

```
% General dynamics of a robot example
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```
clc;
clear;
```

```
syms L g m1 m2 theta1 theta2 theta1_dot theta2_dot theta1_dot_dot theta2_dot_dot
Ix1 Ix2 Ix3 Iy1 Iy2 Iy3 Iz1 Iz2 real
```

```
theta = [theta1; theta2];
thetadot = [theta1_dot; theta2_dot];
thetadotdot = [theta1_dot_dot; theta2_dot_dot];
M1 = [eye(3), [0;0;0]; 0 0 0 1]; % home matrix for link 1
M2 = [eye(3), [L;0;0]; 0 0 0 1]; % home matrix for link 2
```

```
S1 = [0;0;0;1;0;0]; % Prismatic joint
S2 = [0;0;1;0;0;0]; % Revolute joint
```

```
S_eq1 = [S1, [0;0;0;0;0;0]]; % First focus: till first center of mass, a.k.a S2 == 0
S_eq2 = [S1, S2]; % Second focus: till second center of mass, a.k.a S1 == S1, S2 == S2 ... continued
```

```
T_1 = fk(M1, S_eq1, theta);
R_1 = T_1(1:3, 1:3);
JS_1 = simplify(expand(JacS(S_eq1, theta))); % Space Jacobian
Jb_1 = double(adjointM(inv(T_1))*JS_1); % Body Jacobian
J_geometric_1 = simplify(expand([R_1, zeros(3); zeros(3), R_1] * Jb_1)); %
Geometric Jacobian
Jw1 = J_geometric_1(1:3,1:2);
Jv1 = J_geometric_1(4:6, 1:2);
Inertia_1 = [[Ix1 0 0]
              [0 Iy1 0]
              [0 0 Iz1]];
```

```
T_2 = fk(M2, S_eq2, theta)
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```
T_2 =

$$\begin{pmatrix} \cos(\theta_2) & -\sin(\theta_2) & 0 & \theta_1 + L \cos(\theta_2) \\ \sin(\theta_2) & \cos(\theta_2) & 0 & L \sin(\theta_2) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

```

```
R_2 = T_2(1:3, 1:3);
JS_2 = simplify(expand(JacS(S_eq2, theta))); % Space Jacobian
Jb_2 = adjointM(inv(T_2))*JS_2; % Body Jacobian
J_geometric_2 = simplify(expand([R_2, zeros(3); zeros(3), R_2] * Jb_2)); %
Geometric Jacobian
Jw2 = J_geometric_2(1:3,1:2);
```

```
Jv2 = J_geometric_2(4:6, 1:2);
```

```
Inertia_2 = [[Ix2 0 0]
              [0 Iy2 0]
              [0 0 Iz2]];
```

```
Mass_Matrix = simplify(expand(m1*(Jv1'*Jv1) + Jw1'*R_1*Inertia_1*R_1'*Jw1 +
m2*(Jv2'*Jv2) + Jw2'*R_2*Inertia_2*R_2'*Jw2))
```

```
Mass_Matrix =
```

$$\begin{pmatrix} m_1 + m_2 & -L m_2 \sin(\theta_2) \\ -L m_2 \sin(\theta_2) & m_2 L^2 + I_{z_2} \end{pmatrix}$$

```
Coriolis_Matrix = simplify(coriolis(Mass_Matrix, theta, thetadot))
```

```
Coriolis_Matrix =
```

$$\begin{pmatrix} 0 & -L m_2 \dot{\theta}_2 \cos(\theta_2) \\ 0 & 0 \end{pmatrix}$$

```
h1 = T_1(2, 4)
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```
h1 = 0
```

```
h2 = T_2(2, 4)
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```
h2 = L sin(theta_2)
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```
P = g*m1*h1 + g*m2*h2;
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```
gravity_vector = [diff(P, theta1); diff(P, theta2)]
```

```
gravity_vector =
```

$$\begin{pmatrix} 0 \\ L g m_2 \cos(\theta_2) \end{pmatrix}$$

```
tau = (Mass_Matrix*thetadotdot + Coriolis_Matrix*thetadot + gravity_vector)
```

```
tau =
```

$$\begin{pmatrix} -L m_2 \cos(\theta_2) \dot{\theta}_2^2 + \theta_1; (m_1 + m_2) - L m_2 \dot{\theta}_2 \sin(\theta_2) \\ \theta_2; (m_2 L^2 + I_{z_2}) + L g m_2 \cos(\theta_2) - L m_2 \dot{\theta}_1 \sin(\theta_2) \end{pmatrix}$$