

Multiview

Name	Dharini Baskaran
Identity Key	dhba5060

	Level	Completed	Goal	
	Beginner	16	4722	18
	Intermediate	5	5722	20
	Advanced	0	Total Completed	
	Expert	0	21	

Multiview

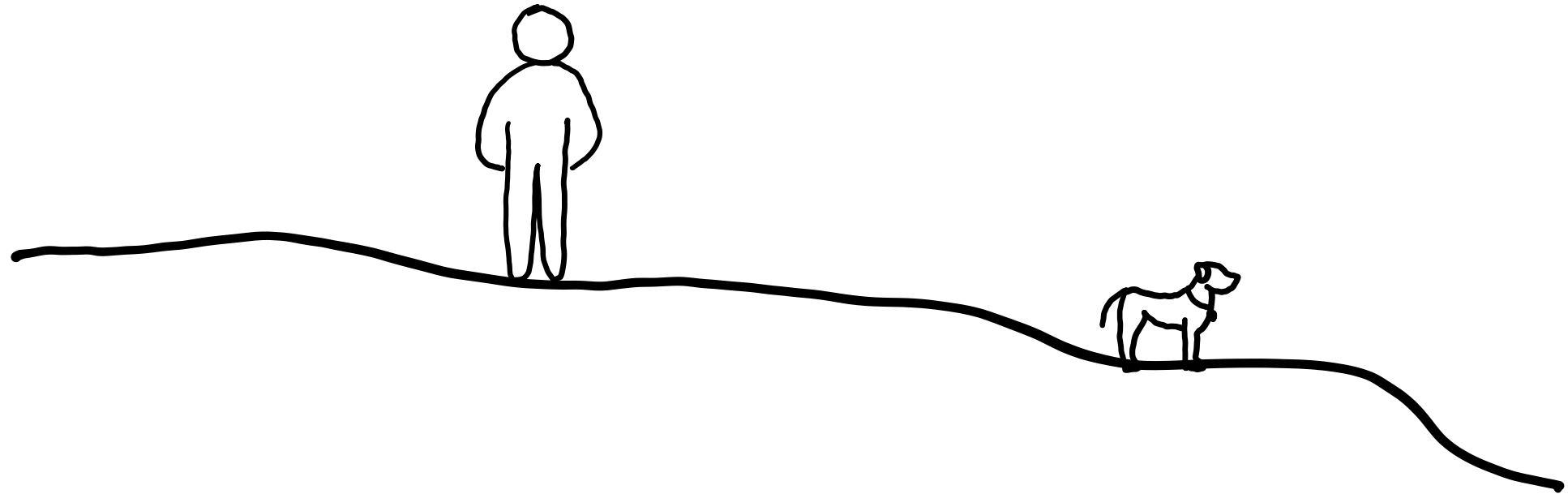
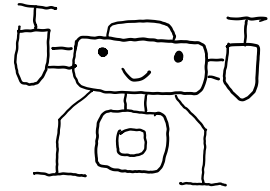
CSCI 5722/4722: Computer Vision

Spring 2024

Dr. Tom Yeh

Dr. Mehdi Moghari

Motivation



Where is the ball in the photo?



Key questions

1. Where is the object in relation to the camera? (Multiple Coordinate Systems)
2. Where is the camera? (3D Translation)
3. Where is the camera pointing at? (3D Rotation)
4. How is the object “seen” by the camera? (Projection)

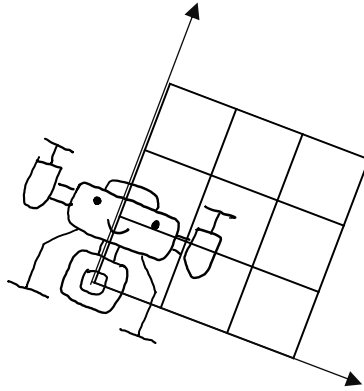
Multiple Coordinate Systems

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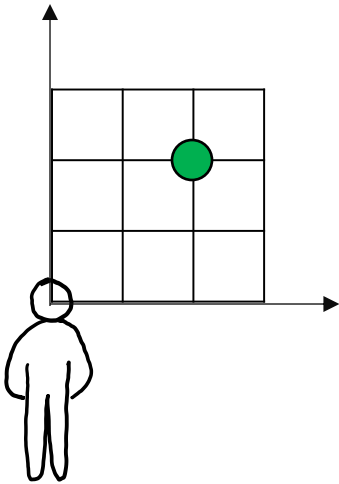
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Same Point in Different Coordinate Systems



P seen from me = _____

P seen from the drone = _____



${}^M\mathbf{p}_1$

${}^R\mathbf{p}_1$

Me (M), Dog (D), and Camera (C)

P seen by me:

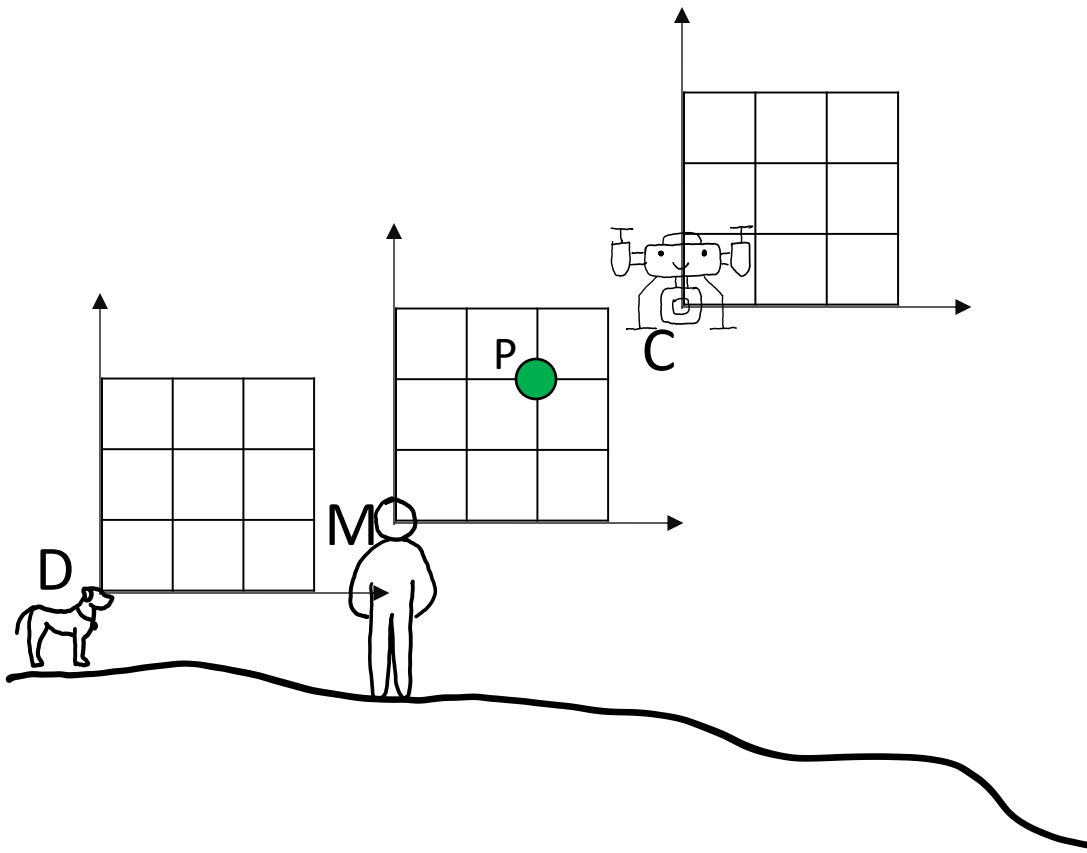
_____ = [,]

P seen by my dog

_____ = [,]

P seen by the drone camera:

_____ = [,]



✓ ○ Me (M), Dog (D), and Camera (C)

P seen by me:

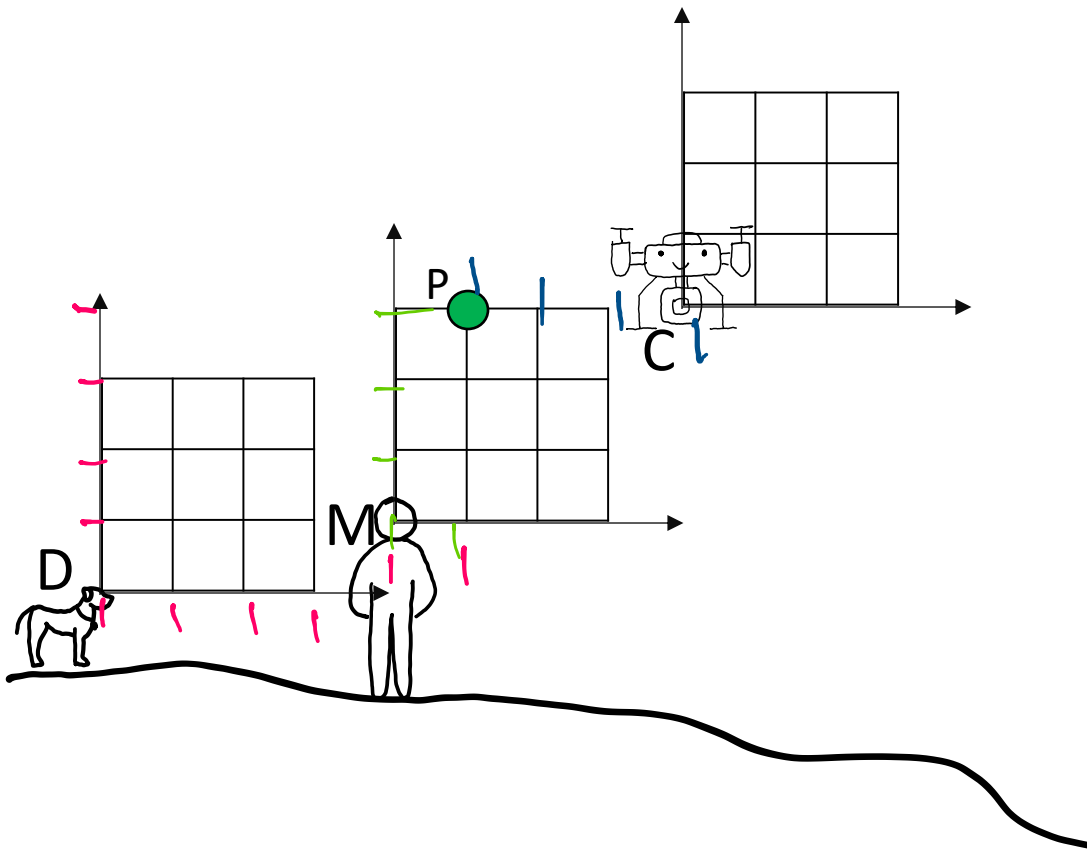
$$^M P = [1 , 3]$$

P seen by my dog

$$^D P = [5 , 4]$$

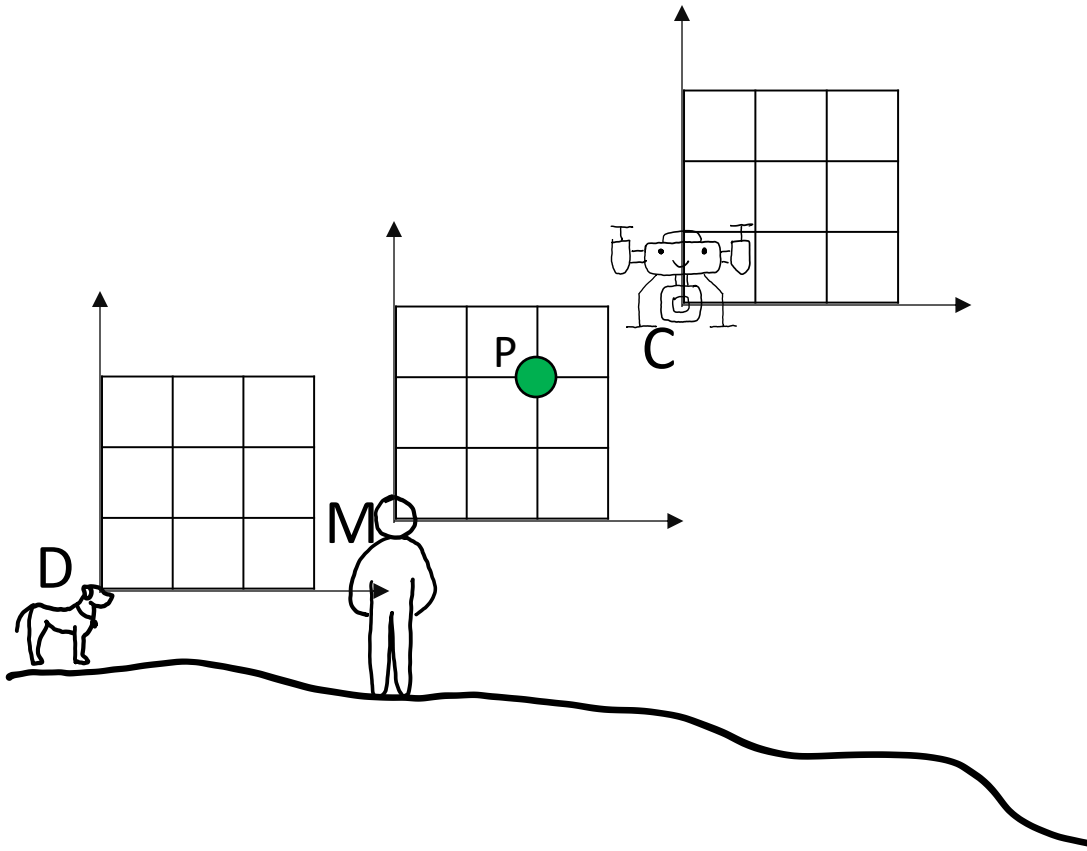
P seen by the drone camera:

$$^C P = [-3 , 0]$$

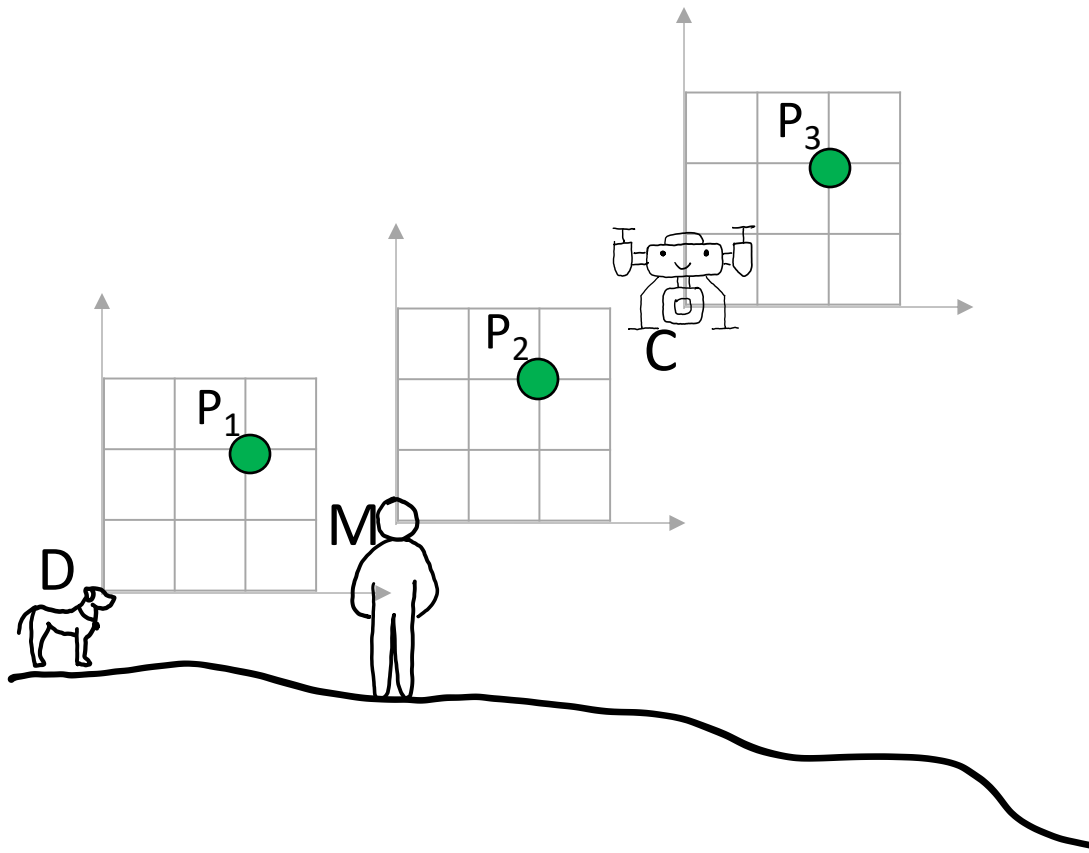


Equal or Not Equal?

M_p ____ C_p ____ D_p



Equal or Not Equal?



$$MP_1 \quad ______ \quad MP_2 \quad ______ \quad MP_3$$

$$DP_1 \quad ______ \quad DP_2 \quad ______ \quad DP_3$$

$$CP_1 \quad ______ \quad CP_2 \quad ______ \quad CP_3$$

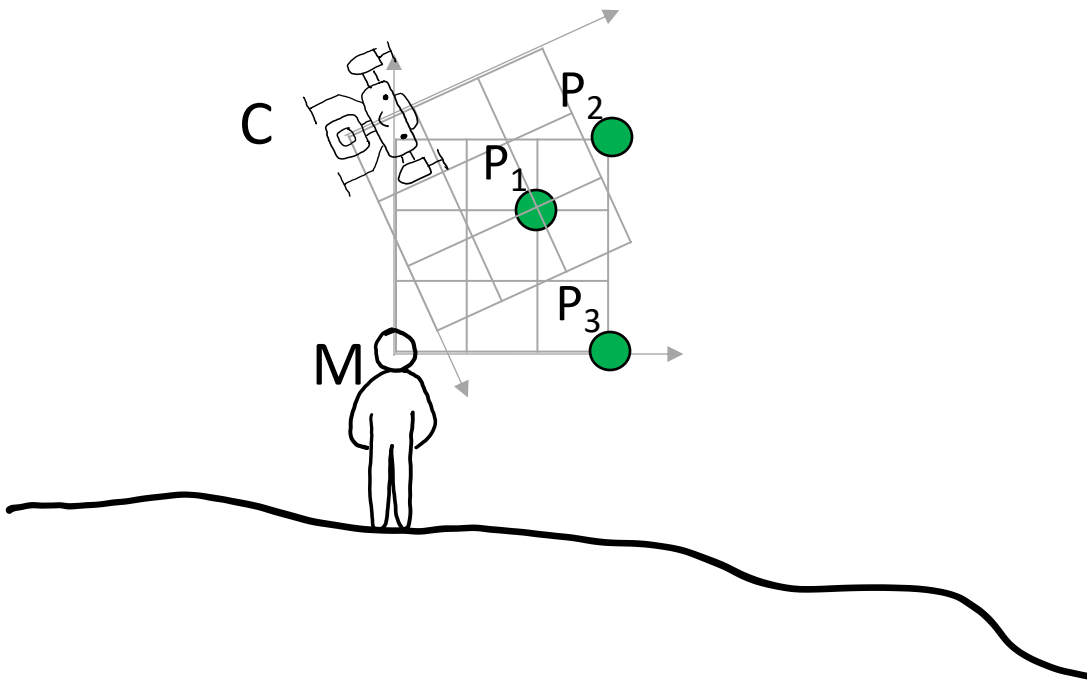
$$MP_1 \quad ______ \quad DP_2 \quad ______ \quad CP_3$$

Equal or Not Equal?

$$MP_1 \text{ ______ } CP_1$$

$$MP_2 \text{ ______ } CP_2$$

$$MP_3 \text{ ______ } CP_3$$



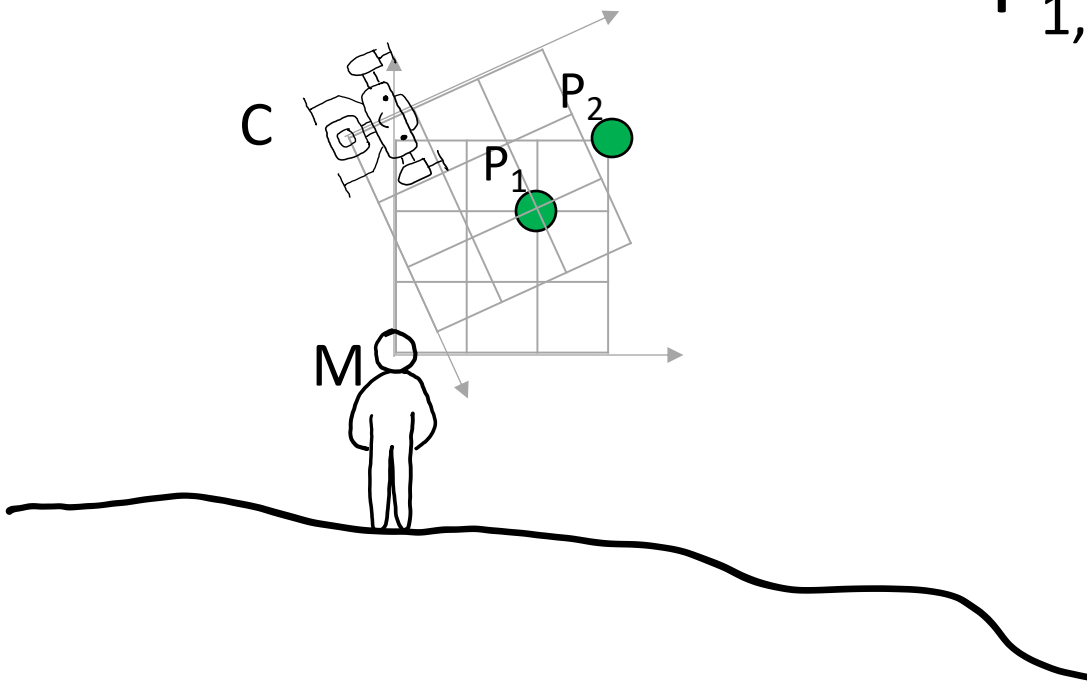
Greater or Less?

$$MP_{1,x} \text{ ______ } MP_{2,x}$$

$$MP_{1,y} \text{ ______ } MP_{2,y}$$

$$CP_{1,x} \text{ ______ } CP_{2,x}$$

$$CP_{1,y} \text{ ______ } CP_{2,y}$$

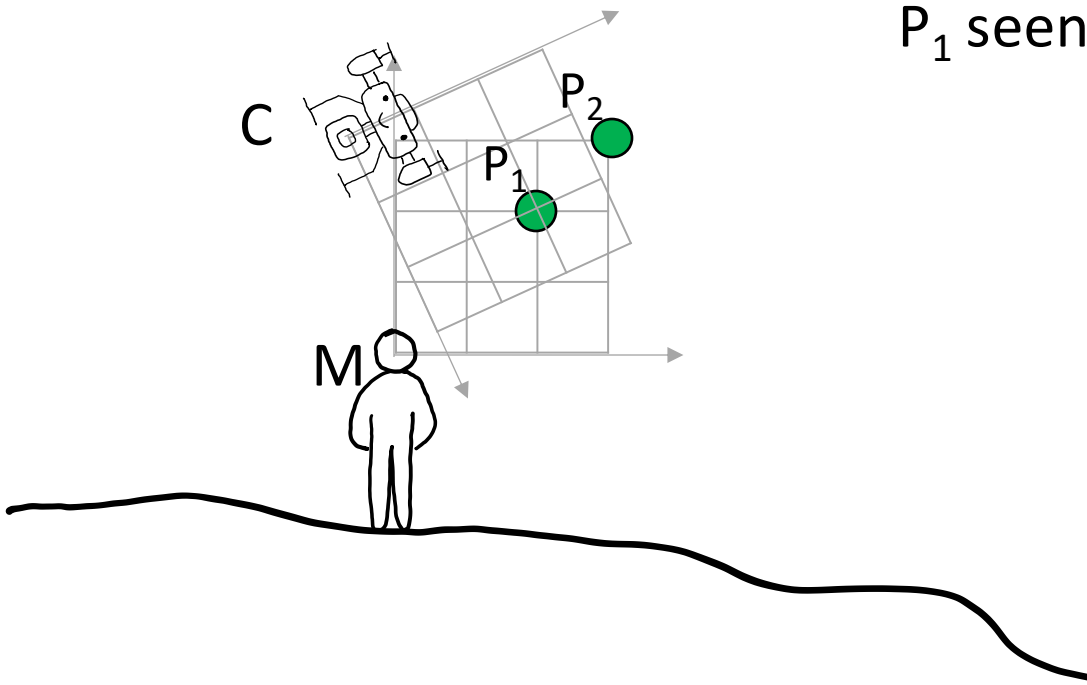


✓ ☒ Me (M) and Camera (C)

P_1 seen by me: ${}^M P_1 = [2, 2]$

P_2 seen by me: ${}^M P_2 = [3, 3]$

P_1 seen by the drone camera: ${}^C P_1 = [2, 2]$





Greater or Less?

$$MP_{1,x} \text{ } \underline{\text{ } < \text{ }} MP_{2,x}$$

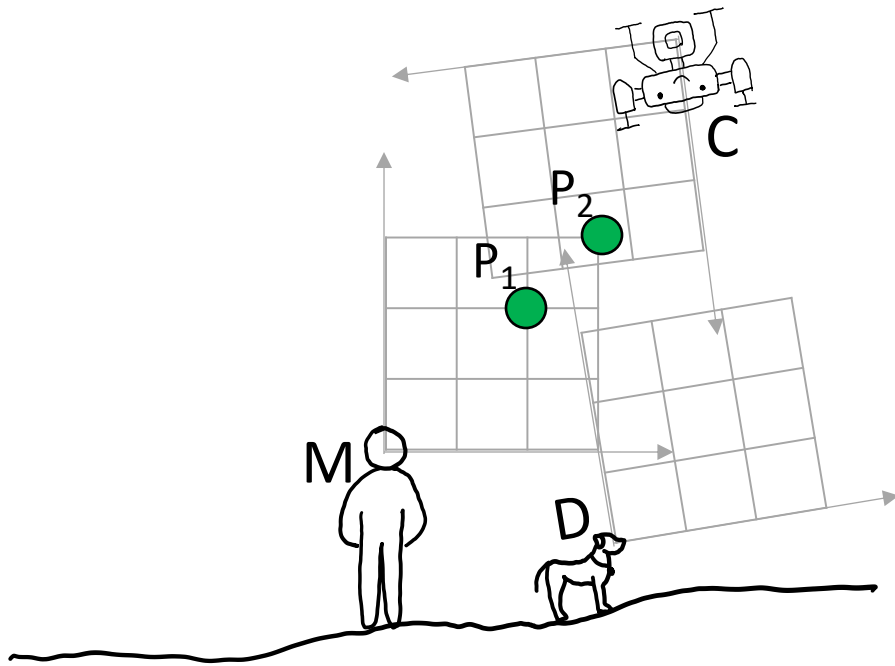
$$MP_{1,y} \text{ } \underline{\text{ } < \text{ }} MP_{2,y}$$

$$CP_{1,x} \text{ } \underline{\text{ } > \text{ }} CP_{2,x}$$

$$CP_{1,y} \text{ } \underline{\text{ } > \text{ }} CP_{2,y}$$

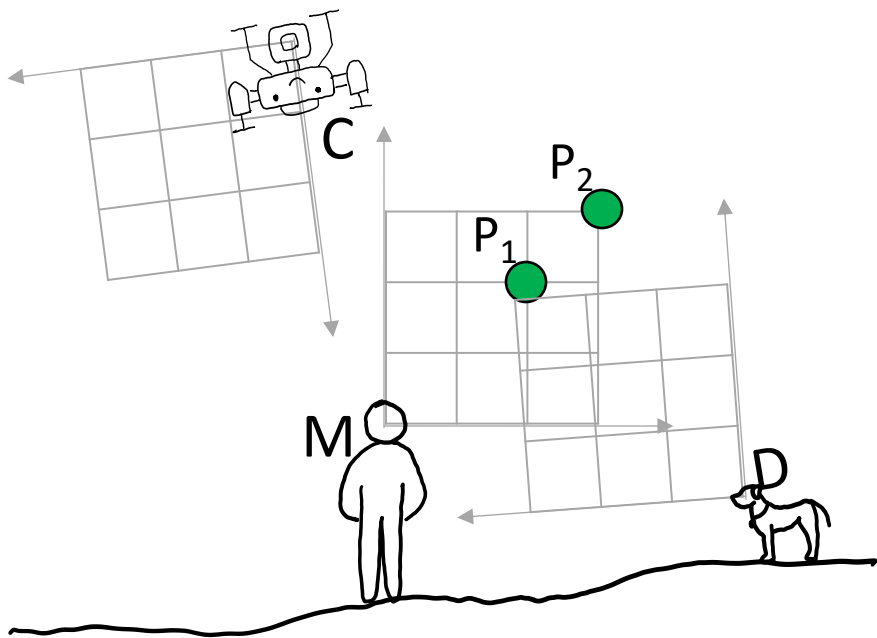
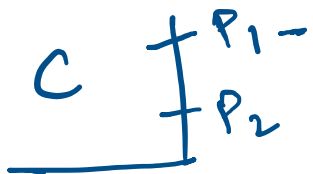
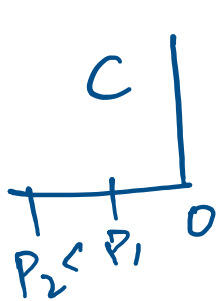
$$DP_{1,x} \text{ } \underline{\text{ } < \text{ }} DP_{2,x}$$

$$DP_{1,y} \text{ } \underline{\text{ } < \text{ }} DP_{2,y}$$





Greater or Less?



$$MP_{1,x} \quad \text{---} \quad MP_{2,x}$$

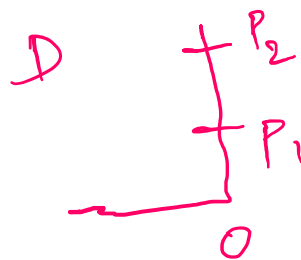
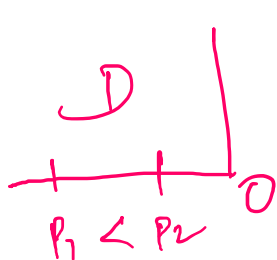
$$M_{P_{1,y}} \prec M_{P_{2,y}}$$

$$C_{P_{1,x}} \succ C_{P_{2,x}}$$

$$c_{p_{1,y}} > c_{p_{2,y}}$$

$$Dp_{1,x} \text{ --- } Dp_{2,x}$$

$$DP_{1,y} \xrightarrow{\quad} DP_{2,y}$$



3D Viewing Planes

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Skull sutures

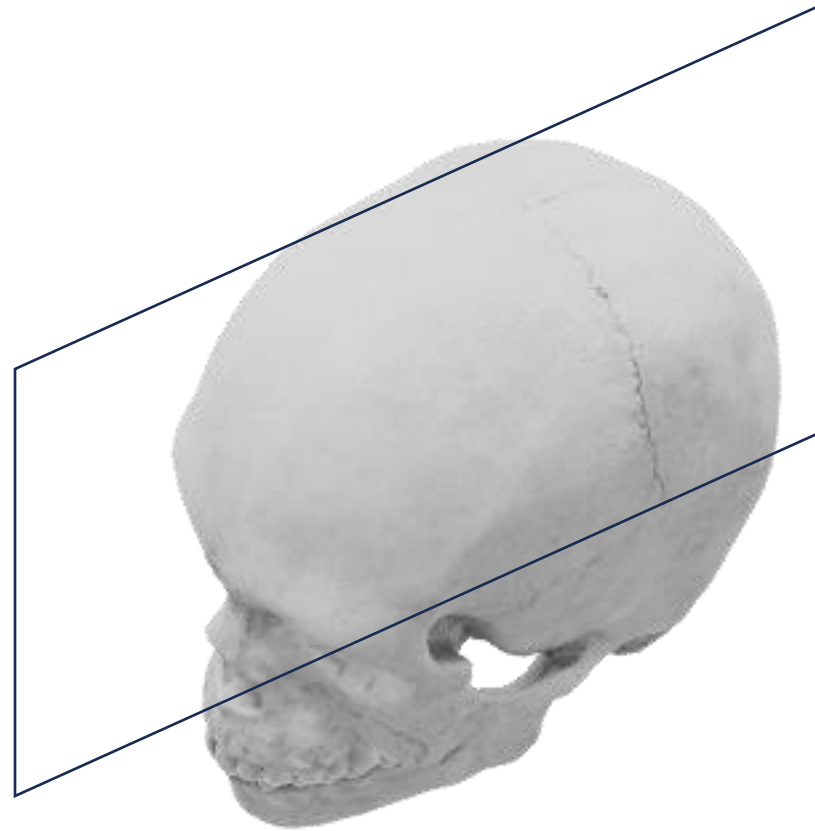


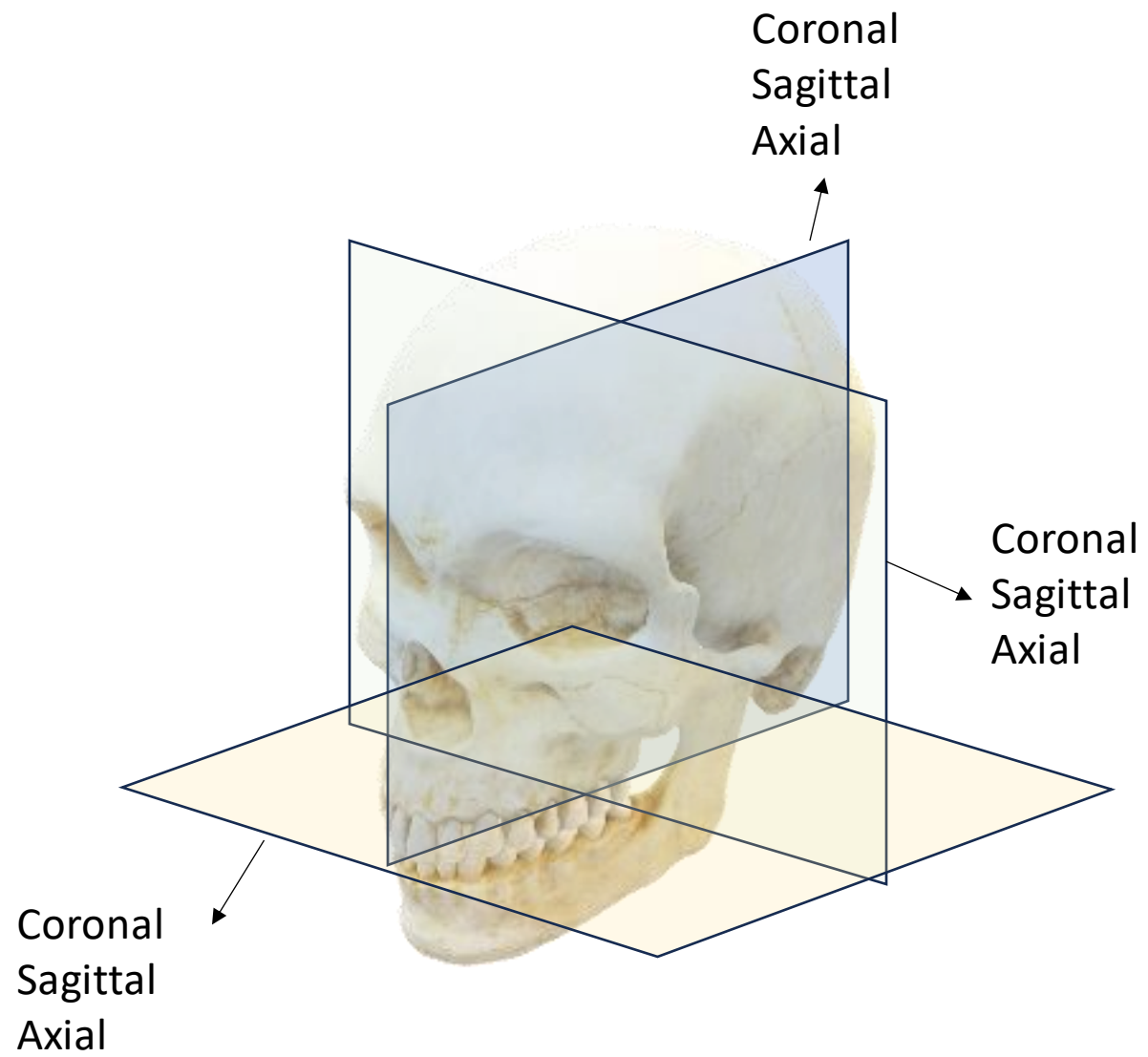
Coronal Plane

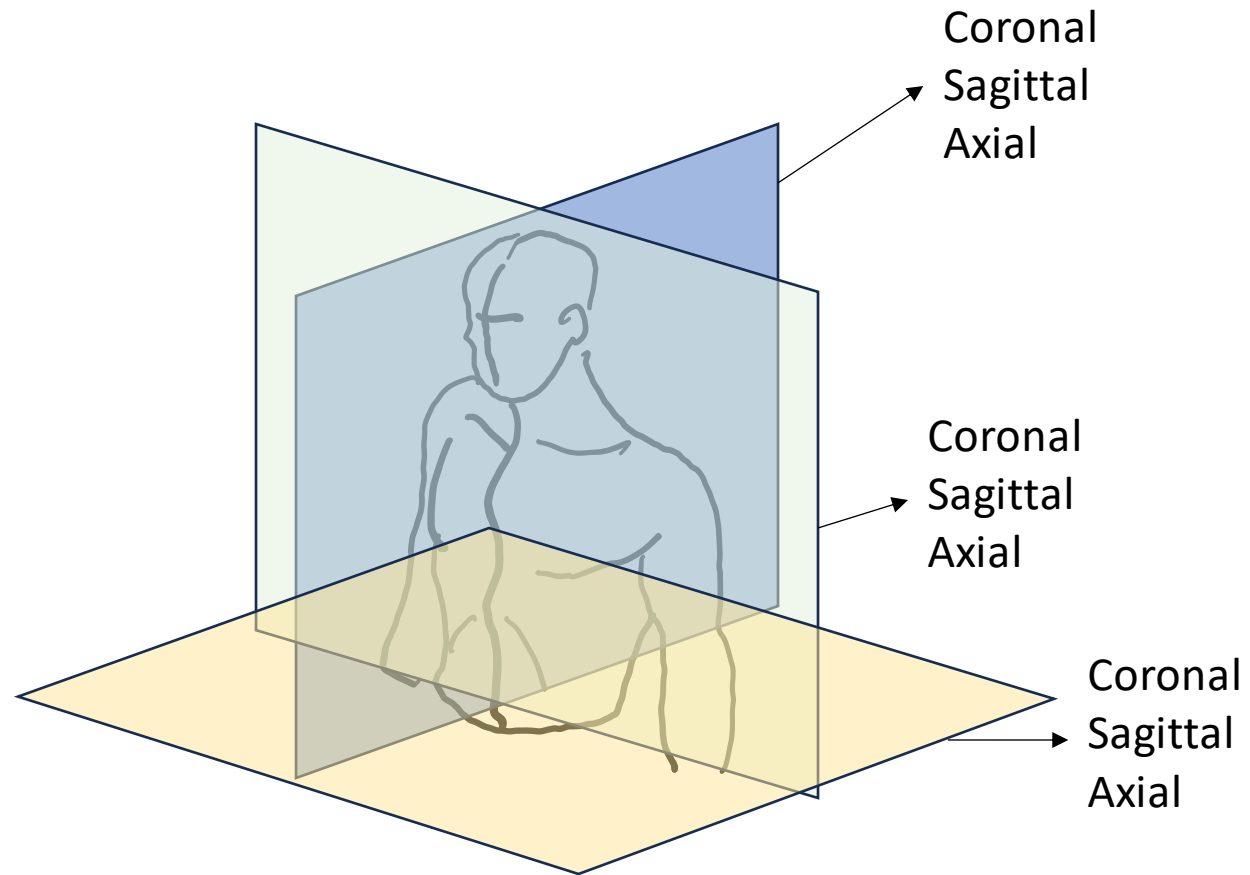




Sagittal Plane



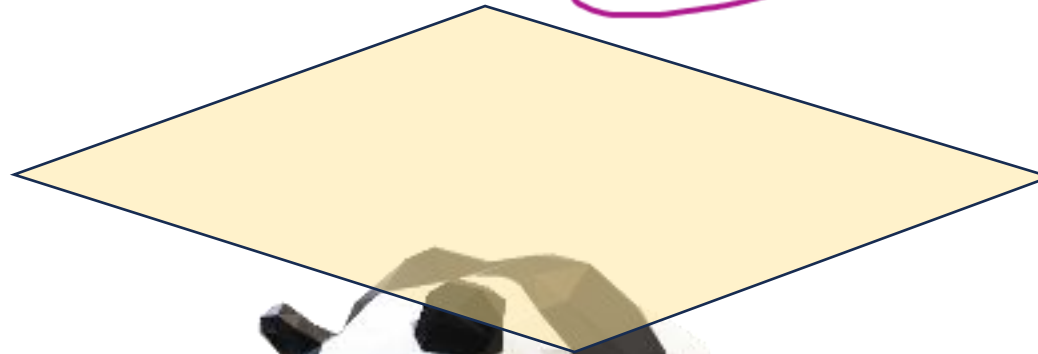




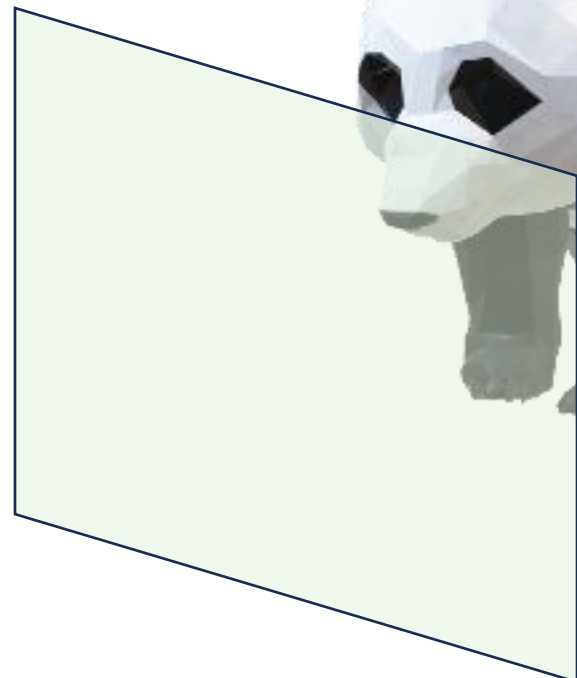


Circle the views

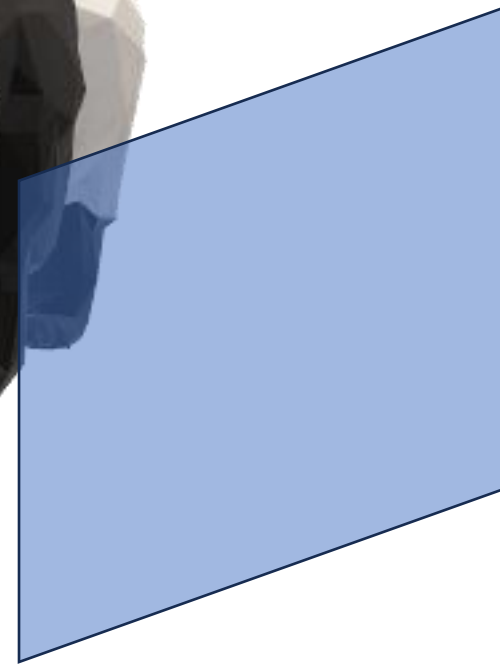
Coronal
Sagittal
Axial



Coronal
Sagittal
Axial

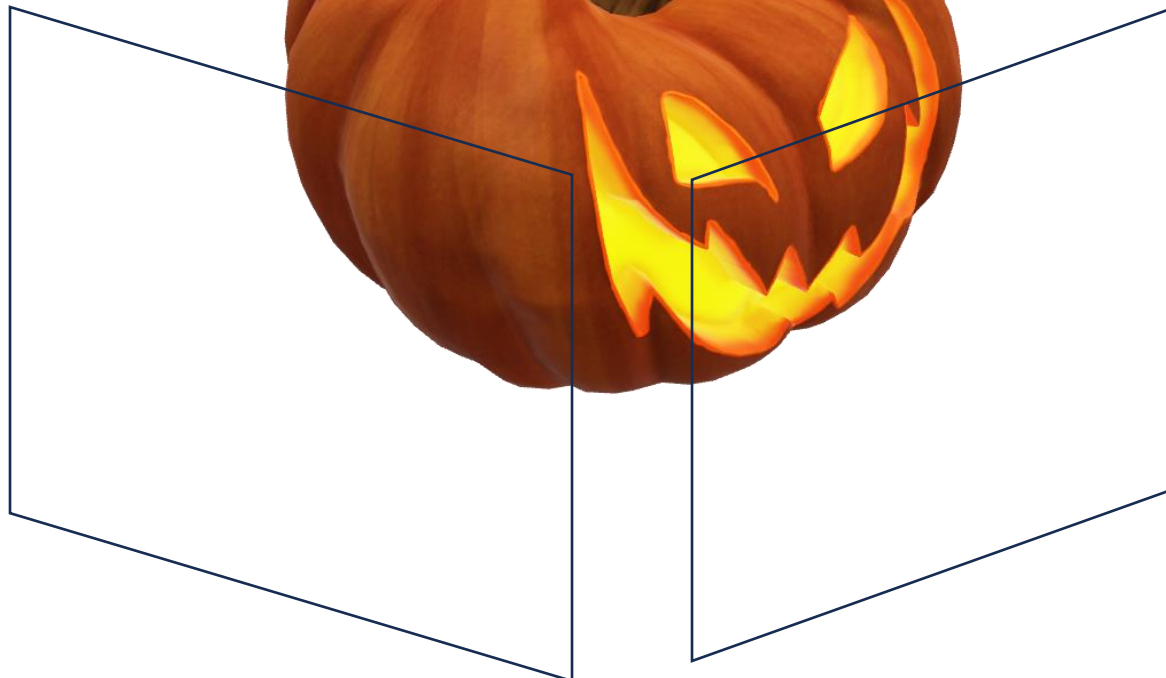


Coronal
Sagittal
Axial



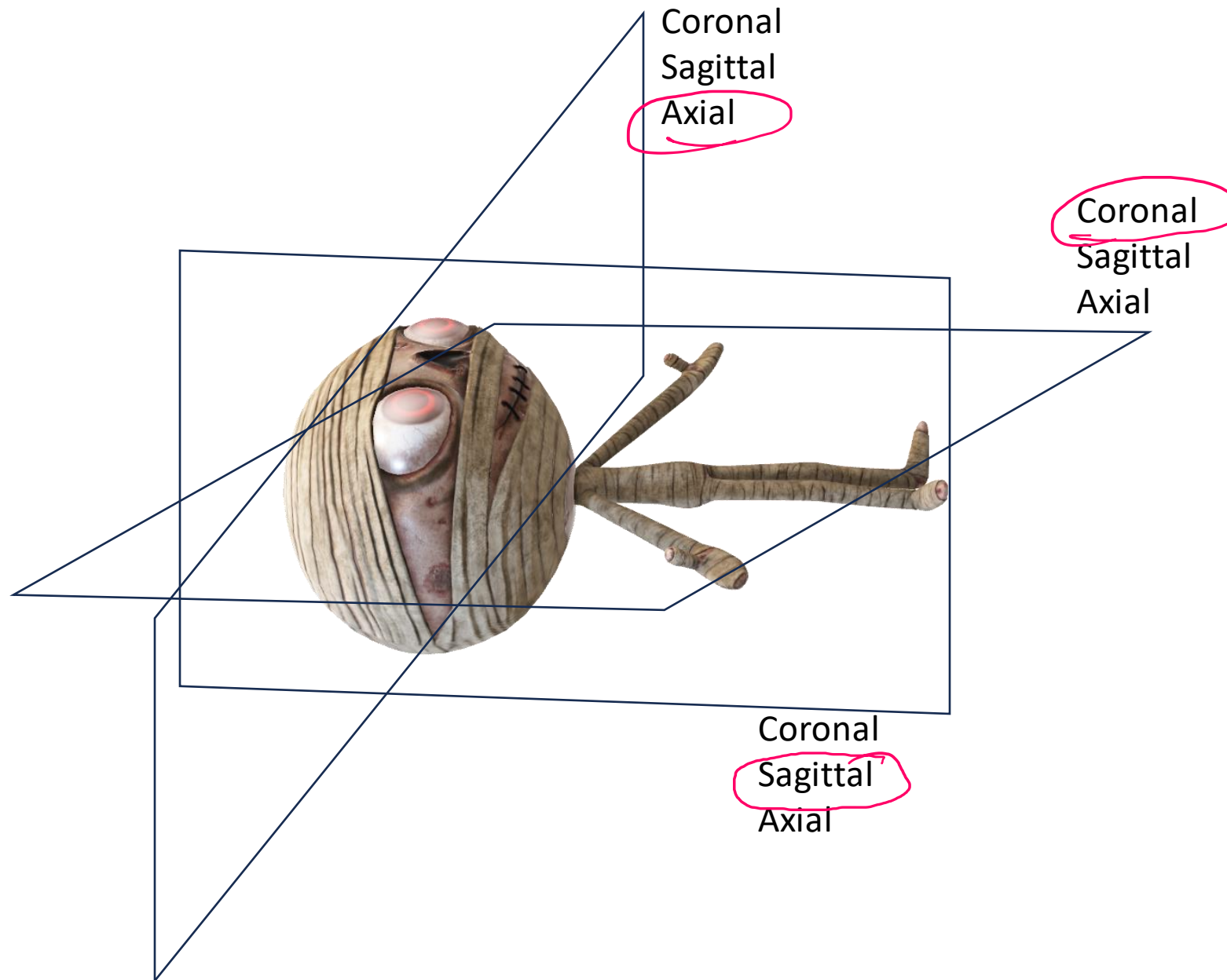


Coronal
Sagittal
Axial



Coronal
Sagittal
Axial

Coronal
Sagittal
Axial



3D Multiview Projection

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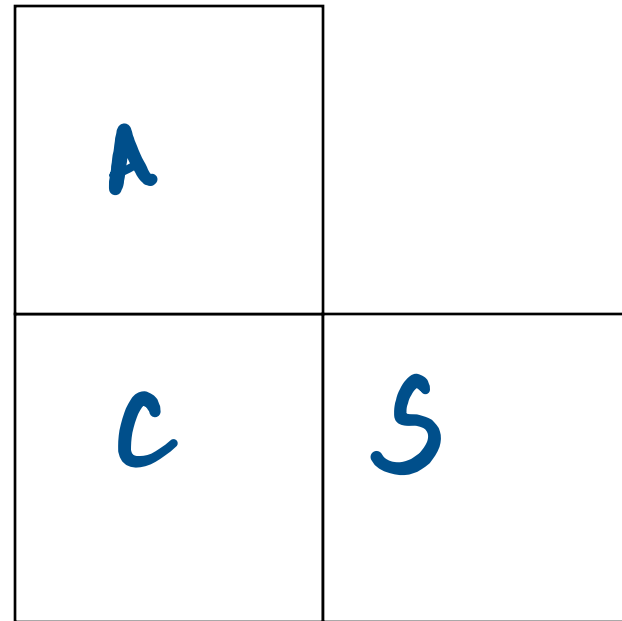
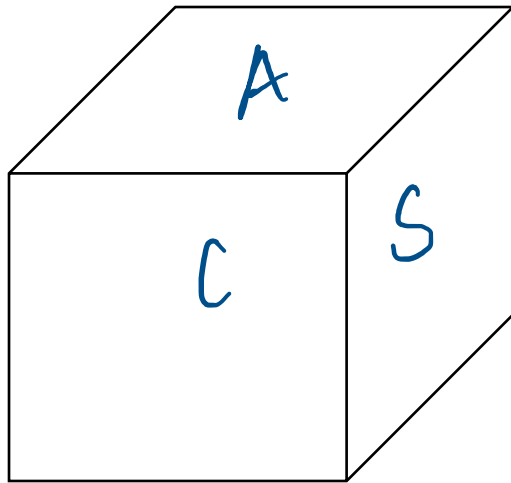
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Mapping CSA Planes

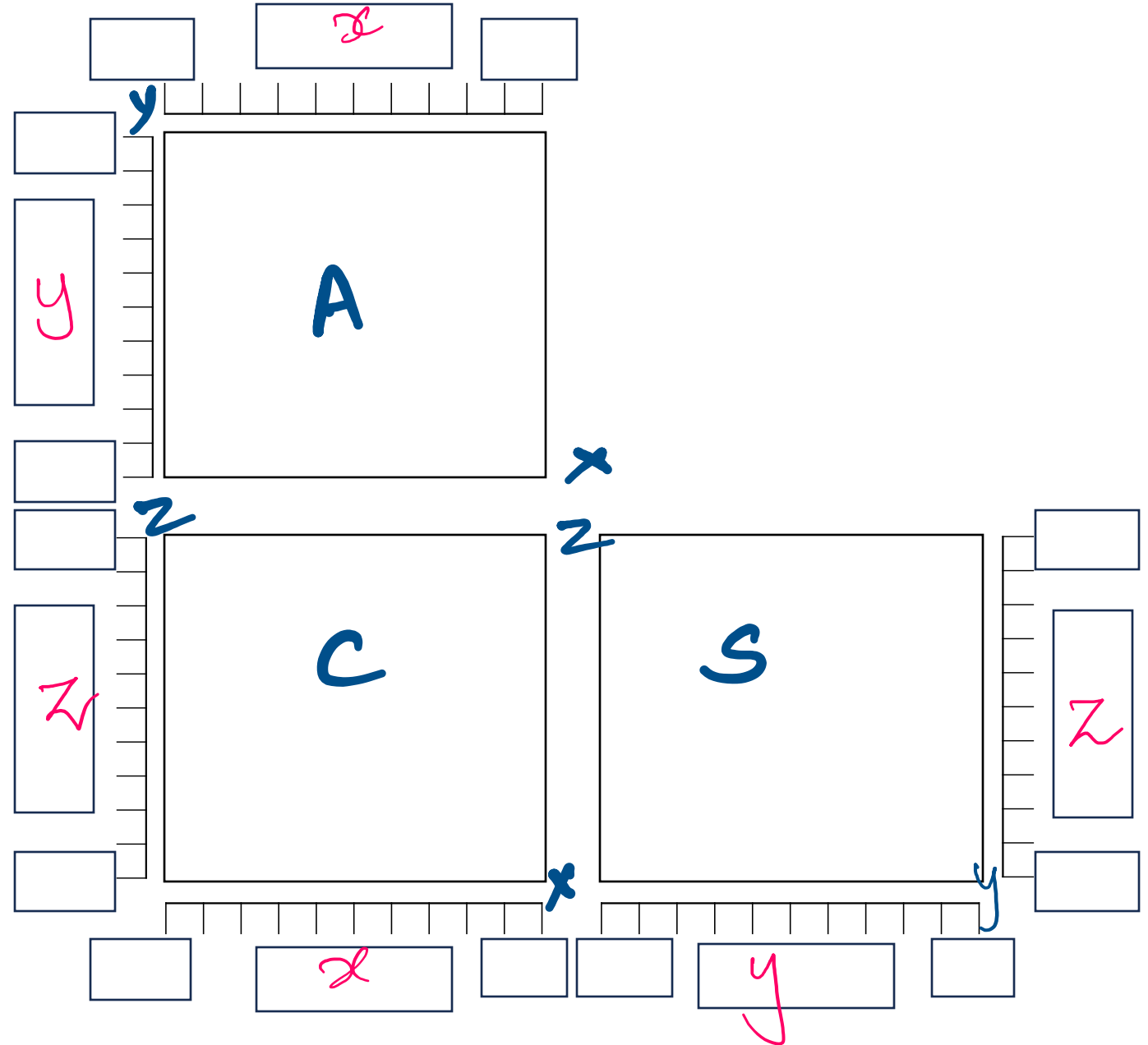
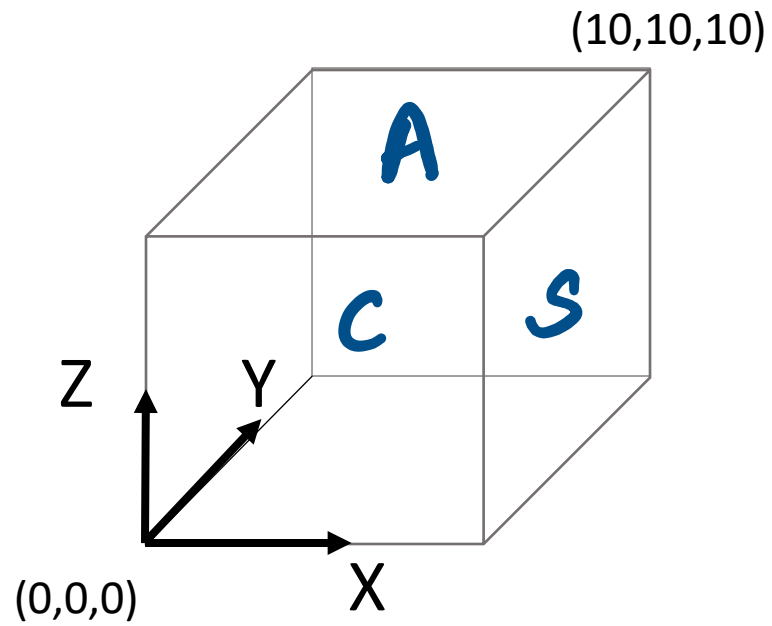
C: Coronal

S: Sagittal

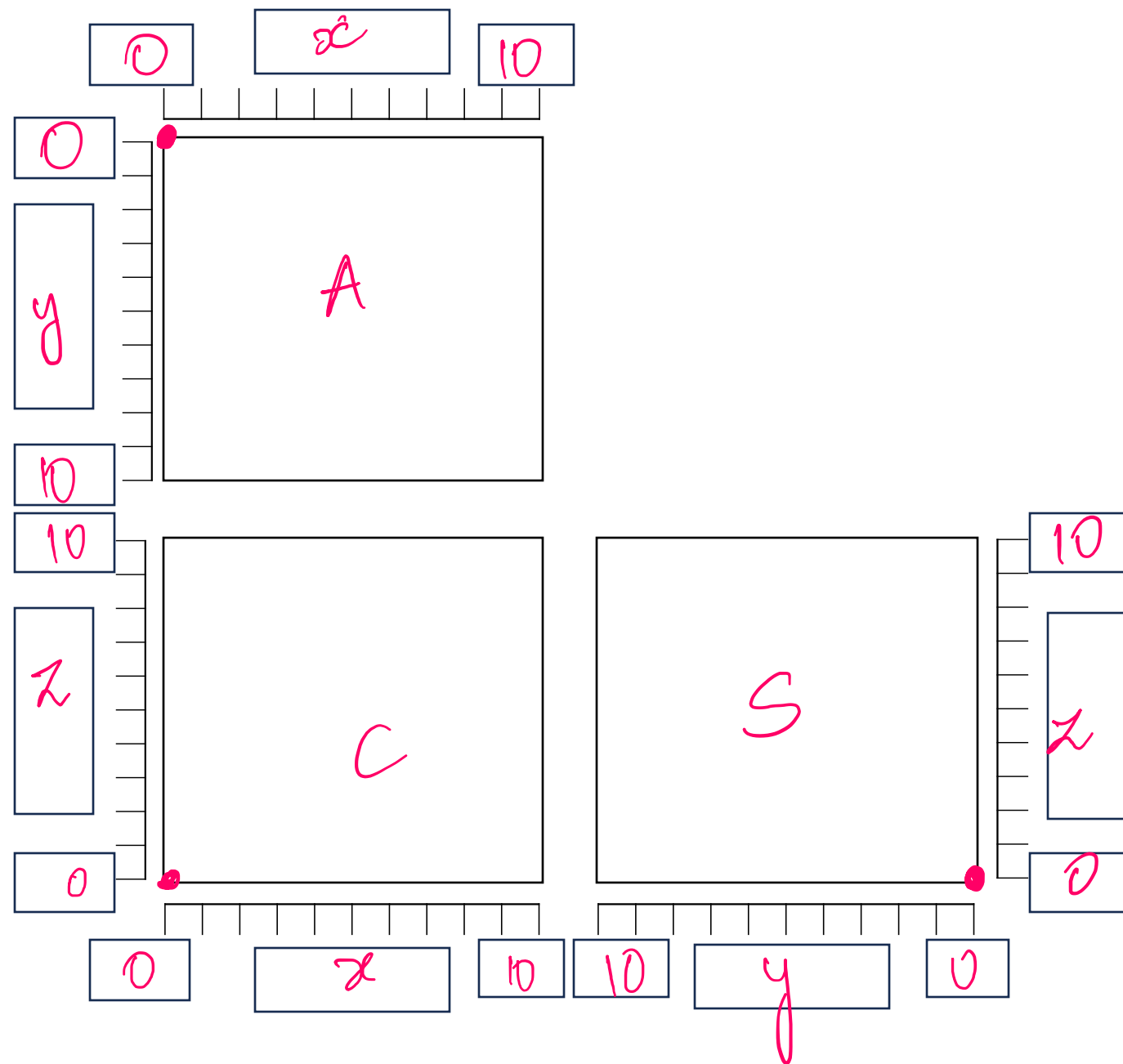
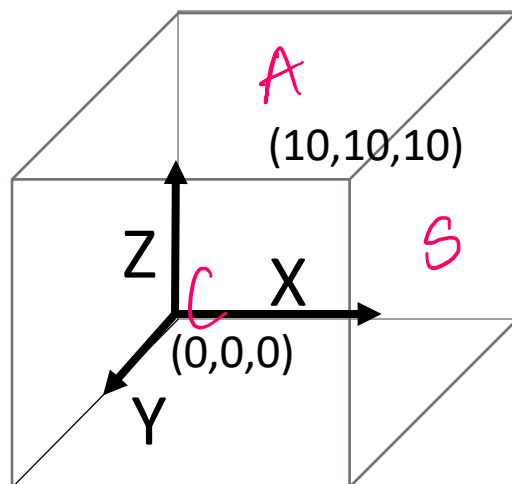
A: Axial



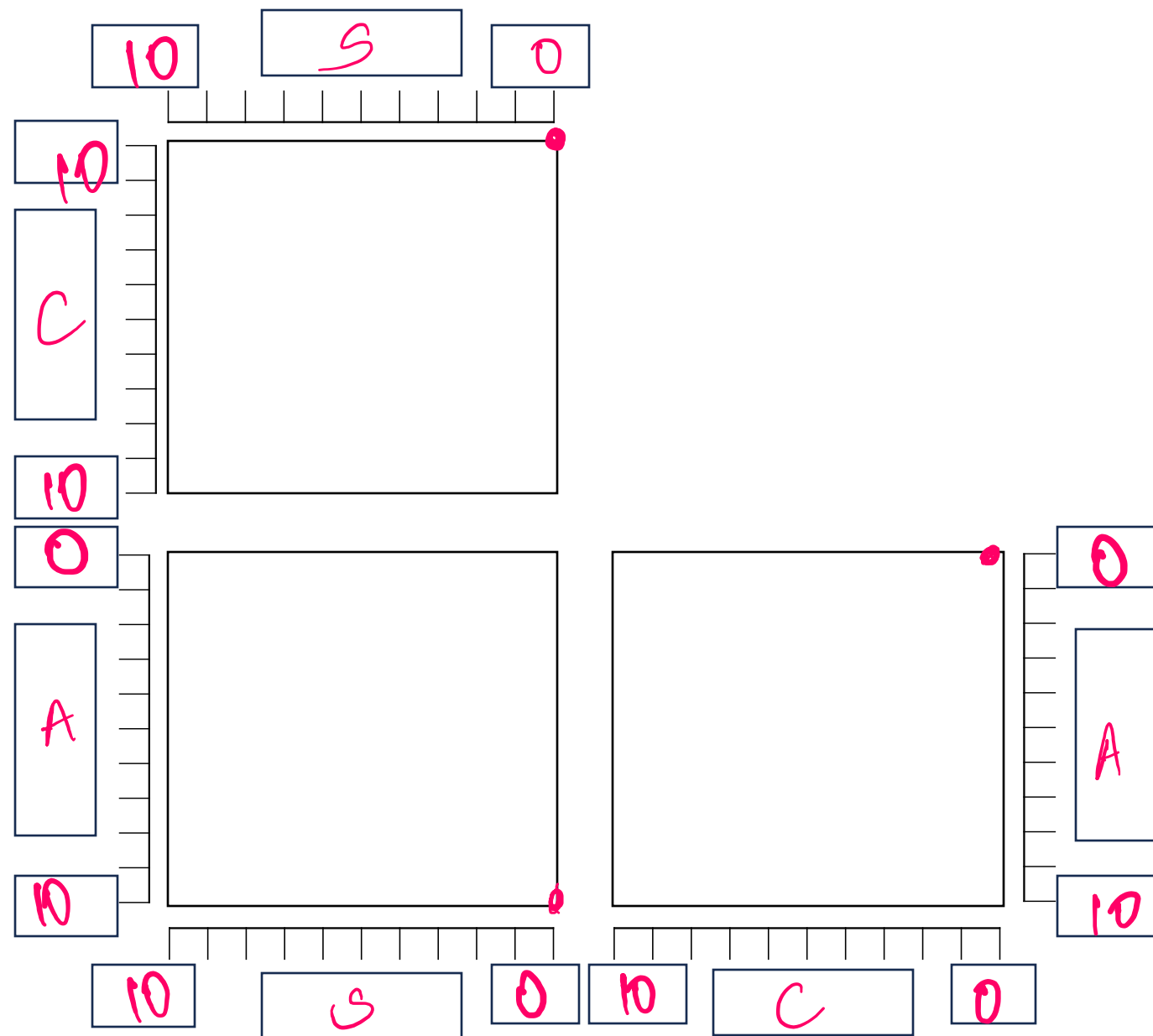
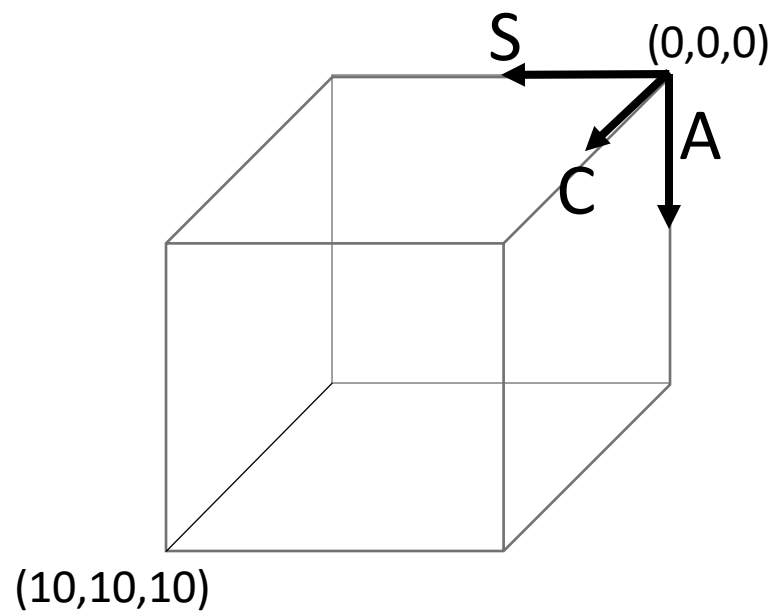
Map the axes



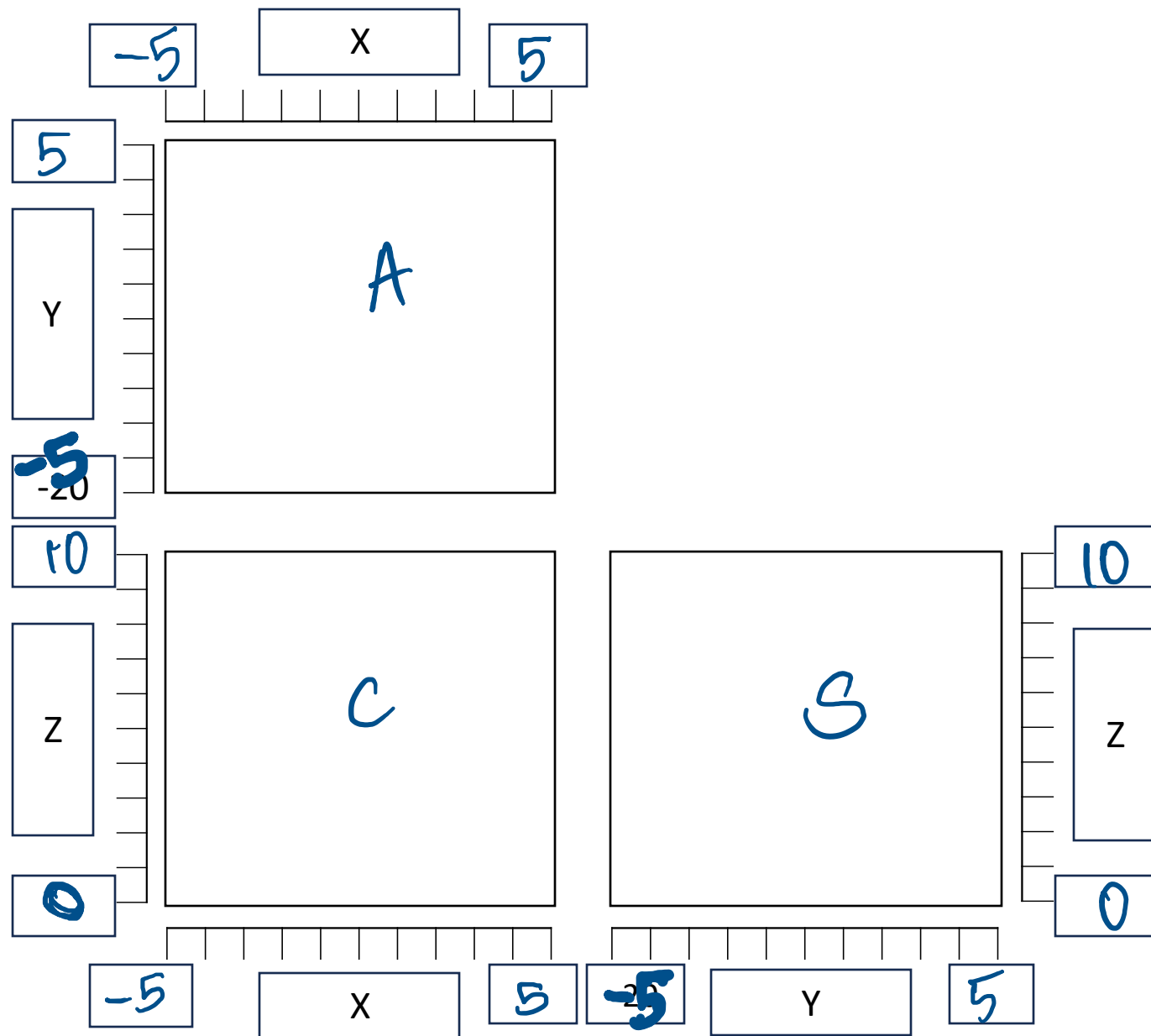
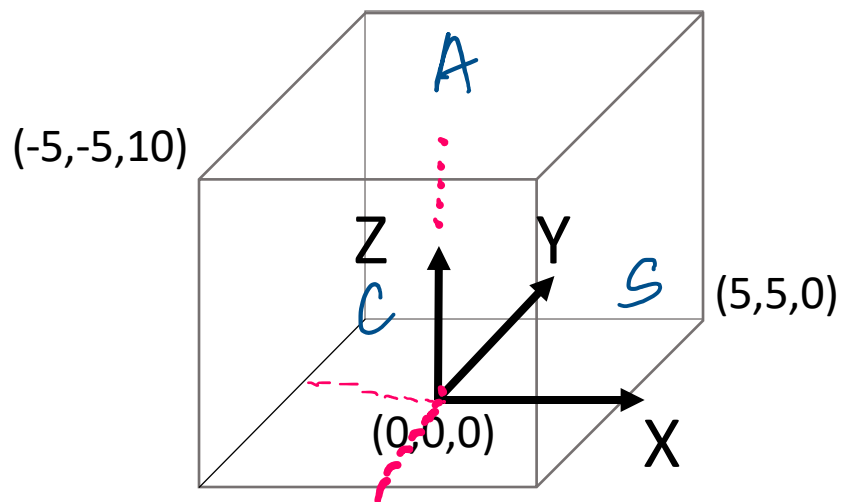
Map the axes



Map the axes

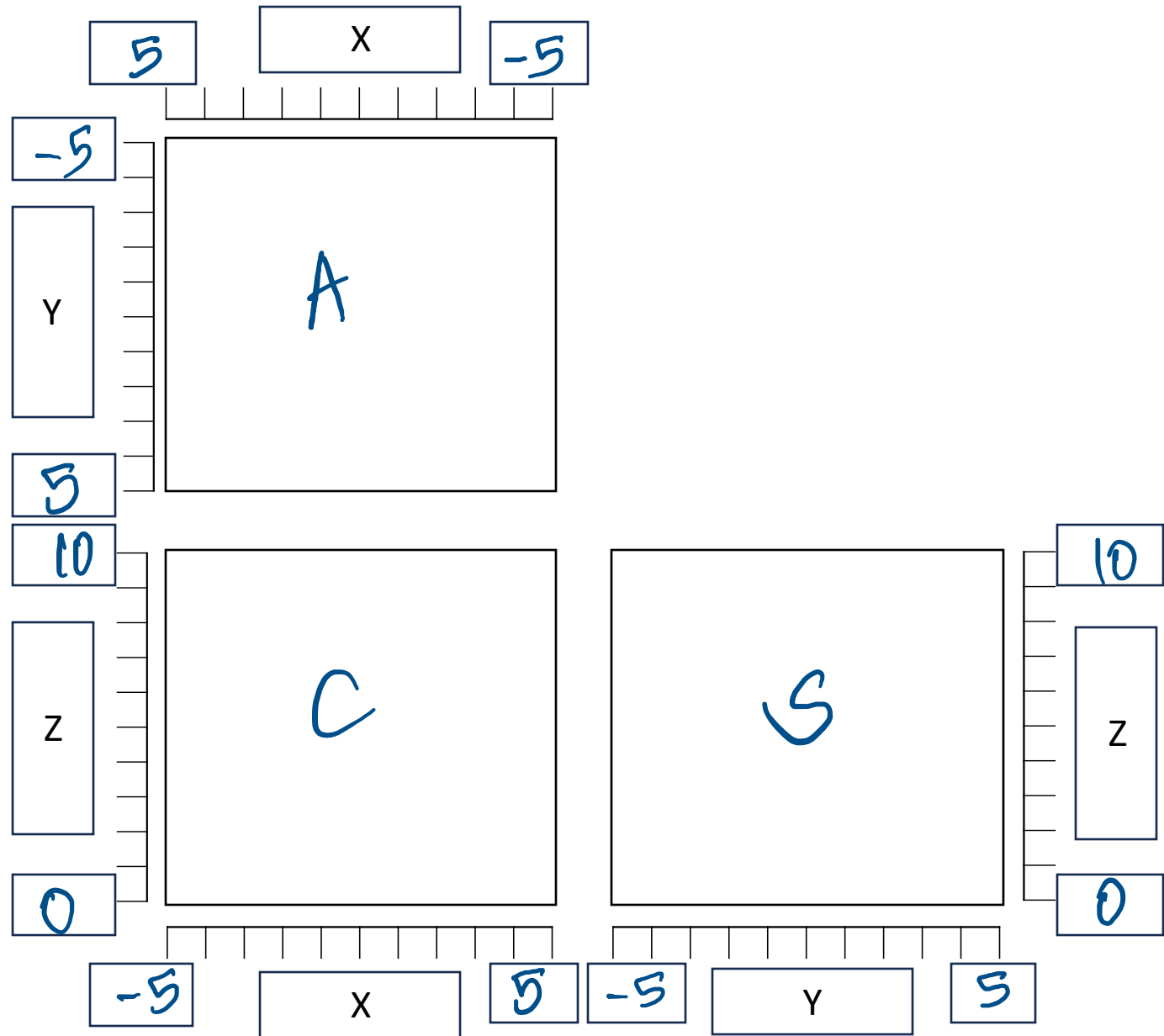
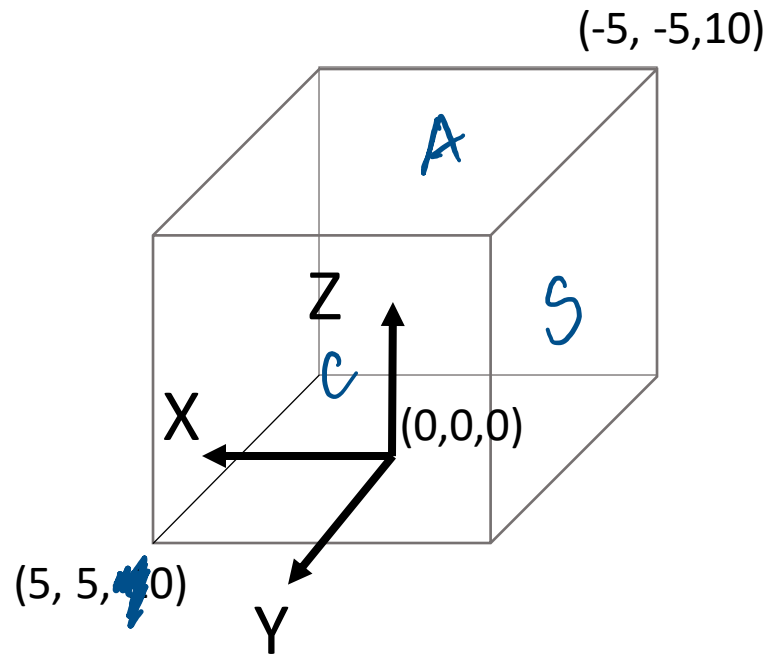


☒ ☐ Map the axes

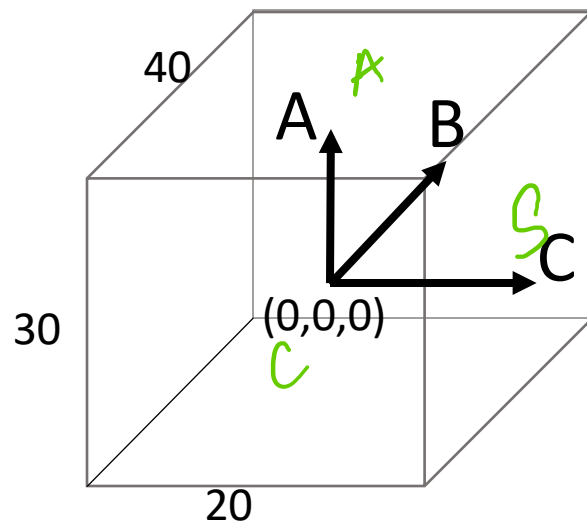




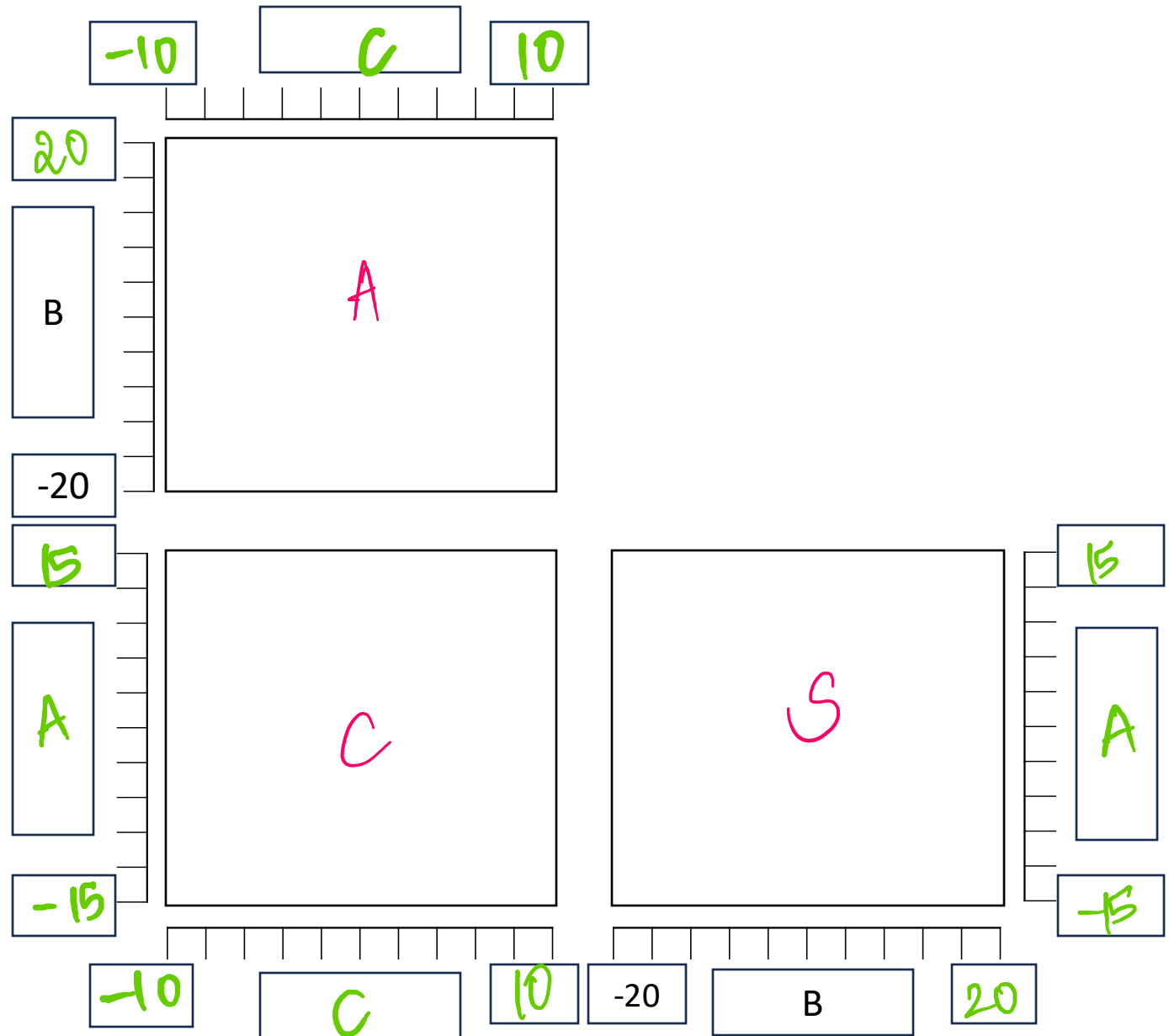
Map the axes



Map the axes

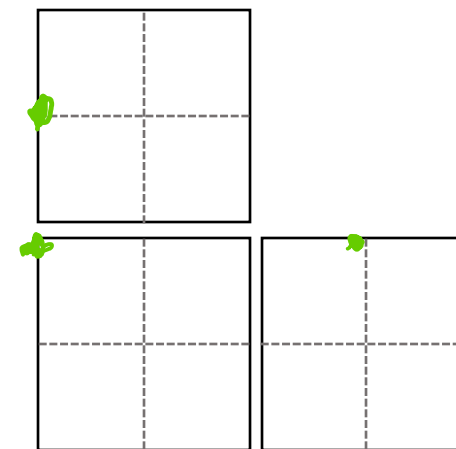
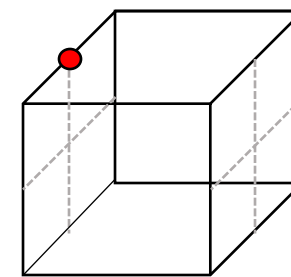
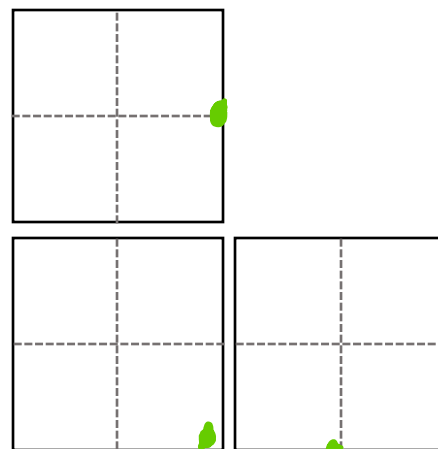
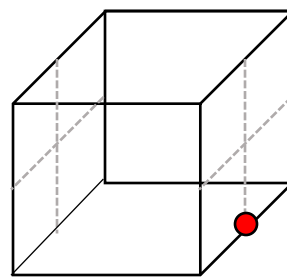
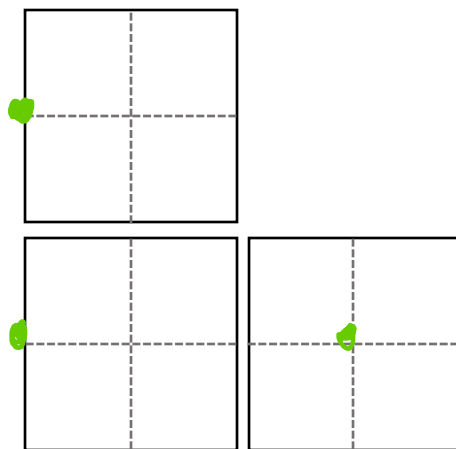
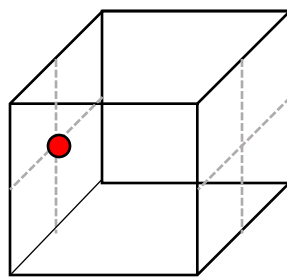
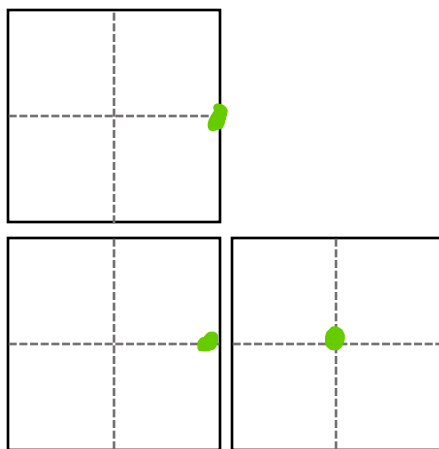
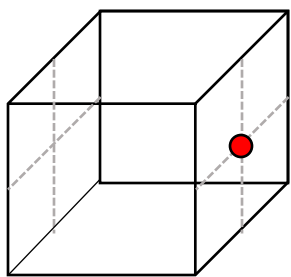


The origin $(0,0,0)$ is in the center of the box. The numbers are the side lengths.

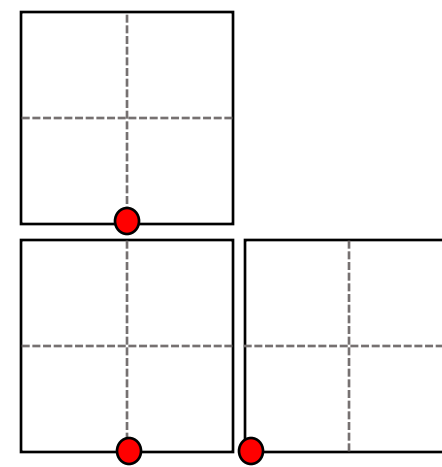
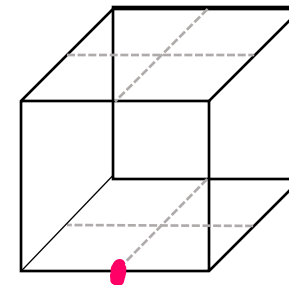
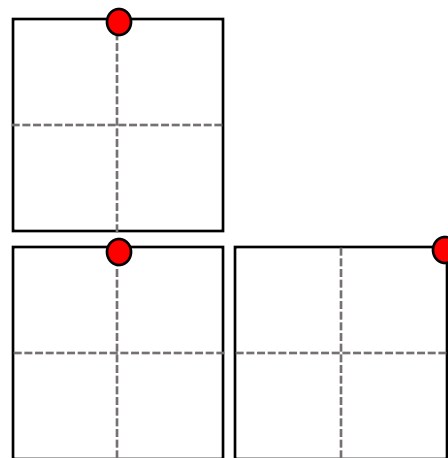
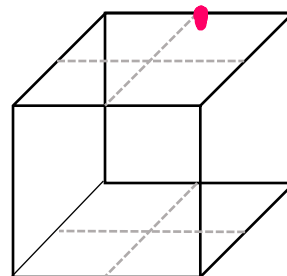
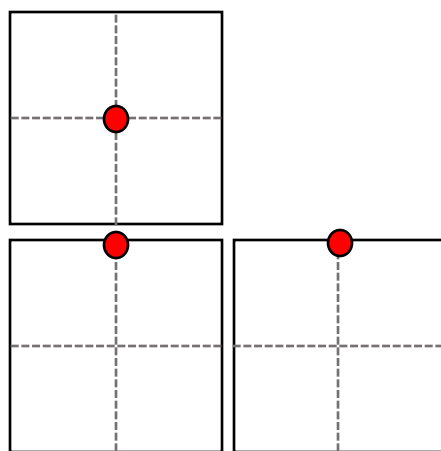
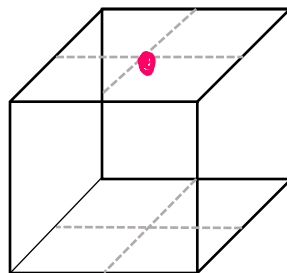
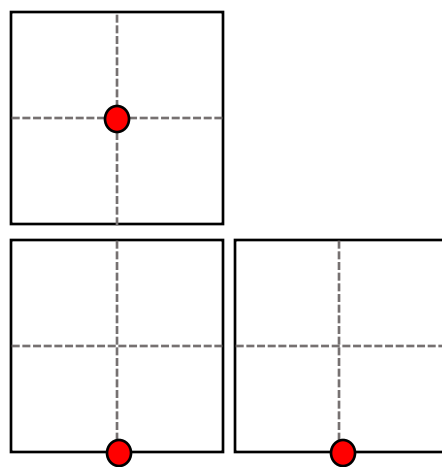
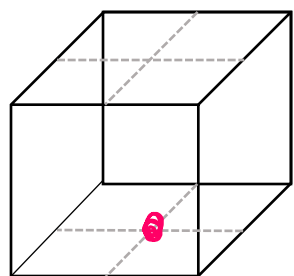


3D Points: Box \rightarrow Multiview

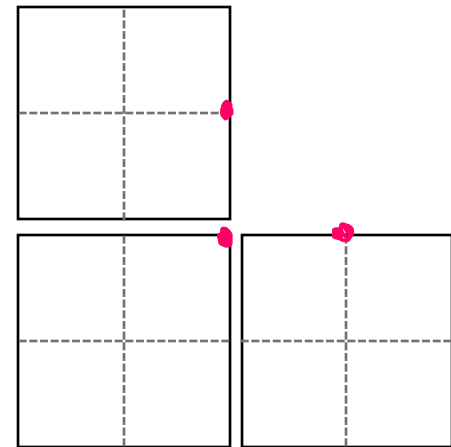
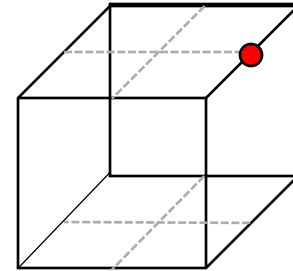
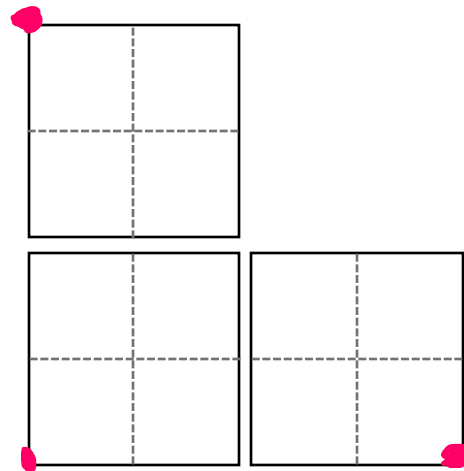
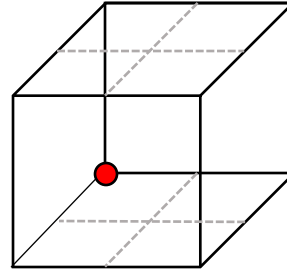
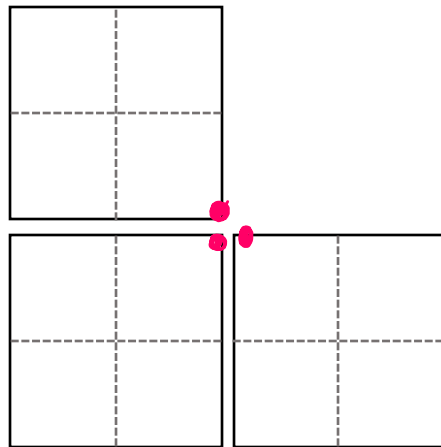
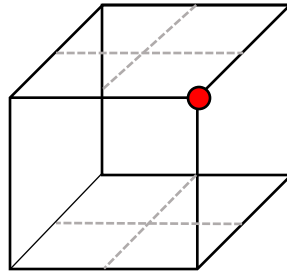
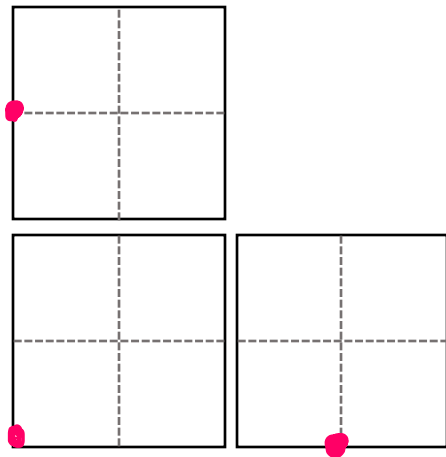
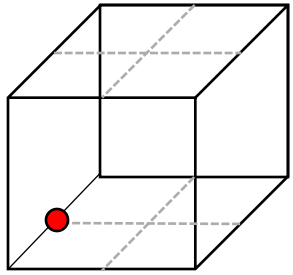
A C S



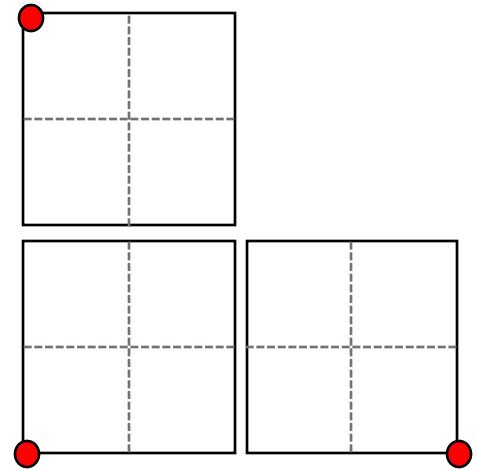
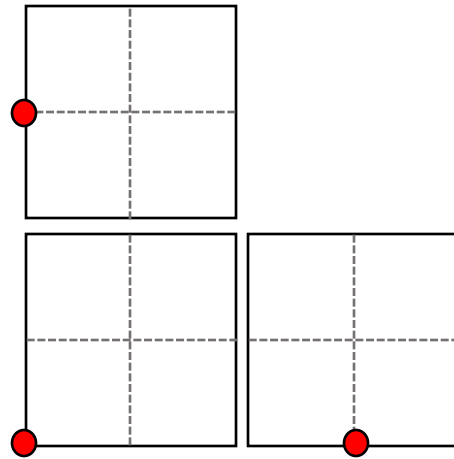
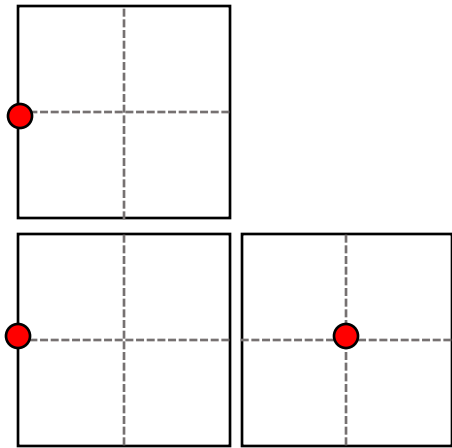
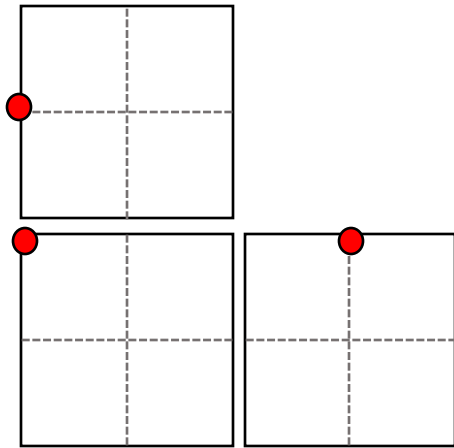
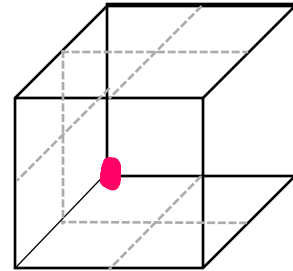
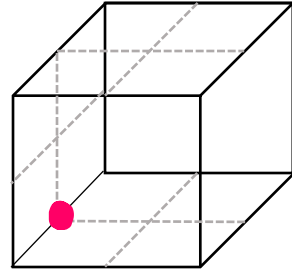
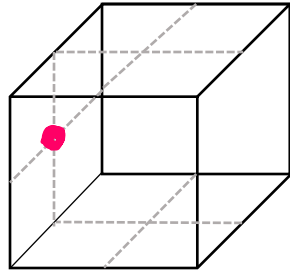
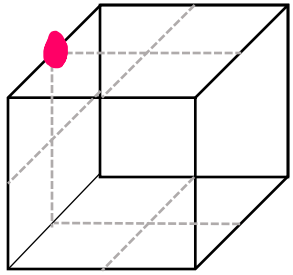
3D Points: Multiview \rightarrow Box



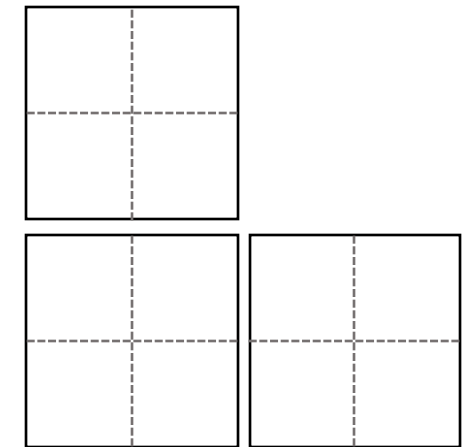
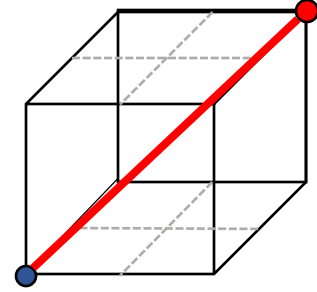
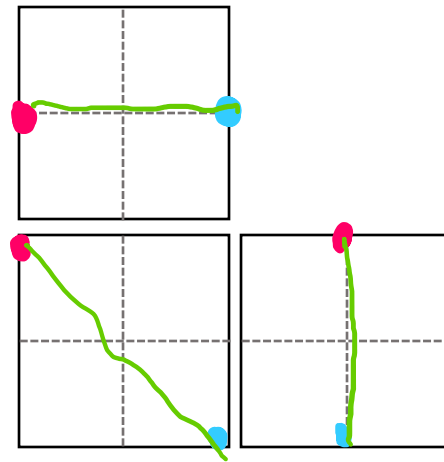
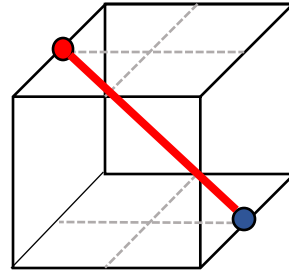
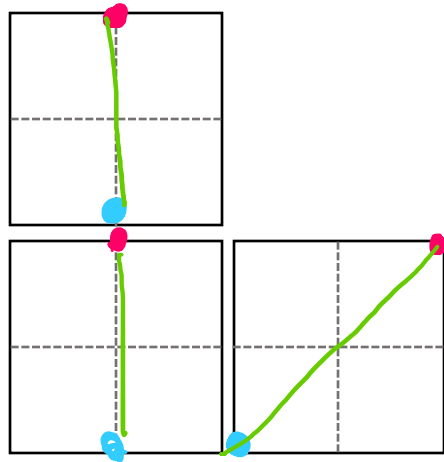
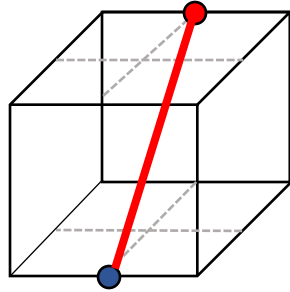
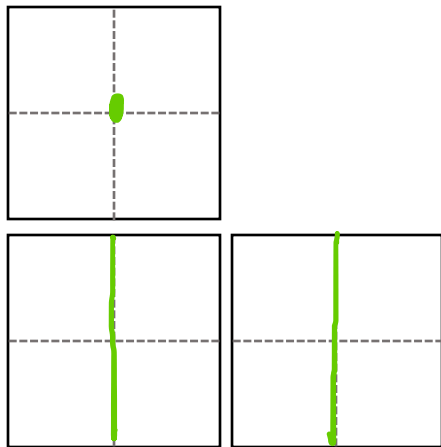
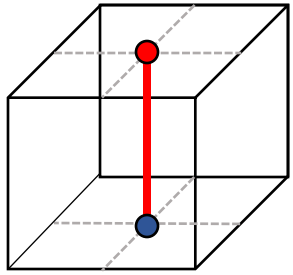
✓ 3D Points: Box → Multiview



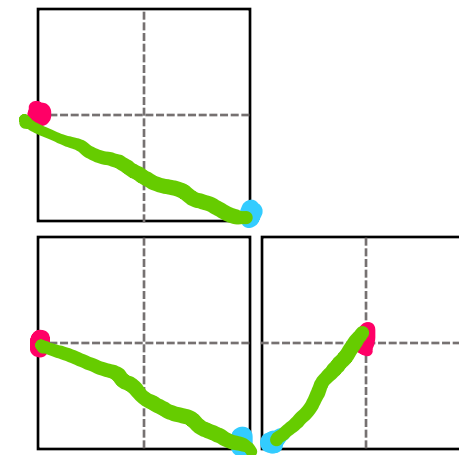
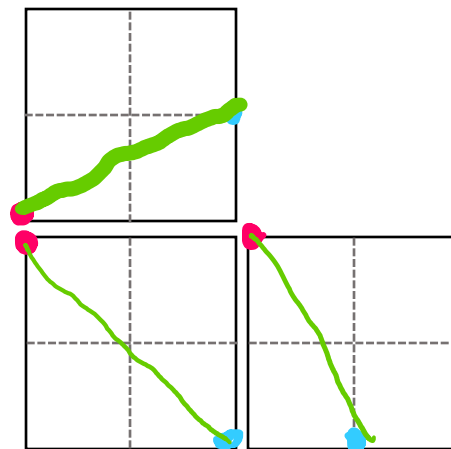
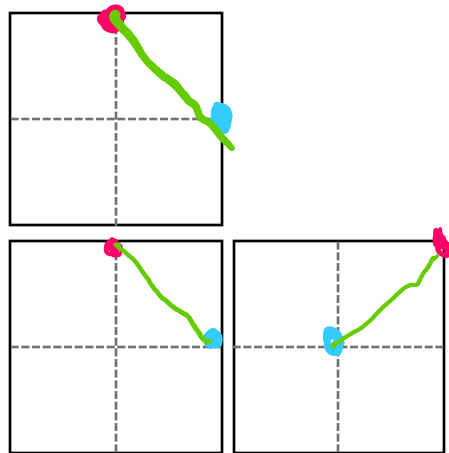
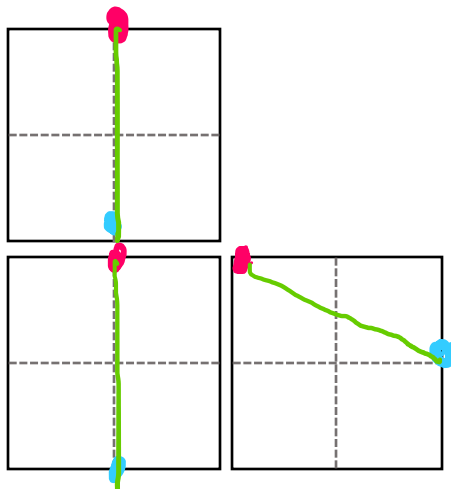
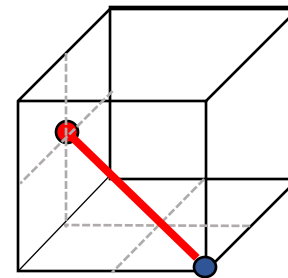
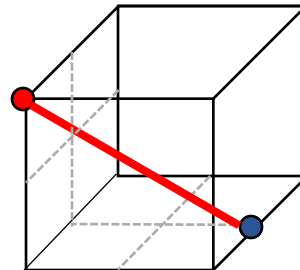
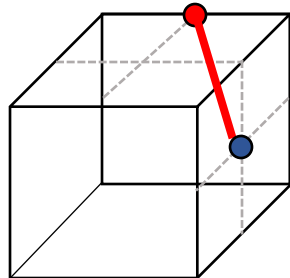
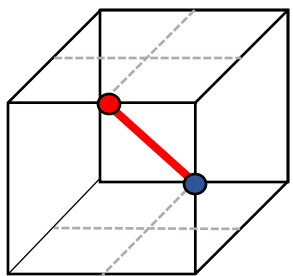
☒ ☐ 3D Points: Multiview \rightarrow Box



3D Lines

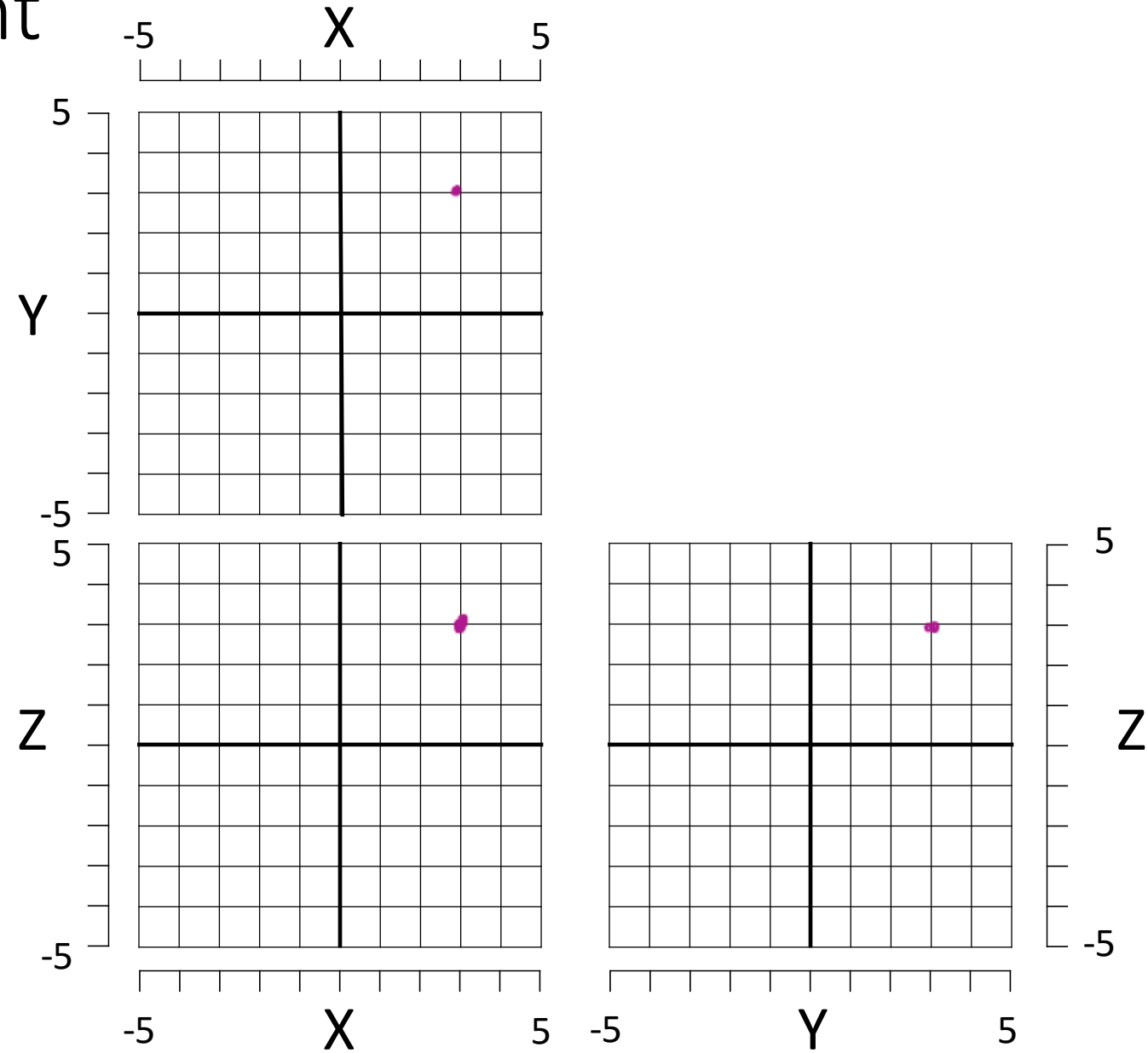


☒ ☐ Draw 3D lines



Draw a point

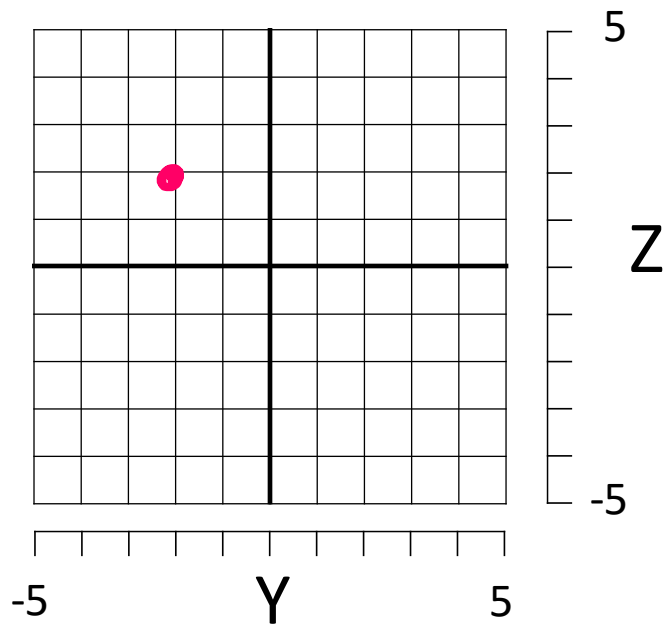
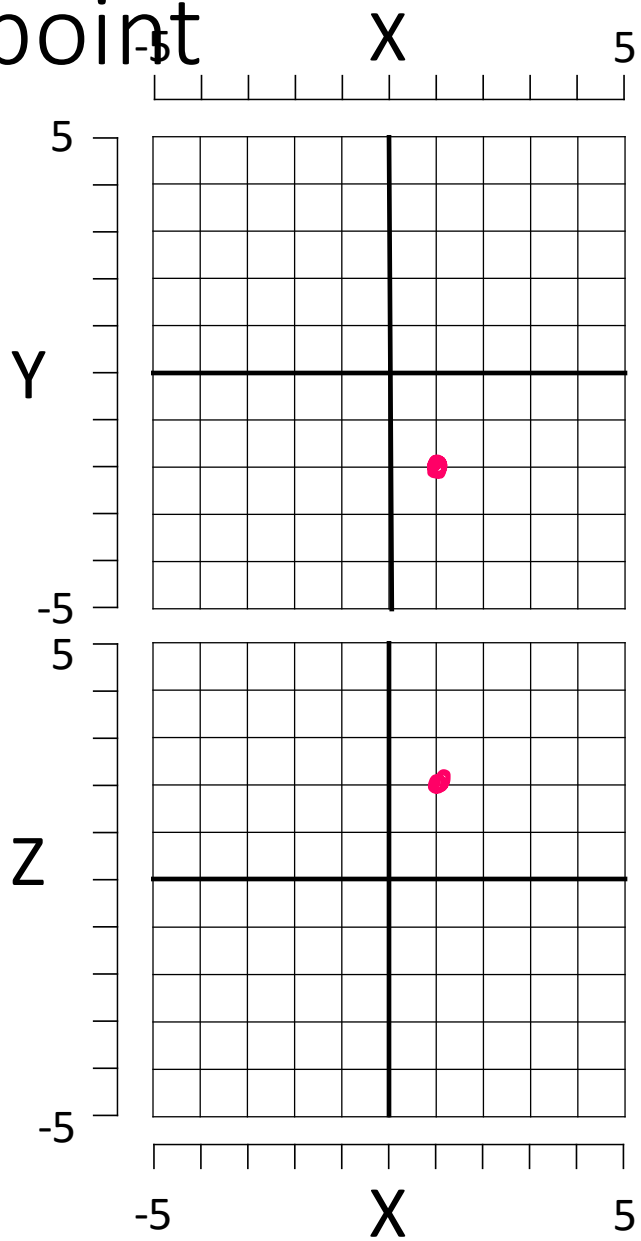
$(3, 3, 3)$





Draw a point

$(1, -2, 2)$

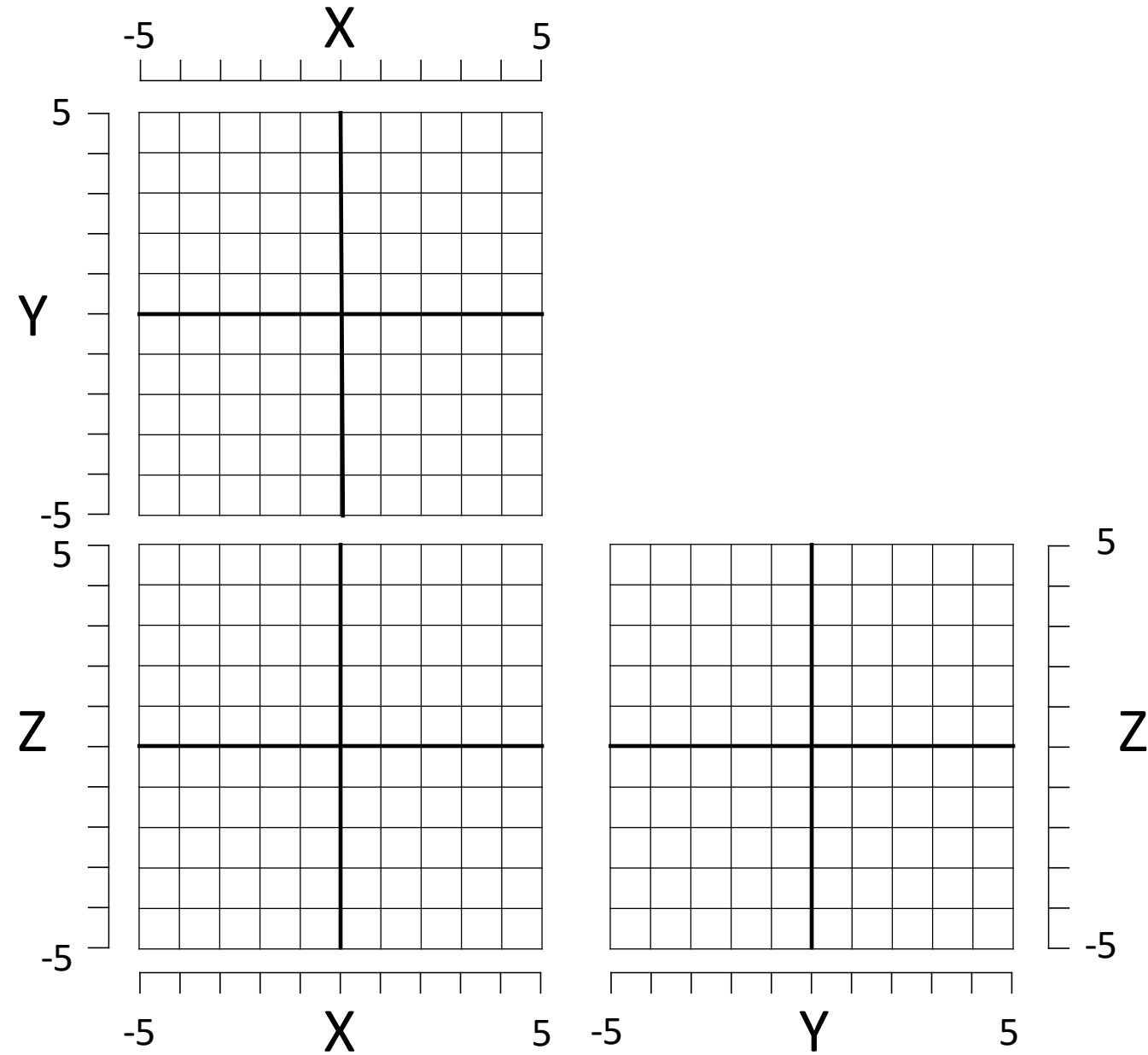


Draw a line

$(0, 1, -1)$

\rightarrow

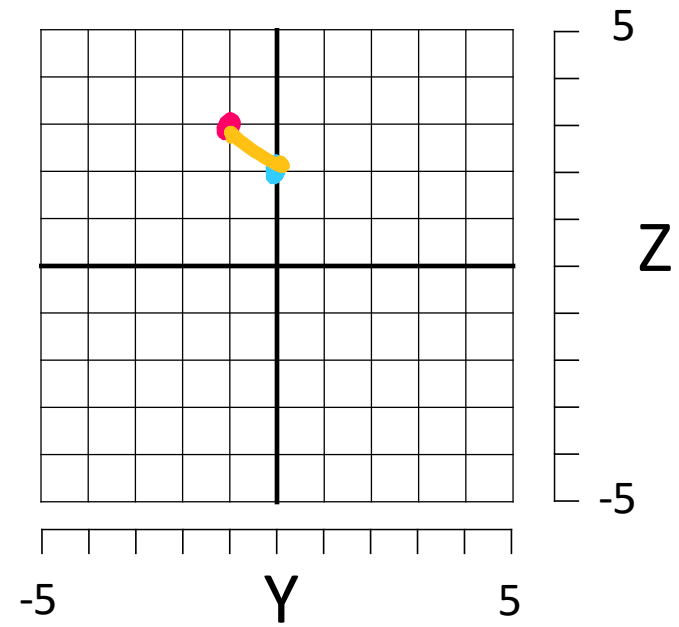
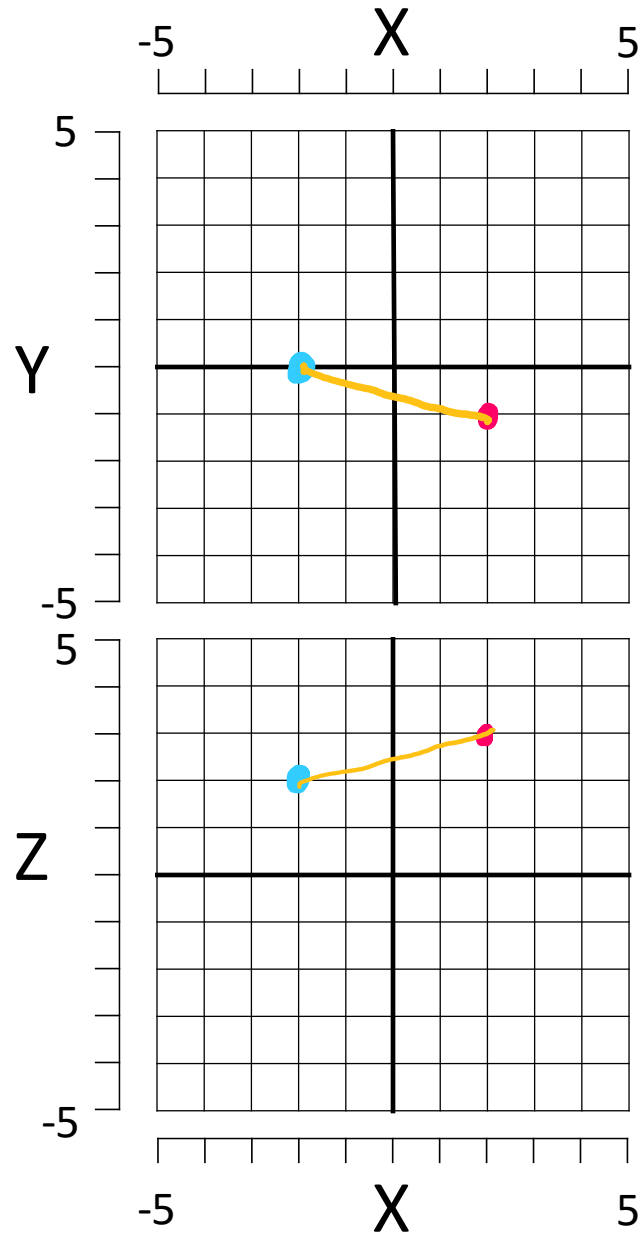
$(3, -2, 1)$



☒ ☐ Draw a line

$(2, -1, 3)$

$(-2, 0, 2)$



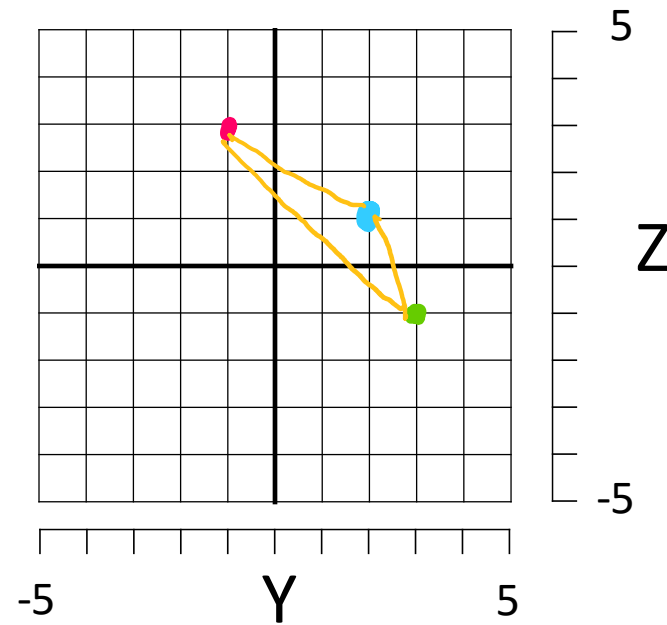
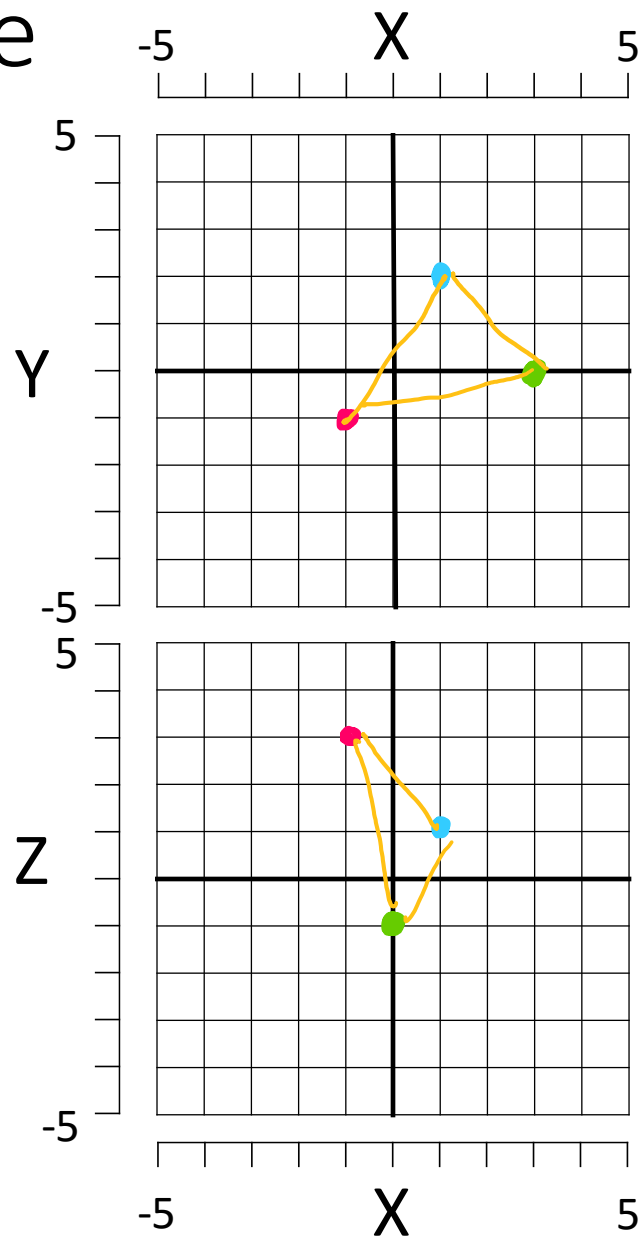


Draw a triangle

$(-1, -1, 3)$ ✖

$(1, 2, 1)$ ✖

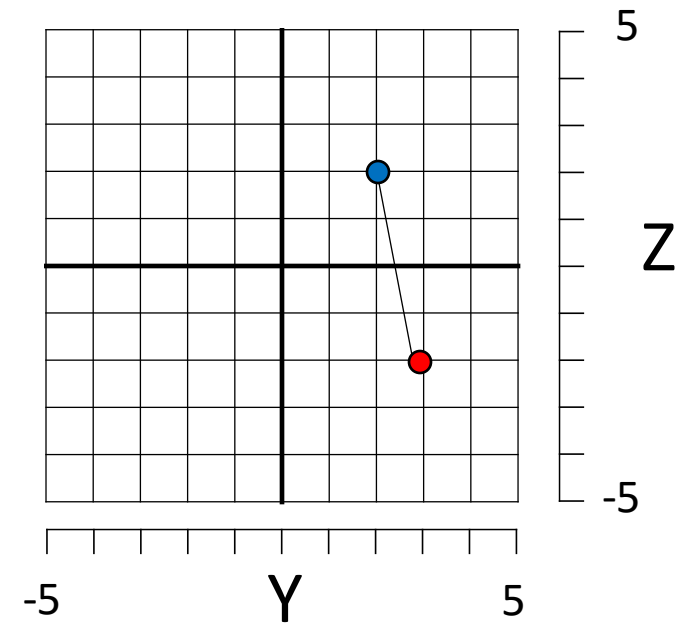
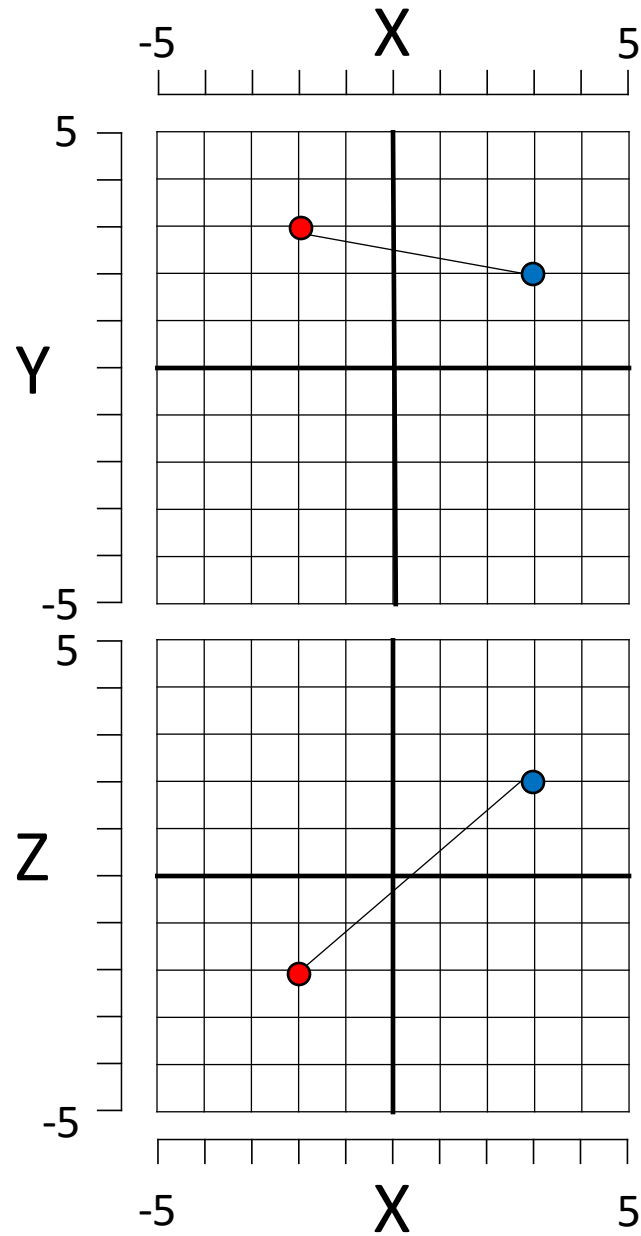
$(0, 3, -1)$ ✖



Read a line

● (__, __, __)

● (__, __, __)

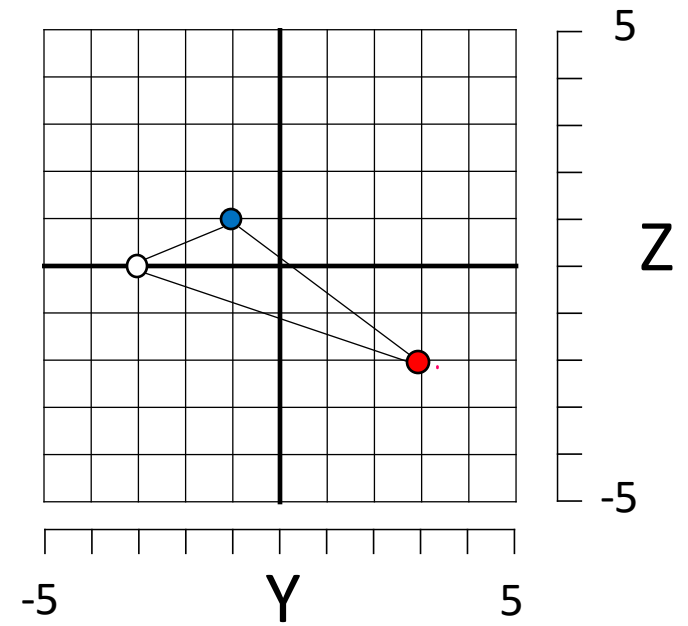
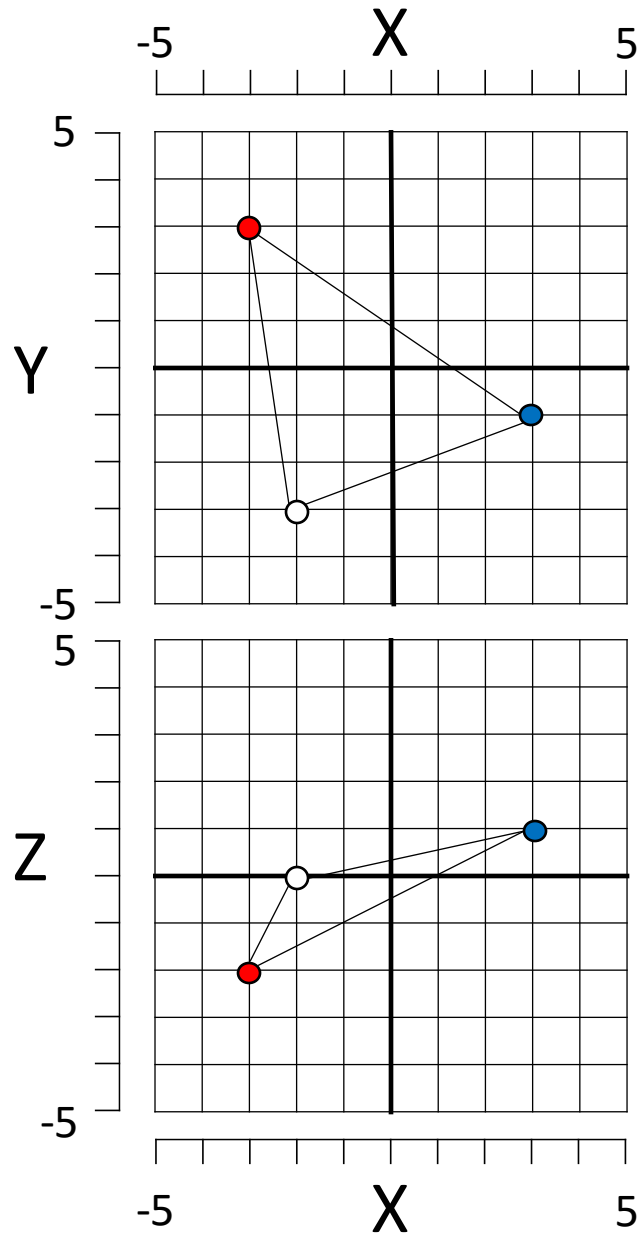


☒ ☐ Read a triangle

● (-3, 3, -2)

● (3, -1, 1)

○ (-2, -3, 0)



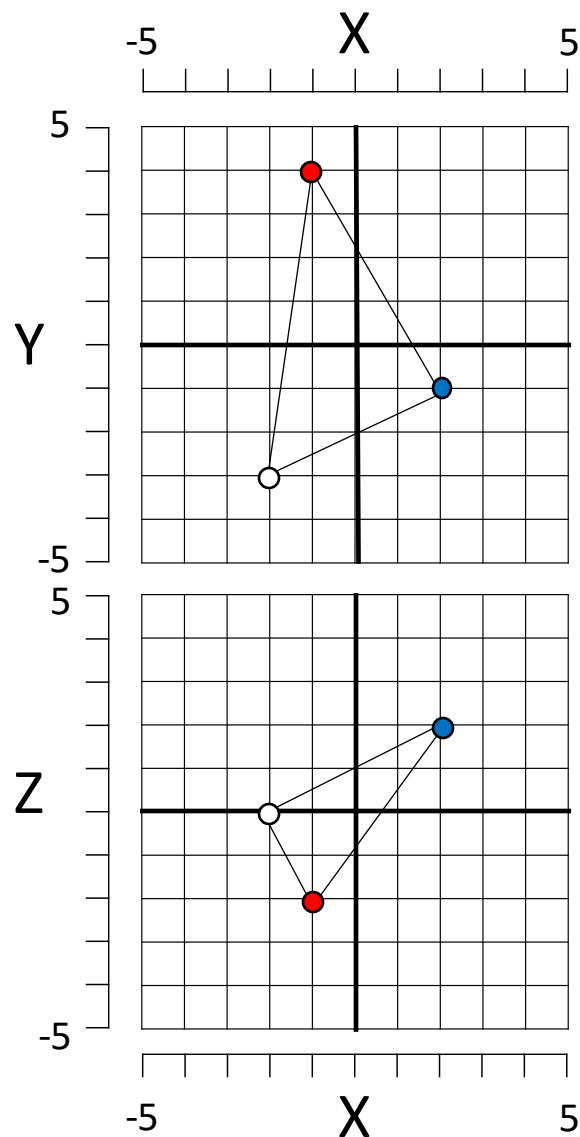


Infer the 3rd view

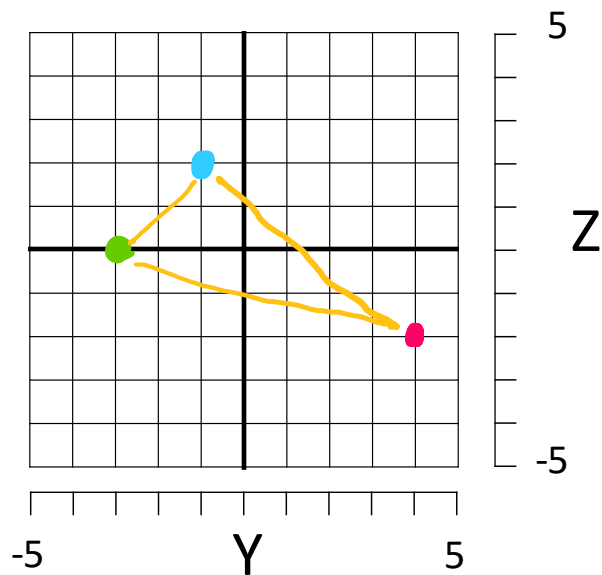
Red $\rightarrow (-1, 4, -2)$

Blue $\rightarrow (2, -1, 2)$

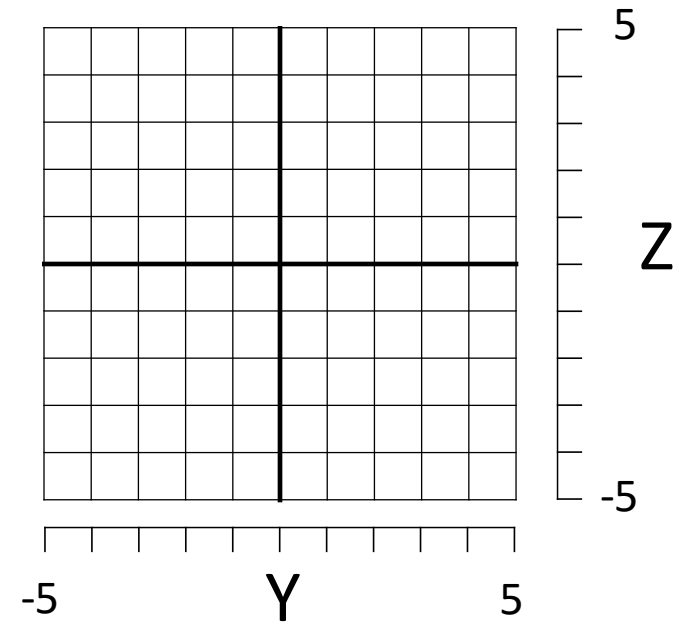
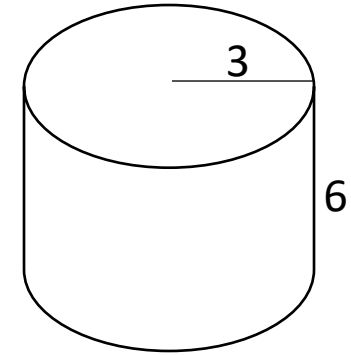
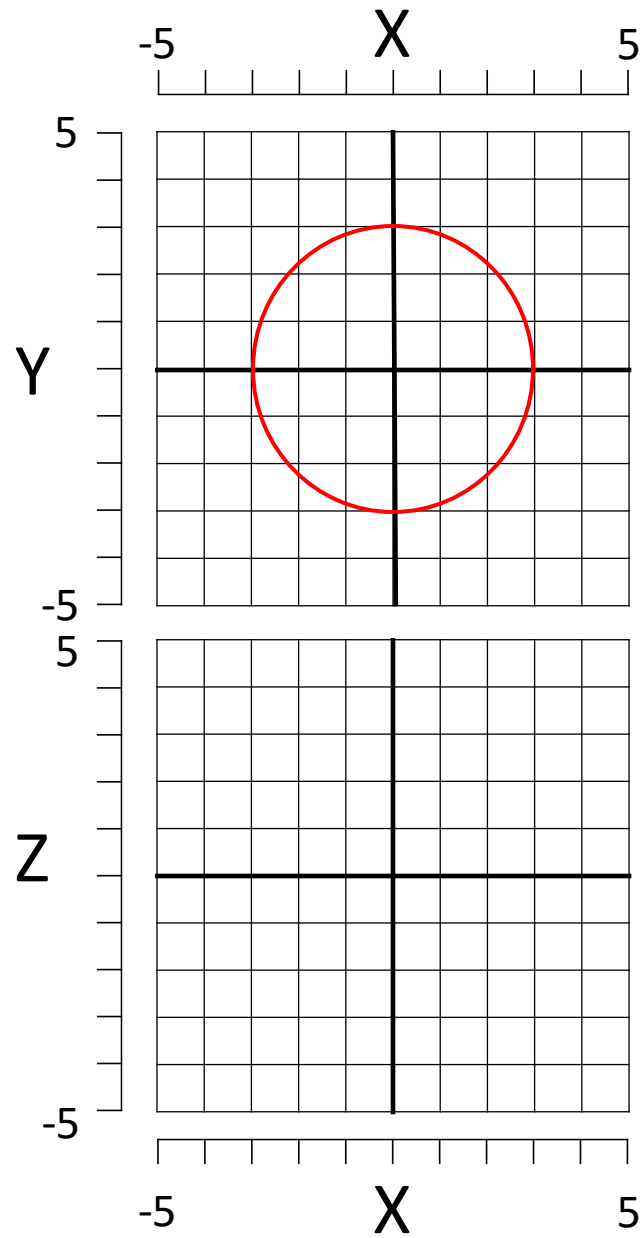
White $\rightarrow (-2, -3, 0)$



Draw what the triangle should look like from the Y-Z view.

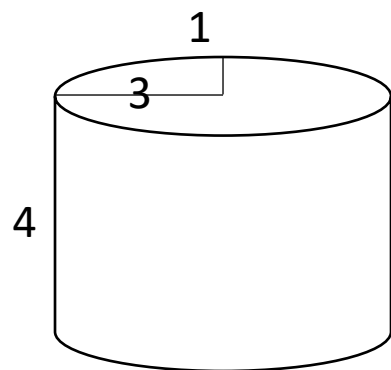


Draw a cylinder

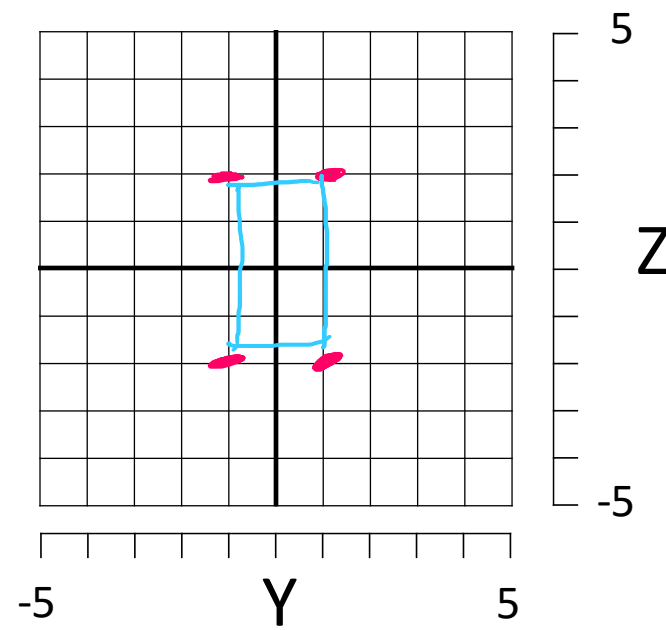
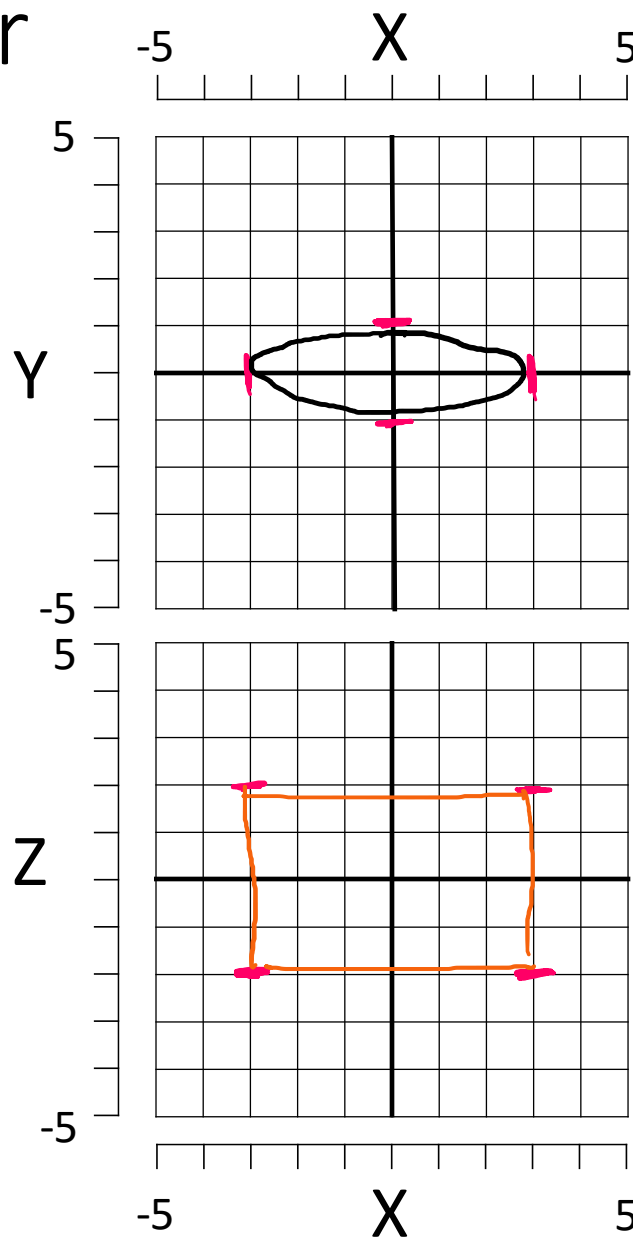




Draw a cylinder

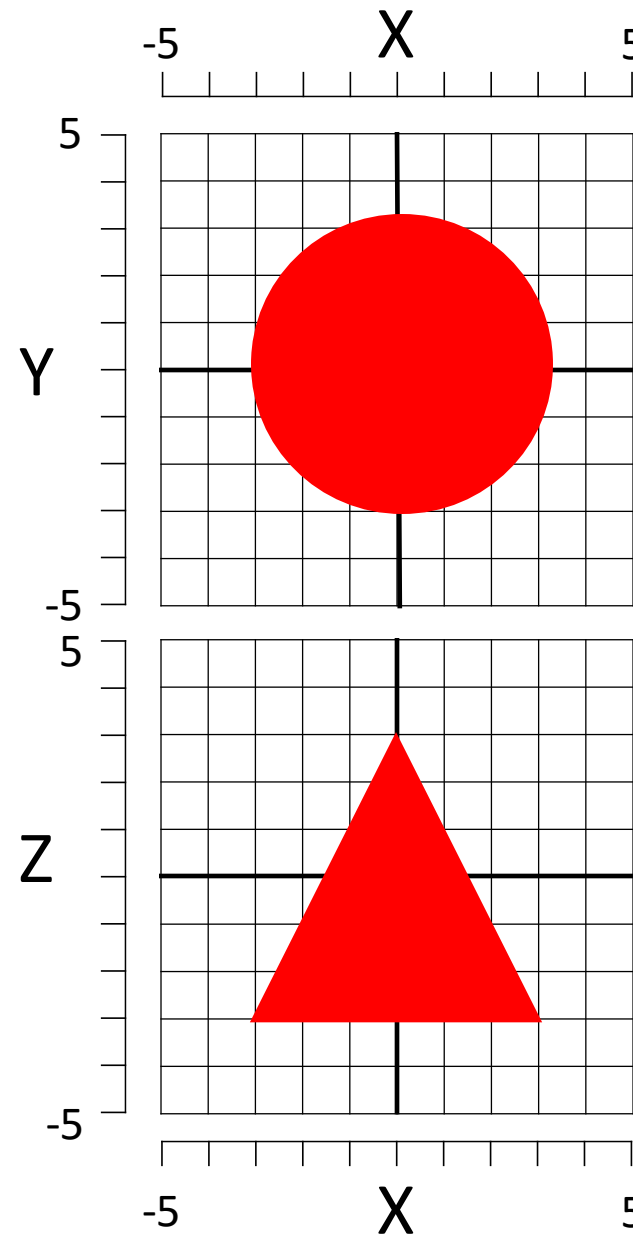


This oval-shaped cylinder is centered at $(0,0,0)$. The short side is parallel to the Y-axis. The long side is parallel to the X-axis.

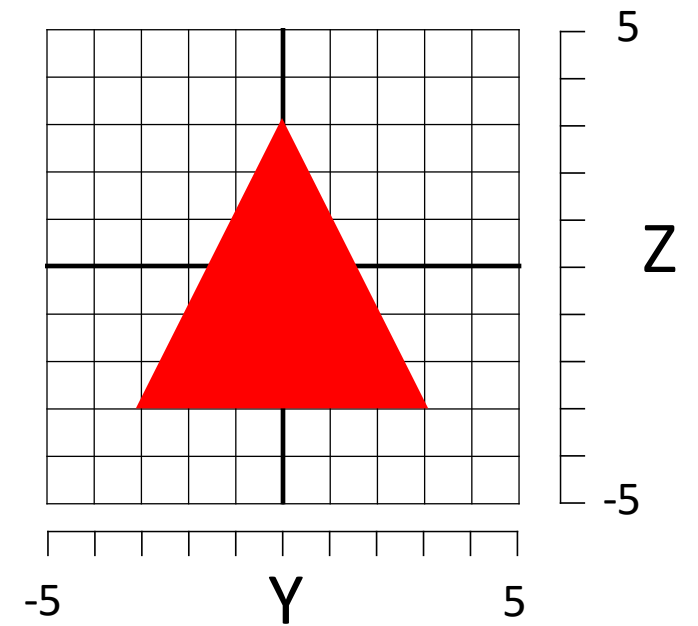


Identify the solid

It is a _____.



Draw here



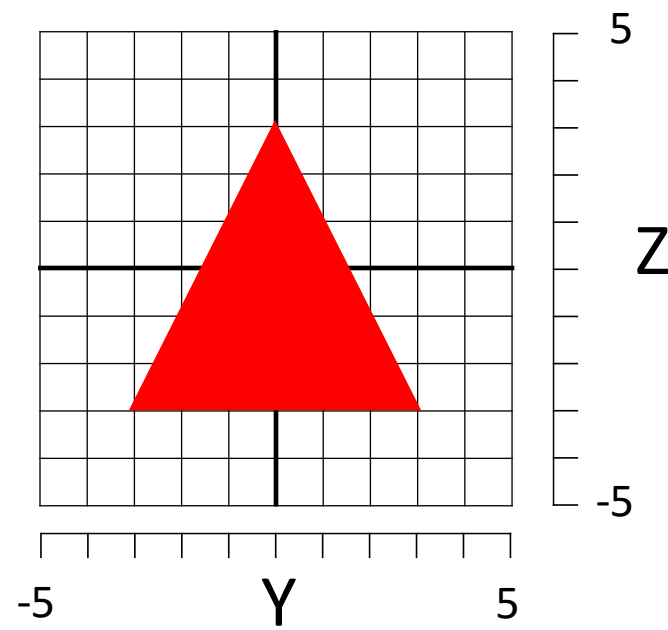
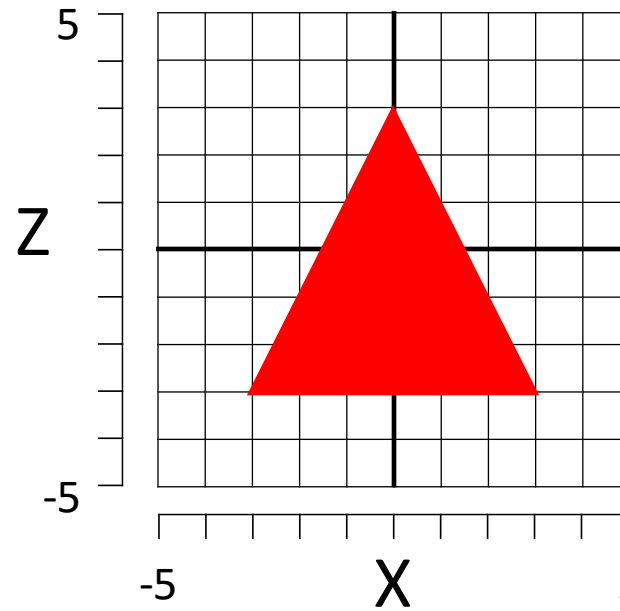
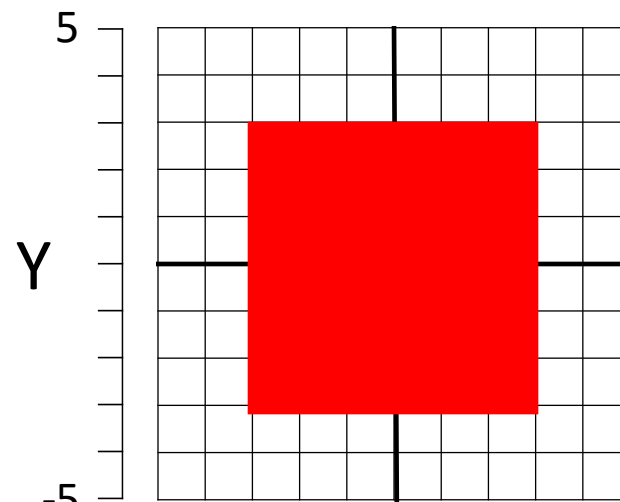


Identify the solid

It is a PYRAMID.

X

Draw here



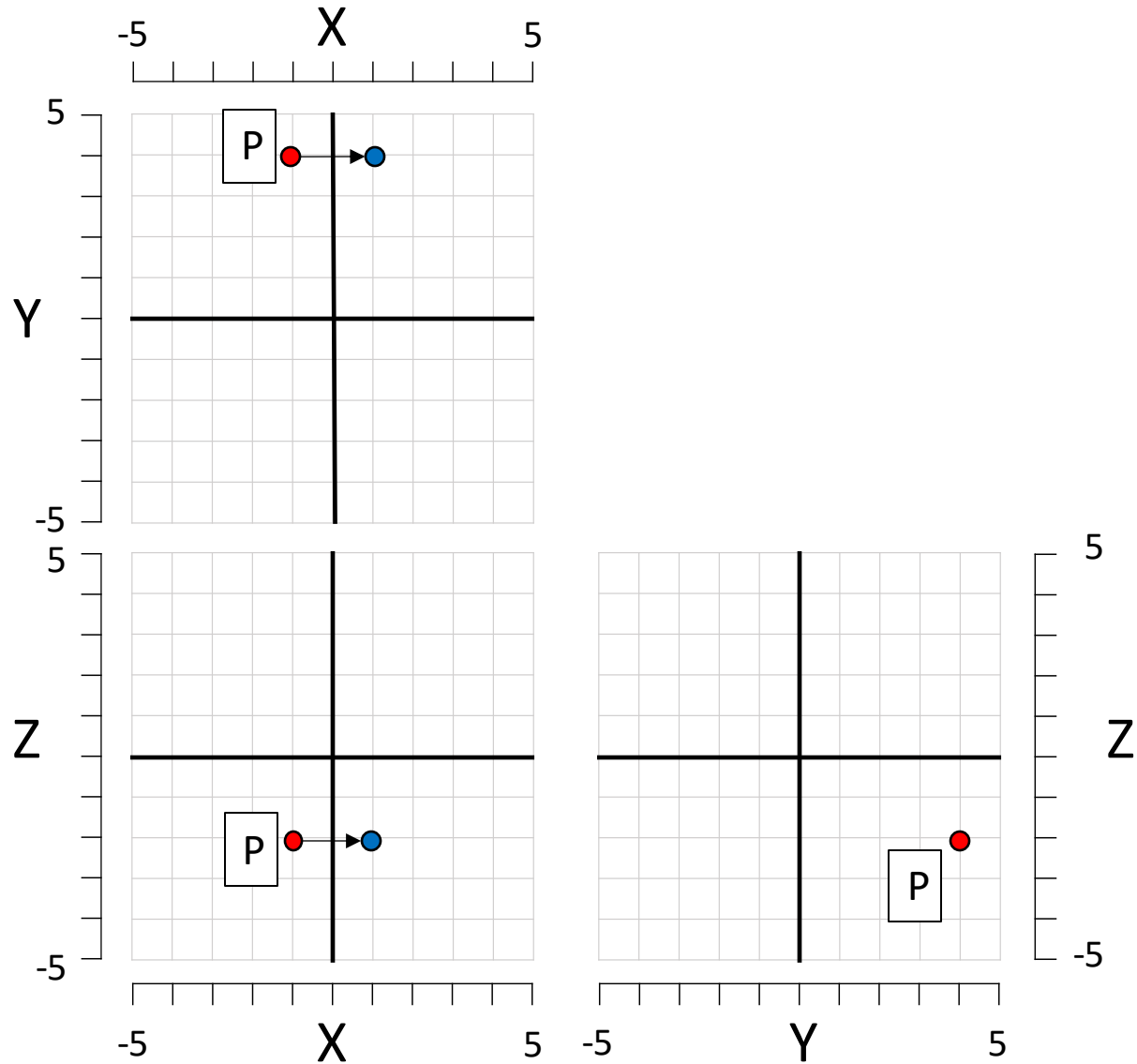
3D Translation

CSCI 5722 Computer Vision



University of Colorado
Boulder

Translate in 3D by matrix multiplication

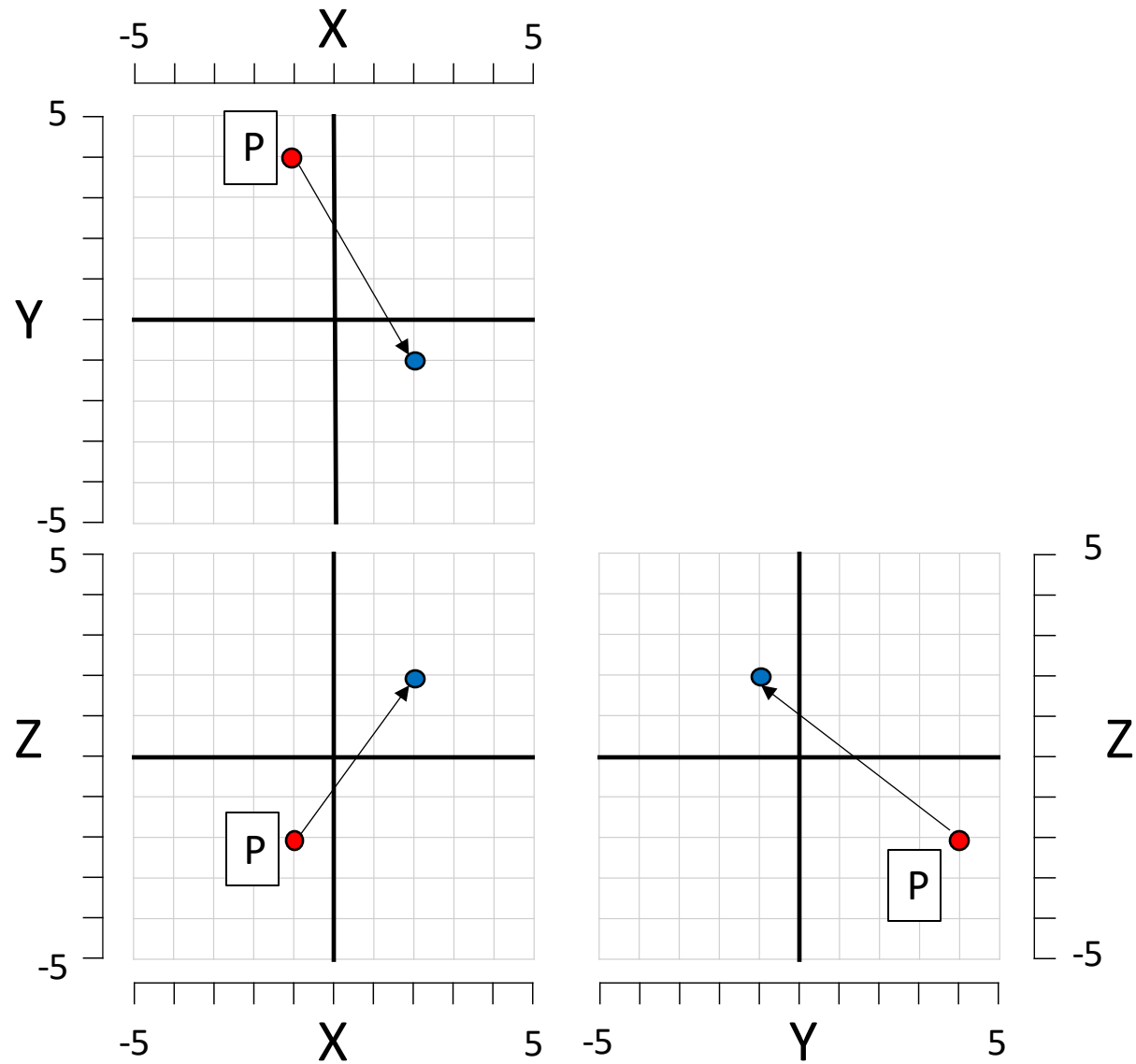


$$\Delta = (2, 0, 0)$$

P

T					T * P

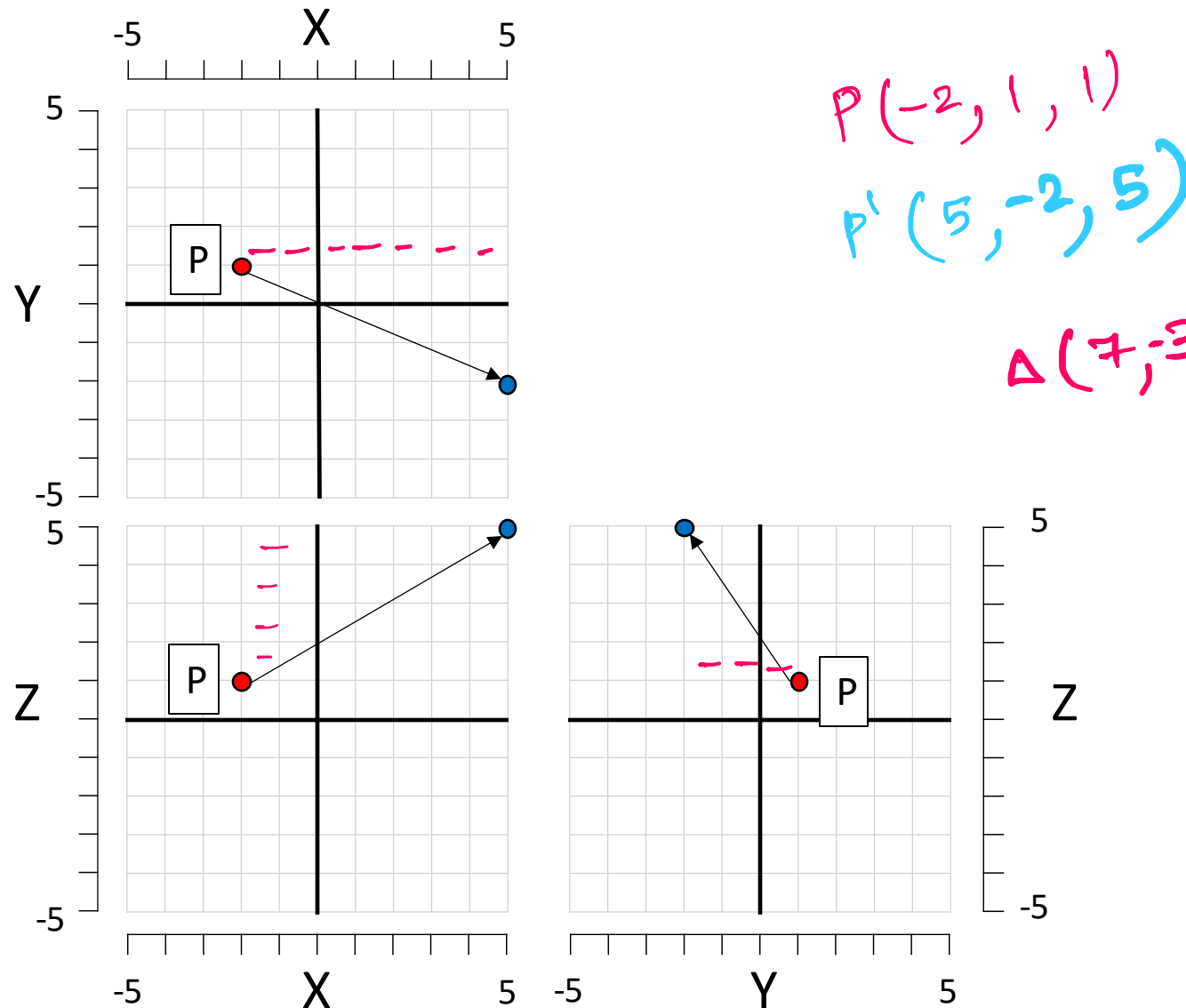
Translate in 3D by matrix multiplication



	P			

T	T * P			

✓ Translate in 3D by matrix multiplication



$$P(-2, 1, 1)$$
$$P'(5, -2, 5)$$

$$\Delta(7, -3, 4)$$

$$P = \begin{bmatrix} -2 \\ 1 \\ 1 \end{bmatrix}$$

$$T = \begin{bmatrix} 1 & 0 & 0 & 7 \\ 0 & 1 & 0 & -3 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
$$T * P = \begin{bmatrix} 5 \\ -2 \\ 5 \\ 1 \end{bmatrix}$$