

1. $248^{321} + 7$ is it divisible by 5?

$$LD(248^{321}) + 7$$

$$= LD(8^{321}) + 7$$

$$= LD(8^{32 \times 4}) + 7$$

$$= LD(8^1) + 7$$

$$= LD(8 + 7)$$

$$= 5$$

so $(248^{321}) + 7$ is divisible by 5.

2. Is $1357^{1002} + 1$ divisible by 2?

$$LD(1357^{1002}) + 1$$

$$= LD(7^{1002}) + 1$$

$$= LD(7^{1002 \cdot 4}) + 1$$

$$= LD(7^2) + 1$$

$$= LD(49 + 1)$$

$$= 0$$

So, it is divisible by 2.

3. $123^{45} + 789^{10}$ What's the last digit?

$$\begin{aligned} & LD(123^{45}) + LD(789^{10}) \\ &= LD(3^{45}) + LD(9^{10}) \\ &= LD(3^{45 \cdot 4}) + LD(9^{10 \cdot 4}) \\ &= LD(3^1) + LD(9^2) \\ &= LD(3+1) \\ &= 4 \end{aligned}$$

So, the last digit of $(123^{45}) + (789^{10})$ is 4.

4. $672^{55} + 8$ is it divisible by 10?

$$\text{LO} (672^{55}) + 8$$

$$= \text{LO} (2^{55}) + 8$$

$$= \text{LO} (2^{55 \times 4}) + 8$$

$$= \text{LO} (2^3) + 8$$

$$= \text{LO} (8 + 8)$$

$$= 6$$

so, $(672^{55}) + 8 = 6$, which is
not divisible by 10

5. $987^{63} - 456^{21}$ what's the last digit?

$$LD(987^{63} - 456^{21})$$

$$= LD(7^{63} - 6^{21})$$

$$= LD(7^{63 \times 4} - 6^{21 \times 4})$$

$$= LD(7^3 - 6^1)$$

$$= LD(3 - 6)$$

$$= LD(-3)$$

$$= -3$$

CAT says the last digit answer is 7.

is -3 (which answer is correct?)

Here, we know
 $987^{63} - 456^{21} > 0$
(Since base is bigger
& power is also bigger
for the minuend).

$$\begin{array}{r} \dots 3 \\ - \dots 6 \\ \hline \dots 7 = 7 \\ \hline \end{array}$$

(Borrow 1 from 10's place)

6. 111^{99}

is $1 \pmod{5}$ and $1 + 4 = 5$

$+4$ is divisible
by 5

because, 111^{99} 's last digit

7. $543^{77} + 222^{33}$ is it an even,
or odd number?

$$= \text{LD}(3^{77} + 2^{33})$$

$$= \text{LD}(3^{77 \cdot 4} + 2^{33 \cdot 4})$$

$$= \text{LD}(3^1 + 2^3)$$

$$= \text{LD}(3 + 8)$$

$$= \text{LD}(11)$$

$$= 1$$

$$\text{LD}(3 + 2)$$

$$= 5$$

The number is an odd number.

8. $12^{20} \times 24^{30}$ What's the last digit?

$$\begin{aligned} & \text{LD}(12^{20} \times 24^{30}) \\ &= \text{LD}(2^{20} \times 4^{30}) \\ &= \text{LD}(2^{20 \div 4} \times 4^{30 \div 4}) \\ &= \text{LD}(2^5 \times 4^2) = \text{LD}(2^4 \times 4^2) \\ &= \text{LD}(1 \times 6) = \text{LD}(6 \times 6) \\ &= \text{LD}(6) = 6 \end{aligned}$$

Do
44, 844, 944 all
end with 1?
% not %

the last digit is 8.

9. $777^{77} + 23$ is it divisible by 10?

$$LD(777^{77} + 23)$$

$$= LD(7^{77} + 23)$$

$$= LD(7^{7 \cdot 11} + 23)$$

$$= LD(7^1 + 23)$$

$$= LD(7 + 23)$$

$$= LD(30)$$

$$= 0$$

it is divisible by 10.

10. $19^{51} + 28^{62} + 37^{73}$ What's the last digit?

because 9's power have last digits as 9, 1, 9, 1 ... and 1 is the remainder when 2 divides 51. So, the last digit is 9.

because 8's powers have last digits as 8, 4, 2, 6 and 2 is the remainder when 4 divides 62. So, last digit is 4.

because 7's powers have last digits as 7, 9, 3, 1 and when we divide 4 with 7, the remainder is 1, so last digit is 7, and $9 + 4 + 7 = 20$

$$= LD(19^{51} + 28^{62} + 37^{73})$$

$$= LD(9^{51 \times 4} + 8^{62 \times 4} + 7^{73 \times 4})$$

$$= LD(9^3 + 8^2 + 7^1)$$

$$= LD(9 + 4 + 7)$$

$$= LD(13 + 7)$$

$$= LD(20)$$

$$= 0$$

the last digit is 0.

11. is $123456^{789} + 1$

divisible by 2?

$$= \text{LD}(123456^{789} + 1)$$

$$= \text{LD}(6^{789 \cdot 4} + 1)$$

$$= \text{LD}(6^1 + 1)$$

$$= \text{LD}(6 + 1)$$

$$= \text{LD}(7)$$

$$= 7$$

So, 123456^{789}

$+ 1$ is not divisible

by 2.

12. $765^{432} + 321^{987}$ - What's the last digit

$$\text{LP}(765^{432} + 321^{987})$$
$$= \text{LP}(5^{432} + 1^{987})$$

$= \text{LP}(5+1) \text{ [} 5^{\text{anything}} \text{ is 5, ans same for]}$

$$= \text{LP}(6)$$

$$= 6$$

So, $765^{432} + 321^{987}$ last digit is 6

$$13. \quad 987654^{32} - 9$$

is it divisible by 5?

$$\begin{aligned} & \text{LD}(4^{32} - 9) \\ &= \text{LD}(4^{31} \times 4 - 9) \\ &= \text{LD}(4^9 - 9) \\ &= \text{LD}(\underline{\underline{4 - 9}}) \\ &= \underline{\underline{-5}} \end{aligned}$$

$$= \text{LD}(4^4 - 9)$$

$$= \text{LD}(6 - 9) = \text{LD}(14 - 9) = 7$$

↳ not
divisible
by 5

CAI says the answer
is 47

987654³² is divisible by 5; AI says the
opposite way;

14. What is the last ^{digit of} $23^{15} \times 47^{25} + 5$?

$$\text{LD} (23^{15} \times 47^{25} + 5)$$

$$= \text{LD} (3^{15} \times 7^{25} + 5)$$

$$= \text{LD} (3^{15 \div 4} \times 7^{25 \div 4} + 5)$$

$$= \text{LD} (3^3 \times 7^1 + 5)$$

$$= \text{LD} (7 \times 7 + 5)$$

$$= \text{LD} (49 + 5)$$

$$= \text{LD} (54)$$

$$= 4$$

Last digit is 4

15. is $10^{1001} + \overset{99}{99}$ divisible by 10?

$$\text{LDC}(10^{1001} + 99)$$

$$= \text{LDC}(10^{1001} + 99)$$

$$= \text{LDC}(1 + 99)$$

$$= \text{LDC}(100)$$

$$= 0$$

Yes!

(6. is $8642^{51} - 1357^{24}$ LD even or odd?

$$\text{LD}(8642^{51} - 1357^{24})$$

$$= \text{LD}(2^{51} - 7^{24})$$

$$= \text{LD}(2^{51 \cdot 4} - 7^{24 \cdot 4})$$

$$= \text{LD}(2^3 - 7^4)$$

$$= \text{LD}(2^3 - 0)$$

$$= \text{LD}(8 - 1)$$

$$= \text{LD}(3)$$

$$= 7$$

$$= 3$$

the answer is odd.

17. What's the last digit ^{of} $11^{11} + 22^{22} + 33^{33}$?

$$LD(11^{11} + 22^{22} + 33^{33})$$

$$= LD(1^{11} + 2^{22} + 3^{33})$$

$$= LD(1^{11} + 2^{2 \cdot 2 \cdot 4} + 3^{33 \cdot 4})$$

$$= LD(1 + 2^2 + 3^1)$$

$$= LD(1 + 4 + 3)$$

$$= LD(5 + 3)$$

$$= LD(8)$$

$$= 8$$

Last digit is 8

18. $456^{78} + 4$ is it divisible by 3?

$$= LD(456^{78} + 4)$$

$$= LD(6^{78} + 4)$$

$$= LD(6 + 4)$$

$$= LD(10)$$

$$= 0$$

it is divisible by 3.

19. What's the last digit of $7^{2025} + 3^{2025}$

$$\text{LDC } 7^{2025 \div 4} + 3^{2025 \div 4}$$

$$= \text{LD}(7' + 3')$$

$$= \text{LD}(7 + 3)$$

$$= \text{LD}(10)$$

$$= 0$$

20. is $99999^9 + 111$ is it divisible by 2 or 10?

$$LD(99999^9 + 111)$$

$$= LD(9^9 + 111)$$

$$= LD(9 + 111)$$

$$= LD(120)$$

$$= 0$$

so, it is divisible by 2, and 10.