

(18)

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Basic of R software

- R is a software for data analysis and statistical computing.
- This software is used for effective data handling and output storage is possible.
- It is possible of graphical display.
- It is a free software.

Ques: $2^2 + \sqrt{25} + 35$

Ans: $2^2 + \sqrt{25} + 35$
[1] 44.

2. $2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$

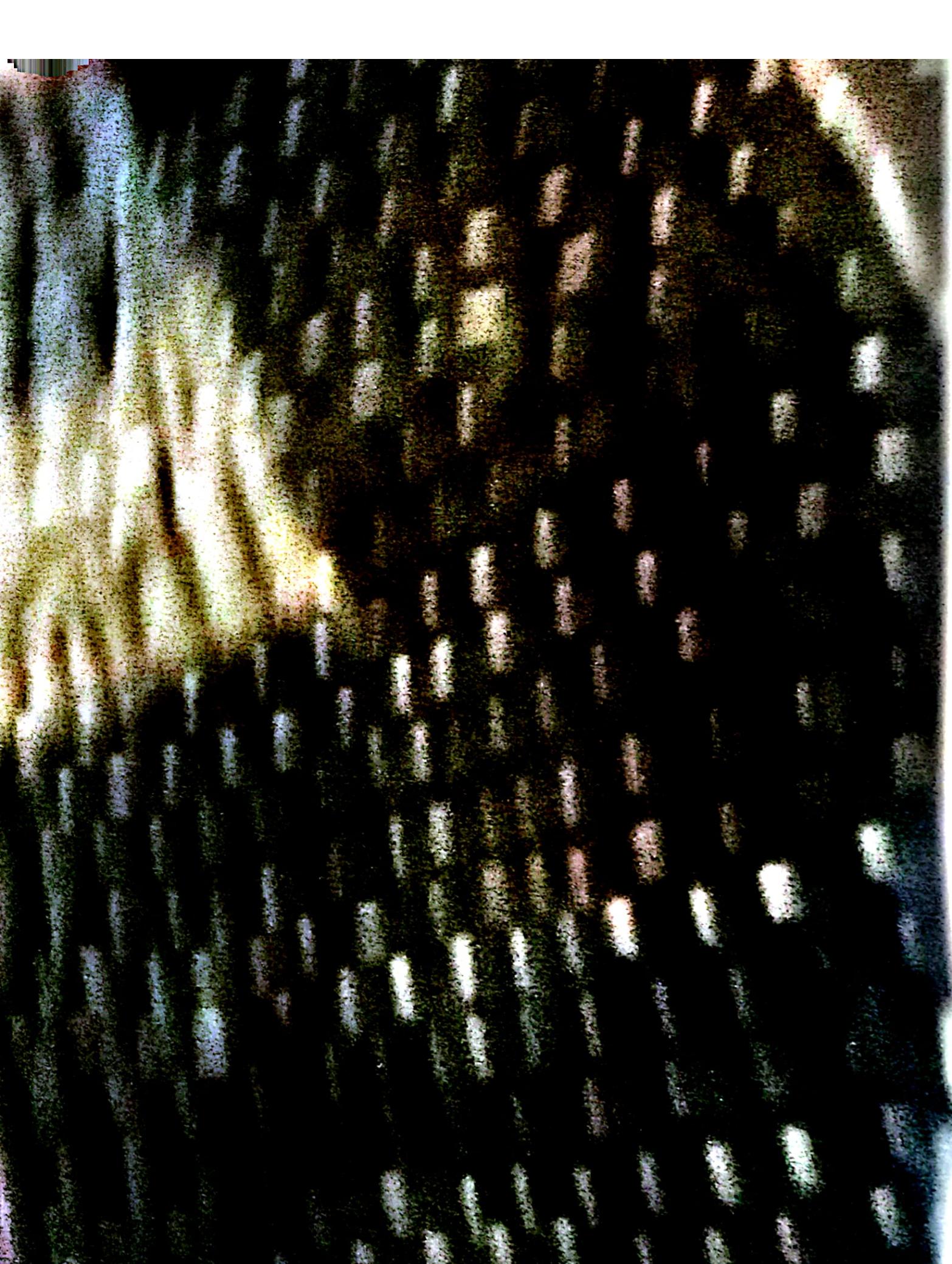
Ans: $2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$
[1] 49.4

3. $\sqrt{76+4 \times 2+9 \div 5}$

Ans: $\sqrt{76+4 \times 2+9 \div 5}$
[1] 128.

4. $42+1-101+7^2+9 \times 8$

Ans: $42+1-\text{abs}(-10)+7^2+9 \times 8$
[1] 128



18.

$$\begin{cases} x=20 \\ y=30 \end{cases}$$

$$\begin{aligned} &x^2+y^2 \\ &x^2-y^2 \\ &\text{[D] } 1300 \end{aligned}$$

$$\begin{aligned} &\text{find } x^2+y^2, \sqrt{y^3-x^3}, x+y, \\ &|x-y| \\ &x+y \\ &x-y \\ &x+y = \text{[D] } 50 \quad \text{[D] } 10 \end{aligned}$$

$$\begin{aligned} &\sqrt{y^3-x^3} \\ &x \\ &x^2+y^2 \\ &\text{[D] } 13^2+8^2 \end{aligned}$$

$$\begin{aligned} 6) \quad &c[2,3,4,5]^2 * 2 \quad c(4,5,6,8)*3 \\ &c[2,3,4,5]^2 \\ &4,6,9,25 \\ &\text{[D] } 12,15,18,24 \end{aligned}$$

$$\begin{aligned} 7) \quad &c(2,3,5,7) * c(-2,-3,-5,-7). \\ &\text{[D] } -4,-9,-25,-28 \end{aligned}$$

$$\begin{aligned} &c(2,3,5,7) * c(8,9) \\ &\text{[D] } 16,27,40,63 \end{aligned}$$

$$\begin{aligned} &c(-2,3,4,5,6)^2 * c(2,3) \\ &\text{[D] } 1,8,9,64,25,216 \end{aligned}$$

Find the sum, product, maximum, minimum of the values

$$5, 8, 6, 7, 9, 10, 15, 6, \dots$$

sol x = c(5, 8, 6, 7, 8, 9, 10, 15, 8)

length(x)

[1] 8

sum(x)

[1] 65

prod(x)

[1] 11340000

max(x)

[1] 15

min(x)

[1] 5

Q⇒ for matrix. $\begin{bmatrix} 1 & 5 \\ 2 & 8 \\ 3 & 9 \\ 4 & 8 \end{bmatrix}$

sol: x <- matrix(nrow=4, ncol=2,
data = c(1, 2, 3, 4, 5, 6, 7, 8)).

[1,1] [1,2]
[1,1] 1 5
[1,2] 2 6
[2,1] 3 7
[2,2] 4 8

Q⇒ $x = \begin{bmatrix} 1 & 4 & 2 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$ $y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 16 & 12 \end{bmatrix}$ find $x+y$, $x \times y$, $2x+3y$.

sol: x <- matrix(nrow=3, ncol=3,
data = c(1, 2, 3, 4, 5, 6, 7, 8, 9))
y <- matrix(nrow=3, ncol=3,
data = c(2, -2, 10, 4, 8, 6, 10, -11, 12)).

$x+y$
[1,1] [1,2] [1,3]
[1,1] 3 8 12
[1,2] 0 13 -3
[1,3] 13 12 21

$x \times y$
[1,1] [1,2] [1,3]
[1,1] 22 16 70
[1,2] -4 40 -88
[1,3] 30 36 108

$2x+3y$

8 20 44
-2 34 -17
36 30 54

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6> $y = c(2, 4, 6, 1, 3, 5, 7, 13, 16, 14, 17, 19, 3, 3, 2, 5, 0, 15, 9, 14, 18, 10, 12)$

6> ~~print(y)~~

6> ~~[2, 3]~~

6> ~~a = table(z)~~

6> ~~transform(a)~~

6> ~~for~~

6> ~~0~~

6> ~~1~~

6> ~~2~~

6> ~~3~~

6> ~~4~~

6> ~~5~~

6> ~~6~~

6> ~~7~~

6> ~~8~~

6> ~~9~~

6> ~~10~~

6> ~~12~~

6> ~~14~~

6> ~~15~~

6> ~~16~~

6> ~~17~~

6> ~~18~~

6> ~~19~~

7> ~~breaks = cut(c, 5)~~

7> ~~b = cut(y, breaks, right = F)~~

7> ~~c = table(b)~~

7> ~~transform(c)~~

8> ~~b~~ ~~Freq~~

8> ~~1 [0,5)~~ ~~8~~

8> ~~2 [5,10)~~ ~~5~~

8> ~~3 [10,15)~~ ~~4~~

8> ~~4 [15,20)~~ ~~6~~

~~breaks~~
~~1 2 3 4 5~~
~~6 7 8 9~~

8> ~~print(b)~~

8> ~~print(c)~~

Practical - 2

Problem on P.d.f and C.d.f.

Q) Can the following be c.d.f?

$$\textcircled{1} \quad f(x) = \begin{cases} 2-x & 1 \leq x \leq 2 \\ 0 & \text{o.w.} \end{cases} \quad \textcircled{2} \quad f(x) = \begin{cases} 3x^2 & 0 < x < 1 \\ 0 & \text{o.w.} \end{cases}$$

$$\textcircled{3} \quad f(x) = \begin{cases} 3x^2 & 0 < x < 1 \\ 0 & \text{o.w.} \end{cases} \quad \textcircled{4} \quad f(x) = \begin{cases} \frac{3x}{2} \left(1 - \frac{x}{2}\right) & 0 \leq x \leq 2 \\ 0 & \text{o.w.} \end{cases}$$

$\textcircled{1}$ Soln:- $\int f(x) dx = 1$ is condition for p.d.f.

$$\textcircled{1} \quad \int_0^2 (2-x) dx \Rightarrow \int_0^2 2dx - \int_0^2 x dx \Rightarrow [2x]_0^2 - [\frac{x^2}{2}]_0^2$$

$$(4-2) - (2-0) \neq 1 \text{ so not P.d.f.}$$

$$\textcircled{2} \quad f(x) = \begin{cases} 3x^2 & 0 < x < 1 \\ 0 & \text{o.w.} \end{cases}$$

$$\textcircled{2} \quad \int_0^1 3x^2 dx = \left[\frac{3x^3}{3} \right]_0^1 = \left[x^3 \right]_0^1 = 1 \quad \text{so it is P.d.f.}$$

$$\textcircled{3} \quad f(x) = \begin{cases} \frac{3x}{2} \left(1 - \frac{x}{2}\right) & 0 \leq x \leq 2 \\ 0 & \text{o.w.} \end{cases}$$

$$\textcircled{3} \quad \text{Soln:- } f(x) = \int_0^2 \frac{3x}{2} - \frac{3x^2}{4} dx \Rightarrow \int_0^2 \frac{3x}{2} dx - \int_0^2 \frac{3x^2}{4} dx$$

$$\left[\frac{3x^2}{4} \right]_0^2 - \left[\frac{x^3}{4} \right]_0^2 \Rightarrow \left[\frac{3 \cdot 4}{4} - 0 \right] - [2] =$$

$$3 - 2 = 1 \quad \text{so it is P.d.f}$$

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2 Can the following be p.m.f

①	x	1	2	3	4	5
	$p(x)$	0.2	0.3	-0.1	0.5	0.1

②	x	0	1	2	3	4	5
	$p(x)$	0.1	0.3	0.2	0.2	0.1	0.6

③	x	10	20	30	40	50
	$p(x)$	0.2	0.3	0.3	0.2	0.2

Sol - i \rightarrow Hence since 1 valid & very simple not p.m.f.

Sol \rightarrow Since $p(x) \geq 0 \quad \forall x$
and $\sum p(x) = 1$ if x - p.m.f.

$$p_{x=0} = c(0.1, 0.3, 0.2, 0.2, 0.1, 0.1)$$

sum($p_{x=0}$)

E.I. 1

$$3 \rightarrow p_{x=0} = c(0.2, 0.3, 0.3, 0.2, 0.2)$$

sum($p_{x=0}$)

E.I. = 1.2 \therefore it is not p.m.f.

35 Find $P(x \leq 2)$, $P(2 \leq x \leq 4)$, $P(\text{at least } 4)$, $P(3 < x < 6)$

∞	0	1	2	3	4	5	6	
$P(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1	

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$$\textcircled{1} P(x \leq 2) = P(0) + P(1) + P(2) = 0.1 + 0.1 + 0.2 = 0.4$$

$$P(2 \leq x \leq 4) = P(2) + P(3) + P(4) = 0.2 + 0.2 + \cancel{0.1} = 0.4$$

$$P(\text{at least } 4) = P(4) + P(5) + P(6) = 0.1 + 0.2 + 0.1 = 0.4$$

$$P(3 < x < 6) = P(4) + P(5) = 0.1 + 0.2 = 0.3$$

Q.4 find c.d.f

∞	0	1	2	3	4	5	6	
$P(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1	

$$\text{prob} = C(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$$

cumsum(prob)

$$[.] = 0.1, 0.2, 0.4, 0.6, 0.7, 0.9, 1.$$

$$F(x) = 0 \quad \text{if } x < 0$$
$$0.1 \quad \text{if } x \leq 0 < 1$$
$$0.2 \quad \text{if } 1 \leq x < 2$$
$$0.4 \quad \text{if } 2 \leq x < 3$$
$$0.6 \quad \text{if } 3 \leq x < 4$$
$$0.7 \quad \text{if } 4 \leq x < 5$$
$$0.9 \quad \text{if } 5 \leq x < 6$$
$$1 \quad \text{if } 6 \leq x$$

$\frac{10}{12}$	$\frac{10}{12}$	$\frac{14}{15}$	$\frac{16}{17}$	$\frac{18}{19}$	$\frac{18}{19}$
$\frac{10}{12}$	$\frac{10}{12}$	$\frac{14}{15}$	$\frac{16}{17}$	$\frac{18}{19}$	$\frac{18}{19}$

② $f(x) = \begin{cases} 0 & \text{if } x < 0 \\ 0.2 & \text{if } 0 \leq x < 12 \\ -0.55 & \text{if } 12 \leq x < 14 \\ -0.7 & \text{if } 14 \leq x < 16 \\ -0.9 & \text{if } 16 \leq x < 18 \\ 1 & \text{if } 18 \leq x \end{cases}$

~~Ans~~

Practical - 5

Probability distribution and binomial distribution

Find the CDF of the following PDF and draw the graph

x	10	20	30	40	50
$p(x)$	0.15	0.25	0.3	0.2	0.1

$$x = c(10, 20, 30, 40, 50)$$

$$\text{prob} = c(0.15, 0.25, 0.3, 0.2, 0.1)$$

cumsum(prob)

$$[0.15 \ 0.40 \ 0.7 \ 0.9 \ 1.00]$$

$$F(x) = 0 \quad \text{if } x < 10$$

$$0.15 \quad 10 \leq x < 20$$

$$0.40 \quad 20 \leq x < 30$$

$$0.70 \quad 30 \leq x < 40$$

$$0.90 \quad 40 \leq x < 50$$

$$1 \quad x \geq 50$$

plot(x, prob, xlab = "values", ylab = "Probability", main = "graph of F(x)", "s")



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Final Question

Suppose there are 12 MCQ in a test. Each question has only one of them correct. Find the probability of getting ① correct answer ② atmost 4 correct answers

It is given that $n=12$, $p=1/4$, $q=3/4$

① Probability of correct answer
 $\rightarrow P(X=8)$

$$= \binom{12}{8} \left(\frac{1}{4}\right)^8 \left(\frac{3}{4}\right)^4$$

$$= 495 \cdot 0.0531824$$

$$= 0.026585$$

∴ Binom(8, 1/4, 3/4)

∴ 0.026585

② Atmost 4

Binom(4, 1/4, 3/4)

∴ 0.9224445

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Q3) There are 10 members in committee. The probability of any member attending a meeting is 0.9. Find probability ① 7 members attended ② at least 5 members attended ③ at most 6 members attended

Soln

① Member

It is given $n=10$, $p=0.9$, $q=0.1$, $x=7$

∴ Binom(7, 10, 0.9)

[1] 0.05739563

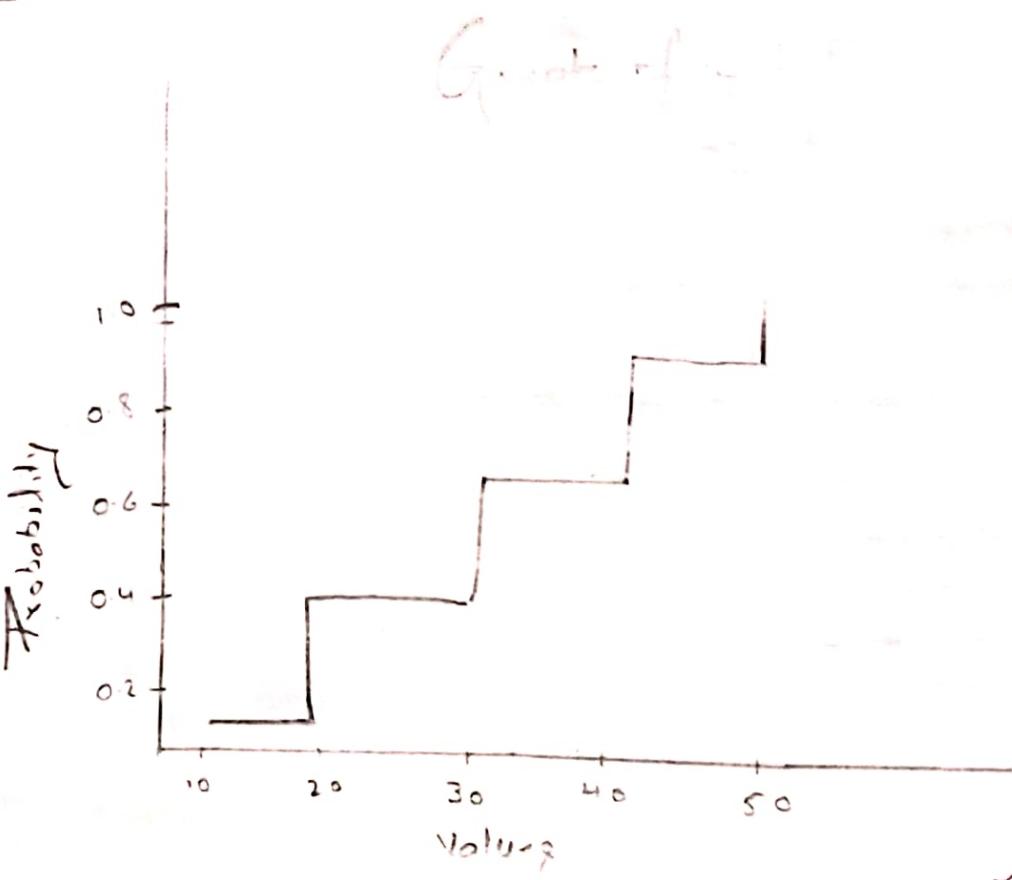
② at least 5 members

1 - Binom(4, 10, 0.9)

[2] ~~0.99983651~~

[1] 0.9998531

①



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③ atmost 6 member

binom(6, 10, 0.9)

[1] 0.0127052

~~Q.7~~ Find the C.D.F and Draw the graph

x	0	1	2	3	4	5	6
P(x)	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$x = \{0, 1, 2, 3, 4, 5, 6\}$$

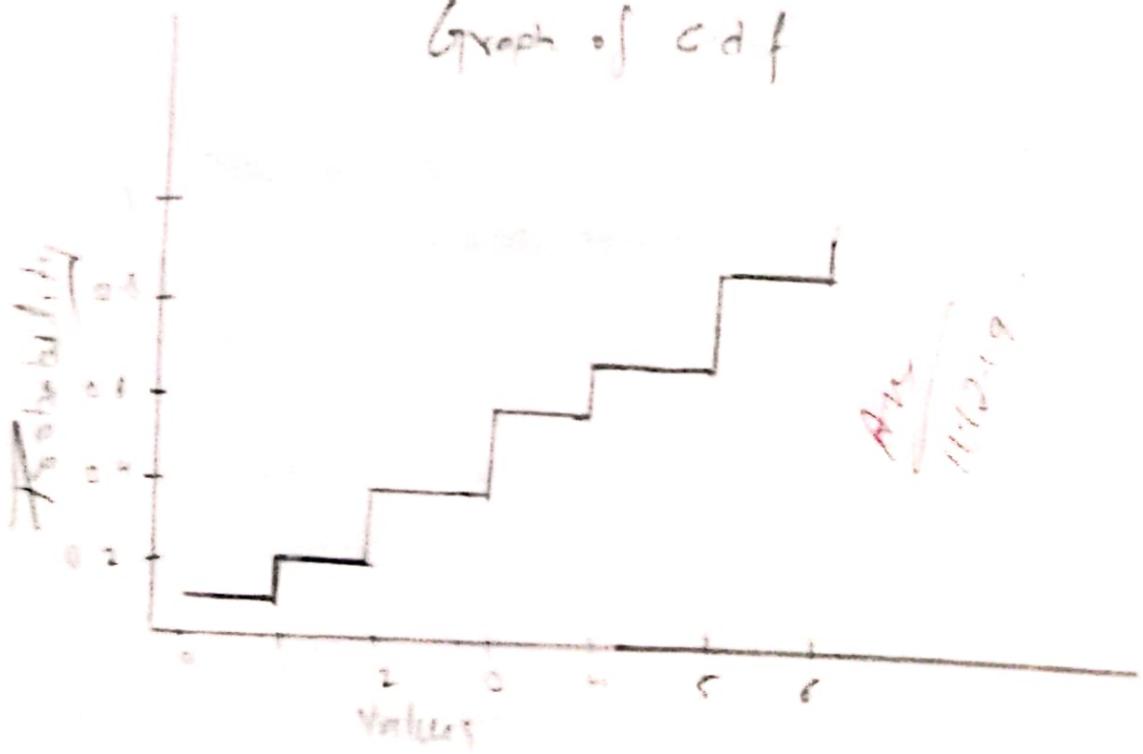
prob = c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)

cumsum (prob)

$$F(x) = \begin{cases} 0 & x < 0 \\ 0.1 & 0 \leq x < 1 \\ 0.2 & 1 \leq x < 2 \\ 0.4 & 2 \leq x < 3 \\ 0.6 & 3 \leq x < 4 \\ 0.7 & 4 \leq x < 5 \\ 0.8 & 5 \leq x < 6 \\ 1 & 6 \leq x \end{cases}$$

plot(x, prob, xlab = "Value", ylab = "Probability", main = "Graph")

Graph of CDF



Practical-4Binomial Distribution

Find the complete binomial distribution when $n=5$ and $p=0.1$.

Find the probability of exactly 10 success in 100 trials with $p=0.1$.

X follows binomial distribution with $n=12$, $P=0.25$, find

$$P(X=5)$$

$$P(X \leq 5)$$

$$P(X \geq 7)$$

$$P(5 \leq X \leq 7)$$

The probability of salesman make a sale to a customer is 0.15
Find the probability

- ① No sale for 10 customers, more than 3 sale in 20 customers.

A student writes 5 MCQs, each question has 4 options out of which 1 correct calculate the probability atleast 3 correct answers.

Q.8

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$$\text{Note: } P(x=x) = \text{dbinom}(x, n, p)$$

$$P(x \leq x) = \text{pbisnom}(x, n, p)$$

$$P(x > x) = 1 - \text{pbisnom}(x, n, p)$$

To find the value of x for which the probability in P , command is $\text{qbinom}(p, n, p)$

$$1) n=5 \quad p=0.1$$

$$\text{dbinom}(0:5, 5, 0.1)$$

$$[1] 0.59049 \quad 0.32805 \quad 0.07290 \quad 0.00810 \quad 0.00049 \\ 0.00001$$

$$2) \text{dbinom}(10, 100, 0.1)$$

$$n=100$$

$$[1] 0.1318653$$

$$3) n=12 \quad p=0.25$$

$$\text{dbinom}(5, 12, 0.25) \quad P(x=5)$$

$$[1] 0.1032414$$

$$4) P(x \leq 5)$$

$$\text{pbisnom}(5, 12, 0.25)$$

$$[1] 0.9455$$

$$5) P(x \geq 7) = 1 - P(x \leq 7) = 1 - \text{pbisnom}(7, 12, 0.25)$$

$$[1] 0.0027815$$

$$6) P(5 < x < 7)$$

$$\text{dbinom}(6, 12, 0.25)$$

$$0.04014945$$

4) (i) $n = 10, p = 0.15, x = 0$
 $dbinom(0, 10, 0.15)$
 [1] 0.1968744.

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(ii) $n = 20, p = 0.15$
 $P(X \geq 3) = 1 - P(X \leq 2) = 1 - dbinom(3, 20, 0.15)$
 [1] 0.3522748

5) $n = 5, p = 0.25, x = 3$
 $P(X \geq 3)$
 $1 - P(X \leq 2)$
 $1 - dbinom(2, 5, 0.25)$
 [1] 0.1035156

Q.6 X follows binomial distribution $n = 10, p = 0.4$ plot the graph of P.d.f and C.d.f

soln $n = 10, p = 0.4 \Rightarrow q = 0.6$

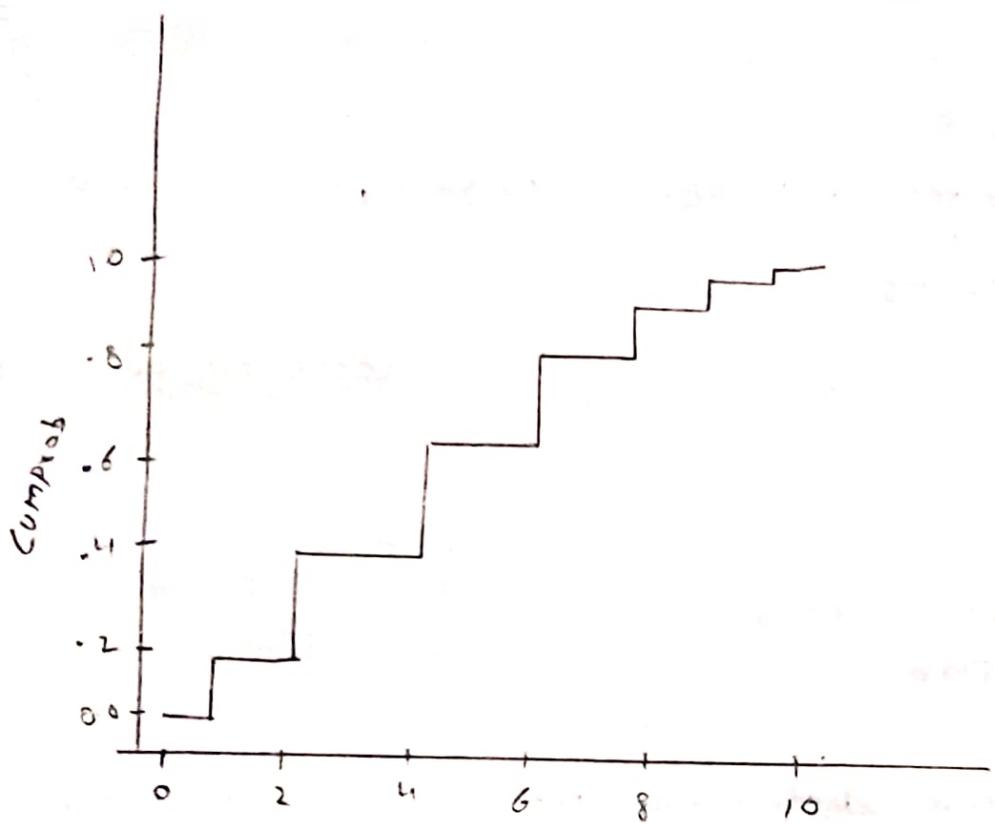
$pprob = dbinom(x, n, p)$

$cumpprob = dbinom(x, n, p)$

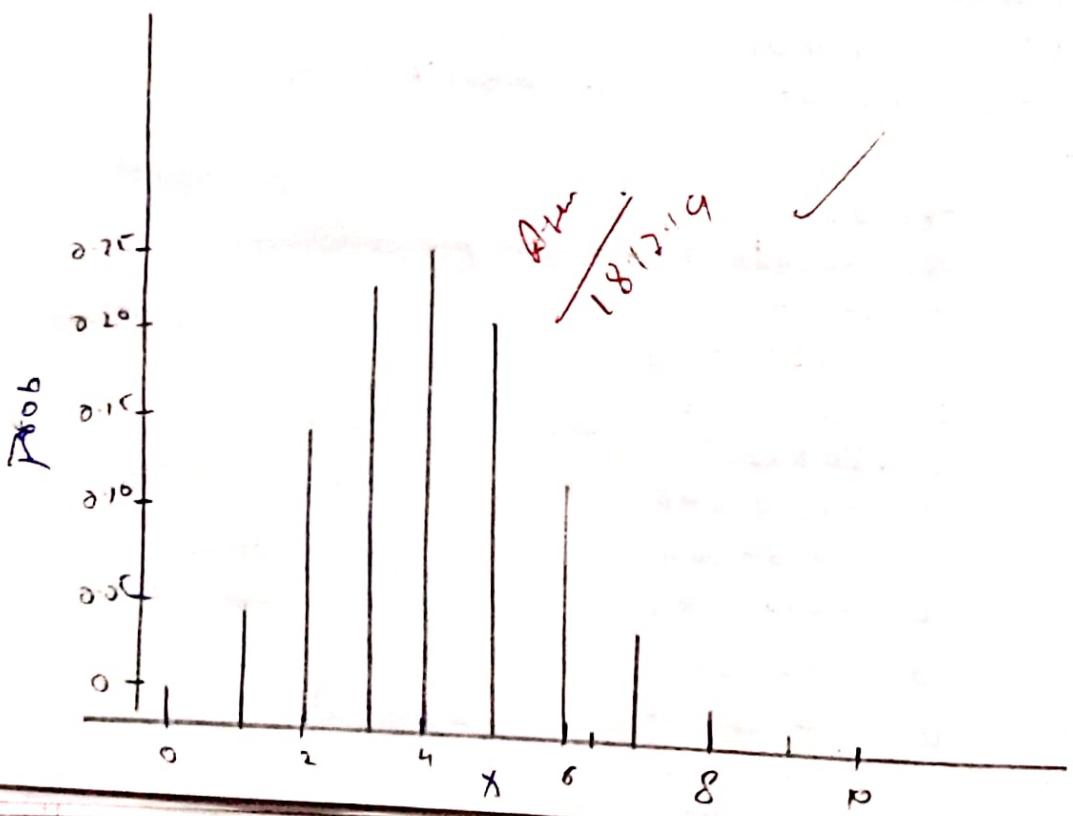
```
d = data.frame("xvalue" = x, "probability" = pprob)
print(d)
```

xvalue	probability
0	0.00606466176
1	0.0403107840
2	0.1209323520
3	0.2149908480
4	0.2508226560
5	0.2006581248
6	0.114767360
7	0.0424673280
8	0.0106168320
9	0.0015728640
10	0.0001048576

Q. Plot (x_{prob} , "S")



plot (x_{prob} , "h")



Practical-5

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8/01/2020

Normal Distribution

1) $P[x = x] = dnorm(x, \mu, \sigma)$

2) $P(x \leq x) = pnorm(x, \mu, \sigma)$

3) $P(x > x) = 1 - pnorm(x, \mu, \sigma)$

4) $P(x_1 < x < x_2) = pnorm(x_2, \mu, \sigma) - pnorm(x_1, \mu, \sigma)$

To find the value of K as shown that

5) $P(x \leq K) = P$, $dnorm(P, \mu, \sigma)$

To generate m random numbers command is

Q1 $x \sim N(\mu = 50, \sigma^2 = 100)$. Find,

- ① $P(x \leq 40)$ ② $P(x > 55)$ ③ $P(42 \leq x \leq 60)$
④ $P(x \leq K) = 0.7$ $K = ?$

1.2 $\Rightarrow x \sim N(\mu = 100, \sigma^2 = 36)$

- ① $P(x \leq 110)$ ② $P(x \leq 95)$ ③ $P(x > 115)$
④ $P(95 \leq x \leq 105)$ ⑤ $P(x \leq K) = 0.9$ $K = ?$

1.3 Generate 10 random numbers from a normal distribution with mean = 60 S.D = 5. Also calculate sample mean, median, S.D. Variance, S.D.

Ques. Be part of standard normal dist.

a)

b)

c)

d)

e)

f)

g)

h)

Ans

$$a = \text{pnorm}(40, 50, 10)$$

cat("P(x > 40) = ", a)

$$\approx P(x \geq 40) = 0.1586553$$

$$b = 1 - \text{pnorm}(55, 50, 10)$$

cat("P(x > 55) = ", b)

$$P(x > 55) = 0.3085375$$

$$c = \text{pnorm}(60, 50, 10) - \text{pnorm}(42, 50, 10)$$

cat("P(42 \leq x \leq 60) = ", c)

$$P(42 \leq x \leq 60) = 0.6294893$$

$$d = \text{qnorm}(0.7, 50, 10)$$

cat("P(x \leq d) = 0.7, K_{0.7} = ", d)

$$P(x \leq K) = 0.7 \quad K_{0.7} = 55.24401$$

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$$\textcircled{1} \quad a = \text{pnorm}(110, 100, 6)$$

$$\text{cat}("p(x \leq 110) = ", a)$$

$$P(X \leq 110) = 0.9522096.$$

$$\textcircled{2} \quad b = \text{pnorm}(95, 100, 6)$$

$$\text{cat}("p(x \leq 95) = ", b)$$

$$P(X \leq 95) = 0.2023284.$$

$$\textcircled{3} \quad c = 1 - \text{pnorm}(115, 100, 6)$$

$$\text{cat}("p(x > 115) = ", c)$$

$$P(X > 115) = 0.006209665$$

$$\textcircled{4} \quad d = \underline{\text{pnorm}(105, 100, 6)} - \text{pnorm}(95, 100, 6)$$

$$\text{cat}("p(95 \leq X \leq 105) = ", d)$$

$$P(95 \leq X \leq 105) = 0.4953032.$$

$$\textcircled{5} \quad e = \text{qnorm}(0.4, 100, 6)$$

$$\text{cat}("p(x \leq 1<) = 0.4 \quad x = ", e)$$

$$p(x \leq 1<) = 0.4 \quad x = 98.47092.$$

$$\textcircled{6} \quad a = \text{rnorm}(10, 60, 5) \quad n = 10 \quad m = 60 \quad s = 5$$

$$\text{[1]} \quad 58.45543 \quad \underline{55.02259} \quad 60.59413 \quad 58.66145 \quad 60.02250$$

$$60.59697 \quad 61.38523 \quad 51.92280 \quad 55.01164 \quad 68.01429$$

mean(a)

$$\text{[1]} \quad 61.18175$$

$$n = 10 \\ \text{variance} = (n-1) * (\bar{x})^2 / n$$

$$\text{[1]} \quad 23.22858.$$

median(a)

$$\text{[1]} \quad 60.27534$$

$$SD = \sqrt{\text{variance}}$$

$$\text{[1]} \quad \frac{\sqrt{0.00304}}{4.819604}$$

sd(a)

$$\text{[1]} \quad 5.080309$$

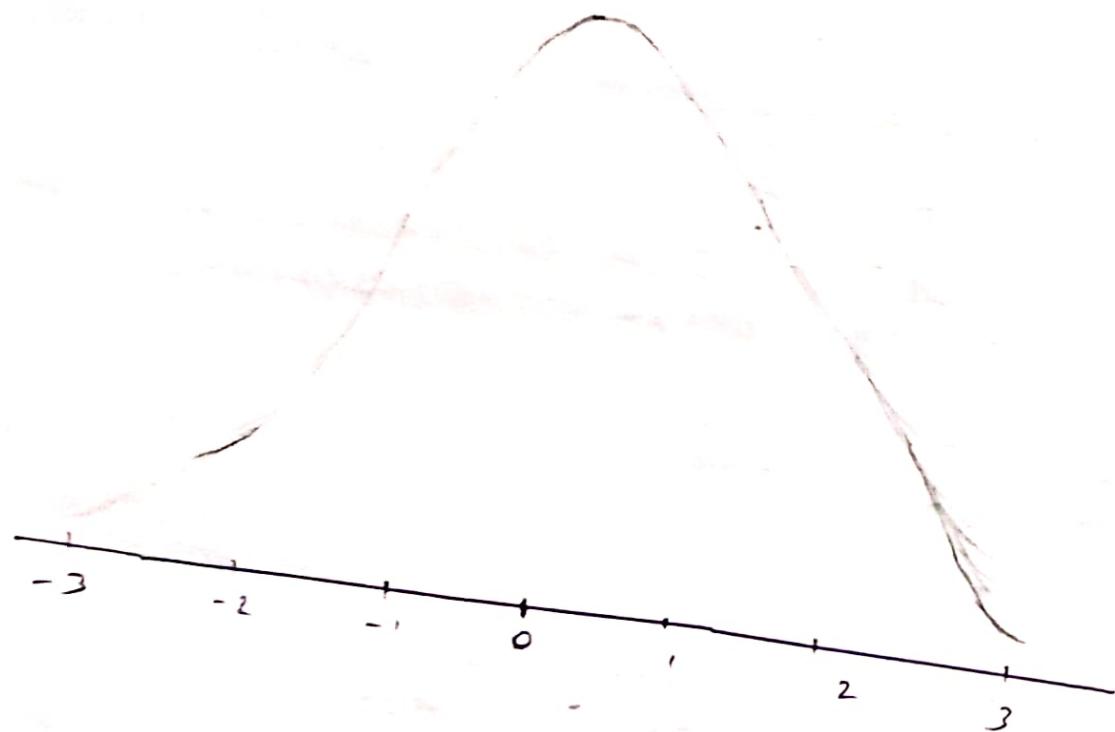
$$\text{[1]} \quad (\text{sd}(a))^2$$

$$\text{[1]} \quad 25.00954$$

$$x = \text{dnorm}(-3, 3, 0.1)$$

$$y = \text{dnorm}(x)$$

plot(x, y, xlab = "x value", ylab = "Probability", main = "R plot",
normal distribution", "x").



Ans/20

Z-Distribution.

Test for Hypothesis.

$$H_0: \mu = 10 \text{ against } H_1: \mu \neq 10$$

A sample of size 400 was collected which gives a mean 10.2 and the standard deviation 2.25

Test the hypothesis at 5% level of significance

$$\mu_0 = (\text{mean of population}) = 10$$

$$\mu_x = (\text{mean of sample}) = 10.2$$

$$sd = 2.25$$

$$n = (\text{sample size}) = 400$$

$$z_{\text{cal}} = (\mu_x - \mu_0) / (sd / \sqrt{n})$$

$$\text{out} = ("z_{\text{cal}}": z_{\text{cal}})$$

$$\approx 1.7778$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\text{pvalue}$$

$$\approx 0.075$$

Note: If result of tested hypothesis ≈ 0.05 then assumed of $H_0: \mu_0 = 10$ is accept.

Test the hypothesis $H_0: \mu = 75$ against $H_1: \mu \neq 75$

A sample of size 100 was selected & the sample mean is 80 with the S.D = 3.

Test of hypothesis at 5% level of significant

$$\mu_0 = (\text{mean of population}) = 75$$

$$\mu_x = (\text{mean of sample}) = 80$$

$$n = (\text{sample size}) = 100$$

$$z_{\text{cal}} = (\mu_x - \mu_0) / (sd / \sqrt{n})$$

1A

cat = ("zcal": "", zcal)

? zcal \$x = 16.6667

pvalue = 2*(1-pnorm(abs(zcal)))

pvalue

?> 0.

Q1) Test of Hypothesis $H_0: \mu = 25$ against $H_1: \mu < 25$ at 5% level of significance.

The following sample of 30 selected.

x = c(20, 24, 27, 35, 30, 40, 26, 27, 10, 20, 30, 37, 35, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 39, 27, 15, 14, 22, 20, 18)

?max = mean(x)

?> m
[1] 26.0667

?n = length(x)

? n
[1] 30

Variance = (n-1)* var(x)/n
Variance

[1] 52.0956

? sd = sqrt(var(x))

sd

[1] 7.229809

m0 = 25

? m2 = 26.0667

n = 30

? sd = 7.229809

? zcal = (m2 - m0) / (sd / sqrt(n))

zcal

[1] 0.8026454

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

42

pvalue

0.422375

The assumed Hypothesis is verified

(e) Experience has show that 20% student of a college are smoke a sample of four hundred student reveal that out of 400 only 50 smoke test the hypothesis that the experience give the correct proportion or not

$$zP = 0.2$$

$$Q = 1 - P$$

$$P = 50/400$$

$$P$$

$$0.125$$

$$n = 400$$

$$z_{\text{cal}} = (p - P) / (\sqrt{P(1-P)/n})$$

$$z_{\text{cal}}$$

$$-3.75$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

pvalue

[1] 0.0001785348

fm

Q) Test the hypothesis $H_0: p=0.5$ against $H_1: p \neq 0.5$. A sample of 200 is selected and the sample portion is cal $p=0.56$ test the hypothesis at level of significance 1%.

$$n = 200$$

$$p = 0.5$$

$$P' = 0.56$$

$$Q = 1 - P$$

$$Z_{\text{cal}} = (p - P) / \sqrt{\frac{P(1-P)}{n}}$$

$$Z_{\text{cal}} = 1.697051$$

$$\text{p-value} = 2 \times (1 - \text{pnorm}(\text{abs}(Z_{\text{cal}})))$$

$$\text{p-value} = 0.08968002$$

Practical = 7

large & small t-test.

- Q) A study of Noise level on 2 hospital is conducted below. Test of hypothesis that of noise level on 2 hospital are same or not.

Nos of Sample	Hos A	Hos B
mean	84	34
s.d.	61	59
s.d.	7	8

Sol:- The Noise level are same.

$$n_1 = 84$$

$$n_2 = 34$$

$$m_x = 61$$

$$m_y = 54$$

$$sdx = 7$$

$$sdy = 8$$

$$z = (m_x - m_y) / \sqrt{(\frac{sdx^2}{n_1} + \frac{sdy^2}{n_2})}$$

$$z = 1.273662$$

rat("z calculated": "z")

$$pvalue = 2 * (1 - pnorm(z))$$

$$pvalue = 0.20766$$

- 2) Random sample of size 1000 & 2000 are drawn from 2 population with a mean 67.5 and 68 respectively with a same s.d. = 2.5. Test the hypothesis that the mean of the population are equal.

Sol:- H_0 : Two population mean are equal.

$$n_1 = 1000$$

$$n_2 = 2000$$

$$m_x = 67.5$$

$$m_y = 68$$

$$sdx = 2.5$$

$$sdy = 2.5$$

$$\frac{Z^2 = (-2 - \bar{z})}{\sqrt{p_1(1-p_1) + p_2(1-p_2)}} = \left(\frac{\text{std } z^2 / n_1}{\text{std } z^2 / n_2}\right)$$

$$[Q] -5.163978$$

> Cal (calculated $n_1=1, n_2=1$)

> calculated $z^2 = 5.1639787$

> pvalue = $2 * (1 - \text{norm}(\text{obt}(2)))$
pvalue

$$[Q] 2.417764 \cdot 10^{-7}$$

Q= In a first year class, 20% of a random sample of 400 students had defective eye sight. In another class, 15.5% of 500 sample student had the same defect. Is the difference of population proportions same?

Sol

H₀: The proportion of population are equal

$$n_1 = 400$$

$$n_2 = 500$$

$$p_1 = 0.2$$

$$p_2 = 0.155$$

$$> p = (n_1*p_1 + n_2*p_2) / (n_1 + n_2)$$

$$> p$$

$$[Q] 0.175$$

$$> q = 1 - p$$

$$> q$$

$$[Q] 0.825$$

$$> Z = (p_1 - p_2) / \sqrt{p_1 q_1 / n_1 + p_2 q_2 / n_2}$$

$$> Z^2$$

$$[Q] 1.76542$$

$$\text{zcal} ("z \text{ calculated or } = 1.76542)$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

pvalue

$$[1] 0.37748489$$

Q:- From each of the box of the apples a sample of 200 is calculated & it is found that there are 44 bad apples in the first sample & 30 bad apples in the second sample. Test the hypothesis that the two boxes are equivalent in terms of no of bad apples.

Q:- In a M.A. class out of the sample of 60, mean height is 63.5 inch with a SD of 2.5. In a M.com class out of 50 student mean height is 60.5 inch with a SD of 2.5. Test of hypothesis that the mean of M.A. and M.com class are same.

Sol:-

H_0 : The two boxes are equivalent in terms of bad apples

$$\text{z} n_1 = 200$$

$$\text{z} n_2 = 200$$

$$\text{z} p_1 = 44/100$$

$$\text{z} p_2 = 30/200$$

$$\text{z} P = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$\text{z} P =$$

$$[1] 0.185$$

$$\text{z} Q = 1.42$$

$$\text{z} Q = 0.815$$

$$\text{z} Z = (p_1 - p_2) / \sqrt{p_1 * p_2 * (1 / (n_1 + n_2))}$$

$$\text{z} Z =$$

$$[1] 1.802741$$

$$\text{z} \text{cal} ("z \text{ calculated or } = 1.8027417)$$

$$\text{z} \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

pvalue

$$[1] 0.07142888$$

If p-value > 0.05 we accept the H_0 at 5% level of significance.

Solⁿ S₂

H_0 : The mean of M.A & M.com are same

$$n_1 = 63$$

$$n_2 = 50$$

$$\bar{m}_x = 63.5$$

$$\bar{m}_y = 69.4$$

$$s_{dx} = 2.4$$

$$s_{dy} = 2.5$$

$$z = (\bar{m}_x - \bar{m}_y) / \sqrt{s_{dx}^2/n_1 + s_{dy}^2/n_2}$$

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[1] 12.53359

> cat("z calculated = ", z)

z calculated = 12.53359

p-value = $2 * (1 - pnorm(abs(z)))$

≤ p-value

[1] 0

As p-value < 0.05, we reject the H_0 at 5%

Practical - 8Small sample test

) The flower 10 selected and the height founded
 $63, 63, 68, 69, 71, 71, 72$ cm Test the hypothesis
 That the mean height 66 cm or not at 1%

$H_0: \mu_{\text{mean}} = 66 \text{ cm}$
 $x = \{63, 63, 68, 69, 71, 71, 72\}$.
 $t\text{-test}(x)$.

one sample t-test

~~data = x~~

~~$t = 47.94, df = 6, p\text{-value} = 5.822e-09$.~~

~~alternative hypothesis : True mean is not equal to 0
as percent confidence interval:~~

~~64.66479 71.62092~~

~~Sample estimate:~~

~~mean of x~~

~~68.14286~~

~~pvalue less than 0.01 we reject H_0 of 1% level
of significance.~~

2 Random sample drawn from 2 different population Sample 1:- 8, 10, 12, 11, 16, 15, 18, 7
 Sample 2:- 20, 15, 18, 9, 8, 10, 11, 12. Test the hypothesis
 that there is no difference mean b/w the populations
 mean at 5%

p-value

Solⁿ

H₀

H₀: There is no difference in population means.

$$x = c(8, 10, 12, 11, 16, 15, 18, 7)$$

$$y = c(20, 15, 18, 9, 10, 11, 12, 8)$$

t-test(x, y).

Welch Two Sample t-test.

data: x and y

$$t = -0.36242, df = 13.832, p\text{-value} = 0.7225$$

alternative hypothesis: True difference in mean

not equal to 0

95 percent confidence interval:

$$-5.192719 \quad 3.892719$$

Sample estimates:

mean of x and y

$$12.125 \quad 12.875$$

p-value greater than 0.05 we accept H₀ at 5% level of significance.

A. Following are the weight 10 people before and after diet program. Test hypothesis that it effective or not.

Before 100, 125, 95, 96, 98, 112, 115, 104, 109, 110

After 95, 80, 95, 98, 90, 100, 110, 85, 100, 101

Solⁿ: H₀: The diet program is not effective

$$x = c(100, 125, 95, 96, 98, 112, 115, 104, 109, 110)$$

$$y = c(95, 80, 95, 98, 90, 100, 110, 85, 100, 101)$$

t-test(x1, y, paired = T, alternative = "less")
Welch Two sample t-test.

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data : x and y

t = -2.6991, df = 17.801, p-value = 0.985

alternative hypothesis: true difference in means is less than
not equal to 0.

95 percent confidence interval:

inf 18.72908

Sample estimates:

mean of the difference

p-value greater than 0.05 we accepting H_0 at 5% level of significance.

Mark before and after a training program are given below.

before: 20, 25, 32, 28, 27, 36, 35, 25

After: 30, 35, 32, 37, 37, 40, 40, 23

Test the Hypothesis ex effective or not.

sol:- H_0 : The training program not effective

x = c(20, 25, 32, 28, 27, 36, 35, 25)

y = c(30, 35, 32, 37, 37, 40, 40, 23)

t-test(x1, y, paired = T, alternative = "greater")

Paired t-test

data : x and y

t = -3.3859, df = 7, p-value = 0.9942

alternative hypothesis: true difference in means is greater than 0

95 percent confidence interval:

-8.967399 Inf

Sample estimates:

mean of the difference

-5.75

p-value greater than 0.05. We accept H_0 at 5% level of significance.

Q.) 2 Random Sample were drawn from 2 random population and the value are.

$$A = 66, 67, 75, 76, 82, 84, 88, 90, 92$$

$$B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97$$

Test whether the population have same variance at 5% level of significant.

H_0 : The variance of 2 population are equal.

$$x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$$

$$y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$$

$$\text{Var.tost}(x, y)$$

F test to compare two variances

data: x and y

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6359

alternative hypothesis: true ratio of variances is not equal to 1
95 percent confidence interval:

0.1833662 3.0360393

Sample estimates:

ratio of variances

0.7068567

p-value greater than 0.05 We accept H_0 at 5% level of significant

The arithmetic mean of sample of 100 observation is 52 if $s.d = 7$ test the hypothesis that the population mean = 55 or not at 5% level of LOS.

$$H_0: \text{Population mean} = 55$$

$$n = 100$$

$$\bar{m}_x = 52$$

$$m_0 = 55$$

$$s.d = 7$$

$$z = (\bar{m}_x - m_0) / (s.d / \sqrt{n})$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$\text{pvalue} = 0.1$$

$$1.82153 < 0.5$$

p-value < 0.05 we reject the 5% level of significant

Ans ✓

Practical - 9

Chi Square Distribution and ANOVA

Q) Use the following data to test whether the cleanliness of home is dependent upon other cleanliness condition or not.

		0.f	home
cleaness of child	clean	20	50
	fairly clean	80	20
	dirty	35	45

H₀: condition of home and the child are independent

$$\mathbf{x} = \begin{pmatrix} 20, 80, 35, 20, 45 \end{pmatrix}$$

$$m = 3$$

$$n = 2$$

$$\mathbf{y} = \text{matrix}(\mathbf{x}, \text{nrow} = m, \text{ncol} = n)$$

y

	[1,]	[2,]
[1,]	70	50
[2,]	80	20
[3,]	35	45

p_value = chisq.test(y)

data = y

$\chi^2 = \text{chisq}^2 = 25.646$, df = 2, P-value = 2.6989e-06

Hence p-value is less than 0.5, we reject H₀ at 5% level.

A table below shows the relation performance
b/w mathematics and computer 48

		<u>Maths</u>		
H	MG	MG	L6	
MG	56	71	12	
COMP	MG	47	163	38
L6	14	42	85	

H_0 : Performance in math and computer

$$\gamma x = c(56, 47, 14, 71, 163, 92, 12, 38, 85)$$

$$m = 3$$

$$n = 3$$

$y = \text{matrix}(x, nxow = m, ncol = n)$

y

	[1]	[2]	[3]
[1,]	56	71	12
[2,]	47	163	38
[3,]	14	42	85

$\gamma pvalue = \text{chi2.test}(y)$

$\gamma pvalue$ Pearson's chi-squared test γ

data: y

$\chi^2 = 145.78$, df = 4, pvalue < 2.2e-18

\therefore Since pvalue less than 0.05 we reject H_0 at 5% los

Q=>

Clear
of d

Q=>

→ Perform Anova for the following data.

Varieties	Observations
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

H_0 : The means of variety of A, B, C, D are equal

$\gamma x_1 = c(50, 52)$

$\gamma x_2 = c(53, 55, 53)$

$\gamma x_3 = c(60, 58, 57, 56)$

$\gamma x_4 = c(52, 54, 54, 55)$

$d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$

$\gamma \text{names}(d)$

[1] "values" "ind"

$\gamma \text{oneway.test}(\text{values} \sim \text{ind}, \text{data} = d, \text{var.equal} = \text{F})$

one-way analysis of variance

data: values and ind

F = 12.779, num df = 3, denom df = 10, p-value = 0.007

$\gamma \text{anova} = \text{aov}(\text{values} \sim \text{ind}, \text{data} = d)$

$\gamma \text{summary(anova)}$

	Df	sum sq	mean sq	F value	p value
Gender	1	41.84	20.92	12.78	0.001
Patients	10	19.15	1.915	24.427	0.000

Hence p value is less than 0.05, we reject null hypothesis.

ANOVA

Types observations

A 2, 7, 8

B 4, 6, 5

C 3, 6, 10

D 2, 7, 9

test

$\Rightarrow F_{(3,10)} = 6.25$

$\Rightarrow F_{(3,10)} > F_{(3,10)}$

$\Rightarrow F_{(3,10)} > F_{(3,10)}$

$\Rightarrow F_{(3,10)} > F_{(3,10)}$

$\Rightarrow F_{(3,10)} > F_{(3,10)}$ (because, $F_{(3,10)} > F_{(3,10)}$ and $F_{(3,10)} > F_{(3,10)}$)

Therefore test values = 6.25, taken d.f. same equal
one way analysis of means

Take values and

so $F_{(3,10)} > F_{(3,10)}$, mean \neq 3, because all

02

R

in
Re

(d)

Summary (anova).

	Df	Sum Sq	mean Sq	F value	P > F
Individuals	2	18	6.00	2.667	0.119
Residuals	8	13	1.625		

Type the data in Excel and save on desktop
filename.csv (MS-DOS)

Then open R software and type `x = read.csv("")`
minimise R software then right click on the
file saved on desktop, click on properties,
copy the location and paste it on.

`x = read.csv("` location`")`

Replace \ mix with / then after location add
filename.csv

Enter x

The data within excel sheet will be seen on
R software.

M/

29

12

1

Q

5

Fisher's or 10 → Permutation test.

Following are amount of sulphur dioxide emitted

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.

apply sing test to test hypothesis that population median 21.5 against the alternative it is less than 21.5

H_0 : Population median 21.5

H_1 : It is less than 21.5

$$x = c(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$$

$$m = 21.5$$

$$sp = \text{length}(x[x > m])$$

$$sn = \text{length}(x[x < m])$$

$$n = sp + sn$$

$$pv = \text{pbinom}(sp, n, 0.5)$$

$$pv$$

$$[1] 0.41190915$$

We accept the H_0 .

If the alternative is greater than median

$$pv = \text{pbinom}(sn, n, 0.5)$$

For the observation 12, 19, 31, 28, 43, 40, 55, 49, 70

63. apply sing test to test population median ≥ 25 against the alternative it \geq more than 25.

H_0 : population median 25

H_1 : It \geq more than 25

$$x = c(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$$

$$m = 25$$

Q2

$$sp = \text{length} ([x_1, x_2, \dots, x_n])$$

$$sn = \text{length} ([x_1, x_2, \dots, x_n])$$

$$n = sp + sn$$

$$pv = \text{pbinom}(sp, n, 0.5)$$

0.8

[1]

0.5981903

We reject the H_0 at significance level α if the alternative less than median
 $pv = \text{pbinom}(sn, n, 0.5)$.

Q3. For following data

60, 65, 63, 89, 61, 71, 58, 51, 48, 66. test the hypothesis using wilcoxon signed rank test, for testing hypothesis median is 60 against the alternative it is greater than 60.

Ans:-

H_0 : median is 60

H_1 : It is greater than 60

$$x = C(60, 65, 63, 89, 61, 71, 58, 51, 48, 66)$$

wilcoxon test (x, gr alter="greater", mu=60)

data x

x = 29 , pvalue = 0.2346

alternative hypothesis: true location is greater than

Notes

If alternative is less than

wilcoxon-test (α , alter = "less", mu = 0)

54

If alternative is not equal.

wilcoxon-test (α , alter = "2-sided", mu =).

Using wilcoxon-test the hypothesis median is 12
and against the alternative of less than 12

12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20.

Null: Median is 12
H1: Less than 12

$X = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)$.

wilcoxon-test (α , alter = "less", mu = 12)

wilcoxon signed rank test with continuity correction

data: X

N = 20.5, p-value = 0.1426

alternative hypothesis: True location is less than 12.

20
4.370