

```

close all
clear
clc

% PROBLEM 2 - 2.2

% create figure
figure
axis([-6, 6, -6, 6])
grid on
hold on

% save as a video file
v = VideoWriter('Problem3_2.mp4', 'MPEG-4');
v.FrameRate = 3;
open(v);

epsilon = 0.85;
%initial joint values
theta = [pi/8; pi/8; pi/8; pi/8; pi/8];
L = 1;

omega = [0;0;1];

q1 = [0;0;0];
q2 = [L;0;0];
q3 = [2*L;0;0];
q4 = [3*L;0;0];
q5 = [4*L;0;0];

S1 = [omega; -cross(omega, q1)];
S2 = [omega; -cross(omega, q2)];
S3 = [omega; -cross(omega, q3)];
S4 = [omega; -cross(omega, q4)];
S5 = [omega; -cross(omega, q5)];

S_eq = [S1, S2, S3, S4, S5];
M = [eye(3), [5*L;0;0]; 0 0 0 1];

% T with initial joint positions
T_0 = fk(M, S_eq, theta)

T_0 = 4x4
    -0.3827    -0.9239         0     1.6310
     0.9239    -0.3827         0     3.9375
         0         0     1.0000         0
         0         0         0     1.0000

R_0 = T_0(1:3, 1:3);
JS = double(JacS(S_eq, theta)) %Space Jacobian

```

```
JS = 6x5
    0         0         0         0         0
    0         0         0         0         0
    1.0000    1.0000    1.0000    1.0000    1.0000
    0         0.3827    1.0898    2.0137    3.0137
    0        -0.9239   -1.6310   -2.0137   -2.0137
    0         0         0         0         0
```

```
Jb = double(adjointM(inv(T_0))*JS) %Body Jacobian
```

```
Jb = 6x5
    0         0         0         0         0
    0         0         0         0         0
    1.0000    1.0000    1.0000    1.0000    1.0000
    3.0137    2.0137    1.0898    0.3827         0
    3.0137    3.0137    2.6310    1.9239    1.0000
    0         0         0         0         0
```

```
J_geometric = double([R_0, zeros(3); zeros(3), R_0] * Jb) %Geometric Jacobian
```

```
J_geometric = 6x5
    0         0         0         0         0
    0         0         0         0         0
    1.0000    1.0000    1.0000    1.0000    1.0000
   -3.9375   -3.5549   -2.8478   -1.9239   -0.9239
    1.6310    0.7071   -0.0000   -0.3827   -0.3827
    0         0         0         0         0
```

```
X = [r2axisangle(R_0);T_0(1:3,4)]
```

```
X = 6x1
    0
    0
    1.9635
    1.6310
    3.9375
    0
```

```
% Problem part 2.2
```

```
% Given desired Transformation matrices T_d
```

```
T_d = [rotz(pi/2), [-2;4;0]; 0 0 0 1]
```

```
T_d = 4x4
    0.9996   -0.0274         0   -2.0000
    0.0274    0.9996         0    4.0000
         0         0    1.0000         0
         0         0         0    1.0000
```

```
R_d = T_d(1:3, 1:3);
Xd = [r2axisangle(R_d);T_d(1:3,4)]
```

```
Xd = 6x1
    0
    0
    0.0274
   -2.0000
    4.0000
    0
```

```
V = Xd - X
```

```
V = 6x1
    0
    0
 -1.9361
 -3.6310
  0.0625
    0
```

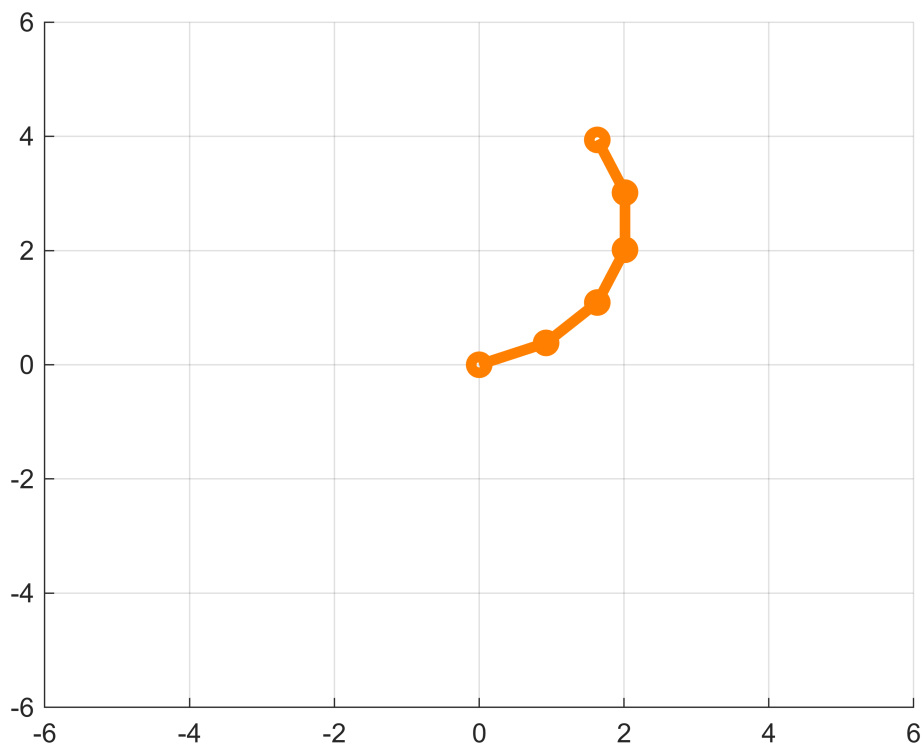
```
while norm(Xd - X) > epsilon
% plot the robot
% 1. get the position of each link
    p0 = [0; 0];
    p1 = [L*cos(theta(1)); L*sin(theta(1))]; % (x,y) position of end of first link
    p2 = [L*cos(theta(1) + theta(2)) + p1(1); L*sin(theta(1) + theta(2)) + p1(2)];
% (x,y) position of end of second link
    p3 = [L*cos(theta(1) + theta(2) + theta(3)) + p2(1); L*sin(theta(1) + theta(2)
+ theta(3)) + p2(2)]; % (x,y) position of end of third link
    p4 = [L*cos(theta(1) + theta(2) + theta(3) + theta(4)) + p3(1); L*sin(theta(1)
+ theta(2) + theta(3) + theta(4)) + p3(2)]; % (x,y) position of end of fourth link
    p_v = [L*cos(theta(1) + theta(2) + theta(3) + theta(4) + theta(5)) + p4(1);
L*sin(theta(1) + theta(2) + theta(3) + theta(4) + theta(5)) + p4(2)]; % (x,y)
position of end-effector
    P_v = [p0, p1, p2, p3, p4, p_v];
% 2. draw the robot and save the frame

    cla;
    plot(P_v(1,:), P_v(2,:), 'o-', 'color',[1, 0.5, 0], 'linewidth',4)
    drawnow
    frame = getframe(gcf);
    writeVideo(v, frame);

% your code here
    V = Xd - X;
    JS = double(JacS(S_eq, theta)); % Updated Space Jacobian
    Jb = double(adjointM(inv(T_0))*JS); %Updated Body Jacobian
    J_geometric = double([R_0, zeros(3); zeros(3), R_0] * Jb); %Updated Geometric
Jacobian
    delta_theta = double(pinv(J_geometric)*V +(eye(5) -
pinv(J_geometric)*J_geometric)*[0;0;0;0;0]) %null space is zero currently as we set
b = 0

    %Updating theta until the while loop is satisfied to get the desired inverse
kinematics (joint positions), thus simulating the robot
    theta = double(0.1 * delta_theta + theta)
    T_0 = fk(M, S_eq, theta)
    R_0 = T_0(1:3, 1:3);
    X = [r2axisangle(R_0);T_0(1:3,4)];

end
```



Warning: The video's width and height has been padded to be a multiple of two as required by the H.264 codec.

delta_theta = 5x1

-2.0384
2.1093
2.9462
0.3450
-5.2982

theta = 5x1

0.1889
0.6036
0.6873
0.4272
-0.1371

T_0 = 4x4

-0.1978	-0.9802	0	1.2475
0.9802	-0.1978	0	3.8200
0	0	1.0000	0
0	0	0	1.0000

delta_theta = 5x1

-0.4784
1.4861
1.5218
-0.6137
-3.6584

theta = 5x1

0.1410
0.7522
0.8395
0.3658
-0.5030

T_0 = 4x4

-0.0248	-0.9997	0	0.9272
0.9997	-0.0248	0	3.7702
0	0	1.0000	0

```

0      0      0      1.0000
delta_theta = 5x1
0.2709
1.2079
0.7480
-0.9455
-2.8496
theta = 5x1
0.1681
0.8730
0.9143
0.2713
-0.7879
T_0 = 4x4
0.1316  -0.9913      0      0.6376
0.9913   0.1316      0      3.7410
0         0      1.0000      0
0         0         0      1.0000
delta_theta = 5x1
0.7827
0.9613
0.1475
-1.0744
-2.2285
theta = 5x1
0.2464
0.9692
0.9290
0.1638
-1.0108
T_0 = 4x4
0.2697  -0.9629      0      0.3720
0.9629   0.2697      0      3.7243
0         0      1.0000      0
0         0         0      1.0000
delta_theta = 5x1
1.1322
0.7033
-0.3194
-1.0773
-1.7091
theta = 5x1
0.3596
1.0395
0.8971
0.0561
-1.1817
T_0 = 4x4
0.3896  -0.9210      0      0.1286
0.9210   0.3896      0      3.7163
0         0      1.0000      0
0         0         0      1.0000
delta_theta = 5x1
1.3558
0.4326
-0.6561
-0.9983
-1.2772
theta = 5x1
0.4952
1.0827
0.8315
-0.0437
-1.3094

```

```

T_0 = 4x4
  0.4921  -0.8706      0  -0.0927
  0.8706   0.4921      0   3.7145
      0      0  1.0000      0
      0      0      0  1.0000
delta_theta = 5x1
  1.4869
  0.1617
 -0.8752
 -0.8720
 -0.9302
theta = 5x1
  0.6439
  1.0989
  0.7440
 -0.1309
 -1.4024
T_0 = 4x4
  0.5789  -0.8154      0  -0.2925
  0.8154   0.5789      0   3.7173
      0      0  1.0000      0
      0      0      0  1.0000
delta_theta = 5x1
  1.5556
 -0.0967
 -1.0011
 -0.7229
 -0.6609
theta = 5x1
  0.7994
  1.0892
  0.6439
 -0.2032
 -1.4685
T_0 = 4x4
  0.6518  -0.7584      0  -0.4717
  0.7584   0.6518      0   3.7232
      0      0  1.0000      0
      0      0      0  1.0000
delta_theta = 5x1
  1.5873
 -0.3369
 -1.0617
 -0.5655
 -0.4566
theta = 5x1
  0.9582
  1.0556
  0.5377
 -0.2598
 -1.5142
T_0 = 4x4
  0.7127  -0.7015      0  -0.6318
  0.7015   0.7127      0   3.7309
      0      0  1.0000      0
      0      0      0  1.0000
delta_theta = 5x1
  1.6029
 -0.5617
 -1.0819
 -0.4055
 -0.3040
theta = 5x1
  1.1185

```

```

0.9994
0.4295
-0.3003
-1.5446
T_0 = 4x4
0.7632 -0.6461 0 -0.7743
0.6461 0.7632 0 3.7394
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5x1
1.6214
-0.7832
-1.0808
-0.2406
-0.1920
theta = 5x1
1.2806
0.9211
0.3214
-0.3244
-1.5638
T_0 = 4x4
0.8051 -0.5932 0 -0.9009
0.5932 0.8051 0 3.7479
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5x1
1.6630
-1.0249
-1.0710
-0.0594
-0.1153
theta = 5x1
1.4469
0.8186
0.2143
-0.3303
-1.5753
T_0 = 4x4
0.8396 -0.5432 0 -1.0128
0.5432 0.8396 0 3.7554
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5x1
1.7554
-1.3331
-1.0573
0.1668
-0.0786
theta = 5x1
1.6225
0.6853
0.1086
-0.3136
-1.5832
T_0 = 4x4
0.8680 -0.4965 0 -1.1111
0.4965 0.8680 0 3.7609
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5x1
1.9510
-1.8177
-1.0240

```

```

0.5158
-0.1172
theta = 5×1
1.8176
0.5035
0.0062
-0.2620
-1.5949
T_0 = 4×4
0.8914 -0.4532 0 -1.1955
0.4532 0.8914 0 3.7619
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5×1
2.3703
-2.8380
-0.8243
1.2789
-0.4298
theta = 5×1
2.0546
0.2197
-0.0762
-0.1342
-1.6379
T_0 = 4×4
0.9106 -0.4133 0 -1.2617
0.4133 0.9106 0 3.7516
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5×1
2.4824
-6.0518
2.0930
4.4540
-3.3763
theta = 5×1
2.3028
-0.3855
0.1331
0.3112
-1.9755
T_0 = 4×4
0.9264 -0.3766 0 -1.2541
0.3766 0.9264 0 3.6514
0 0 1.0000 0
0 0 0 1.0000
delta_theta = 5×1
-0.5774
2.6534
-1.2700
-2.7358
1.5711
theta = 5×1
2.2451
-0.1201
0.0061
0.0377
-1.8184
T_0 = 4×4
0.9393 -0.3432 0 -1.3056
0.3432 0.9393 0 3.6483
0 0 1.0000 0
0 0 0 1.0000

```



```
close(v);  
close all
```