

We know,

Circle equation, $(x-h)^2 + (y-k)^2 = R^2$

$$\Rightarrow (x-0)^2 + (y-0)^2 = R^2 \quad [\text{if centre is } (0,0)]$$

$$\therefore x^2 + y^2 - R^2 = 0$$

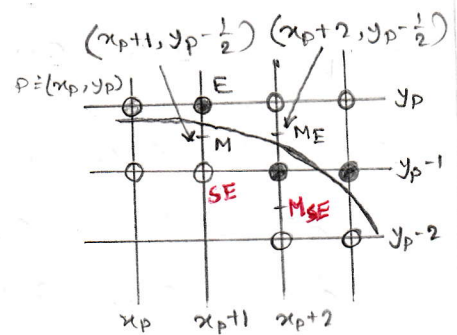
$$\therefore F(x, y) = x^2 + y^2 - R^2$$

$$\begin{aligned} \therefore F(P) &= F(x_p, y_p) \\ &= x_p^2 + y_p^2 - R^2 \end{aligned}$$

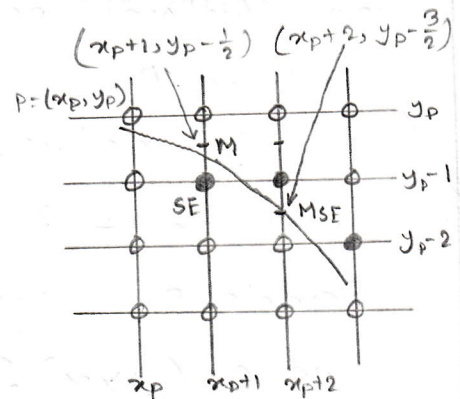
$$\begin{aligned} \therefore F(M) &= F(x_{p+1}, y_{p-\frac{1}{2}}) \\ &= (x_{p+1})^2 + (y_{p-\frac{1}{2}})^2 - R^2 \end{aligned}$$

$$\begin{aligned} \therefore F(M_E) &= F(x_{p+2}, y_{p-\frac{1}{2}}) \\ &= (x_{p+2})^2 + (y_{p-\frac{1}{2}})^2 - R^2 \end{aligned}$$

$$\begin{aligned} \therefore F(M_{SE}) &= F(x_{p+2}, y_{p-\frac{3}{2}}) \\ &= (x_{p+2})^2 + (y_{p-\frac{3}{2}})^2 - R^2 \end{aligned}$$



If $d_{init} \leq 0$



If $d_{init} > 0$

Now,

$$\begin{aligned} d_{init} &= F(M) - F(P) \\ &= (x_{p+1})^2 + (y_{p-\frac{1}{2}})^2 - R^2 - x_p^2 - y_p^2 + R^2 \\ &= x_p^2 + 2x_p + 1 + y_p^2 - y_p + \frac{1}{4} - x_p^2 - y_p^2 \\ &= 2x_p - y_p + \frac{5}{4} \end{aligned}$$

$$\begin{aligned} \therefore d_E &= F(M_E) - F(M) \\ &= (x_{p+2})^2 + (y_{p-\frac{1}{2}})^2 - R^2 - (x_{p+1})^2 - (y_{p-\frac{1}{2}})^2 + R^2 \\ &= x_p^2 + 4x_p + 4 - x_p^2 - 2x_p - 1 \\ &= 2x_p + 3 \end{aligned}$$