



ZONE-4 :  $(x_1 < x_0)$  &  $(y_1 \leq y_0)$

Therefore,

$$R(P) = F(x_p, y_p) = Ax_p + By_p + c$$

$$F(M) = F(x_{p-1}, y_{p-1/2}) = A(x_{p-1}) + B(y_{p-1/2}) + c$$

$$F(M_w) = F(x_{p-2}, y_{p-1/2}) = A(x_{p-2}) + B(y_{p-1/2}) + c$$

$$F(M_{sw}) = F(x_{p-2}, y_{p-1-1/2}) = A(x_{p-2}) + B(y_{p-1-1/2}) + c$$

Now, Calculating Diviation.

$$D_{int} = F(M) - F(P)$$

$$= A(x_p - 1) + B(y_p - \frac{1}{2}) + c - Ax_p - By_p - c$$

$$= \cancel{Ax_p} - A + \cancel{By_p} - \frac{B}{2} + \cancel{c} - \cancel{Ax_p} - \cancel{By_p} - \cancel{c}$$

$$= -A - \frac{B}{2}$$

$$= -dy + \frac{dx}{2} \quad [A=dy, B=-dx]$$

And,

$$D_{Mw} = F(M_w) - F(M)$$

$$= A(x_p - 2) + B(y_p - \frac{1}{2}) + c - A(x_p - 1) - B(y_p - \frac{1}{2}) - c$$

$$= Ax_p - 2A - Ax_p + A$$

$$= -A \quad [A=dy]$$

$$= -dy$$

And,

$$D_{M_{sw}} = F(M_{sw}) - F(M)$$

$$= A(x_p - 2) + B(y_p - 1 - \frac{1}{2}) + c - \{A(x_p - 1) + B(y_p - \frac{1}{2}) + c\}$$

$$= \cancel{Ax_p} - 2A + \cancel{By_p} - B - \frac{B}{2} + \cancel{c} - \cancel{Ax_p} + A - \cancel{By_p} + \frac{B}{2} - \cancel{c}$$

$$= -A - B$$

$$= -dy + dx \quad [A=dy, B=-dx]$$

There's a fraction in deviation. We can simply ~~reduce~~ remove it by multiply by 2 every deviation.

Therefore,

$$D_{init} = -2dy + dx$$
$$D_{nw} = -2dy$$
$$D_{sw} = -2dy + 2dx$$

Algorithm.

```
void midpointLine (int x0, int y0, int x1, int y1, int color)
{
    int dx = x1 - x0, dy = y1 - y0;
    int x = x0, y = y0;

    int Dinit = -2dy + dx, Dnw = -2dy, Dsw = -2dy + 2dx;
    writePixel (x, y, color);
    while (x <= x1)
    {
        if (Dinit < 0) Dinit += Dnw;
        else { Dinit += Dsw;
              y++;
              x++;
            }
        writePixel (x, y, color);
    }
}
```