

Statistics for IT

POISSON DISTRIBUTION

Week 4

Binomial Experiment

- It is used for events that occurs randomly in a specified unit of space, distance or time
 - A fixed number of trials (n)
 - Each trial should be success or failure
 - The trials are independent
 - The probability of success (p) at each trial is a constant

Binomial random variable

- A binomial random variable is the number of successes (s) in 'n' repeated trials of a binomial experiment

Binomial Distribution

- The probability distribution of a binomial random variable is called a binomial distribution

$$X \sim \text{Bin}(n, p)$$

- The probability function of a binomial distribution is

$$P(x) = {}^n C_x p^x q^{n-x} \text{ where } q=1-p$$

- Eg: A coin is tossed 10 times. Find the probability of getting exactly 3 heads

$$\begin{aligned} P(x) &= {}^n C_x p^x q^{n-x} \\ P(3) &= {}^{10} C_3 0.5^3 0.5^{10-3} \\ &= 0.117 \end{aligned}$$

Mean & variance of a binomial distribution

- $E(x) = np$
- $V(x) = npq$