

# Zero Knowledge Proof (ZKP) Explanation and Verification

## 1. What is Zero Knowledge Proof (ZKP)?

Zero Knowledge Proof (ZKP) is a cryptographic method where one party (the **Prover**) proves to another party (the **Verifier**) that they know a secret, **without revealing the secret itself**.

**Example:** - Imagine you're trying to prove you know the password to a vault without saying the password. Instead, you show actions that can only be performed by someone who knows the password. This concept is at the heart of ZKP.

ZKPs are used in various real-world applications like secure authentication, blockchain, and privacy-preserving systems.

## 2. High-Level Overview of the Process

The process of a Zero Knowledge Proof consists of the following steps:

1. **Setup Phase:** A large prime number  $p$  and a generator  $g$  are shared between the Prover (Peggy) and Verifier (Victor). The Prover knows the secret  $x$  (the password).
2. **Commitment:** The Prover computes a value  $y = g^x \mod p$  and sends it to the Verifier. This is the public commitment tied to the secret.
3. **Challenge:** The Verifier sends a random challenge value  $c$  to the Prover.
4. **Response:** The Prover computes a response using  $c$ , their secret  $x$ , and another random value  $v$ . The Prover then sends this response back to the Verifier.
5. **Verification:** The Verifier checks if the response is correct by using the public values  $g$ ,  $y$ , and  $p$ . If the response is valid, the Verifier is convinced that the Prover knows the secret, but the secret  $x$  is never revealed.

## 3. How Does It Ensure Authenticity?

ZKP ensures authenticity through the following principles:

- **Challenge-Response Mechanism:** The random challenge  $c$  ensures that the Prover cannot fake knowledge. If the Prover does not know  $x$ , they cannot generate a correct response consistently.
- **No Information Leak:** Only public values ( $p$ ,  $g$ , and  $y$ ) and a one-time challenge-response pair are exchanged. The Verifier learns nothing about

### 1. Start with the LHS (Verifier's Computation)

The Verifier computes the Left-Hand Side:

$$\text{LHS} = g^r \cdot y^c \mod p$$

### 2. Substitute $y = g^x \mod p$

Substitute the definition of  $y$  into  $y^c$ :

$$\text{LHS} = g^r \cdot (g^x)^c \mod p$$

### 3. Simplify $(g^x)^c$

Using the power rule  $(a^b)^c = a^{b \cdot c}$ , we have:

$$(g^x)^c = g^{x \cdot c} \mod p$$

Substituting this back:

$$\text{LHS} = g^r \cdot g^{x \cdot c} \mod p$$

### 4. Combine the Exponents

Using the rule  $a^m \cdot a^n = a^{m+n}$ :

$$\text{LHS} = g^{r+x \cdot c} \mod p$$

### 5. Substitute $r = v - c \cdot x \mod (p-1)$

Now, replace  $r$  with the Prover's response  $r = v - c \cdot x \mod (p-1)$ :

$$\text{LHS} = g^{(v-c \cdot x)+c \cdot x} \mod p$$

Simplify the exponent:

$$\text{LHS} = g^v \mod p$$

## 6. Compare with the RHS

The Prover sent  $t = g^v \bmod p$  to the Verifier. Thus:

$$\text{LHS} = \text{RHS} = g^v \bmod p$$

## 5. Conclusion

The equation holds because:

- $r = v - c \cdot x \bmod (p-1)$  ensures the Prover's response encodes the secret  $x$ .
- The LHS combines  $g^r$  and  $y^c$ , reconstructing  $g^v$  without exposing  $x$ .

By proving  $\text{LHS} = \text{RHS}$ , the Verifier is convinced the Prover knows  $x$ , without learning  $x$  itself.

## 7. Addressing Questions

**Q: How does this ensure security?** The challenge-response mechanism ensures that each round is unique. Without knowing the secret  $x$ , it is computationally infeasible to generate a valid response.

**Q: What if someone intercepts the data?** Even if someone intercepts the public values or the challenge, they cannot derive the secret  $x$  from the intercepted data alone.

Secure Coding Practices Applied in the Project

## Secure Coding Practices Applied in the Project

Below are the secure coding practices applied in the project setup, ensuring it is resistant to common vulnerabilities:

### 1 Modularization

**Practice:** The project is broken into multiple phases, each handling a specific task (e.g., key generation, hashing, authentication).

**Why it's secure:** Modularization prevents monolithic code that's harder to debug and secure. Each phase can be independently verified and updated, minimizing risks of unintended side effects.

## 2 Use of Cryptographic Techniques

**Practice:** Secure password hashing and modular arithmetic are used (e.g.,  $g^x \bmod p$ ).

**Why it's secure:**

- Passwords are **never stored in plaintext**; only their hashed versions are used.
- The use of large prime numbers  $p$  and secure generators  $g$  ensures cryptographic strength, making brute-force attacks computationally infeasible.

## 3 Zero-Knowledge Proof (ZKP) Design

**Practice:** The algorithm ensures that sensitive information (e.g., the password  $x$ ) is never transmitted directly.

**Why it's secure:**

- Even if an attacker intercepts communications, they cannot reconstruct  $x$ , thanks to modular arithmetic and random challenges.

## 4 Secure Randomness

**Practice:** The use of random challenges  $c$ , private values  $v$ , and primes ensures non-repetition in cryptographic operations.

**Why it's secure:**

- Randomized values prevent replay attacks and ensure that the proof is unique for every interaction.

## 5 Defense Against Replay Attacks

**Practice:** Random values (like  $c$ ) are generated fresh for each verification attempt.

**Why it's secure:** If an attacker tries to replay previously captured messages, the verification process will fail because the challenges and responses won't align.

## 6 Safe Handling of File Operations

**Practice:** File reading and writing operations are error-checked (e.g., verifying file existence and handling `FileNotFoundException`).

**Why it's secure:**

- Prevents crashes or undefined behavior if files like `status.txt` are missing or corrupted.

- Helps mitigate **path traversal attacks** by using hardcoded file paths and limited file operations.

## 7 Use of Python Subprocess for External Programs

**Practice:** The `subprocess` module is used to invoke external programs (e.g., C++ binaries) in a controlled way.

**Why it's secure:** This approach prevents shell injection vulnerabilities by separating the command and arguments safely (e.g., `subprocess.Popen(["./program", "arg"])`).

## 8 Input Validation

**Practice:** User inputs (e.g., phase choices in `main.cpp`) are validated for correctness.

**Why it's secure:**

- Reduces the risk of undefined behavior or improper program execution caused by invalid inputs.

## 9 Error Handling

**Practice:** Proper error handling ensures the program gracefully handles issues like invalid inputs, missing files, or failed subprocess executions.

**Why it's secure:**

- Prevents crashes and potential exploits caused by unhandled exceptions.

## 10 Least Privilege

**Practice:** The code follows the principle of least privilege, where only necessary actions are performed for each phase.

**Why it's secure:**

- Reduces the attack surface and ensures no unnecessary sensitive operations are exposed.

## 11 Explicitly Compiled C++ Programs

**Practice:** Each C++ phase is precompiled into binaries (e.g., `connections.exe`, `phase4.exe`).

**Why it's secure:**

- Precompiled code minimizes the risk of source code tampering and ensures consistent behavior during execution.

## 12 GUI Feedback

**Practice:** The GUI provides clear feedback on the status of each phase (e.g., connection status, password hashing, etc.).

**Why it's secure:**

- Helps users quickly detect anomalies (e.g., if connections are not established or a phase fails).

## 13 Avoidance of Hardcoded Secrets

**Practice:** No secrets (e.g., passwords or keys) are hardcoded in the source code.

**Why it's secure:**

- Protects against reverse-engineering attacks that aim to extract sensitive information.

## Conclusion

These practices collectively ensure that the project is resistant to a wide range of vulnerabilities and adheres to secure coding standards. If you would like, I can help refine specific parts of the code to strengthen it further.