$7y + x = 31$$

d)
$$x - 7y = 30$$

56. The line passing through the point of intersection of x + y = 2, x - y = 0 and is parallel to x + 2y = 5 is

a)
$$x + 2y = 1$$

b)
$$x + 2y = 2$$

c)
$$x + 2y = 4$$

d)
$$x + 2y = 3$$

- 57. The line parallel to the X-axis and passing through the intersection of the lines ax + 2by + 3b = 0 and bx - 2ay - 3a = 0, where $(a, b) \neq (0, 0)$ is
 - a) above the X-axis at a distance of 3/2 from it
 - b) above the X-axis at a distance of 2/3 from it
 - c) below the X-axis at a distance of 3/2 from it.
 - d) below the X-axis at a distance of 2/3 from it
- **58.** The angle between the lines

 $x \cos \alpha + y \sin \alpha = a$ and $x \sin \beta - y \cos \beta = a$ is

a)
$$\beta - \alpha$$

b)
$$\pi + \beta - \alpha$$

c)
$$\frac{\pi}{2} + \beta + \alpha$$
 d) $\frac{\pi}{2} - \beta + \alpha$

d)
$$\frac{\pi}{2} - \beta + \alpha$$

- **59.** A line passes through the point of intersection of the lines 3x + y + 1 = 0 and 2x - y + 3 = 0 and makes equal intercepts with axes. The equation of the line is
 - a) 5x + 5y 3 = 0 b) x + 5y 3 = 0
 - c) 5x y 3 = 0
- d) 5x + 5y + 3 = 0
- **60.** The length of the straight line x 3y = 1intercepted by the hyperbola $x^2 - 4y^2 = 1$, is
 - a) $\sqrt{10}$ units

b)
$$\frac{6}{5}$$
 units

- c) $\frac{6}{\sqrt{10}}$ units d) $\frac{6}{5}\sqrt{10}$ units

- **61.** The straight lines x + y = 0, 5x + y = 4 and x + 5y = 4 form
 - a) an isosceles triangle
 - b) an equilateral triangle
 - c) a scalene triangle
 - d) a right angled triangle

6.3 Distance of a point from a line

62. The points on the X-axis whose perpendicular distance from the line $\frac{x}{1} + \frac{y}{1} = 1$ is a, are

a)
$$\left[\frac{a}{b} \left(b \pm \sqrt{a^2 + b^2}\right), 0\right]$$

b)
$$\left[\frac{b}{a} (b \pm \sqrt{a^2 + b^2}), 0\right]$$

c)
$$\left[\frac{a}{b}\left(a\pm\sqrt{a^2+b^2}\right),0\right]$$

- d) None of these
- **63.** The distance between the lines 3x + 4y = 9 and 6x + 8y = 15 is

a)
$$\frac{3}{2}$$

a)
$$\frac{3}{2}$$
 b) $\frac{3}{10}$

- c) 6
- d) None of these
- 64. The length of the perpendicular drawn from origin upon the straight line $\frac{x}{3} - \frac{y}{4} = 1$ is

a)
$$2\frac{2}{5}$$

b)
$$3\frac{1}{5}$$

c)
$$4\frac{2}{5}$$

d)
$$3\frac{2}{5}$$

- **65.** Two points A and B have co-ordinates (1, 1) and (3, -2) respectively. The co-ordinates of a point distant $\sqrt{85}$ from B on the line through B perpendicular to AB are
 - a) (4, 7)
- b) (7,4)
- (5,7)
- d) (-5, -3)
- **66.** The equation of the base of an equilateral triangle is x + y = 2 and the vertex is (2, 1). The length of the side of the triangle is
 - a) $\sqrt{3/2}$
- b) $\sqrt{2}$
- c) $\sqrt{2/3}$
- d) None of these

- 67. Let α be the distance between the lines -x + y = 2 and x - y = 2 and β be the distance between the lines 4x - 3y = 5 and 6y - 8x = 1,
 - a) $20\sqrt{2} \beta = 11\alpha$ b) $20\sqrt{2} \alpha = 118$
 - c) $11\sqrt{2}\beta = 20\alpha$
- d) None of these
- **68.** Choose the correct statement which describe the position of .the point (-6, 2) relative to straight lines 2x + 3y - 4 = 0 and 6x + 9y + 8 = 0?
 - a) Below both the lines
 - b) Above both the lines
 - c) In between the lines
 - d) None of these
- **69.** If the equation of base of an equilateral triangle is 2x - y = 1 and the vertex is (-1, 2), then the length of the side of the triangle is
 - a) $\sqrt{\frac{20}{3}}$ b) $\frac{2}{\sqrt{15}}$
- **70.** The vertices of a triangle are (2, 1), (5, 2) and (4, 4). The lengths of the perpendicular from these vertices on the opposite sides are

 - a) $\frac{7}{\sqrt{5}}, \frac{7}{\sqrt{13}}, \frac{7}{\sqrt{6}}$ b) $\frac{7}{\sqrt{6}}, \frac{7}{\sqrt{8}}, \frac{7}{\sqrt{10}}$

 - c) $\frac{7}{\sqrt{5}}, \frac{7}{\sqrt{8}}, \frac{7}{\sqrt{15}}$ d) $\frac{7}{\sqrt{5}}, \frac{7}{\sqrt{13}}, \frac{7}{\sqrt{10}}$
- 71. The vertices of a triangle OBC are (0, 0), (-3, -1) and (-1, -3) respectively. Then the equation of line parallel to BC which is at $\frac{1}{2}$ unit distant from origin and cuts OB and OC, is
 - a) $2x + 2y + \sqrt{2} = 0$ b) $2x 2y \sqrt{2} = 0$
 - c) $2x 2v + \sqrt{2} = 0$ d) None of these
- 72. The line L given by $\frac{x}{5} + \frac{y}{b} = 1$ passes through the point (13, 32). The line K is parallel to K and the equation $\frac{x}{c} + \frac{y}{3} = 1$. Then, the distance between L and K is

- 73. The equation of one of the lines parallel to 4x - 3y = 5 and at a unit distance from the point (-1, -4) is

 - a) 3x + 4y 3 = 0 b) 3x + 4y + 3 = 0

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- c) 4x 3y + 3 = 0 d) 4x 3y 3 = 0
- 74. The length of the perpendicular from the origin
 - on the line $\frac{x \cos \alpha}{b} \frac{y \cos \alpha}{a} 1 = 0$ is
- 75. The number of points on the line x + y = 4 which are unit distance apart from the line 2x + 2y = 5is
 - a) 0
- b) 1
- c) 2
- d) Infinity
- **76.** The distance between the parallel lines y = x + a, y = x + b is
 - a) $\frac{|a-b|}{\sqrt{2}}$ b) |a-b|

 - c) |a + b| d) $\frac{|a + b|}{\sqrt{2}}$
- 77. The equation of straight line equally inclined to the axis and equidistant from the points (1, -2)and (3, 4) is ax + by + c = 0, where

 - a) a = 1, b = 1, c = 1 b) a = 1, b = 1, c = -1
 - c) a = 1, b = 1, c = 2 d) None of these
- **78.** A straight line passes through the points (5, 0) and (0, 3). The length of perpendicular from the point (4, 4) on the line is
 - a) $\frac{15}{\sqrt{34}}$
- b) $\frac{\sqrt{17}}{2}$

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Evaluation Test

- If the line y = 7x 25 meets the circle $x^2 + y^2 = 25$ at the points A, B, then the distance between A and Bis
 - a) $\sqrt{10}$
- b) 10
- c) $5\sqrt{2}$
- d) 5
- If $f(\alpha) = x \cos \alpha + y \sin \alpha p(\alpha)$, then the lines $f(\alpha) = 0$ and $f(\beta) = 0$ are perpendicular to each other, if

 - a) $\alpha = \beta$ b) $\alpha + \beta = \frac{\pi}{2}$
 - c) $|\alpha \beta| = \frac{\pi}{2}$ d) none of these
- The locus of the orthocentre of the triangle formed by the lines (1 + p)x - py + p(1 + p) = 0, (1 + q)x - qy + q(1 + q) = 0 and y = 0, where $p \neq q$, is
 - a) a hyperbola
- b) a parabola
- c) an ellipse
- d) a straight line
- 4. If the straight line ax + by + c = 0 make a triangle of constant area with coordinate axes, then
 - a) a, b, c are in G.P. b) a, c, b are in G.P.
 - c) c, a, b are in G.P. d) none of these
- 5. Let $0 < \alpha < \frac{\pi}{2}$ be a fixed angle.

If $P = (\cos\theta, \sin\theta)$ and $Q = (\cos(\alpha - \theta), \sin(\theta - \theta))$, then Q is obtained from P by

- a) clockwise rotation around origin through an angle α
- b) anti-clockwise rotation around origin through an angle α
- c) reflection in the line through origin with slope
- d) reflection in the line through origin with slope $\frac{\tan \alpha}{2}$
- Let P(-1, 0), Q(0, 0) and R(3, $3\sqrt{3}$) be three points. The equation of the bisector of the angle POR is
 - a) $\frac{\sqrt{3}}{2}x + y = 0$ b) $x + \sqrt{3}y = 0$

 - c) $\sqrt{3}x + y = 0$ d) $x + \frac{\sqrt{3}}{2}y = 0$

- A square of side V lies above the X-axis and has one vertex at the origin. The side passing through the origin makes an angle $\alpha(0 < \alpha < \pi/4)$ with the positive direction of X-axis. The equation of its diagonal not passing through the origin is
 - a) $y(\cos \alpha + \sin \alpha) + x(\cos \alpha \sin \alpha) = a$
 - b) $y(\cos \alpha \sin \alpha) x(\sin \alpha \cos \alpha) = a$
 - c) $y(\cos \alpha + \sin \alpha) + x(\sin \alpha \cos \alpha) = a$
 - d) $y(\cos \alpha + \sin \alpha) + x(\sin \alpha + \cos \alpha) = a$
- A line L passes through the points (1, 1) and
 - (2,0) and another line L' passes through $\left(\frac{1}{2},0\right)$

and perpendicular to L. Then the area of the triangle formed by the lines L, L' and Y-axis is

- The number of integer values of m, for which the x-co-ordinate of the point of intersection of the lines 3x + 4y = 9 and y = mx + 1 is also an integer,
 - a) 2
- b) 0
- c) 4
- d) 1
- 10. If straight lines ax + by + p = 0 and $x \cos \alpha + y$

 $\sin \alpha - p = 0$ are inclined at an angle $\frac{\pi}{4}$ and

meet the straight line x sin α – y cos α = 0 at the same point, then the value of $a^2 + b^2$ is equal to

- a) 1
- b) 2
- c) 3
- d) 4
- 11. A line Ax + y = 1 passes through the point A(2, -7) meets the line BC whose equation is 3x - 4y + 1 = 0 at the point B. The equation to the line AC so that AB = AC is
 - a) 52x + 89y + 519 = 0
 - b) 52x + 89y 519 = 0
 - c) 89x + 52y + 519 = 0
 - d) 89x + 52y 519 = 0

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Answer Key



Classical Thinking

- 5. (A) 7. (A) 8. (D) 9. (C) 10. (B) (A) 3. (A) 4. (B) (A) 6. (A) 2. 13. (C) 14. (A) 15. (B) (B) 17. (C) 18. (A) 19. (D) 20. (A) 11. (A) 12. (A) 16. 30. (B) 21. (D) 22. (B) 23. (C) 24. (B) 25. (C) 26. (C) 27. (C) 28. (B) 29. (B) 34. (C) 35. (B) 36. (A) 37. (B) 38. (D) 39. (B) 40. (B) 31. (A) 32. (C) 33. (A)
- 41. (A) 42. (B) 43. (A) 44. (C) 45. (A) 46. (A) 47. (D)

Critical Thinking

- (D) 10. (B) (C) 2. (A) 3. (B) 5. (B) (A) 7. (A) 8. (C) (B) 4. 6. 11. (C) 12. (A) 13. (A) 14. (D) 15. (B) 16. (B) 17. (A) 18. (C) 19. (A) 20. (D) 24. (A) (D) 25. (A) 26. 27. 28. (B) 29. (B) 30. (A) 21. (D) 22. (B) 23. (B) (C) 31. (C) 32. (D) 33. (D) 34. (D) 35. (B) 36. (C) 37. (C) 38. (B) 39. (A) 40. (B) 42. (B) 43. (B) 44. (C) 45. (B) 46. (A) 47. (D) 48. (C) 49. (B) 50. (B) 41. (A) 51. (C) 52. (A) 53. (C) 54. (D) 55. (A) 56. (C) 57. (D) 58. (B) 59. (B) 60. (B) 61. (C) 62. (C) 63. (D) 64. (A) 65. (C) 66. (B) 67. (C) 68. (A) 69. (B) 70. (A) 71. (D) 72. (D)
- 8

Competitive Thinking

5. 7. (B) 8. (A) (A) 10. (B) (A) (B) 3. (B) 4. (D) (B) 6. (D) 2. 11. (A) 12. (A) 13. (C) 14. (A) 15. (A) (C) 17. (A) 18. (C) 19. (A) 20. (D) 16. 22. (C) 23. (C) 24. (C) 25. (B) 26. (C) 27. (A) 28. (B) 29. (D) 30. (A) 21. (D) 31. (B) 32. (B) 33. (C) 34. (B) 35. (A) 36. (A) 37. (B) 38. (A) 39. (C) 40. (C) 41. (B) 42. (A) 43. (C) 44. (A) 45. (A) 46. (C) 47. (A) 48. (C) 49. (D) 50. (C) 51. (A) 52. (D) 53. (C) 54. (A) 55. (C) 56. (D) 57. (C) 58. (D) 59. (A) 60. (D) 61. (A) 62. (A) 63. (B) 64. (A) 65. (C) 66. (C) 67. (A) 68. (A) 69. (A) 70. (D) 73. (D) 75. (A) 76. (A) 77. (B) 71. (A) 72. (D) 74. (D) 78. (D)

Answers to Evaluation Test

1. C) 2. C) 3. D) 4.B) 5. D) 6. C) 7. A) 8. D) 9. (A) 10. (B) 11. (A)

MATHEMATICS - XI OBJECTIVE



Answer Key



Classical Thinking

- (A) 2. (A) 3. (A) 4. (B) 5. (A) 6. (A) 7. (A) 8. (D) 9. (C) 10. (B) 17. (C) 18. (A) 19. (D) 20. (A) 11. (A) 12. (A) 13. (C) 14. (A) 15. **(B)** 16. (B) 25. (C) 26. (C) 27. (C) 28. (B) 29. (B) 30. (B) 21. (D) 22. (B) 23. (C) 24. (B)
- 33. (A) 34. (C) 35. (B) 36. (A) 37. (B) 38. (D) 39. (B) 40. (B) 31. (A) 32. (C) 41. (A) 42. (B) 43. (A) 44. (C) 45. (A) 46. (A) 47. (D)

Critical Thinking

(A) (D) (C) 2. (A) 3. (B) 4. (B) 5. (B) 6. (A) 7. 8. (C) 9. 10. (B) 1. 15. 12. (A) 13. (A) (B) 17. (A) 18. (C) 19. (A) 20. (D) 11. (C) 14. (D) 16. (B) 25. (A) 28. (B) 30. (A) 21. (D) 22. (B) 23. (B) 24. (A) 26. (D) 27. (C) 29. (B) 32. (D) 33. (D) 35. (B) 36. (C) 37. (C) 38. (B) 39. (A) 40. (B) 31. (C) 34. (D) 45. (B) 48. (C) 41. (A) 42. (B) 43. (B) 44. (C) 46. (A) 47. (D) 49. (B) 50. (B) 51. (C) 52. (A) 53. (C) 54. (D) 55. (A) 56. (C) 57. (D) 58. (B) 59. (B) 60. (B) 61. (C) 62. (C) 63. (D) 64. (A) 65. (C) 66. (B) 67. (C) 68. (A) 69. (B) 70. (A) 71. (D) 72. (D)



Competitive Thinking

10. (B) (A) 2. (B) 3. (B) 4. (D) 5. (B) 6. (D) 7. (B) 8. (A) 9. (A) 1. 11. (A) 12. (A) 13. (C) 14. (A) 15. (A) 16. (C) 17. (A) 18. (C) 19. (A) 20. (D) 25. (B) 26. (C) 21. (D) 22. (C) 23. (C) 24. (C) 27. (A) 28. (B) 29. (D) 30. (A) 31. (B) 32. (B) 33. (C) 34. (B) 35. (A) 36. (A) 37. (B) 38. (A) 39. (C) 40. (C) 45. (A) 47. (A) 49. (D) 43. (C) 46. (C) 48. (C) 50. (C) 41. (B) 42. (A) 44. (A) 51. (A) 55. (C) 57. (C) 58. (D) 59. (A) 52. (D) 53. (C) 54. (A) 56. (D) 60. (D) 65. (C) 67. (A) 61. (A) 62. (A) 63. (B) 64. (A) 66. (C) 68. (A) 69. (A) 70. (D)

76. (A)



73. (D)

74. (D)

Hints

75. (A)



Classical Thinking

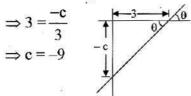
The equation of line is $\frac{x}{a} + \frac{y}{a} = 1$. 1.

72. (D)

$$\Rightarrow x + y - a = 0$$

71. (A)

- Slope = $-\frac{\text{coefficient of } x}{\text{coefficient of } y} = -1$
- From the figure, $m = \tan \theta = \frac{-c}{3}$ 2.



Hence, the required equation is y = 3x - 9

Midpoint is (3; 4) and

77. **(B)**

78. (D)

slope of AB =
$$\frac{6}{4}$$

- Slope of perpendicular = $\frac{-1}{6/4} = \frac{-2}{3}$
- the required equation is

$$y-4 = \frac{-2}{3}(x-3)$$
$$\Rightarrow 2x+3y=18$$

- 4. Slope of perpendicular = $\frac{-y'}{2a}$ \therefore the required equation is $y y' = -\frac{y'}{2a}$ (x x')

5.
$$\mathbf{m} = \frac{-1}{\frac{\mathbf{b'} - \mathbf{b}}{\mathbf{a'} - \mathbf{a}}} = \frac{\mathbf{a'} - \mathbf{a}}{\mathbf{b} - \mathbf{b'}}$$

Midpoint is
$$\left(\frac{a+a'}{2}, \frac{b+b'}{2}\right)$$

:. the required equation is

$$y - \left(\frac{b+b'}{2}\right) = \frac{a'-a}{b-b'} \left[x - \left(\frac{a+a'}{2}\right) \right]$$

$$\Rightarrow 2(b-b')y + 2(a-a')x = b^2 - b'^2 + a^2 - a'^2$$

- 6. $m = \frac{5-0}{-4-0} = \frac{5}{-4}$
- \therefore the required equation is 5x + 4y = 0.
- 7. Here, intercept on X-axis is 3 and intercept on Y-axis is -2. So, using double intercept form, the required equation of the line is $\frac{x}{3} \frac{y}{2} = 1$.
- 8. The required equation passing through (3, -4) and having gradient $\frac{4}{3}$ is $y+4=\frac{4}{3}(x-3)$.
- 9. The required equation which passes through (1, 2) and its gradient m = 3, is y 2 = 3(x 1).
- 10. The required equation passing through (0, 0) and having gradient $m = \frac{1}{0}$, is $y = \frac{1}{0}x$

11. Midpoint =
$$(4, -9)$$
 and slope = $\frac{-1}{3+1} = \frac{3}{2}$

Hence, the required line is $y + 9 = \frac{3}{2}(x - 4)$

$$\Rightarrow 3x - 2y = 30$$

- 12. Intersection point on X-axis is $(2x_1, 0)$ and on Y-axis is $(0, 2y_1)$. Thus, equation of line passing through these points is $\frac{x}{x_1} + \frac{y}{y_1} = 2$.
- 13. The required equation which passes through (c, d) and its gradient $-\frac{a}{b}$, is $y-d=-\frac{a}{b}(x-c)$ $\Rightarrow a(x-c)+b(y-d)=0$

- 14. The required equation is $y + 6 = \tan 45^{\circ}(x 4)$ $\Rightarrow x - y - 10 = 0$
 - 15. Equation of a line passing through the given points is $\frac{y-(-6)}{-6-10} = \frac{x-(-5)}{-5-3}$ $\Rightarrow \frac{y+6}{-16} = \frac{x+5}{-8} \Rightarrow 2x-y+4=0$
- 16. Using double intercept form, we get $\frac{x}{2a \sec \theta} + \frac{y}{2a \csc \theta} = 1$ $\Rightarrow x \cos \theta + y \sin \theta = 2a$
- 17. Equation of line is y = mx + c $\Rightarrow y = (\tan 135^\circ)x - 5 \Rightarrow y = -x - 5$ $\Rightarrow x + y + 5 = 0$
- 19. Since, the given line passes through (2, -3) and (4, -5).
- $\therefore \frac{2}{a} \frac{3}{b} = 1 \text{ and } \frac{4}{a} \frac{5}{b} = 1$ $\Rightarrow b = -1, a = -1$
- 20. Equation of line perpendicular to ax + by + c = 0 is $bx ay + \lambda = 0$ (i) It passes through (a, b).
- .. $ab ab + \lambda = 0 \Rightarrow \lambda = 0$ Putting $\lambda = 0$ in (i), we get bx - ay = 0 which is the required equation.
- 21. The equation of a line passing through (2, 2) and perpendicular to 3x + y = 3 is $y-2=\frac{1}{3}(x-2)$ or x-3y+4=0.

Putting x = 0 in this equation, we get $y = \frac{4}{3}$

So,
$$y - \text{intercept} = \frac{4}{3}$$

23. Y $R(3,3\sqrt{3})$ X' P(-1,0) Q(0,0) X

Slope of QR =
$$\frac{3\sqrt{3}-0}{3-0} = \sqrt{3}$$
 i.e., $\theta = 60^{\circ}$
Clearly, $\angle PQR = 120^{\circ}$

OQ is the angle bisector of the angle PQR, so line OQ makes 120° with the positive direction of X-axis.

Therefore, equation of the bisector of $\angle PQR$ is $y = \tan 120^{\circ}x \Rightarrow y = -\sqrt{3}x \Rightarrow \sqrt{3}x + y = 0$

25. Gradient of the line which passes through

(1, 0) and (-2,
$$\sqrt{3}$$
) is $m = \frac{\sqrt{3} - 0}{-2 - 1} = -\frac{1}{\sqrt{3}}$

$$\Rightarrow \tan \theta = -\frac{1}{\sqrt{3}}$$

$$\Rightarrow \theta = \tan^{-1} \left(-\frac{1}{\sqrt{3}} \right) = 150^{\circ}$$

- 26. The point of intersection is (0, 0)Thus, the equation of line passing through the points (0, 0) and (2, 2) is y = x.
- 27. Let $L_1 = 2x + 5y 7 = 0$ and $L_2 = 2x 5y 9 = 0$, so that $m_1 = -\frac{2}{5}$, $m_2 = \frac{2}{5}$ Lines are neither parallel nor perpendicular,

also not coincident.

Hence, the lines are intersecting.

28.
$$m_1 = \sqrt{3}$$
, $m_2 = 0$

$$\therefore \tan \theta = \left| \frac{\sqrt{3} - 0}{1 + 0} \right|$$

$$\Rightarrow \theta = 60^\circ = \sqrt{3}$$

29.
$$\theta = \tan^{-1} \left| \frac{2 - \sqrt{3} - 2 - \sqrt{3}}{1 + 4 - 3} \right| = \tan^{-1} (-\sqrt{3})$$

Considering smaller angle $\theta' = 60^{\circ}$.

30. Slope of given line is $\frac{1}{2}$

Thus,
$$\tan 45^\circ = \pm \frac{m - \frac{1}{2}}{1 + m \cdot \frac{1}{2}} \implies m = 3 \text{ or } \frac{-1}{3}$$

Hence option (B) is correct.

31. The lines are concurrent, if $\begin{vmatrix} 7 & -8 & 5 \\ 3 & -4 & 5 \\ 4 & 5 & k \end{vmatrix} = 0$ $\Rightarrow 7(-4k - 25) + 8(3k - 20) + 5(15 + 16) = 0$ $\Rightarrow k = -45$

- 32. 3(12x+10y-3)-2(15x-18y+1)= 6x+66y-11=0Hence, the lines are concurrent.
- 33. $u = a_1x + b_1y + c_1 = 0$, $v = a_2x + b_2y + c_2 = 0$ let $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} = c$ $\Rightarrow a_2 = \frac{a_1}{c}$, $b_2 = \frac{b_1}{c}$, $c_2 = \frac{c_1}{c}$ Given that, u + kv = 0 $\Rightarrow a_1x + b_1y + c_1 + k(a_2x + b_2y + c_2) = 0$ $\Rightarrow a_1x + b_1y + c_1 + k\left(\frac{a_1}{c}\right)x + k\left(\frac{b_1}{c}\right)y + k\left(\frac{c_1}{c}\right) = 0$ $\Rightarrow a_1x\left(1 + \frac{k}{c}\right) + b_1y\left(1 + \frac{k}{c}\right) + c_1\left(1 + \frac{k}{c}\right) = 0$ $\Rightarrow a_1x + b_1y + c_1 = 0 = u$
- 34. Equation of lines are $\frac{x}{a} \frac{y}{b} = 1$ and $\frac{x}{b} \frac{y}{a} = 1$ $\Rightarrow m_1 = \frac{b}{a} \text{ and } m_2 = \frac{a}{b}$ $\therefore \theta = \tan^{-1} \left| \frac{\frac{b}{a} \frac{a}{b}}{1 + \frac{b}{a} \cdot \frac{a}{b}} \right| = \tan^{-1} \frac{b^2 a^2}{2ab}$
- 35. $\theta = \tan^{-1} \left| \frac{-\cot 30^{\circ} + \cot 60^{\circ}}{1 + \cot 30^{\circ} \cot 60^{\circ}} \right|$ $= \tan^{-1} \left| \frac{\tan 60^{\circ} \tan 30^{\circ}}{1 + \tan 30^{\circ} \tan 60^{\circ}} \right| = 30^{\circ}$
- 36. $\begin{vmatrix} \mathbf{m}_1 & -1 & \mathbf{c}_1 \\ \mathbf{m}_2 & -1 & \mathbf{c}_2 \\ \mathbf{m}_3 & -1 & \mathbf{c}_3 \end{vmatrix} = 0$ $\Rightarrow \mathbf{m}_1(\mathbf{c}_2 \mathbf{c}_3) + \mathbf{m}_2(\mathbf{c}_3 \mathbf{c}_1) + \mathbf{m}_3(\mathbf{c}_1 \mathbf{c}_2) = 0$
- 38. $p = \left| \frac{ab}{\sqrt{a^2 + b^2}} \right|$ $\Rightarrow \frac{a^2 + b^2}{a^2 b^2} = \frac{1}{p^2} \Rightarrow \frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{p^2}$
- 39. Length of perpendicular is

$$\frac{\left| \frac{\frac{b}{a} - \frac{a}{b} - 1}{\sqrt{\left(\frac{1}{a}\right)^2 + \left(-\frac{1}{b}\right)^2}} \right| = \left| \frac{b^2 - a^2 - ab}{\sqrt{a^2 + b^2}} \right|$$

40. Straight line
$$y - y' = \frac{y'' - y'}{x'' - x'}(x - x')$$

$$= \frac{x'(y'' - y') - y'(x'' - x')}{\sqrt{(x'' - x')^2 + (y'' - y')^2}}$$
$$= \frac{x'y'' - y'x''}{\sqrt{(x'' - x')^2 + (y'' - y')^2}}$$

41. Required distance =
$$\left| \frac{-7}{\sqrt{12^2 + 5^2}} \right| = \frac{7}{13}$$

42. Required length =
$$\left| \frac{4(3) + 3(1) + 20}{5} \right| = 7$$

43. Required distance =
$$\left| \frac{-2 - 3 - 5}{\sqrt{1 + 1}} \right| = \frac{10}{\sqrt{2}} = 5\sqrt{2}$$

44. Given lines are
$$5x + 3y - 7 = 0$$
(i) and $15x + 9y + 14 = 0$ or

$$5x + 3y + \frac{14}{3} = 0$$
(ii)

Lines (i) and (ii) are parallel.

$$\therefore \text{ Required distance} = \left| \frac{c_1 - c_2}{\sqrt{a^2 + b^2}} \right| = \frac{\left| -7 - \frac{14}{3} \right|}{\left| \sqrt{5^2 + 3^2} \right|}$$
$$= \left| \frac{-35}{3\sqrt{34}} \right| = \frac{35}{3\sqrt{34}}$$

45.
$$L_1(8, -9) = 2(8) + 3(-9) - 4 = -15$$

 $L_2(8, -9) = 6(8) + 9(-9) + 8 = -25$
Hence, point lies on same side of the lines.

46. Here, equation of line is
$$y = x \tan \alpha + c$$
, $c > 0$
Length of the perpendicular drawn on line
from point (a cos α , a sin α) is

$$p = \left| \frac{-a \sin \alpha + a \cos \alpha \tan \alpha + c}{\sqrt{1 + \tan^2 \alpha}} \right| = \frac{c}{\sec \alpha} = c \cos \alpha$$

$$b^3 - c^3 = k(b-c), c^3 - a^3 = k(c-a),$$

 $a^3 - b^3 = k(a-b)$

$$\Rightarrow$$
 b-c=0 or $b^2 + c^2 + bc = k$

$$\Rightarrow c - a = 0 \text{ or } c^2 + a^2 + ac = k$$

$$\Rightarrow$$
 a-b=0 or $a^2 + b^2 + ab = k$

$$\Rightarrow$$
 b = c, c = a, a = b
or $b^2 + c^2 + bc = c^2 + a^2 + ca$

or
$$b^2 + c^2 + bc = c^2 + a^2 + ca$$

$$\Rightarrow b^2 - a^2 = c(a - b)$$

$$\Rightarrow$$
 b = a or a + b + c = 0

Critical Thinking

Since the hour, minute and second hands 1. always pass through origin because one end of these hands is always at origin.

> Now, at 4 O' clock, the hour hand makes 30° angle in fourth quadrant.

So, the equation of hour hand is

$$y = mx \Rightarrow y = -\frac{1}{\sqrt{3}}x$$

$$\Rightarrow x + \sqrt{3}y = 0$$

$$Y$$

$$0$$

$$30^{\circ}$$

$$3$$

$$4$$

Mid point of (a $\cos\alpha$, a $\sin\alpha$) and 2. (a $\cos\beta$, a $\sin\beta$) is

$$P\left(\frac{a(\cos\alpha + \cos\beta)}{2}, \frac{a(\sin\alpha + \sin\beta)}{2}\right)$$

$$Y$$

$$A(a\cos\alpha, a\sin\alpha)$$

$$P$$

$$B(a\cos\beta, a\sin\beta)$$

$$X$$

Slope of line AB is ...

$$\frac{a\sin\beta - a\sin\alpha}{a\cos\beta - a\cos\alpha} = \frac{\sin\beta - \sin\alpha}{\cos\beta - \cos\alpha} = m_1$$

and slope of OP is
$$\frac{\sin \alpha + \sin \beta}{\cos \alpha + \cos \beta} = m_2$$

Now,
$$m_1 \times m_2 = \frac{\sin^2 \beta - \sin^2 \alpha}{\cos^2 \beta - \cos^2 \alpha} = -1$$

Hence, the lines are perpendicular.

3. A line perpendicular to the line 5x - y = 1 is given by $x + 5y - \lambda = 0 = L$

In intercept form
$$\frac{x}{\lambda} + \frac{y}{\lambda/5} = 1$$

So, area of triangle is $\frac{1}{2}$ × (Multiplication of

$$\Rightarrow \frac{1}{2}(\lambda) \times \left(\frac{\lambda}{5}\right) = 5$$

$$\Rightarrow \lambda = \pm 5\sqrt{2}$$

Hence, the equation of required line is $x + 5y = \pm 5\sqrt{2}$

4. Given, $a + b = 14 \Rightarrow a = 14 - b$ Hence, the equation of straight line is

$$\frac{x}{14-b} + \frac{y}{b} = 1$$

Also, it passes through (3, 4)

$$\therefore \frac{3}{14-b} + \frac{4}{b} = 1$$

$$\Rightarrow \mathbf{b} = 8 \text{ or } 7$$

Therefore, equations are 4x + 3y = 24 and x + y = 7

5. Mid point = $\left(\frac{1+1}{2}, \frac{3-7}{2}\right) = (1,-2)$

Therefore, required line is

$$y+2=\frac{2}{3}(x-1) \implies 2x-3y=8$$

- 6. Let the intercept be a and 2a, then the equation of line is $\frac{x}{a} + \frac{y}{2a} = 1$, but it also passes through (1, 2), therefore a = 2. Hence, the required equation is 2x + y = 4
- 7. $x \cos \theta y \sin \theta = a(\cos^4 \theta \sin^4 \theta) = a \cos 2\theta$
- 8. B(0,b)
 (-4,3)

By the section formula, we get $a = -\frac{32}{3}$ and

$$b = \frac{24}{5}$$

Hence, the required equation is given by

$$\frac{x}{-(32/3)} + \frac{y}{(24/5)} = 1$$

$$\Rightarrow 9x - 20y + 96 = 0$$

- 9. Let the equation of the line be $\frac{x}{a} + \frac{y}{b} = 1$ The co-ordinates of the mid point of the intercept AB between the axes are $\left(\frac{a}{2}, \frac{b}{2}\right)$
- $\therefore \frac{a}{2} = 1, \frac{b}{2} = 2 \Rightarrow a = 2, b = 4$ Hence, the equation of the line is

$$\frac{x}{2} + \frac{y}{4} = 1 \Rightarrow 2x + y = 4$$

10. Point P(a, b) is on 3x + 2y = 13So, 3a + 2b = 13(i) Point Q(b, a) is on 4x - y = 5So, 4b - a = 5(ii) By solving (i) and (ii), we get a = 3, b = 2Now, equation of PQ is

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

$$\Rightarrow y - 2 = \frac{3 - 2}{2 - 3}(x - 3)$$

$$\Rightarrow y - 2 = -(x - 3)$$

$$\Rightarrow x + y = 5$$

- 11. Given, line AB makes 0 intercepts on X-axis and Y axis so, $(x_1, y_1) = (0, 0)$ Slope of perpendicular = $\frac{4}{3}$
- $\therefore \quad \text{Equation is } y 0 = \frac{4}{3} (x 0)$ $\Rightarrow 4x 3y = 0$
- 12. Perpendicular to $\sqrt{3}\sin\theta + 2\cos\theta = \frac{4}{r}$ is $\sqrt{3}\sin\left(\frac{\pi}{2} + \theta\right) + 2\cos\left(\frac{\pi}{2} + \theta\right) = \frac{k}{r}$ It is passing through $(-1, \pi/2)$ $\sqrt{3}\sin\pi + 2\cos\pi = \frac{k}{-1} \Rightarrow k = 2$

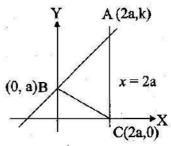
$$\therefore \quad \sqrt{3}\cos\theta - 2\sin\theta = \frac{2}{r}$$

$$\Rightarrow 2 = \sqrt{3}r\cos\theta - 2r\sin\theta$$

13. Slope
$$=\frac{8-2}{3-1}=3$$

The diagonal is $y-2=3(x-1)$
 $\Rightarrow 3x-y-1=0$

14. Line AB will pass through (0, a) and (2a, k)



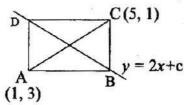
But as we are given AB = AC

$$\Rightarrow k = \sqrt{4a^2 + (k - a)^2} \implies k = \frac{5a}{2}$$

Hence, the required equation is 3x-4y+4a=0

is

15. Let ABCD be a rectangle. Given, A (1, 3) and C (5, 1).



Intersecting point of diagonal of a rectangle is same or at midpoint.

So, midpoint of AC is (3, 2).

Also,
$$y = 2x + c$$
 passes through $(3, 2)$.

Hence, c = -4

16. Let p be the length of the perpendicular from the origin on the given line. Then its equation in normal form is

$$x \cos 30^{\circ} + y \sin 30^{\circ} = p \text{ or } \sqrt{3}x + y = 2p$$

This meets the coordinate axes at $A\left(\frac{2p}{\sqrt{3}},0\right)$

and B(0, 2p)

$$\therefore \quad \text{Area of } \Delta \text{OAB} = \frac{1}{2} \left(\frac{2p}{\sqrt{3}} \right) 2p = \frac{2p^2}{\sqrt{3}}$$

$$\Rightarrow \frac{2p^2}{\sqrt{3}} = \frac{50}{\sqrt{3}} \Rightarrow p = \pm 5.$$

Hence, the lines are $\sqrt{3}x + y \pm 10 = 0$

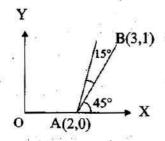
17. Here, slope of AB = 1 $\Rightarrow \tan \theta = m_1 = 1$

or
$$\theta = 45^{\circ}$$

 \therefore tan $(45^{\circ} + 15^{\circ}) = \tan 60^{\circ}$

(: It is rotated anticlockwise so the angle will be $45^{\circ} + 15^{\circ} = 60^{\circ}$)

Thus, slope of new line is $\sqrt{3}$



Hence, the equation is $y = \sqrt{3}x + c$, but it still passes through (2,0), $c = -2\sqrt{3}$

Thus, required equation is

$$y = \sqrt{3}x - 2\sqrt{3}$$

18.
$$\left(\frac{-2}{3a}\right)\left(\frac{-3}{4}\right) = -1 \text{ or } a = \frac{-1}{2}$$

19. The slope of line x + y = 1 is -1.

. It makes an angle of 135° with X-axis.

The equation of line passing through (1, 1) and making an angle of 135° is,

$$\frac{x-1}{\cos 135^\circ} = \frac{y-1}{\sin 135^\circ} = r$$

$$\Rightarrow \frac{x-1}{-1/\sqrt{2}} = \frac{y-1}{1/\sqrt{2}} = \mathbf{r}$$

.. Co-ordinates of any point on this line are

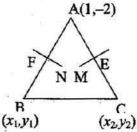
$$\left(1-\frac{\mathbf{r}}{\sqrt{2}},1+\frac{\mathbf{r}}{\sqrt{2}}\right)$$

If this point lies on 2x - 3y = 4, then

$$2\left(1-\frac{\mathbf{r}}{\sqrt{2}}\right)-3\left(1+\frac{\mathbf{r}}{\sqrt{2}}\right)=4$$

$$\Rightarrow r = \sqrt{2}$$

20. Let the equation of perpendicular bisector FN of AB is x-y+5=0(i)



The middle point F of AB $\left(\frac{x_1+1}{2}, \frac{y_1-2}{2}\right)$ Which lies on line (i).

$$x_1 - y_1 = -13$$
(ii)

Also AB is perpendicular to FN. So the product of their slopes is -1.

i.e.,
$$\frac{y_1+2}{x_1-1} \times 1 = -1$$
 or $x_1 + y_1 = -1$ (iii)

On solving (ii) and (iii), we get B(-7, 6)

Similarly, C
$$\left(\frac{11}{5}, \frac{2}{5}\right)$$

Hence, the equation of BC is 14x+23y-40=0

21. S = midpoint of QR =
$$\left(\frac{6+7}{2}, \frac{-1+3}{2}\right)$$

= $\left(\frac{13}{2}, 1\right)$

:. 'm' of PS =
$$\frac{2-1}{2-\frac{13}{2}} = -\frac{2}{9}$$

 $\therefore \text{ The required equation is } y+1=\frac{-2}{9}(x-1)$ i.e., 2x+9y+7=0

22. Let the co-ordinates of axes are A (a, 0) and B(0, b), but the point (-5, 4) divides the line AB in the ratio of 1 : 2. Therefore, the co-ordinates of axes are $\left(\frac{-15}{2},0\right)$ and (0, 12).

Therefore, the equation of line passing through these coordinate axes is given by 8x - 5y + 60 = 0

23. The equation of any line parallel to 2x + 6y + 7 = 0 is 2x + 6y + k = 0.

This meets the axes at $A\left(-\frac{k}{2},0\right)$ and

$$B\!\!\left(0,\!-\frac{k}{6}\right)$$

By hypothesis, AB = 10

$$\Rightarrow \sqrt{\frac{k^2}{4} + \frac{k^2}{36}} = 10 \Rightarrow \sqrt{\frac{10k^2}{36}} = 10$$

$$\Rightarrow 10k^2 = 3600 \Rightarrow k = \pm 6\sqrt{10}$$

Hence, there are two lines given by $2x + 6y \pm 6\sqrt{10} = 0$

24. Take two perpendicular lines as the coordinate axes. If a, b be the intercepts made by the moving line on the coordinate axes, then the equation of the line is

$$\frac{x}{a} + \frac{y}{b} = 1 \qquad \dots$$

Let
$$\frac{1}{a} + \frac{1}{b} = \frac{1}{k}$$

i.e.,
$$\frac{k}{a} + \frac{k}{b} = 1$$
(ii)

The result (ii) shows that the straight line (i) passes through a fixed point (k, k).

25. The equation of line passing through

A(-5, -4) is
$$\frac{x+5}{\cos \theta} = \frac{y+4}{\sin \theta}$$

Let $AB = r_1$, $AC = r_2$, $AD = r_3$

The co-ordinate of B is

 $(r_1 \cos \theta - 5, r_1 \sin \theta - 4)$

which lies on x + 3y + 2 = 0

$$r_1 = \frac{15}{\cos\theta + 3\sin\theta}$$

Similarly, $\frac{10}{AC} = 2\cos\theta + \sin\theta$ and

$$\frac{6}{AD} = \cos\theta - \sin\theta$$

Putting in the given relation, we get $(2\cos\theta + 3\sin\theta)^2 = 0$

$$\Rightarrow \tan \theta = -\frac{2}{3}$$

 $\therefore \quad \text{The equation of line is } y+4=-\frac{2}{3}(x+5)$

$$\Rightarrow 2x + 3y + 22 = 0$$

26. Let the required line through the point (1,2) be inclined at an angle θ to the axis of X. Then its

equation is
$$\frac{x-1}{\cos \theta} = \frac{y-2}{\sin \theta} = r$$
(i)

The co-ordinates of a point on the line (i) are $(1 + r \cos \theta, 2 + r \sin \theta)$

If this point is at a distance $\frac{\sqrt{6}}{3}$ form (1, 2),

then
$$r = \frac{\sqrt{6}}{3}$$

Therefore, the point is

$$\left(1+\frac{\sqrt{6}}{3}\cos\theta, \ 2+\frac{\sqrt{6}}{3}\sin\theta\right).$$

But this point lies on the line x + y = 4

$$\Rightarrow \frac{\sqrt{6}}{3}(\cos\theta + \sin\theta) = 1 \text{ or}$$

$$\sin\theta + \cos\theta = \frac{3}{\sqrt{6}}$$

$$\Rightarrow \frac{1}{\sqrt{2}}\sin\theta + \frac{1}{\sqrt{2}}\cos\theta = \frac{\sqrt{3}}{2}$$

....(Dividing both sides by $\sqrt{2}$)

$$\Rightarrow \sin(\theta + 45^{\circ}) = \sin 60^{\circ} \text{ or } \sin 120^{\circ}$$

$$\Rightarrow \theta = 15^{\circ} \text{ or } 75^{\circ}$$

27. The four vertices on solving are A(-3, 3), B(1, 1), C(1, -1) and D(-2, -2).

$$m_1 = \text{slope of AC} = -1$$
,

$$m_2 = \text{slope of BD} = 1$$

 $m_1 m_2 = -1$

Hence, the angle between diagonals AC and BD is 90°.

28. The point of intersection of the lines is (1, 1).

and slope of the line 2y - 3x + 2 = 0 is $\frac{3}{2}$

Hence, the equation is $y - 1 = \frac{3}{2}(x - 1)$

$$\Rightarrow 3x - 2y = 1$$

29. From option (B),

$$\begin{vmatrix} 1 & 2 & -10 \\ 2 & 1 & 5 \\ 5 & 4 & 0 \end{vmatrix} = 1(0 - 20) - 2(-25) - 10(3) = 0$$

Hence, option (B) is the correct answer.

30. The point of intersection of 5x - 6y - 1 = 0 and 3x + 2y + 5 = 0 is (-1, -1).

Now the line perpendicular to

3x - 5y + 11 = 0 is 5x + 3y + k = 0, but it passes through (-1, -1)

$$\Rightarrow$$
 -5 - 3 + k = 0 \Rightarrow k = 8

Hence, required line is 5x + 3y + 8 = 0.

31. The intersection point of lines x - 2y = 1 and x + 3y = 2 is $\left(\frac{7}{5}, \frac{1}{5}\right)$ and the slope of required

line =
$$-\frac{3}{4}$$

: Equation of required line is

$$y - \frac{1}{5} = \frac{-3}{4} \left(x - \frac{7}{5} \right)$$

$$\Rightarrow \frac{3x}{4} + y = \frac{21}{20} + \frac{1}{5} \Rightarrow 3x + 4y = 5$$

$$\Rightarrow 3x + 4y - 5 = 0$$

- 32. Intersection point of the line is $\left(\frac{ab}{a+b}, \frac{ab}{a+b}\right)$, which is satisfying all the equations given in options (A), (B) and (C). Hence, (D) is correct.
- 33. Here, equation of AB is x + 4y 4 = 0(i) and equation of BC is 2x + y 22 = 0(ii) Thus angle between (i) and (ii) is given by

$$\tan^{-1}\frac{-\frac{1}{4}+2}{1+\left(-\frac{1}{4}\right)(-2)} = \tan^{-1}\frac{7}{6}$$

34. Let θ be the acute angle which the line y = mx + 4 makes with the lines y = 3x + 1 and 2y = x + 3.

Then,

$$\tan \theta = \left| \frac{m-3}{1+3m} \right|$$
 and $\tan \theta = \left| \frac{m-\frac{1}{2}}{1+\frac{m}{2}} \right|$

$$\Rightarrow \left| \frac{m-3}{1+3m} \right| = \left| \frac{2m-1}{m+2} \right|$$

$$\Rightarrow m^2 - m - 6 = \pm (6m^2 - m - 1)$$

$$\Rightarrow 5m^2 + 5 = 0 \text{ or } 7m^2 - 2m - 7 = 0$$

$$\Rightarrow 7m^2 - 2m - 7 = 0$$

$$\Rightarrow m = \frac{1 \pm 5\sqrt{2}}{7}$$

35.
$$\theta = \tan^{-1} \left| \frac{-\cot \alpha_1 + \cot \alpha_2}{1 + \cot \alpha_1 \cot \alpha_2} \right|$$
$$= \tan^{-1} \left| \frac{\tan \alpha_1 - \tan \alpha_2}{1 + \tan \alpha_2 \tan \alpha_1} \right| = \alpha_1 - \alpha_2$$

36.
$$\frac{k - (2 + \sqrt{3})}{1 + k(2 + \sqrt{3})} = \sqrt{3}$$
$$\Rightarrow k - 2 - \sqrt{3} = \sqrt{3} + 2k\sqrt{3} + 3k$$
$$\Rightarrow k = \frac{-2(1 + \sqrt{3})}{2(1 + \sqrt{3})} = -1$$

37.
$$\begin{vmatrix} \mathbf{p} - \mathbf{q} & \mathbf{q} - \mathbf{r} & \mathbf{r} - \mathbf{p} \\ \mathbf{q} - \mathbf{r} & \mathbf{r} - \mathbf{p} & \mathbf{p} - \mathbf{q} \\ \mathbf{r} - \mathbf{p} & \mathbf{p} - \mathbf{q} & \mathbf{q} - \mathbf{r} \end{vmatrix} = \begin{vmatrix} 0 & \mathbf{q} - \mathbf{r} & \mathbf{r} - \mathbf{p} \\ 0 & \mathbf{r} - \mathbf{p} & \mathbf{p} - \mathbf{q} \\ 0 & \mathbf{p} - \mathbf{q} & \mathbf{q} - \mathbf{r} \end{vmatrix} = 0$$
[By C₁ \rightarrow C₁ + C₂ + C₃]
Hence, the lines are concurrent.

38. Check by options. From option (A), we get

$$\begin{vmatrix} 3 & 4 & 6 \\ 6 & 5 & 9 \\ 2 & 3 & 5 \end{vmatrix} = 3(25 - 27) - 4(12) + 6(8) \neq 0$$

From option (B), we get

$$\begin{vmatrix} 3 & 4 & 6 \\ 6 & 5 & 9 \\ 3 & 3 & 5 \end{vmatrix} = 3(25 - 27) - 4(3) + 6(3) = 0$$

39. The three lines are concurrent, if

$$\begin{vmatrix} 1 & 2 & -9 \\ 3 & 5 & -5 \\ a & b & -1 \end{vmatrix} = 0$$

$$\Rightarrow 35a - 22b + 1 = 0$$
which is true if the line $35x - 22$

which is true if the line 35x - 22y + 1 = 0 passes through (a, b).

40. If the given lines are concurrent, then

$$\begin{vmatrix} a & 1 & 1 \\ 1 & b & 1 \\ 1 & 1 & c \end{vmatrix} = 0 \Rightarrow \begin{vmatrix} a & 1-a & 1-a \\ 1 & b-1 & 0 \\ 1 & 0 & c-1 \end{vmatrix} = 0$$

$$[By C_2 \to C_2 - C_1 \text{ and } C_3 \to C_3 - C_1]$$

$$\Rightarrow a(b-1)(c-1) - (b-1)(1-a) - (c-1)$$

$$(1-a) = 0$$

$$\Rightarrow \frac{a}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 0$$
[Divide by $(1-a)(1-b)(1-c)$]
$$\Rightarrow \frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1$$

- It is given that the lines ax + 2y + 1 = 0, 41. bx + 3y + 1 = 0 and cx + 4y + 1 = 0 are concurrent, therefore $\begin{vmatrix} b & 3 & 1 \end{vmatrix} = 0$ \Rightarrow -a+2b-c=0 \Rightarrow 2b=a+c \Rightarrow a, b, c are in A. P.
- The set of lines is 4ax + 3by + c = 0, where 42. a + b + c = 0. Eliminating c, we get 4ax + 3by - (a + b) = 0 \Rightarrow a(4x - 1) + b(3y - 1) = 0 This passes through the intersection of the lines 4x - 1 = 0 and 3y - 1 = 0i.e, $x = \frac{1}{4}$, $y = \frac{1}{3}$ i.e., $\left(\frac{1}{4}, \frac{1}{3}\right)$.
- Given lines are 3x + 4y = 5, 5x + 4y = 4. 43. $\lambda x + 4y = 6$. These lines meet at a point if the point of intersection of first two lines lies on the third line. From 3x + 4y = 5 and 5x + 4y = 4

We get $x = \frac{-1}{2}$, $y = \frac{13}{8}$

This lies on $\lambda x + 4y = 6$, if $\lambda \left(-\frac{1}{2}\right) + 4\left(\frac{13}{8}\right) = 6$

 $\Rightarrow \lambda = 1$

44. Equation of line through the point of intersection of lines 2x + 3y + 1 = 0 and 3x - 5y - 5 = 0 is given by (2+3k)x + (3-5k)y + (1-5k) = 0Slope of line is given by $\tan 45^\circ = -\frac{(2+3k)}{3-5k}$

 $\Rightarrow \mathbf{k} = \frac{5}{2}$

- Equation of line is 19x 19y 23 = 0
- 45. Equation of line passing through point of intersection of u = 0 and v = 0 is u + kv = 0
- (x+2y+5)+k(3x+4y+1)=0... It is passing through (3, 2)

- $(3+2\times2+5)+k(3\times3+4\times2+1)=0$
- equation of line will be

$$(x+2y+5) - \frac{2}{3}(3x+4y+1) = 0$$

$$\Rightarrow 3x+2y-13=0$$

46. Equation of line passing through point of intersection of x + 2y + 3 = 0 and 3x + 4y + 7 = 0 is (x+2y+3)+k(3x+4y+7)=0

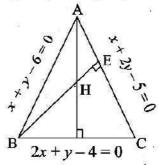
 \Rightarrow (1 + 3k)x + (2 + 4k) y + 3 + 7k = 0 (i)

Slope of equation (i) is $m_1 = \frac{-(1+3k)}{2+4k}$

and slope of given line is $m_2 = \frac{-1}{1} = 1$ (ii)

Since (i) and (ii) represent perpendicular lines.

- $_{1}m_{2}=-1$ $\frac{-(1+3k)}{\cdot(2+4k)}\times 1=-1$
- equation of required line is (x+2y+3)-1(3x+4y+7)=0 $\Rightarrow x + y + 2 = 0$
- 47. Equation of AD is (x+y-6)+k(x+2y-5)=0 \Rightarrow (1+k)x + (1+2k)y - (6+5k) = 0(i)



Slope of AD = $m_1 = \frac{-(1+k)}{(1+2k)}$

and Slope of BC = $m_2 = -2$

- =-1 [: AD \perp BC]
- $k = -\frac{3}{4}$
- From (i), equation of AD is x - 2y = 9....(ii)

Similarly, equation of BE is

2x - y = -12....(iii) By solving equation (ii) and (iii), we get

x = -11, y = -10

 $H \equiv (-11, -10)$

48. Any line through (1, -10) is given by y + 10 = m(x - 1)

Since, it makes equal angle say ' α ' with the given lines 7x - y + 3 = 0 and x + y - 3 = 0

$$\tan \alpha = \frac{m-7}{1+7m} = \frac{m-(-1)}{1+m(-1)}$$

$$\Rightarrow$$
 m = $\frac{1}{3}$ or -3

Hence, the two possible equations of third side are 3x + y + 7 = 0, x - 3y - 31 = 0.

49. Putting k = 1, 2, we get

$$3x + 2y = 12$$
(i

$$4x + 3y = 19$$
 ... The given lines are not parallel.

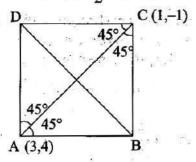
Hence on solving them, we get

$$x = -2, y = 9$$

Therefore, the lines pass through (-2, 9)

- Since, the distance between the parallel lines lx + my + n = 0 and lx + my + n' = 0 is same as the distance between parallel lines mx + y + n = 0 and mx + ly + n' = 0. Therefore, the parallelogram is a rhombus. Since, the diagonals of a rhombus are at right angles, therefore the required angle is $\frac{\pi}{2}$.
- 51. Slope of AC = 5/2. Let m be the slope of a line inclined at an angle of 45° to AC,

Then
$$\tan 45^{\circ} = \pm \frac{m - \frac{5}{2}}{1 + m \cdot \frac{5}{2}} \implies m = -\frac{7}{3}, \frac{3}{7}$$



Thus, let the slope of AB or DC be $\frac{3}{7}$ and that

of AD or BC be
$$-\frac{7}{3}$$
.

Then, equation of AB is 3x-7y+19=0.

Also the equation of BC is 7x + 3y - 4 = 0

On solving these equations, we get $B\left(-\frac{1}{2}, \frac{5}{2}\right)$

Now let the co-ordinates of the vertex D be (h, k). Since the middle points of AC and BD are same

$$\frac{1}{2} \left(h - \frac{1}{2} \right) = \frac{1}{2} (3+1) \Rightarrow h = \frac{9}{2}$$

$$\Rightarrow \frac{1}{2} \left(k + \frac{5}{2} \right) = \frac{1}{2} (4-1)$$

$$\Rightarrow k = \frac{1}{2}$$

Hence,
$$D = \left(\frac{9}{2}, \frac{1}{2}\right)$$

52. By the given condition of a + b + c = 0, the three lines reduce to

$$x-y=\frac{p}{a}$$
 or $\frac{p}{b}$ or $\frac{p}{c}(p \neq 0)$.

All these lines are parallel. Hence, they do not intersect in finite plane.

53. Required line should be

$$(3x - y + 2) + \lambda(5x - 2y + 7) = 0 \qquad \dots (i)$$

$$\Rightarrow (3 + 5\lambda)x - (2\lambda + 1)y + (2 + 7\lambda) = 0$$

$$\Rightarrow y = \frac{3 + 5\lambda}{2\lambda + 1}x + \frac{2 + 7\lambda}{2\lambda + 1} \qquad \dots (ii)$$

As the equation (ii), has infinite slope,

$$2\lambda + 1 = 0$$

$$\Rightarrow \lambda = -1/2$$

Putting $\lambda = -1/2$ in equation (i) we have

$$(3x-y+2) + (-1/2)(5x-2y+7) = 0$$

 $\Rightarrow x = 3$

54. Here,

Slope of Ist diagonal =
$$m_1 = \frac{2-0}{2-0} = 1$$

$$\Rightarrow \theta_1 = 45^{\circ}$$

Slope of Π^{nd} diagonal = $m_2 = \frac{2-0}{1-1} = \infty$

$$\Rightarrow \theta_2 = 90^{\circ}$$

$$\Rightarrow \theta_2 - \theta_1 = 45^\circ = \frac{\pi}{4}$$

55. Let the point be (h, k), then h + k = 4....(i)

$$1 = \left| \frac{4\mathbf{h} + 3\mathbf{k} - 10}{\sqrt{4^2 + 3^2}} \right|$$

$$\Rightarrow$$
 4h + 3k = 15(ii) and

$$4h + 3k = 5$$
(iii)

On solving (i) and (ii), and (i) and (iii), we get the required points (3, 1) and (-7, 11).

56. Here,
$$p = \frac{-k}{\sqrt{\sec^2 \alpha + \csc^2 \alpha}}$$

and $p' = \frac{-k \cos 2\alpha}{\sqrt{\cos^2 \alpha + \sin^2 \alpha}}$

$$\therefore 4p^2 + p'^2 = \frac{4k^2}{\sec^2 \alpha + \csc^2 \alpha}$$

$$k^2(\cos^2 \alpha)$$

$$+ \frac{k^2(\cos^2\alpha - \sin^2\alpha)^2}{1}$$

$$= 4k^2\sin^2\alpha\cos^2\alpha + k^2(\cos^4\alpha + \sin^4\alpha)$$

$$- 2k^2\cos^2\alpha\sin^2\alpha$$

$$= k^2(\sin^2\alpha + \cos^2\alpha)^2$$

57. Let the distance of both lines be p_1 and p_2 from origin, then $p_1 = -\frac{8}{5}$ and $p_2 = -\frac{3}{5}$.

Hence, distance between both the lines $= |p_1 - p_2| = \frac{5}{5} = 1$

58.
$$|AD| = \left| \frac{2-2-1}{\sqrt{1^2+2^2}} \right|$$

$$= \frac{1}{\sqrt{5}}$$

$$\tan 60^\circ = \frac{AD}{BD}$$

$$\Rightarrow \sqrt{3} = \frac{1/\sqrt{5}}{BD}$$

$$\Rightarrow BD = \frac{1}{\sqrt{15}}$$

$$A(2,-1)$$

$$A(2,-1)$$

$$B = \frac{1}{\sqrt{5}}$$

$$A(2,-1)$$

$$B = \frac{1}{\sqrt{5}}$$

59.
$$p_{1} \cdot p_{2} = \left(\frac{b\sqrt{a^{2} - b^{2}}\cos\theta + 0 - ab}{\sqrt{b^{2}\cos^{2}\theta + a^{2}\sin^{2}\theta}}\right)$$

$$\times \left(\frac{-b\sqrt{a^{2} - b^{2}}\cos\theta - ab}{\sqrt{b^{2}\cos^{2}\theta + a^{2}\sin^{2}\theta}}\right)$$

$$= \frac{-[b^{2}(a^{2} - b^{2})\cos^{2}\theta - a^{2}b^{2}]}{(b^{2}\cos^{2}\theta + a^{2}\sin^{2}\theta)}$$

$$= \frac{b^{2}[a^{2} - a^{2}\cos^{2}\theta + b^{2}\cos^{2}\theta]}{b^{2}\cos^{2}\theta + a^{2}\sin^{2}\theta}$$

$$= \frac{b^{2}[a^{2}\sin^{2}\theta + b^{2}\cos^{2}\theta]}{b^{2}\cos^{2}\theta + a^{2}\sin^{2}\theta}$$

$$= b^{2}$$

 $BC = 2BD = 2/\sqrt{15}$

60. Lines 3x + 4y + 2 = 0 and 3x + 4y + 5 = 0 are on the same side of the origin. The distance between these lines is $d_1 = \left| \frac{2-5}{\sqrt{3^2+4^2}} \right| = \frac{3}{5}$.

Lines 3x + 4y + 2 = 0 and 3x + 4y - 5 = 0 are on the opposite sides of the origin. The distance

between these lines is
$$d_2 = \left| \frac{2+5}{\sqrt{3^2+4^2}} \right| = \frac{7}{5}$$
.

Thus, 3x + 4y + 2 = 0 divides the distance between 3x + 4y + 5 = 0 and 3x + 4y - 5 = 0 in the ratio $d_1 : d_2$ i.e., 3 : 7.

61.
$$2p = \left| \frac{0+0-1}{\sqrt{\frac{1}{a^2} + \frac{1}{b^2}}} \right|$$

$$\Rightarrow \frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{4p^2} \Rightarrow \frac{1}{a^2} + \frac{1}{b^2} = \frac{2}{8p^2}$$

$$\Rightarrow a^2, 8p^2, b^2 \text{ are in H.P.}$$

- 62. Lengths of perpendicular from (0,0) on the given lines are each equal to 2.
- 63. $L_{(-1,-1)} = 3(-1) 8(-1) 7 < 0$ $L_{(3,7)} = 3 \times 3 - 8 \times 7 - 7 < 0$ Hence, (-1,-1) and (3,7) lie on the same side of line.
- 64. Let $L_1 = 2x + 3y 7 = 0$ and $L_2 = 2x + 3y 5 = 0$ Here, slope of L_1 = slope of $L_2 = -\frac{2}{3}$ Hence, the lines are parallel.
- 65. Equation of any line through (0, a) is y-a=m(x-0) or mx-y+a=0(i) If the length of perpendicular from (2a, 2a) to the line (i) is 'a', then $a=\pm\frac{m(2a)-2a+a}{\sqrt{m^2+1}}$ $\Rightarrow m=0,\frac{4}{3}$ Hence, the required equations of lines are y-a=0, 4x-3y+3a=0
- 66. If the given lines represent the same line, then the length of the perpendiculars from the origin to the lines are equal, so that $\frac{c}{\sqrt{1+m^2}} = \frac{p}{\sqrt{\cos^2 \alpha + \sin^2 \alpha}}$ $\Rightarrow c = p\sqrt{1+m^2}$

67. Point of intersection is (2, 3).

Therefore, the equation of line passing through (2, 3) is y-3 = m(x-2)

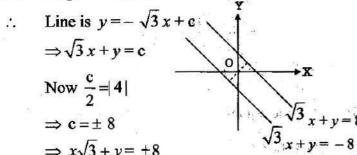
or mx - y - (2m - 3) = 0

According to the condition,

$$\left| \frac{3m-2-(2m-3)}{\sqrt{1+m^2}} \right| = \frac{7}{5} \Rightarrow m = \frac{3}{4}, \frac{4}{3}$$

Hence, the equations are 3x - 4y + 6 = 0 and 4x - 3y + 1 = 0.

68. Slope = $-\sqrt{3}$



- 69. Since, m (gradient) and x_1 are fixed and y_1 is variate, then they, form a set of parallel lines because gradient of every line remains 'm'.
- 70. The equation of lines passing through (1, 0) is given by y = m(x 1).

Its distance from origin is $\frac{\sqrt{3}}{2}$

$$\Rightarrow \left| \frac{-m}{\sqrt{1+m^2}} \right| = \frac{\sqrt{3}}{2} \Rightarrow m = \pm \sqrt{3}$$

Hence, the lines are $\sqrt{3}x + y - \sqrt{3} = 0$ and

$$\sqrt{3}x - y - \sqrt{3} = 0$$

- 71. As $(\sin \theta, \cos \theta)$ and (3, 2) lie on the same side of x + y 1 = 0, they should be of same sign.
- $\therefore \sin \theta + \cos \theta 1 > 0 \text{ as } 3 + 2 1 > 0$ $\Rightarrow \sqrt{2} \sin \left(\theta + \frac{\pi}{4} \right) > 1$

$$\Rightarrow \sin\left(\theta + \frac{\pi}{4}\right) > \frac{1}{\sqrt{2}} \Rightarrow 0 < \theta < \frac{\pi}{4}$$

72. Given form is 3x + 3y + 7 = 0

$$\Rightarrow \frac{3}{\sqrt{3^2 + 3^2}} x + \frac{3}{\sqrt{3^2 + 3^2}} y + \frac{7}{\sqrt{3^2 + 3^2}} = 0$$
$$\Rightarrow \frac{3}{3\sqrt{2}} x + \frac{3}{3\sqrt{2}} y = \frac{-7}{3\sqrt{2}}$$

$$\therefore \qquad \mathbf{p} = \left| \frac{-7}{3\sqrt{2}} \right| = \frac{7}{3\sqrt{2}}$$



Competitive Thinking

- 1. The points are (1, 3) and (3, 15). Hence, gradient = $\frac{15-3}{3-1} = \frac{12}{2} = 6$
- 2. $m_1 = \frac{6+4}{-2-3} = \frac{10}{-5} = -2$ and $m_2 = \frac{-18-6}{9-(-3)} = -2$ Hence, the lines are parallel.
- 3. Since, $m_1 m_2 = (2) \left(-\frac{1}{2} \right) = -1$
- the lines are perpendicular.
- 4. $m_1 m_2 = -1$ $\Rightarrow \left(\frac{k-3}{2-4}\right) (2) = -1 \Rightarrow 2k-6 = 2 \Rightarrow k = 4$
- 5. The equation of a line perpendicular to x-y=0 is -x-y+c=0(i) Since, the line passes through (3, 2).
- $\therefore -3-2+c=0$
- c = 5Putting c = 5 in (i), we get x + y = 5
- The given line is bx ay = ab(i)
 It cuts X-axis at (a, 0).
 The equation of a line perpendicular to (i) is ax + by = k.
 Since, the line passes through (a, 0) ⇒ k = a²
 Hence, required equation of line is ax + by = a²
 i.e., x/b + y/a = a/b
- 7. The equation of a line perpendicular to x+y+1=0 is $x-y+\lambda=0$. Since, the line passes through the point (1, 2).
- $1-2+\lambda=0$ $\Rightarrow \lambda=1$ Hence, required equation of line is y-x-1=0
- 8. Let the equation be $\frac{x}{a} + \frac{y}{-a} = 1$. $\Rightarrow x - y = a$ (i) But, it passes through (-3, 2)
- A a=-3-2=-5Putting the value of a in (i), we get x-y+5=0

9. The required equation passing through (-1, 1) and having gradient $\frac{3}{2}$ is

$$y-1 = \frac{3}{2}(x+1) \Rightarrow 2(y-1) = 3(x+1)$$

- 10. Midpoint \equiv (3, 2).
- the required equation is y-2=2(x-3) $\Rightarrow 2x-y-4=0$
- 11. Any line through the middle point M(1, 5) of the intercept AB may be taken as

$$\frac{x-1}{\cos\theta} = \frac{y-5}{\sin\theta} = r \qquad(i)$$

Since, the points A and B are equidistant from M and on the opposite sides of it.

Therefore, if the co-ordinates of A are obtained by putting r = d in (i), then the co-ordinates of B are given by putting r = -d.

Now, the point A(1 + d $\cos\theta$, 5 + d $\sin\theta$) lies on the line 5x - y - 4 = 0 and

point B(1 – d cos θ , 5 – d sin θ) lies on the line 3x + 4y - 4 = 0.

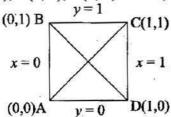
 $5(1 + d\cos\theta) - (5 + d\sin\theta) - 4 = 0$ and $3(1 - d\cos\theta) + 4(5 - d\sin\theta) - 4 = 0$ Eliminating 'd', we get $\frac{\cos\theta}{35} = \frac{\sin\theta}{83}$

Hence, the required line is $\frac{x-1}{35} = \frac{y-5}{83}$ or 83x - 35y + 92 = 0.

12. Midpoint \equiv (2, 7)

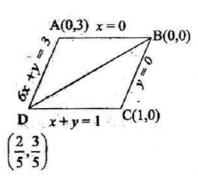
Slope of perpendicular = -6

- the required equation is y-7=-6 (x-2) $\Rightarrow 6x+y-19=0$
- 13. The required diagonal passes through the midpoint of AB and is perpendicular to AB. So, its equation is y 2 = -3(x 2) or y + 3x 8 = 0.
- 14. Co-ordinates of the vertices of the square are A(0, 0), B(0, 1), C(1, 1) and D(1, 0).



Now, the equation of AC is y = x and of BD is $y - 1 = -\frac{1}{1}(x - 0) \Rightarrow x + y = 1$

15.



From figure, diagonal BD is passing through origin, therefore its equation is given by

$$\left(y - \frac{3}{5}\right) = \frac{-(3/5)}{-(2/5)} \left(x - \frac{2}{5}\right)$$

$$\Rightarrow 3x - 2y = 0$$

- 16. Let the equation of the line be $\frac{x}{a} + \frac{y}{b} = 1$. Given, a = bSo, equation of line is x + y = a
- Since, this line passes through (2, 4). $\therefore 2+4=a$ $\Rightarrow a=6$
- :. the required equation of line is x + y = 6i.e., x+y-6=0
- 17. Here, a + b = -1
- $\therefore \quad \text{required line is } \frac{x}{a} \frac{y}{1+a} = 1 \quad \dots (i)$

Since, line (i) passes through (4, 3).

- $\therefore \frac{4}{a} \frac{3}{1+a} = 1$ $\Rightarrow 4 + 4a 3a = a + a^{2}$ $\Rightarrow a^{2} = 4$ $\Rightarrow a = \pm 2$
- $\therefore \text{ the required lines are } \frac{x}{2} \frac{y}{3} = 1 \text{ and } \frac{x}{-2} + \frac{y}{1} = 1.$
- Equation of the line has its intercepts on the X-axis and Y-axis in the ratio 2: 1 i.e., 2a and a
- $\therefore \frac{x}{2a} + \frac{y}{a} = 1 \Rightarrow x + 2y = 2a \qquad \dots (i)$

Line (i) also passes through midpoint of (3, -4) and (5, 2) i.e., (4, -1)

 $\therefore 4+2(-1)=2a \Rightarrow a=1$ Hence, the equation of required line is x+2y=2

- 19. ax + by + c = 0 always passes through (1, -2).
- $a-2b+c=0 \Rightarrow 2b=a+c$ Therefore, a, b and c are in A.P.
- 20. Midpoint of the line joining the points (4, -5) and (-2, 9) is $\left(\frac{4-2}{2}, \frac{-5+9}{2}\right)$ i.e., (1, 2)
- :. Inclination of straight line passing through point (-3, 6) and midpoint (1, 2) is

$$m = \frac{2-6}{1+3}$$

$$\Rightarrow$$
 tan $\theta = -1$

$$\Rightarrow \theta = \frac{3\pi}{4}$$

21. The equation of lines in intercept form are

$$\frac{x}{-8/a} + \frac{y}{-8/b} = 1$$

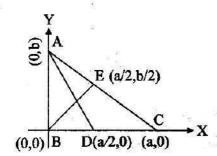
$$\frac{x}{-3} + \frac{y}{2} = 1$$

According to the given condition,

$$-\frac{8}{a} = -(-3)$$
 and $-\frac{8}{b} = -2$

$$\Rightarrow$$
 a = $-\frac{8}{3}$ and b = 4

22.



From figure,

$$\left(\frac{b/2}{a/2}\right) \left(\frac{b}{-a/2}\right) = -1$$

$$\Rightarrow a^2 = 2b^2 \Rightarrow a = \pm \sqrt{2}b$$

23. Let the points of the required line on X-axis and Y-axis be A(a, 0) and B(0, b) respectively.

Since,
$$\left(\frac{3}{2}, \frac{5}{2}\right)$$
 is midpoint of AB.

$$\therefore \frac{a+0}{2} = \frac{3}{2} \text{ and } \frac{0+b}{2} = \frac{5}{2} \Rightarrow a = 3 \text{ and } b = 5$$

$$\therefore \text{ the equation of line is } \frac{x}{3} + \frac{y}{5} = 1$$

$$\Rightarrow 5x + 3y - 15 = 0$$

24. Since, the line makes an angle of measure 30° with Y-axis. Therefore, the line will make an angle of measure 60° or - 60° with X-axis.

Slope of line =
$$\tan 60^{\circ}$$
 or $\tan(-60^{\circ})$
= $\sqrt{3}$ or $-\sqrt{3} = \pm \sqrt{3}$

- 25. Since, l, m, n are in A.P.
- .. 2m = l + nGiven equation of line is lx + my = n = 0Consider, option (B),

If the point (1, -2) satisfy the given equation.

- $\therefore l-2m+n=0 \Rightarrow 2m=l+n$ $\Rightarrow l, m, n \text{ are A.P.}$
- 26. The required equation of line is

$$\frac{x}{6} + \frac{y}{8} = 0 \implies 4x + 3y = 24$$

27. Slope =
$$\frac{(2-1)}{1-(-\frac{1}{2})} = \frac{1}{(\frac{3}{2})} = \frac{2}{3}$$

So, equation of the line is $y-2=\frac{2}{3}(x-1)$

$$\Rightarrow y = \frac{2}{3}x + \frac{4}{3}$$

Putting y = 0, to find x-intercept, $\frac{2}{3}x + \frac{4}{3} = 0$

$$\Rightarrow x = -2$$

- $\therefore x-intercept = -2$
- 28. Midpoint of given line segment = (2, -1)Now, slope of the line segment = $\frac{-8}{8} = -1$

Slope of the required line segment is 1

- .. the required equation of line is y + 1 = 1 (x 2) $\Rightarrow x - y = 3$
- 29. Here, the straight line is parallel to X-axis. So, the slope of such a line = 0.
- 30. Since, the required line will be a line passing through A and B.

$$\therefore \frac{y-6}{6-(-4)} = \frac{x-1}{1-3}$$

$$\Rightarrow 10x - 10 = -2y + 12 \Rightarrow 5x + y - 11 = 0$$

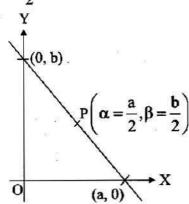
31. Since, px - qy = r intersects at X-axis and Y-axis

$$\therefore \quad \mathbf{a} = \frac{\mathbf{r}}{\mathbf{p}} \text{ and } \mathbf{b} = -\frac{\mathbf{r}}{\mathbf{q}}$$

$$\therefore a+b=\frac{r}{p}-\frac{r}{q}=r\left(\frac{q-p}{pq}\right)$$

- 32. Let $P\left(\alpha = \frac{a}{2}, \beta = \frac{b}{2}\right)$ be the midpoint of the line joining (a, 0) and (0, b).
- $\therefore \quad \alpha = \frac{a}{2} \Rightarrow a = 2\alpha \qquad \dots (i)$

and
$$\beta = \frac{b}{2} \Rightarrow b = 2\beta$$
(ii)

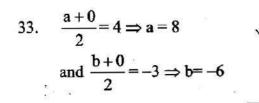


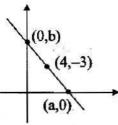
: Equation of a straight line cutting off intercepts a and b on X-axis and Y-axis respectively is

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\Rightarrow \frac{x}{2\alpha} + \frac{y}{2\beta} = 1 \qquad[From (i) and (ii)]$$

$$\Rightarrow \frac{x}{\alpha} + \frac{y}{\beta} = 2$$

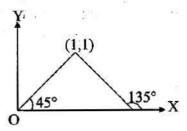




- .. the required equation of the line is $\frac{x}{8} + \frac{y}{-6} = 1$ $\Rightarrow \frac{3x - 4y}{24} = 1 \Rightarrow 3x - 4y = 24$
- 34. Here, $m_1 = -1$, $m_2 = -\frac{1}{k}$.

 For orthogonal lines, $m_1 m_2 = -1 \Rightarrow \frac{1}{k} = -1 \Rightarrow k = -1$
- 35. Point of intersection of the lines is (3, -2)Also, slope of perpendicular = $\frac{2}{7}$ Hence, the equation is $y + 2 = \frac{2}{7}(x - 3)$ $\Rightarrow 2x - 7y - 20 = 0$

- 36. Point of intersection is $y = -\frac{21}{5}$ and $x = \frac{23}{5}$
- $3x+4y=\frac{3(23)+4(-21)}{5}=\frac{69-84}{5}=-3$ Hence, required line is 3x+4y+3=0
- 37. Slopes of the lines are 1 and -1



Since, the point of intersection is (1, 1)Hence, the required equations are $y-1=\pm 1(x-1)$

38. The lines are bx + ay - ab = 0 and bx - ay - ab = 0. Hence, the required angle is

$$\tan^{-1} \left| \frac{ab - (-ab)}{b^2 + (-a^2)} \right| = \tan^{-1} \left| \frac{2ab}{b^2 - a^2} \right|$$

$$= 2 \tan^{-1} \frac{b}{a} \left[\because 2 \tan^{-1} \frac{y}{x} = \tan^{-1} \left| \frac{2xy}{y^2 - x^2} \right| \right]$$

39. The given lines are perpendicular because $m_1 m_2 = (2) \left(\frac{-1}{2}\right) = -1$

Hence, the angle between the two lines is 90°.

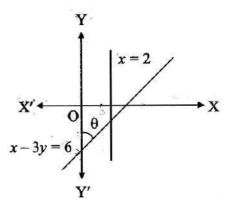
40. $a_1a_2 + b_1b_2 = \frac{1}{ab'} + \frac{1}{a'b} = 0$

Therefore, the lines are perpendicular.

41.
$$\theta = 90^{\circ} - \tan^{-1}\left(\frac{1}{3}\right)$$

$$\Rightarrow \tan \theta = \cot\left[\tan^{-1}\left(\frac{1}{3}\right)\right] = 3$$

$$\Rightarrow \theta = \tan^{-1}(3)$$



- 42. The slopes of the lines are $m_1 = \frac{-1}{2}$, $m_2 = 2$
- $m_1 m_2 = -1$ So, the lines are perpendicular i.e., $\theta = 90^\circ$
- 43. Here, the given lines are ax + by + c = 0bx + cy + a = 0

$$cx + cy + a = 0$$
$$cx + ay + b = 0$$

The lines will be concurrent, if $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0$

$$\Rightarrow a^3 + b^3 + c^3 - 3abc = 0$$

44. Here the lines are x - 3 = 0, y - 4 = 0 and 4x - 3y + a = 0.

These will be concurrent, if

$$\begin{vmatrix} 1 & 0 & -3 \\ 0 & 1 & -4 \\ 4 & -3 & a \end{vmatrix} = 0 \Rightarrow a = 0$$

45. Given lines are concurrent, if $\begin{vmatrix} 2 & 1 & -1 \\ a & 3 & -3 \\ 3 & 2 & -2 \end{vmatrix} = 0$

$$\Rightarrow -\begin{vmatrix} 2 & 1 & 1 \\ a & 3 & 3 \\ 3 & 2 & 2 \end{vmatrix} = 0$$

This is true for all values of a because C_2 and C_3 are identical.

46. Lines are concurrent, if $\begin{vmatrix} 4 & 3 & -1 \\ 1 & -1 & 5 \\ b & 5 & -3 \end{vmatrix} = 0$

$$\Rightarrow 4(3-25)-3(-3-5b)-1(5+b)=0$$

\Rightarrow -88+9+15b-5-b=0

$$\Rightarrow -84 + 14b = 0$$

$$\Rightarrow$$
 b = 6

- 47. (a-2b)x + (a+3b)y + 3a + 4b = 0or a(x+y+3) + b(-2x+3y+4) = 0, which represents a family of straight lines through point of intersection of x + y + 3 = 0 and -2x + 3y + 4 = 0 i.e, (-1, -2).
- 48. a, b, c are in H. P., then $\frac{2}{b} = \frac{1}{a} + \frac{1}{c}$ (i)

Given, line is
$$\frac{x}{a} + \frac{y}{b} + \frac{1}{c} = 0$$
(ii)

From (i) and (ii), we get

$$\frac{1}{a}(x-1) + \frac{1}{b}(y+2) = 0$$

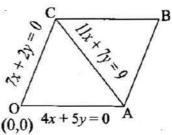
Since, $a \ne 0$, $b \ne 0$

So,
$$(x-1) = 0$$
 and $(y+2) = 0$

$$\Rightarrow x = 1$$
 and $y = -2$

- 49. Two sides x 3y = 0 and 3x + y = 0 of the given triangle are perpendicular to each other. Therefore, its orthocentre is the point of intersection of x 3y = 0 and 3x + y = 0 i.e., (0, 0).
- 50. Since, equation of diagonal 11x + 7y = 9 does not pass through origin, so it cannot be the equation of the diagonal OB. Thus, on solving the equation AC with the equations OA and

OC, we get
$$A\left(\frac{5}{3}, -\frac{4}{3}\right)$$
 and $C\left(\frac{-2}{3}, \frac{7}{3}\right)$



Therefore, the midpoint of AC is $\left(\frac{1}{2}, \frac{1}{2}\right)$.

Hence, the equation of OB is y = x i.e., x - y = 0.

51. The vertices of triangle are the intersection points of these given lines. The vertices of Δ are A(0, 4), B(1, 1), C(4, 0)

$$AB = \sqrt{(0-1)^2 + (4-1)^2} = \sqrt{10}$$

BC =
$$\sqrt{(1-4)^2 + (1-0)^2} = \sqrt{10}$$

$$AC = \sqrt{(0-4)^2 + (4-0)^2} = 4\sqrt{2}$$

- \therefore AB = BC
- ∴ Δ is isosceles.
- 52. Dividing both sides of relation 3a+2b+4c=0 by 4, we get $\frac{3}{4}a+\frac{1}{2}b+c=0$, which shows that for all values of a, b and c each member of the set of lines ax + by + c = 0 passes through the point $\left(\frac{3}{4}, \frac{1}{2}\right)$

53. Given lines are ax + by + c = 0and $x = \alpha t + \beta$, $y = \gamma t + \delta$ After eliminating t, we get $\gamma x - \alpha y + \alpha \delta - \gamma \beta = 0$ For parallelism condition, $\frac{a}{y} = \frac{b}{a\alpha} \Rightarrow a\alpha + b\gamma = 0$

54. The equation of a straight line passing through (3, -2) is y + 2 = m(x - 3)(i) The slope of the line $\sqrt{3}x + y = 1$ is $-\sqrt{3}$

So,
$$\tan 60^\circ = \pm \frac{m - (-\sqrt{3})}{1 + m (-\sqrt{3})}$$

On solving, we get

$$m = 0$$
 or $\sqrt{3}$

Putting the values of m in (i), the required equation of lines are y + 2 = 0 and

$$\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$$

- 55. Since, the point (-4, 5) does not lie on the diagonal 7x y + 8 = 0, so point will lie on the other diagonal.
 - Also, diagonals are perpendicular.
- $\therefore \quad \text{Slope of other diagonal} = \frac{-1}{7}$
- : equation of the other diagonal is

$$y-5 = -\frac{1}{7}(x+4) \implies 7y+x=31$$

56. Required equation of line which is parallel to x + 2y = 5 is x + 2y + k = 0(i)

Given equation of lines are

$$x + y = 2 \qquad \qquad \dots (ii)$$

$$x - y = 0 \qquad \qquad \dots (iii)$$

Adding (ii) and (iii), we get $2x = 2 \Rightarrow x = 1$ From (iii), we get y = 1

- .. Point of intersection is (1, 1).
 - Putting x = 1, y = 1 in (i), we get k = -3
- \therefore the required equation of line is x + 2y = 3.
- 57. The lines passing through the intersection of the lines ax + 2by + 3b = 0 and bx 2ay 3a = 0 is $ax + 2by + 3b + \lambda(bx 2ay 3a) = 0$ $\Rightarrow (a + b\lambda)x + (2b 2a\lambda)y + 3b 3\lambda a = 0$...(i) Line (i) is parallel to X-axis,

$$a + b\lambda = 0 \Rightarrow \lambda = \frac{-a}{b}$$

Putting the value of λ in (i), we get

$$ax + 2by + 3b - \frac{a}{b}(bx - 2ay - 3a) = 0$$

 $\Rightarrow y\left(2b + \frac{2a^2}{b}\right) + 3b + \frac{3a^2}{b} = 0$

$$\Rightarrow y \left(\frac{2b^2 + 2a^2}{b} \right) = -\left(\frac{3b^2 + 3a^2}{b} \right)$$

$$\Rightarrow y = \frac{-3(a^2 + b^2)}{2(b^2 + a^2)} = \frac{-3}{2}$$

So, it is 3/2 unit below X-axis.

- 58. Here, $m_1 = -\cot \alpha$, $m_2 = \tan \beta$
- $\therefore \quad \tan \theta = \frac{-\cot \alpha \tan \beta}{1 \cot \alpha \tan \beta}$
- $\therefore \tan \theta = -\cot(\alpha \beta)$
- $\therefore \quad \theta = \frac{\pi}{2} \beta + \alpha$
- 59. The point of intersection of the lines 3x + y + 1 = 0 and 2x y + 3 = 0 are $\left(\frac{-4}{5}, \frac{7}{5}\right)$.

The equation of line which makes equal intercepts with the axes is x + y = a.

$$\therefore \quad -\frac{4}{5} + \frac{7}{5} = a \Rightarrow a = \frac{3}{5}$$

: the required equation of the line is

$$x+y-\frac{3}{5}=0$$
 i.e., $5x+5y-3=0$

60.
$$x-3y=1$$
(i)

and
$$x^2 - 4y^2 = 1$$
(ii)

On solving (i) and (ii), we get

A(1,0) and B
$$\left(-\frac{13}{5}, -\frac{6}{5}\right)$$

These are the points of intersection of the straight line and hyperbola.

:. Length of straight line intercepted by the hyperbola

$$= \sqrt{\left(-\frac{13}{5} - 1\right)^2 + \left(-\frac{6}{5}\right)^2}$$

$$= \sqrt{\left(-\frac{18}{5}\right)^2 + \left(-\frac{6}{5}\right)^2} = \sqrt{\frac{324 + 36}{25}}$$

$$= \sqrt{\frac{360}{25}} = \frac{6}{5}\sqrt{10} \text{ units}$$

- 61. The point of intersection of the given lines are (-1, 1), (1, -1) and (2/3, 2/3) which is the vertices of an isosceles triangle.
- 62. Let the point be (h, 0), then $a = \left| \frac{bh + 0 ab}{\sqrt{a^2 + b^2}} \right|$ $\Rightarrow bh = \pm a\sqrt{a^2 + b^2} + ab$ $\Rightarrow h = \frac{a}{b}(b \pm \sqrt{a^2 + b^2})$

Hence, the points are $\left\{\frac{a}{b}(b\pm\sqrt{a^2+b^2}),0\right\}$.

63. Here, the lines are 3x + 4y - 9 = 0 and 6x + 8y - 15 = 0 or $3x + 4y - \frac{15}{2} = 0$.

Required distance =
$$\left| \frac{-9 - \left(\frac{-15}{2} \right)}{\sqrt{3^2 + 4^2}} \right| = \left| \frac{-3}{10} \right| = \frac{3}{10}$$

64. The line is 4x - 3y - 12 = 0.

Required length =
$$\left| \frac{-12}{\sqrt{4^2 + (-3)^2}} \right| = \frac{12}{5} = 2\frac{2}{5}$$

65. From option (C),

$$(1, 1)A \longrightarrow B(3, -2)$$

$$BP = \sqrt{(5-3)^2 + (7+2)^2}$$
$$= \sqrt{4+81} = \sqrt{85}$$

Hence, option (C) is correct.

66. Let p be the length of the perpendicular from the vertex (2, -1) to the base x + y = 2.

Then,
$$p = \left| \frac{2 - 1 - 2}{\sqrt{1^2 + 1^2}} \right| = \frac{1}{\sqrt{2}}$$

If 'a' is the length of the side of triangle, then $p = a \sin 60^{\circ}$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{a\sqrt{3}}{2}$$

$$\Rightarrow a = \sqrt{\frac{2}{3}}$$

67. Distance between lines -x + y = 2 and x - y = 2 is $\alpha = \left| \frac{2+2}{\sqrt{2}} \right| = 2\sqrt{2}$ (i)

Distance between lines 4x - 3y = 5 and 6y - 8x = 1 is

$$\beta = \left| \frac{5 - \left(\frac{-1}{2} \right)}{5} \right| = \frac{11}{10} \qquad(ii)$$

From (i) and (ii), we get

$$\frac{\alpha}{\beta} = \frac{2\sqrt{2}}{11/10}$$

$$\Rightarrow 20\sqrt{2}\beta = 11\alpha$$

68.
$$L = 2x + 3y - 4 = 0$$
,
 $L_{(-6,2)} = -12 + 6 - 4 < 0$
 $L' = 6x + 9y + 8 = 0$,
 $L'_{(-6,2)} = -36 + 18 + 8 < 0$

Hence, the point is below both the lines.

69. AD =
$$\left| \frac{-2 - 2 - 1}{\sqrt{(2)^2 + (-1)^2}} \right| = \left| \frac{-5}{\sqrt{5}} \right| = \sqrt{5}$$

Since, $\tan 60^{\circ} = \frac{AD}{BD}$ $\Rightarrow \sqrt{3} = \frac{\sqrt{5}}{BD}$ $\Rightarrow BD = \sqrt{\frac{5}{3}}$ BC = 2BD A(-1, 2) A(-1, 2) $BD = \sqrt{\frac{5}{3}}$ BC = 2BD

$$BC = 2BD$$

$$= 2\sqrt{\frac{5}{3}} = \sqrt{\frac{20}{3}}$$

70.
$$L_{12} \equiv x - 3y + 1 = 0$$

 $L_{23} \equiv 2x + y - 12 = 0$
 $L_{13} \equiv 3x - 2y - 4 = 0$

Therefore, the required distances are

$$D_{3} = \left| \frac{4 - 3 \times 4 + 1}{\sqrt{10}} \right| = \frac{7}{\sqrt{10}}$$

$$D_{1} = \left| \frac{4 + 1 - 12}{\sqrt{5}} \right| = \frac{7}{\sqrt{5}}$$

$$D_{2} = \left| \frac{3 \times 5 - 2 \times 2 - 4}{\sqrt{9 + 4}} \right|$$

$$= \frac{7}{\sqrt{13}}$$

71. Gradient of BC = -1 and its equation is x + y + 4 = 0. Therefore, the equation of line parallel to BC is $x + y + \lambda = 0$.

Also, it is $\frac{1}{2}$ unit distant from origin.

Thus,
$$\frac{\lambda}{\sqrt{2}} = \frac{1}{2} \Rightarrow \lambda = \frac{\sqrt{2}}{2}$$

Hence, the required equation of line is $2x + 2y + \sqrt{2} = 0$

72. Line L passes through (13, 32).

$$\therefore \frac{13}{5} + \frac{32}{b} = 1$$

$$\Rightarrow b = -20$$

So, equation of L is $\frac{x}{5} - \frac{y}{20} = 1 \Rightarrow 4x - y = 20$

Slope of L is $m_1 = 4$.

Slope of
$$\frac{x}{c} + \frac{y}{3} = 1$$
 is $m_2 = -\frac{3}{c}$

$$\Rightarrow -\frac{3}{c} = 4$$

$$\Rightarrow$$
 c = $-\frac{3}{4}$

Equation of line K is $-\frac{4x}{3} + \frac{y}{3} = 1$

$$\Rightarrow 4x - y = -3$$

Distance between L and K is $\left| \frac{20+3}{\sqrt{16+1}} \right| = \frac{23}{\sqrt{17}}$

73. Equation of straight line parallel to 4x - 3y = 5 is $4x - 3y = \lambda$

According to the given condition,

$$\frac{4(-1)-3(-4)-\lambda}{\sqrt{16+9}} = \pm 1$$

$$\Rightarrow 8 - \lambda = \pm 5$$

$$\Rightarrow \lambda = 3, 13$$

the equation of one of the lines is 4x - 3y - 3 = 0

74. Given, equation of line is

$$\frac{x\sin\alpha}{b} - \frac{y\cos\alpha}{a} - 1 = 0$$

:. perpendicular distance from origin

$$= \frac{\left| 0.\frac{\sin \alpha}{b} - \frac{0.\cos \alpha}{a} - 1 \right|}{\sqrt{\frac{\sin^2 \alpha}{b^2} + \frac{\cos^2 \alpha}{a^2}}} = \frac{|ab|}{\sqrt{a^2 \sin^2 \alpha + b^2 \cos^2 \alpha}}$$

75. Since x + y = 4 and 2x + 2y = 5 are parallel. Take (4, 0) on the line x + y = 4. Distance of (4, 0) from the line 2x + 2y - 5 = 0 $\frac{|2.4 + 2.0 - 5|}{\sqrt{2^2 + 2^2}} = \frac{3}{2\sqrt{2}} = \frac{3\sqrt{2}}{4} > 1$

.. Both lines are parallel and at a distance greater than unity.

 \therefore There is no point on the line x + y = 4.

76. Given equation of parallel lines are x-y+a=0, x-y+b=0

$$\therefore \quad \text{required distance} = \left| \frac{a - b}{\sqrt{(1)^2 + (-1)^2}} \right| = \frac{|a - b|}{\sqrt{2}}$$

77. Slope of given line ax + by + c = 0 is $-\frac{a}{b}$.

$$\therefore \quad -\frac{a}{b} = \pm 1 \Rightarrow a = \pm b \qquad \dots (i)$$

Distance of line ax + by + c = 0 from (1, -2)

$$=\frac{|a-2b+c|}{\sqrt{a^2+b^2}}$$

Distance of line ax + by + c = 0 from (3, 4)

$$=\frac{|3a+4b+c|}{\sqrt{a^2+b^2}}$$

According to the given condition,

$$\frac{|a-2b+c|}{\sqrt{a^2+b^2}} = \frac{|3a+4b+c|}{\sqrt{a^2+b^2}}$$

$$\Rightarrow 3a + 4b + c = \pm(a - 2b + c)$$

$$\Rightarrow$$
 a + 3b = 0 (taking +ve)(ii)

$$\Rightarrow$$
 2a + b + c = 0 (taking-ve)(iii)

From, (i) and (ii), we get a = b = 0 which is not possible so taking (i) and (iii), (taking a = -b) we get

$$\mathbf{a} + \mathbf{c} = \mathbf{0} \Rightarrow \mathbf{c} = -\mathbf{a}$$

$$a:b:c=a:-a:-a=1:-1:-1$$

or
$$a = 1$$
, $b = -1$, $c = -1$

From (i) and (iii) (taking a = b), we get

$$3a + c = 0 \Rightarrow c = -3a$$

$$a:b:c=a:a:-3a=1:1:-3$$

. option (B) is the correct answer.

78. Equation of the line is

$$y-0=\left(\frac{3-0}{-5}\right)(x-5)$$

$$\Rightarrow$$
 3x + 5y - 15 = 0

$$d = \left| \frac{3(4) + 5(4) - 15}{\sqrt{3^2 + 5^2}} \right| = \frac{17}{\sqrt{34}} = \sqrt{\frac{17}{2}}$$