

Chapter 4

Machine Language

These slides support chapter 4 of the book

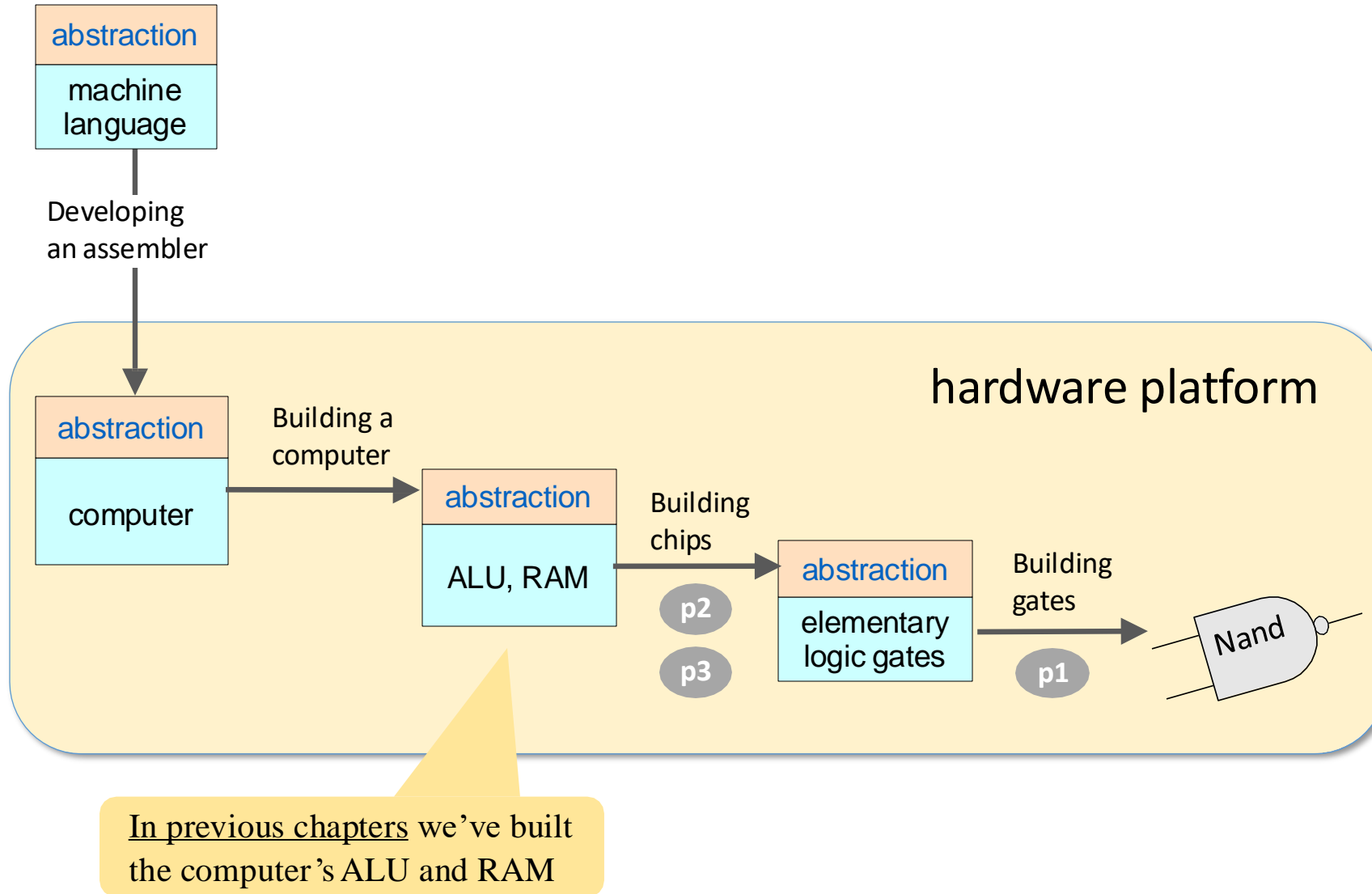
The Elements of Computing Systems

(1st and 2nd editions)

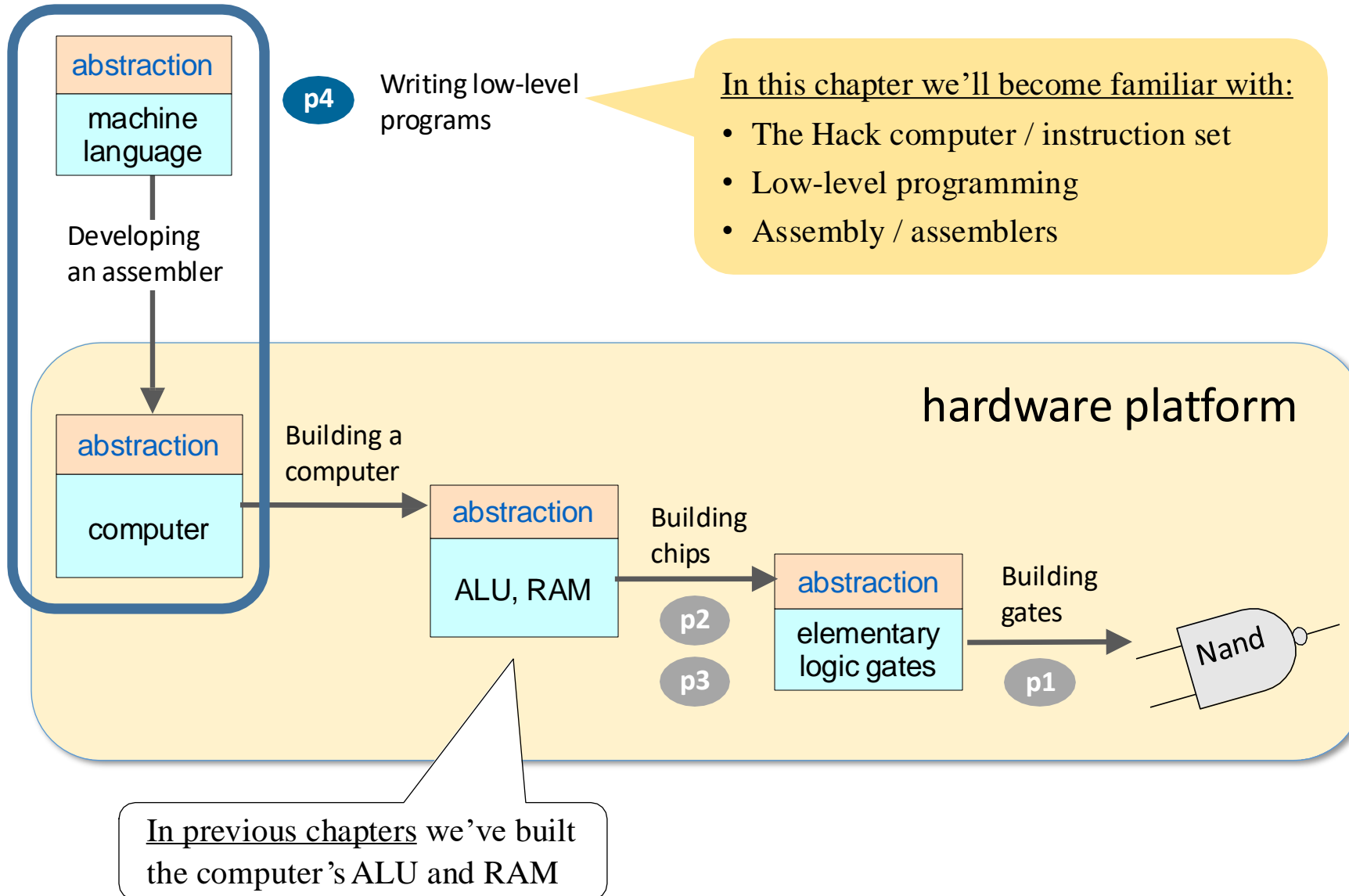
By Noam Nisan and Shimon Schocken

MIT Press

Nand to Tetris Roadmap (Part I: Hardware)



Nand to Tetris Roadmap (Part I: Hardware)



Computers are flexible and versatile

Same **hardware** can run many different programs (**software**)

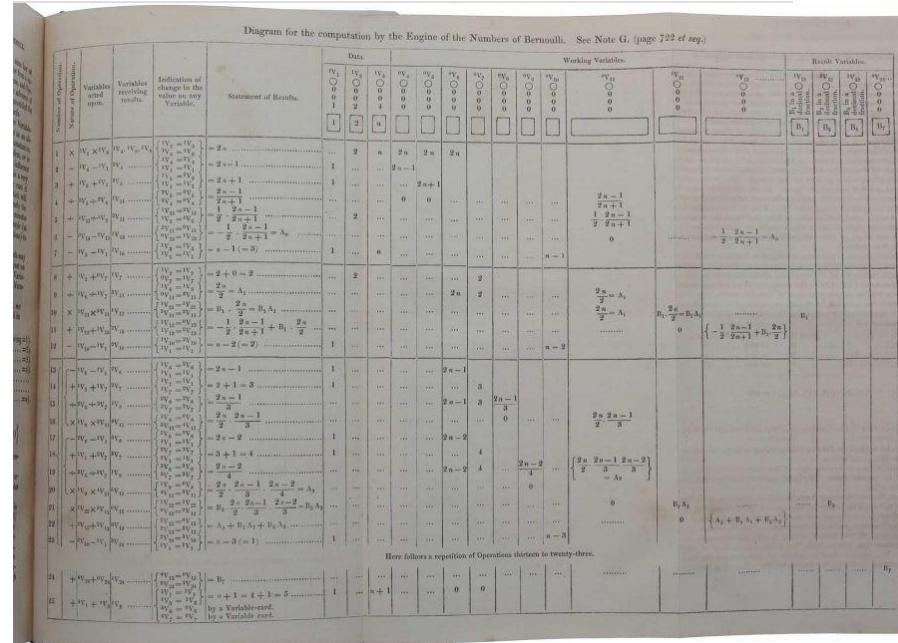


Computers are flexible and versatile

Same **hardware** can run many different programs (**software**)



Ada Lovelace
(1843)



Early symbolic program

Landmark “proof of concept” that computers
can be programmed

Computers are flexible and versatile

Same **hardware** can run many different programs (**software**)



Alan Turing
(1936)

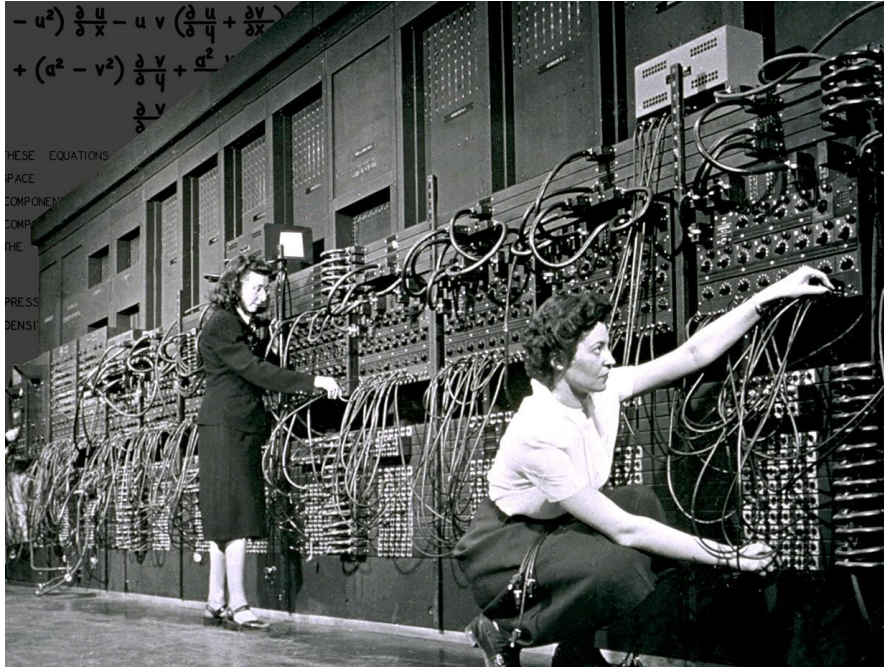
1936.]	ON COMPUTABLE NUMBERS.	245
sim	$f'(sim_1, sim_1, z)$	sim . The machine marks out the instructions. That part of the instructions which refers to operations to be carried out is marked with u , and the final m -configuration with y . The letters z are erased.
sim_1	$con(sim_2,)$	
sim_2	$\begin{cases} A & sim_3 \\ not A & R, Pu, R, R, R & sim_2 \end{cases}$	
sim_3	$\begin{cases} not A & L, Py & c(mf, z) \\ A & L, Py, R, R, R & sim_3 \end{cases}$	
mf	$g(mf, :)$	mf . The last complete configuration is marked out into four sections. The configuration is left unmarked. The symbol directly preceding it is marked with x . The remainder of the complete configuration is divided into two parts, of which the first is marked with v and the last with w . A colon is printed after the whole. $\rightarrow sh$.
mf_1	$\begin{cases} not A & R, R & mf_1 \\ A & L, L, L, L & mf_2 \end{cases}$	
mf_2	$\begin{cases} C & R, Px, L, L, L & mf_2 \\ : & & mf_4 \\ D & R, Px, L, L, L & mf_3 \end{cases}$	
mf_3	$\begin{cases} not : & R, Pv, L, L, L & mf_3 \\ : & & mf_4 \end{cases}$	

Universal Turing Machine

Landmark article, describing a theoretical general-purpose computer

Computers are flexible and versatile

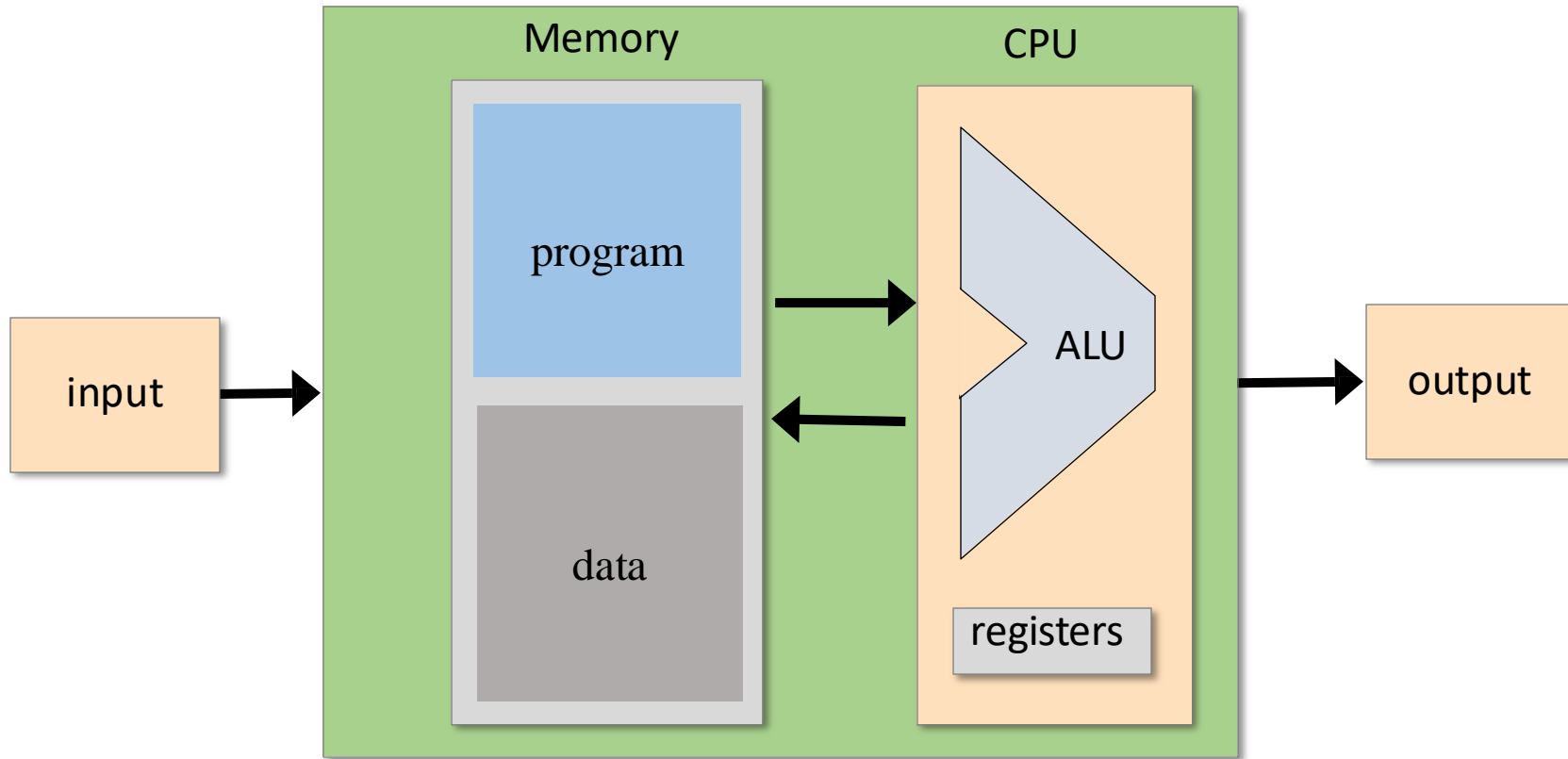
Same **hardware** can run many different programs (**software**)



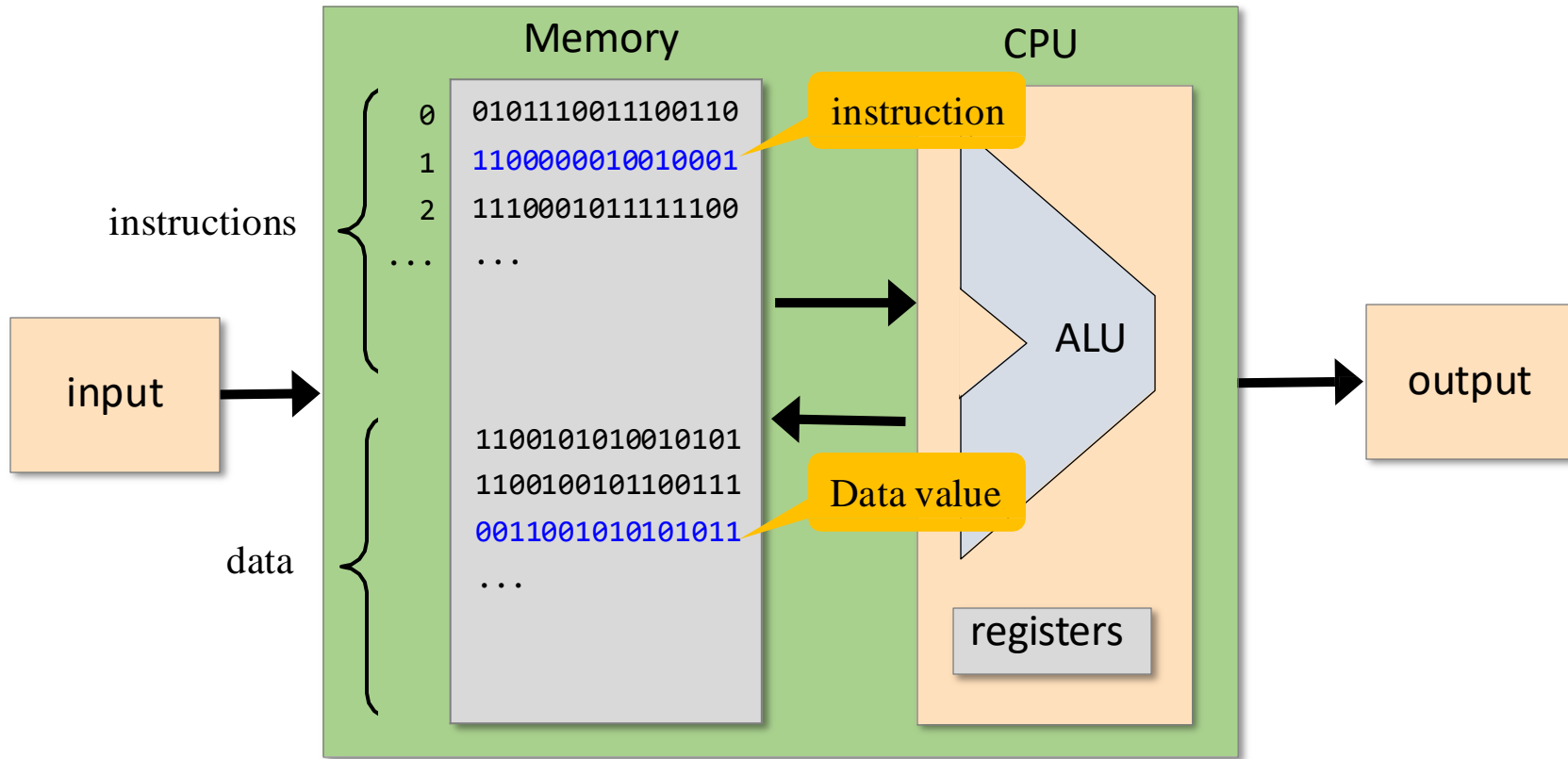
First general-purpose computer

Eniac, University of Pennsylvania, 1945

Computer architecture



Computer architecture



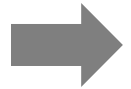
Stored program concept

- The computer memory can store programs, just like it stores data
- Programs = data.

One of the most important ideas in the history of computer science

Chapter 4: Machine Language

Overview



Machine languages

- The Hack computer
- The Hack instruction set
- The Hack CPU Emulator

Low Level Programming

- Basic
- Iteration
- Pointers

Symbolic programming

- Control
- Variables
- Labels

The Hack Language

- Usage
- Specification
- Output
- Input
- Project 4

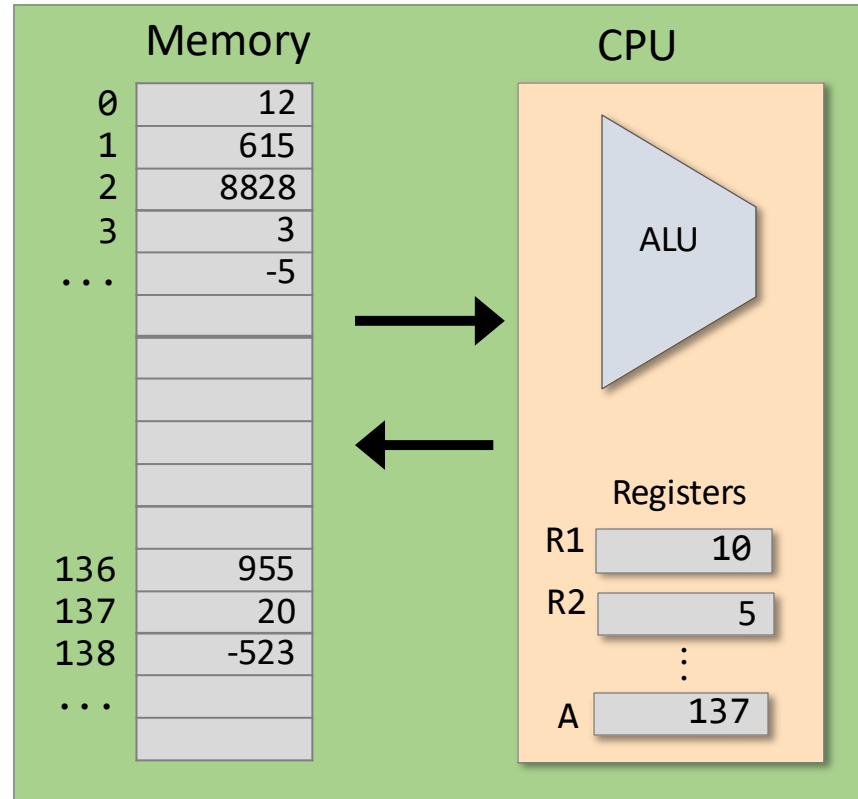
Machine Language

Computer

(Conceptual definition):

A *processor* (CPU) that manipulates a set of *registers*:

- CPU-resident registers
(few, accessed directly, by name)
- Memory-resident registers
(many, accessed by supplying an address)



Machine language

A formalism specifying how to access and manipulate registers.

Registers

Data registers:

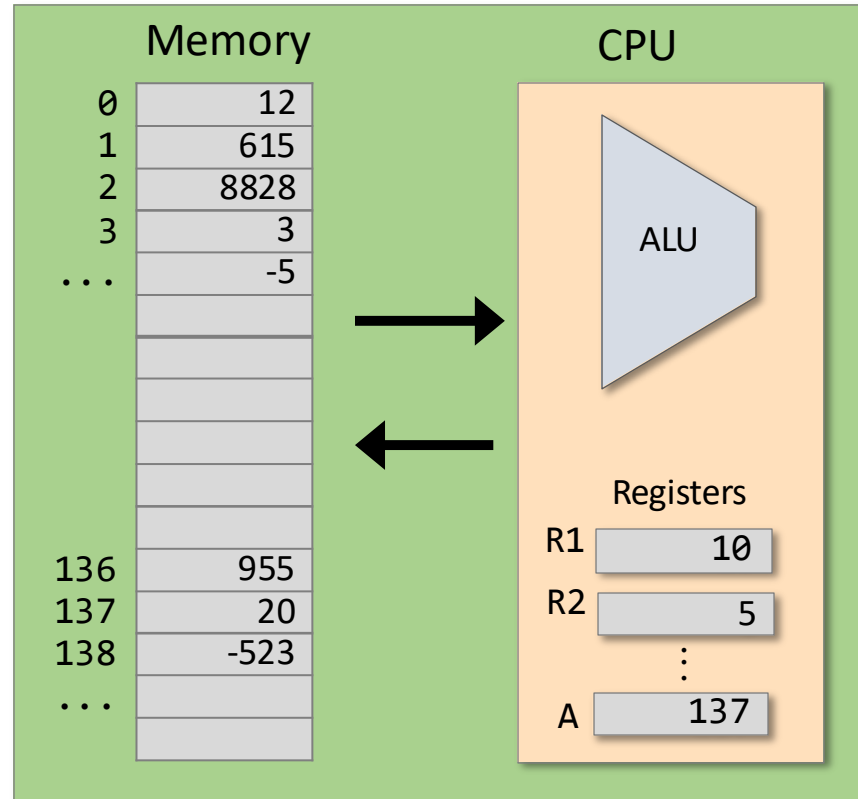
Hold data values

Address register:

Holds an address

Instruction register:

Holds an instruction



- All these registers are... registers (containers that hold bits)
- The number and bit-width of the registers vary greatly from one computer to another.

Typical operations

// $R1 \leftarrow 73$

load R1, 73

// $R1 \leftarrow R1 + R2$

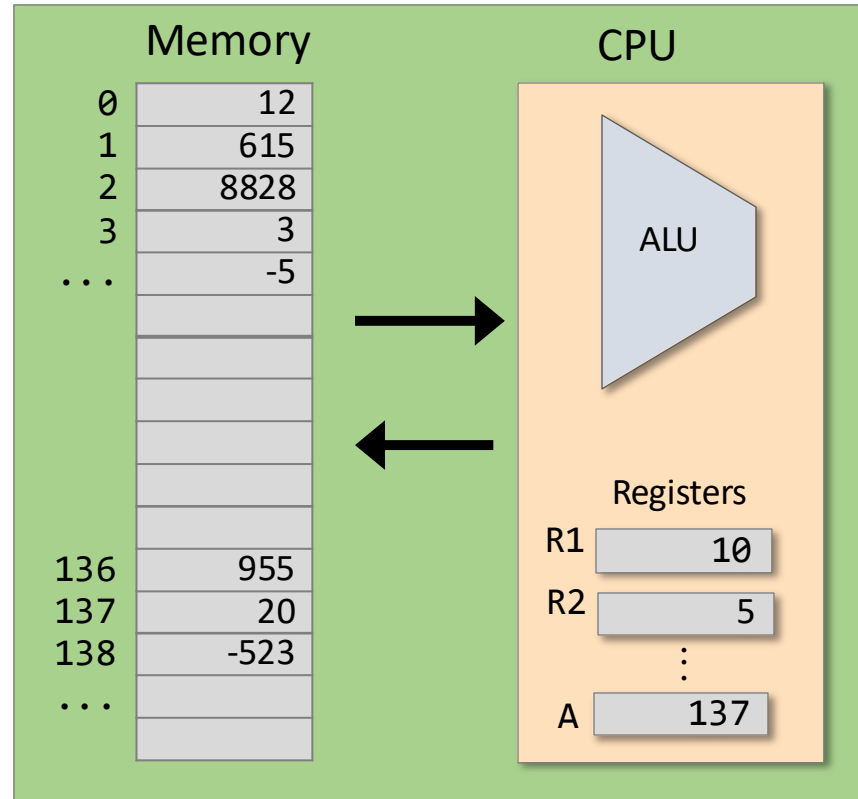
add R1, R2

// $R1 \leftarrow R1 + \text{Memory}[137]$

add R1, M[137]

// $R1 \leftarrow \text{Memory}[A]$

load R1, @A

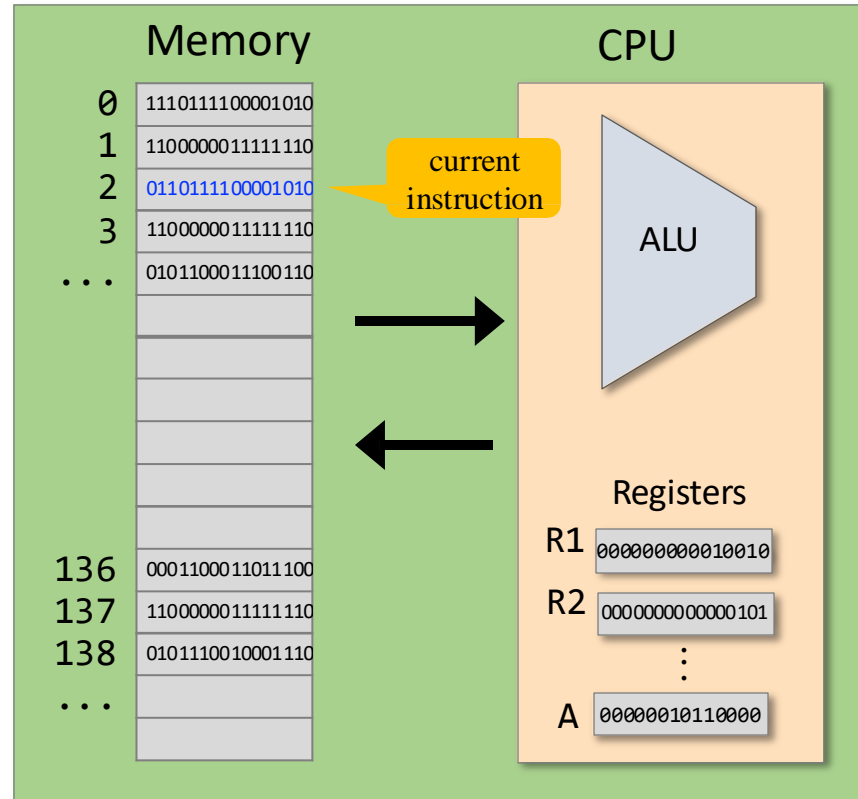


The syntax of machine languages varies greatly from one computer to another, but all of them are designed to do the same thing: Manipulate registers.

Control

Which instruction should be executed next?

- By default, the CPU executes the *next instruction*
- Sometimes we want to “jump” to execute another instruction



Control

Unconditional branching

- Execute some instruction other than the next one
- Example: Embarking on a new iteration in a loop

Basic version

```
...  
// Adds 1 to R1, repetitively  
13  add R1,1  
...  ...  
27  goto 13  
...  ...
```

- Line numbers
- Physical addresses

Symbolic version

```
...  
// Adds 1 to R1, repetitively  
(LOOP)  
add R1,1  
...  
goto LOOP  
...
```

- No line numbers
- Symbolic addresses

Programs with symbolic references are ...

- Easier to develop
- Readable
- Relocatable.

Control

Conditional branching

Sometimes we want to “jump” to execute another instruction, but only if a certain condition is met

Symbolic program

```
// Set R1 to abs(R1).  
// if R1 > 0 goto CONT  
jgt R1, CONT  
  
// R1 ← -R1  
store R2, R1  
store R1, 0  
subt R1, R2  
  
CONT:  
// Here R1 is non-negative  
...
```

How can we actually execute the program?

Control

Conditional branching

Sometimes we want to “jump” to execute another instruction, but only if a certain condition is met

Symbolic program

```
// Set R1 to abs(R1).  
// if R1 > 0 goto CONT  
jgt R1, CONT  
  
// R1 ← -R1  
store R2, R1  
store R1, 0  
subt R1, R2  
  
CONT:  
// Here R1 is non-negative  
...
```

Assembly

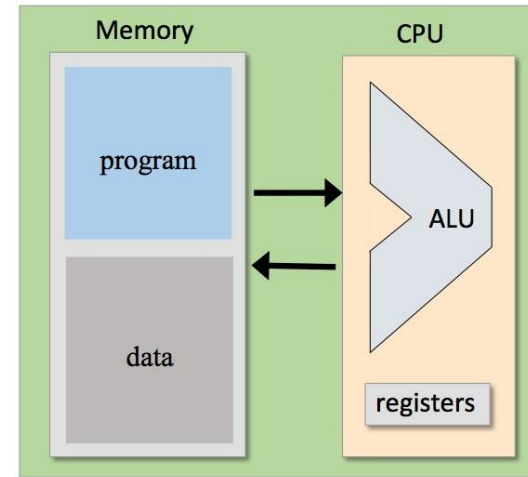
Binary code

```
0101111100111100  
1010101010101010  
1100000010101010  
1011000010000001  
...
```

Assembler

translate

load and
execute



Chapter 4: Machine Language

Overview



Machine languages



The Hack computer

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- The Hack CPU Emulator

Low Level Programming

- Basic
- Iteration
- Pointers

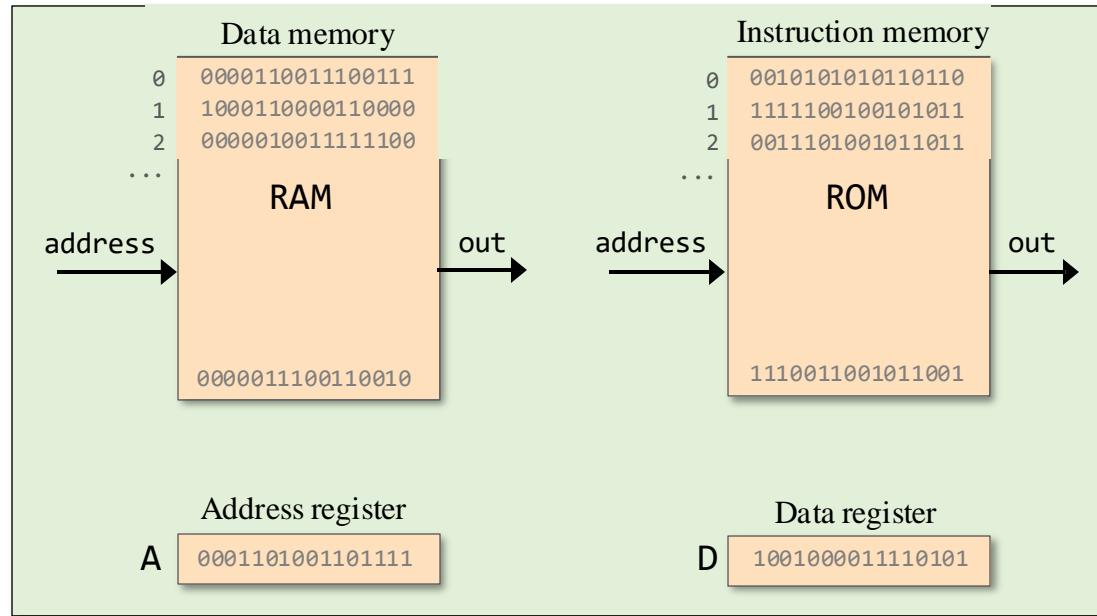
Symbolic programming

- Control
- Variables
- Labels

The Hack Language

- Usage
- Specification
- Output
- Input
- Project 4

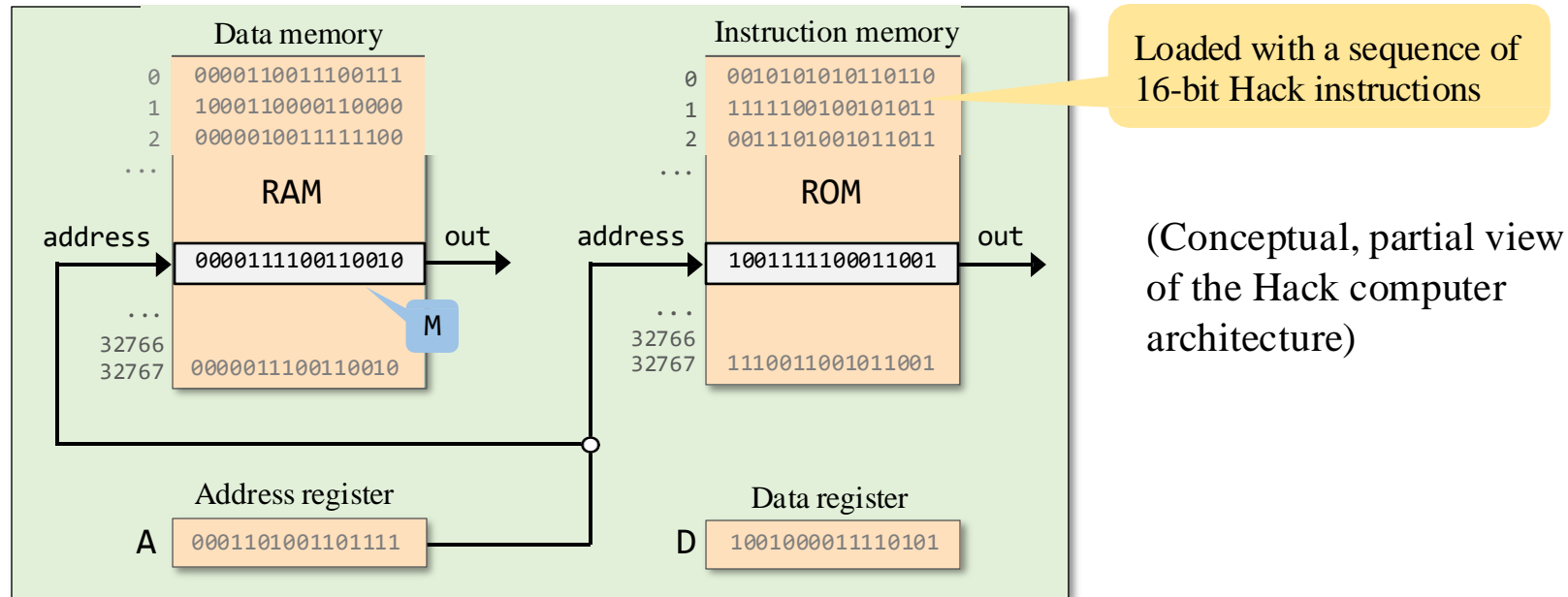
The Hack computer



(Conceptual, partial view
of the Hack computer
architecture)

- Hack is a 16-bit computer, featuring two memory units
- The address input of each memory unit is 15-bit wide
- **Question:** How many words can each memory unit have?
- **Answer:** The *address space* of each memory unit is $2^{15} = 32\text{K}$ words.

Memory



RAM

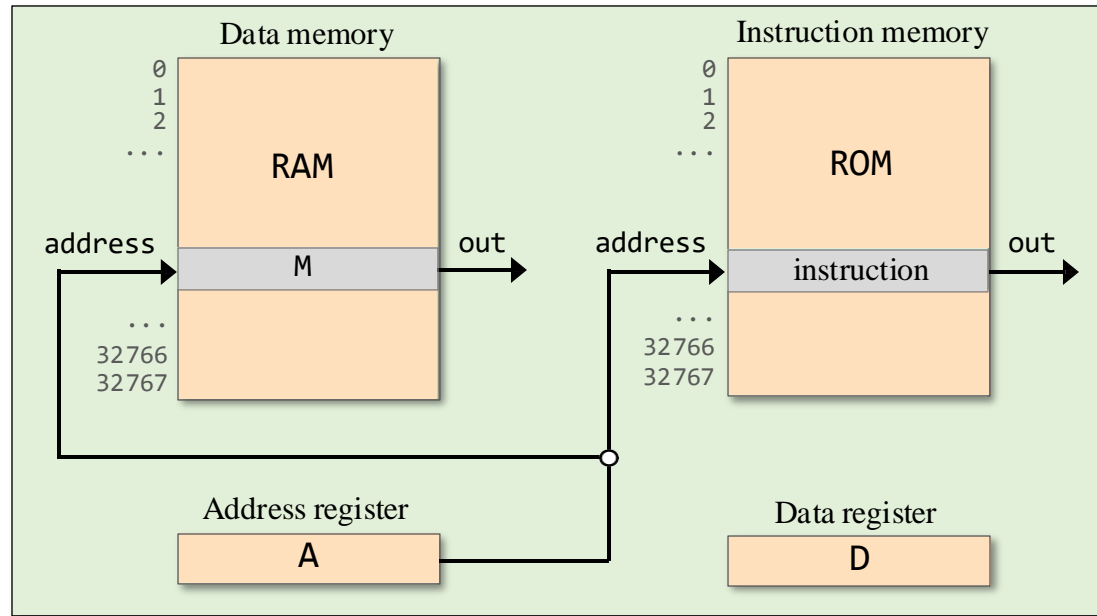
- Read-write data memory
- Addressed by the A register
- The selected register, $\text{RAM}[A]$, is represented by the symbol *M*

ROM

- Read-only instruction memory
- Addressed by the (same) A register
- The selected register, $\text{ROM}[A]$, contains the “current instruction”

- Should we focus on $\text{RAM}[A]$, or on $\text{ROM}[A]$?
- Depends on the current instruction (later)

Registers



(Conceptual, partial view
of the Hack computer
architecture)

D: data register

A: address register

M: the selected RAM register

Chapter 4: Machine Language

Overview



Machine languages



The Hack computer



The Hack instruction set

- The Hack CPU Emulator

Symbolic programming

- Control
- Variables
- Labels

Low Level Programming

- Basic
- Iteration
- Pointers

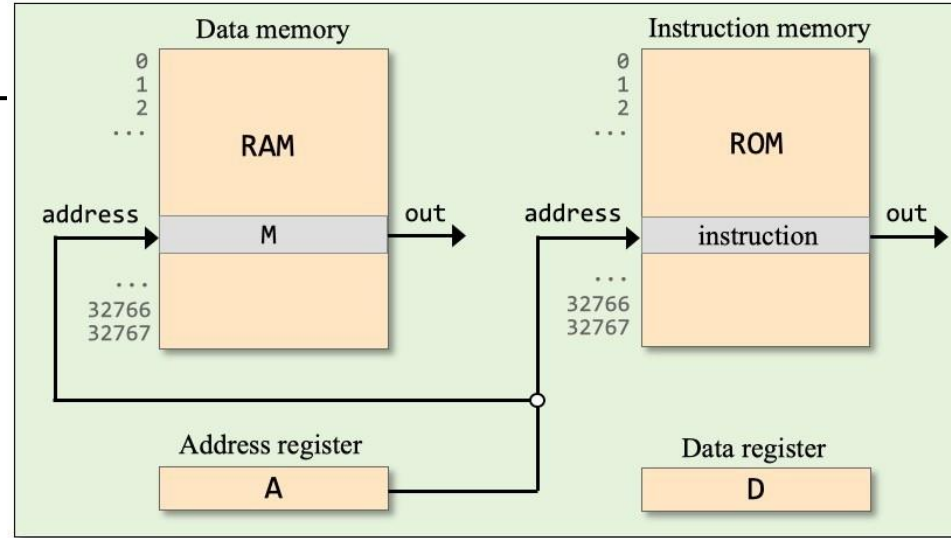
The Hack Language

- Usage
- Specification
- Output
- Input
- Project 4

Hack instructions

Instruction set

- ➔ A instruction
- C instruction



Syntax:

@const

where *const* is
a constant

(Complete / formal syntax, later).

Example:

@19

Semantics:

$A \leftarrow 19$

Side effects:

- RAM[A] (called M) becomes selected
- ROM[A] becomes selected

Hack instructions

Instruction set

- A instruction

- 
- C instruction

Syntax:

$reg = \{0|1|-1\}$

where $reg = \{A|D|M\}$

$reg_1 = reg_2$

where $reg_1 = \{A|D|M\}$

$reg_2 = [-]\{A|D|M\}$

$reg = reg_1 \text{ op } reg_2$

where $reg, reg_1 = \{A|D|M\}$, $op = \{+|- \}$, and
 $reg_2 = \{A|D|M|1\}$ and $reg_1 \neq reg_2$

Examples:

D=0

A=-1

M=1

...

D=A

D=M

M=-M

...

D=D+M

A=A-1

M=D+1

...

(Complete / formal
syntax, later).

Hack instructions

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

$D = 1$

$D = A$

$D = D + 1$

...

$D = D + A$

$D = M$

$M = 0$

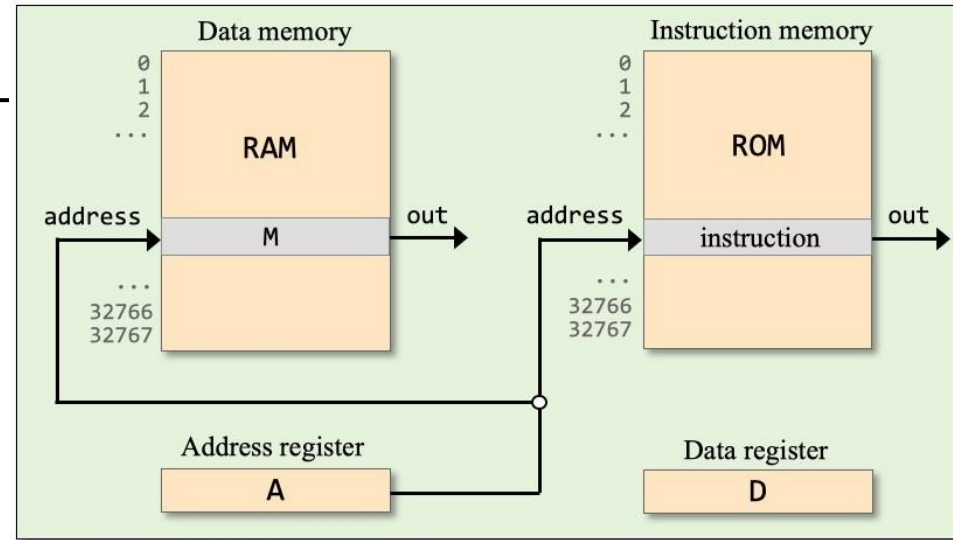
...

$M = D$

$D = D + A$

$M = M - D$

...



Examples:

// $D \leftarrow 2$

?

The game: We show some typical Hack instructions (top left), and practice writing code examples that use subsets of these instructions.

Hack instructions

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

$D = 1$

$D = A$

$D = D + 1$

...

$D = D + A$

$D = M$

$M = 0$

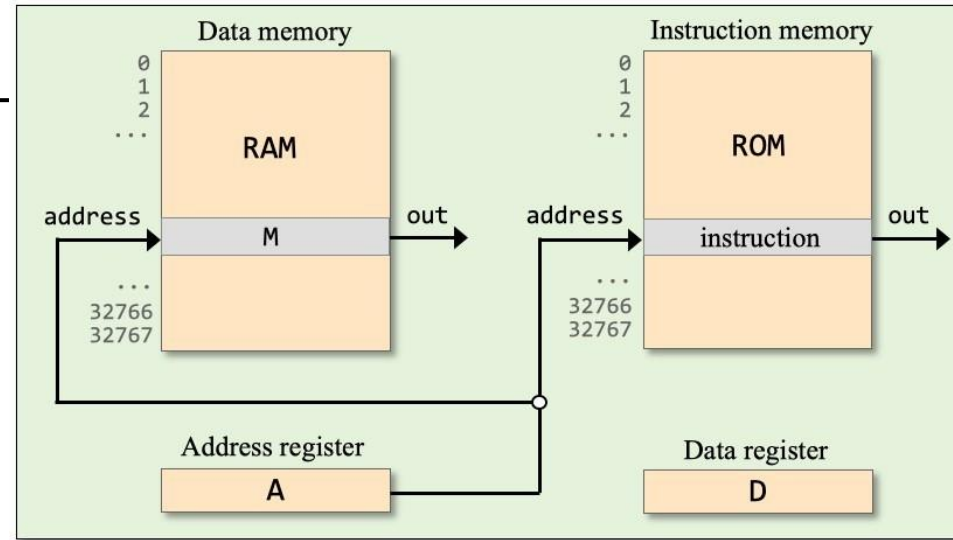
...

$M = D$

$D = D + A$

$M = M - D$

...



Examples:

`// D ← 2`

$D = 1$

$D = D + 1$

`// D ← 1954`

?

Use only the instructions
shown in this slide

Hack instructions

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

`D=1`

`D=A`

`D=D+1`

`...`

`D=D+A`

`D=M`

`M=0`

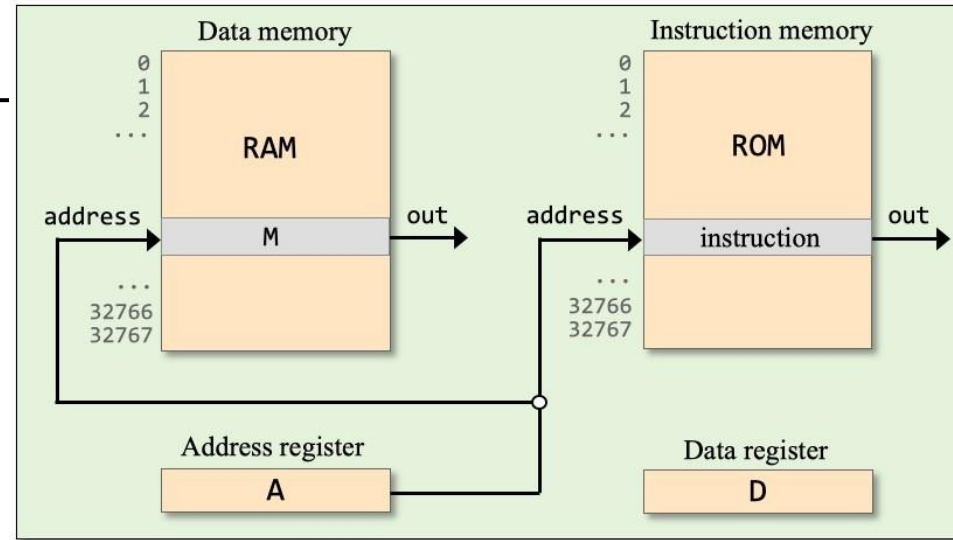
`...`

`M=D`

`D=D+A`

`M=M-D`

`...`



Examples:

`// D ← 2`

`D=1`

`D=D+1`

`// D ← 1954`

`@1954`

`D=A`

`// D ← D + 23`

?

Use only the instructions
shown in this slide

Hack instructions

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

`D=1`

`D=A`

`D=D+1`

`...`

`D=D+A`

`D=M`

`M=0`

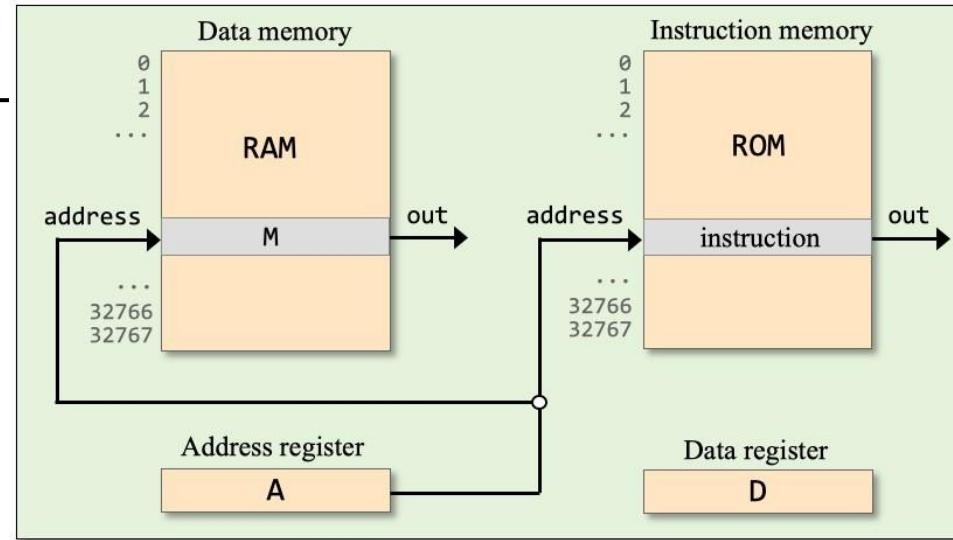
`...`

`M=D`

`D=D+A`

`M=M-D`

`...`



Examples:

`// D ← 2`

`D=1`

`D=D+1`

`// D ← 1954`

`@1954`

`D=A`

`// D ← D + 23`

`@23`

`D=D+A`

Observation

In these examples we use the address register A as a *data register*:

The addressing side-effects of A are ignored.

Hack instructions

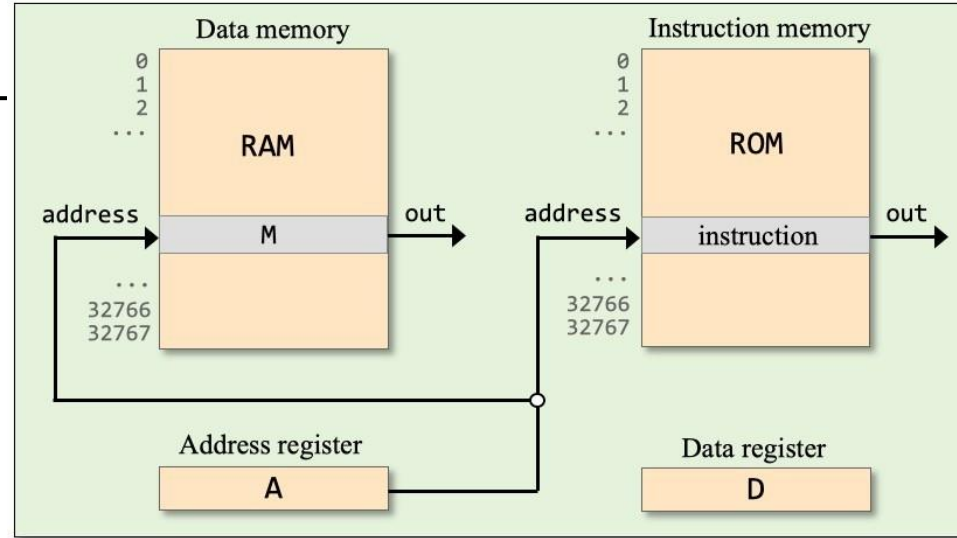
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

D=1
D=A
D=D+1
...

D=D+A
D=M
M=0
...

M=D
D=D+A
M=M-D
...



More examples:

```
// RAM[100] ← 0
@100
M=0
```

```
// RAM[100] ← 17
@17
D=A
@100
M=D
```

- First pair of instructions:
A is used as a *data register*
- Second pair of instructions:
A is used as an *address register*

Hack instructions

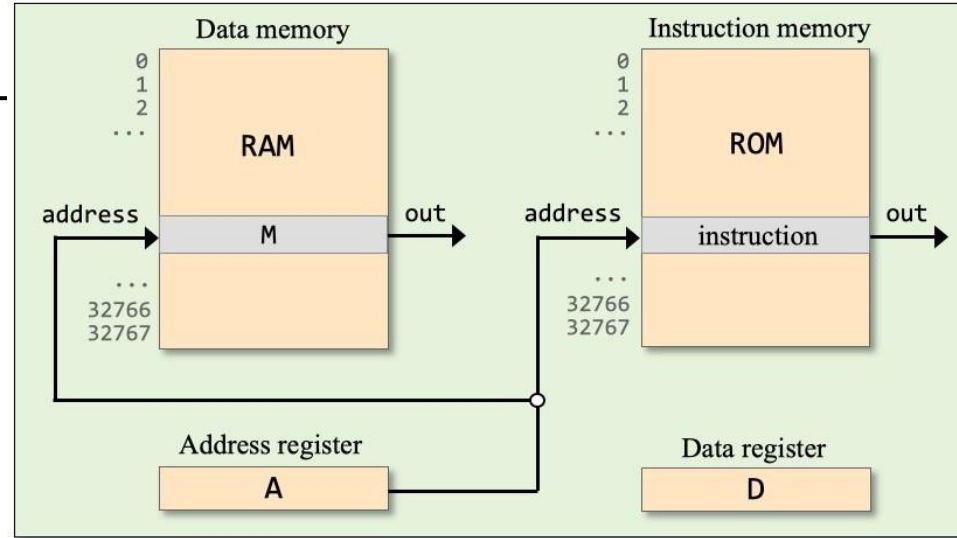
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

`D=1`
`D=A`
`D=D+1`
...

`D=D+A`
`D=M`
`M=0`
...

`M=D`
`D=D+A`
`M=M-D`
...



More examples:

```
// RAM[100] ← 0
@100
M=0
```

```
// RAM[100] ← 17
@17
D=A
@100
M=D
```

```
// RAM[100] ← RAM[200]
?
```

Hack instructions

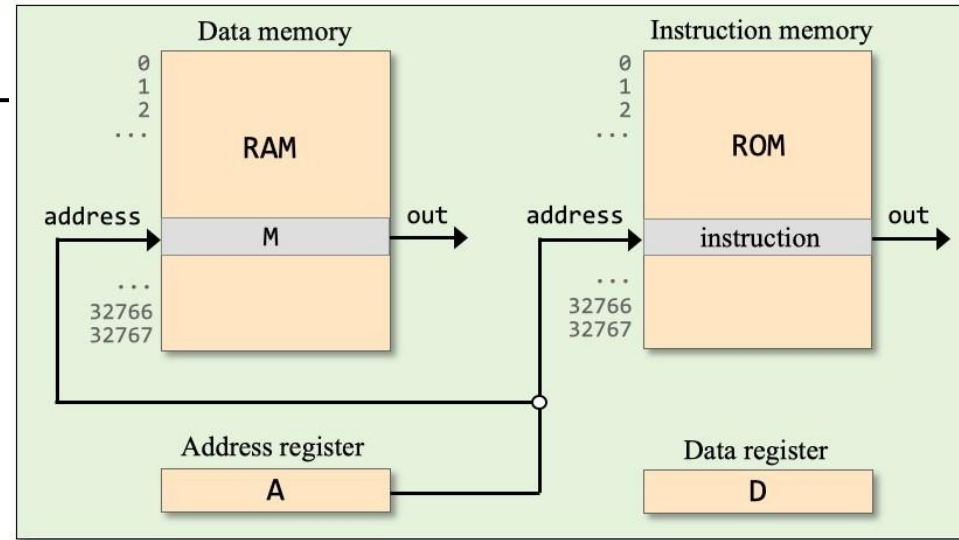
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

D=1
D=A
D=D+1
...

D=D+A
D=M
M=0
...

M=D
D=D+A
M=M-D
...



More examples:

```
// RAM[100] ← 0
@100
M=0
```

```
// RAM[100] ← 17
@17
D=A
@100
M=D
```

```
// RAM[100] ←
RAM[200] @200
D=M
@100
M=D
```

When we want to operate on a memory register, we typically need a pair of instructions:

- A instruction: Selects a memory register
- C instruction: Operates on the selected register.

Hack instructions

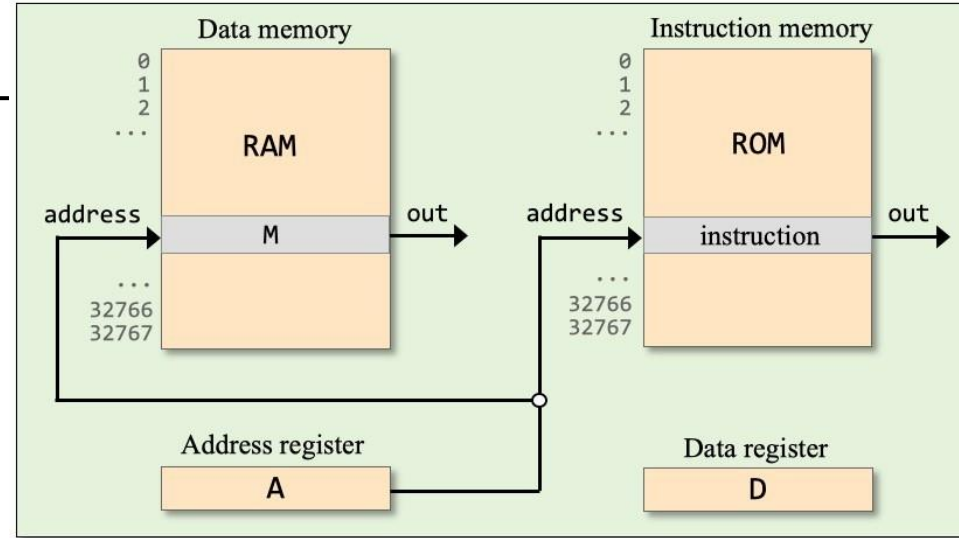
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

$D = 1$
 $D = A$
 $D = D + 1$
...

$D = D + A$
 $D = M$
 $M = 0$
...

$M = D$
 $D = D + A$
 $M = M - D$
...



```
// RAM[3] ← RAM[3] - 15
```

?

Use only the instructions
shown in the current slide

Hack instructions

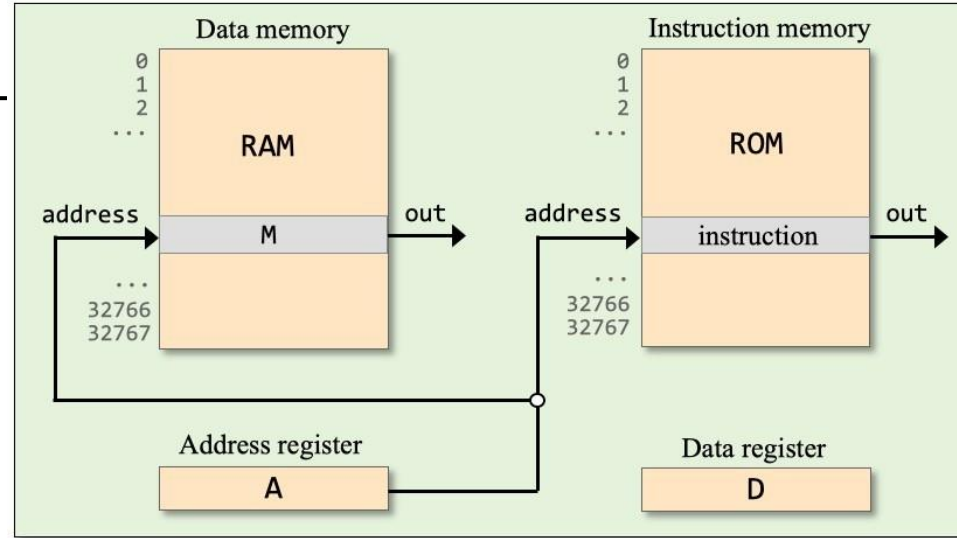
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

`D=1`
`D=A`
`D=D+1`
...

`D=D+A`
`D=M`
`M=0`
...

`M=D`
`D=D+A`
`M=M-D`
...



```
// RAM[3] ← RAM[3] - 15
@15
D=A
@3
M=M-D
```

Use only the instructions
shown in the current slide

```
// RAM[3] ← RAM[4] + 1
?
```

Hack instructions

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

$D = 1$

$D = A$

$D = D + 1$

...

$D = D + A$

$D = M$

$M = 0$

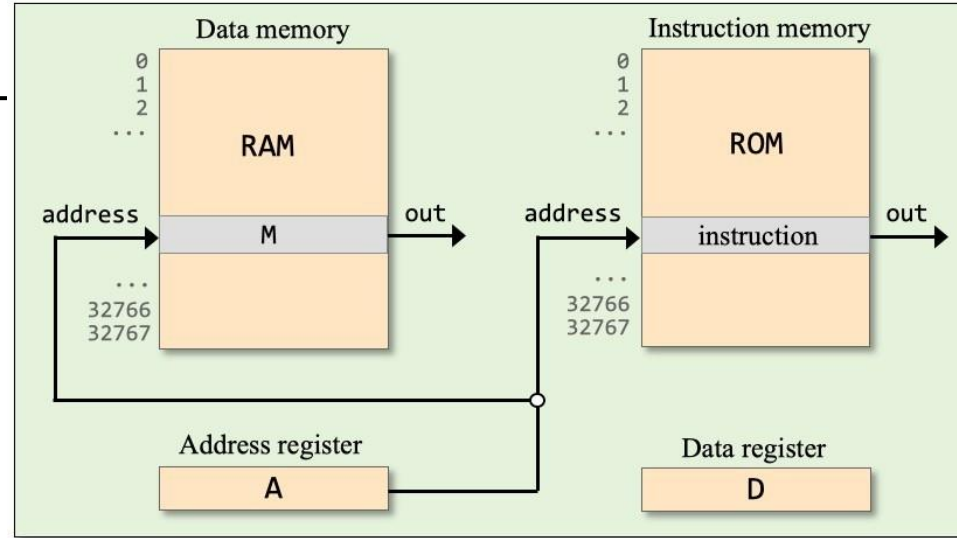
...

$M = D$

$D = D + A$

$M = M - D$

...



```
// RAM[3] ← RAM[3] - 15
```

```
@15
```

```
D=A
```

```
@3
```

```
M=M-D
```

Use only the instructions
shown in the current slide

```
// RAM[3] ← RAM[4] + 1
```

```
@4
```

```
D=M+1
```

```
@3
```

```
M=D
```

Hack instructions

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

$A = 1$

$D = -1$

$M = 0$

...

$A = M$

$D = M$

$M = D$

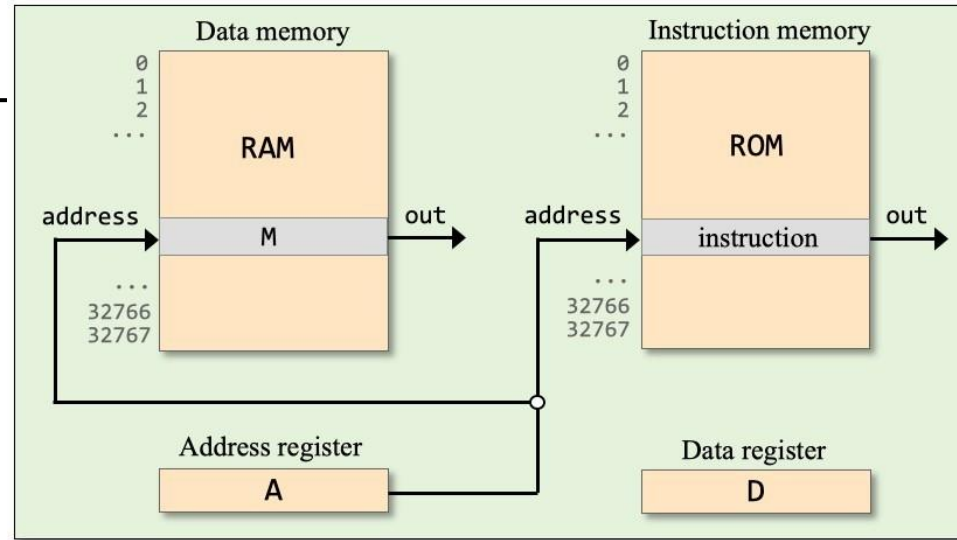
...

$A = D - A$

$D = D + A$

$D = D + M$

...



Add.asm

```
// Computes: RAM[2] = RAM[0] + RAM[1] + 17
```

?

Use only the instructions
shown in the current slide

Hack instructions

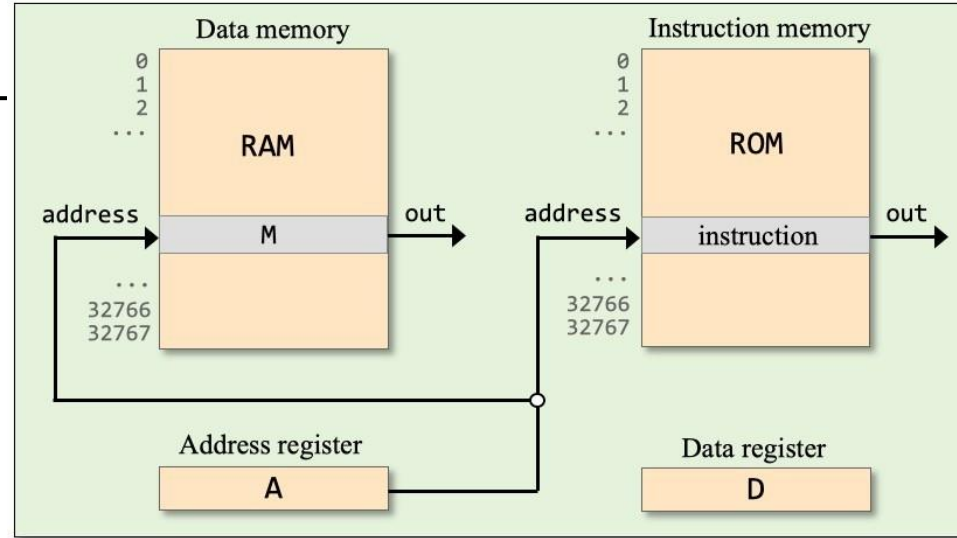
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

A=1
D=-1
M=0
...

A=M
D=M
M=D
...

A=D-A
D=D+A
D=D+M
...

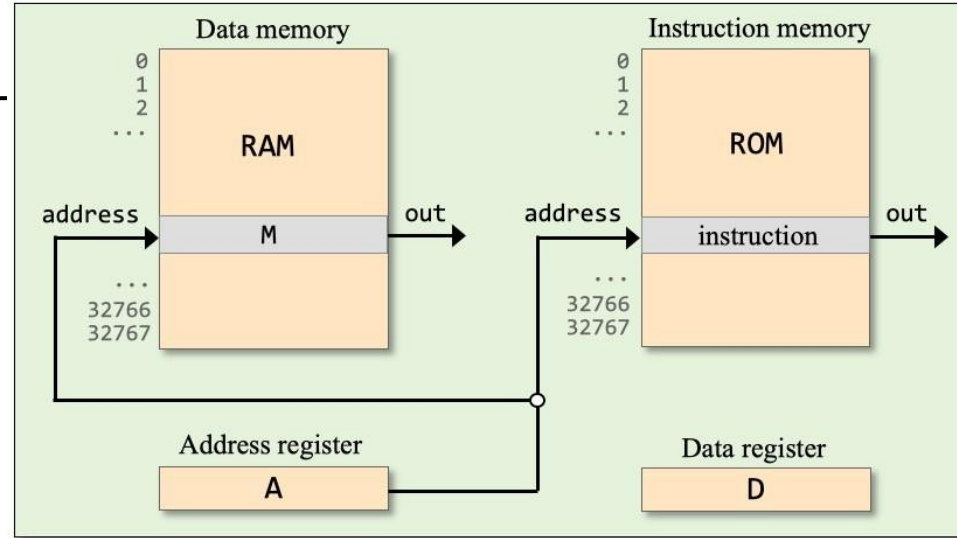
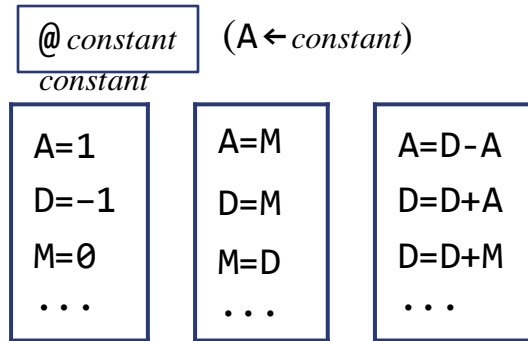


Add.asm

```
// Computes: RAM[2] = RAM[0] + RAM[1] + 17
// D = RAM[0]
@0
D=M
// D = D + RAM[1]
@1
D=D+M
// D = D + 17
@17
D=D+A
// RAM[2] = D
@2
M=D
```


Hack instructions

Typical instructions:



Add.asm

```
// Computes: RAM[2] = RAM[0] + RAM[1] + 17
// D = RAM[0]
@0
D=M
// D = D + RAM[1]
@1
D=D+M
// D = D + 17
@17
D=D+A
// RAM[2] = D
@2
M=D
```

How can we tell that a given program *actually works*?

- ➡ Testing / simulating
- Formal verification

Chapter 4: Machine Language

Overview

- ✓ Machine languages
- ✓ The Hack computer
- ✓ The Hack instruction set

➡ The Hack CPU Emulator

Symbolic programming

- Control
- Variables
- Labels

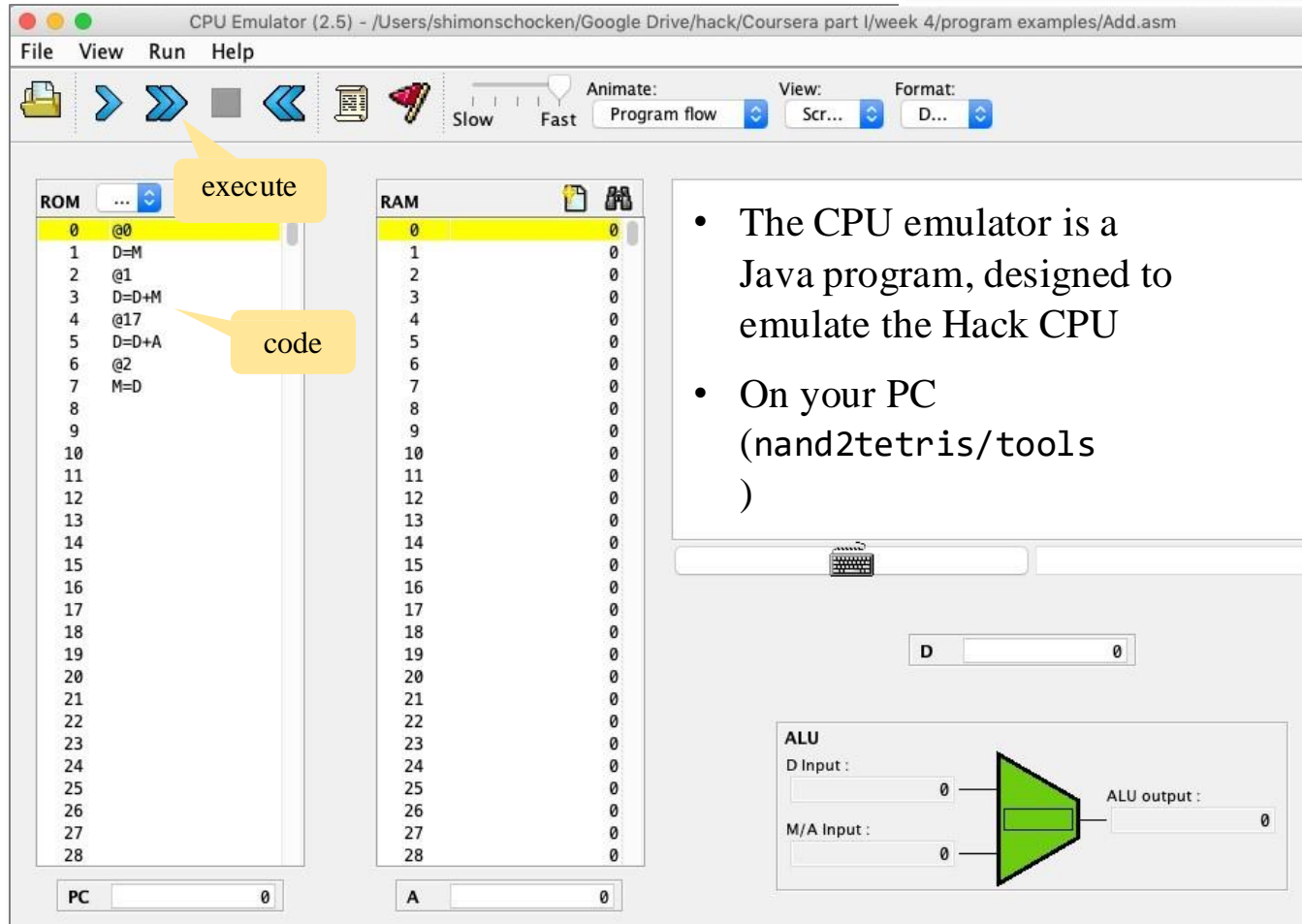
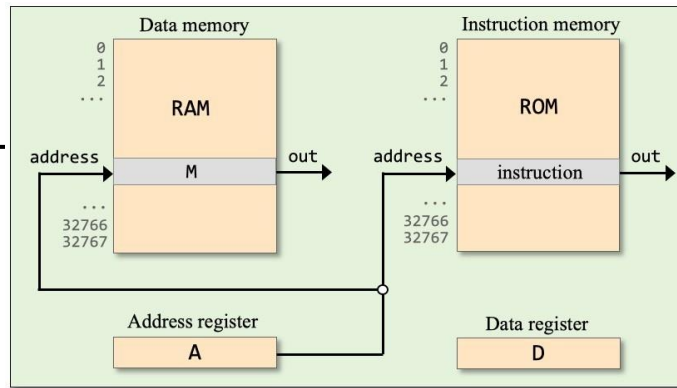
Low Level Programming

- Basic
- Iteration
- Pointers

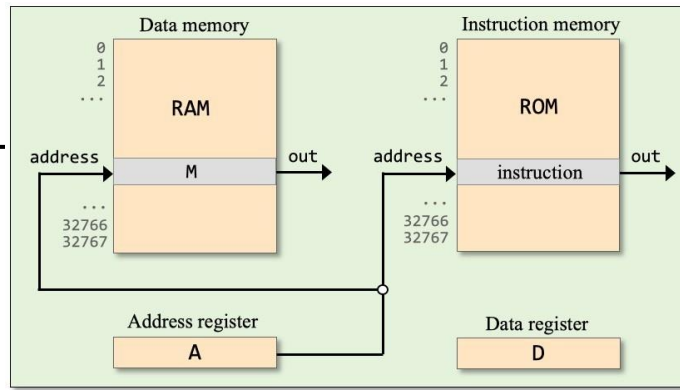
The Hack Language

- Usage
- Specification
- Output
- Input
- Project 4

The CPU emulator



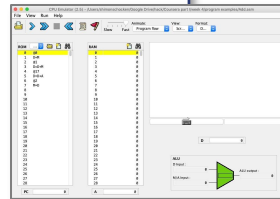
The CPU emulator



Add.asm (example)

```
// Computes: RAM[2] = RAM[0] + RAM[1] + 17
// D = RAM[0]
@0
D=M
// D = D + RAM[1]
@1
D=D+M
// D = D + 17
@17
D=D+A
// RAM[2] = D
@2
M=D
```

Load into the
CPU emulator



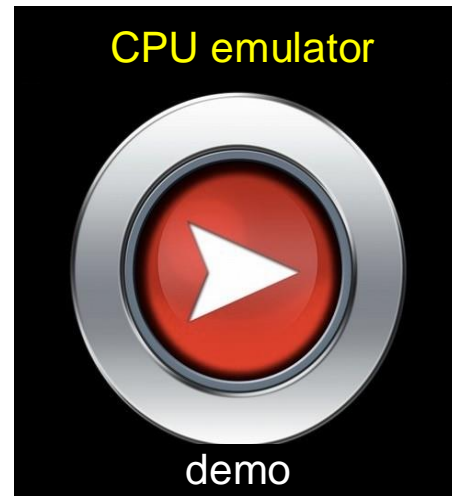
Binary

```
0000000000000000
1000010010001101
0000000000000001
1010011001100001
0000000000001001
1001111100110011
0000000000000010
1110010010010011
```

Execute

When loading a symbolic program into the CPU emulator, the emulator translates it into binary code (using a built-in assembler)

The CPU emulator



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- Machine languages
- The Hack computer
- The Hack instruction set
- The Hack CPU Emulator



Symbolic programming



- Control
- Variables
- Labels

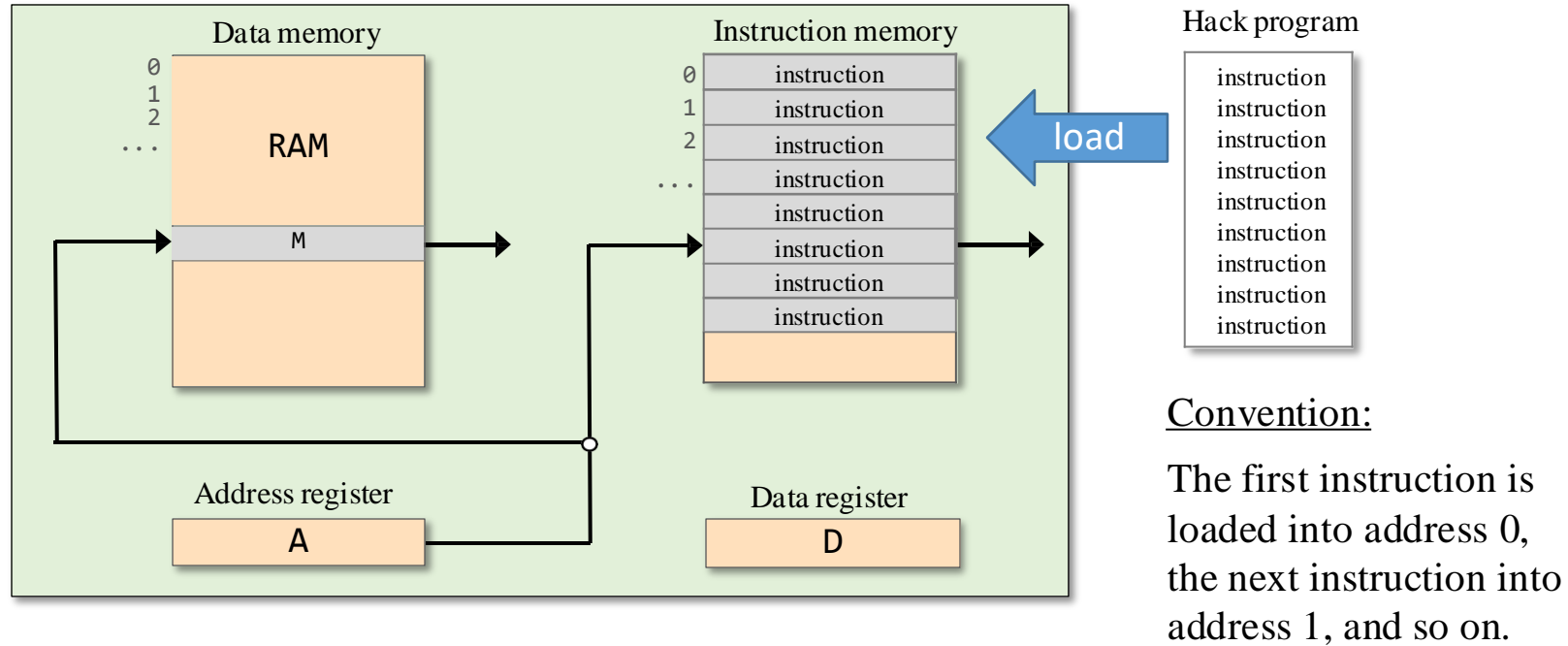
Low Level Programming

- Basic
- Iteration
- Pointers

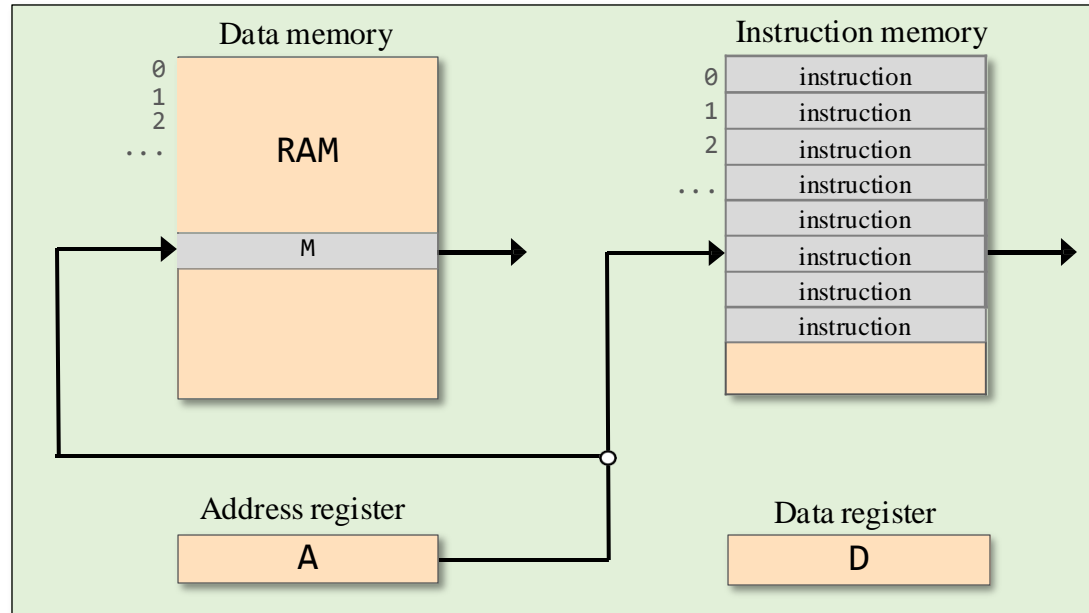
The Hack Language

- Usage
- Specification
- Output
- Input
- Project 4

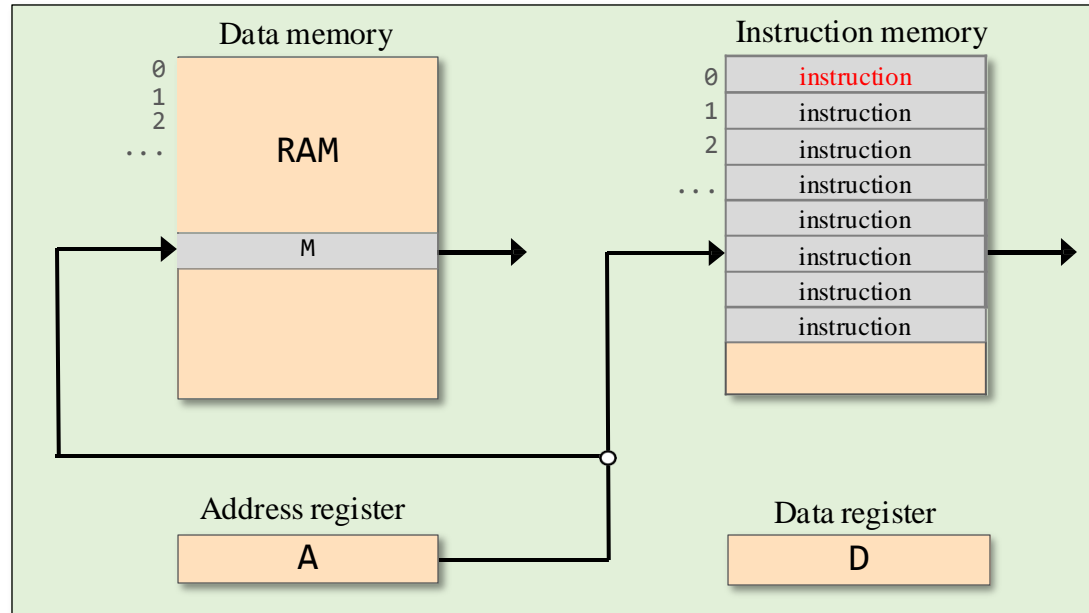
Loading a program



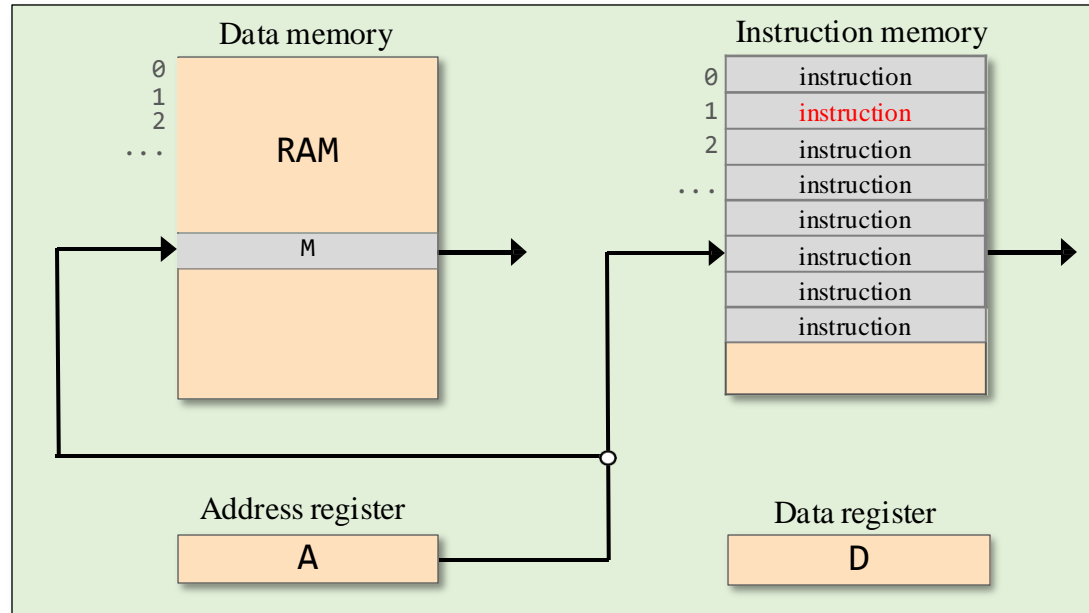
Executing a program



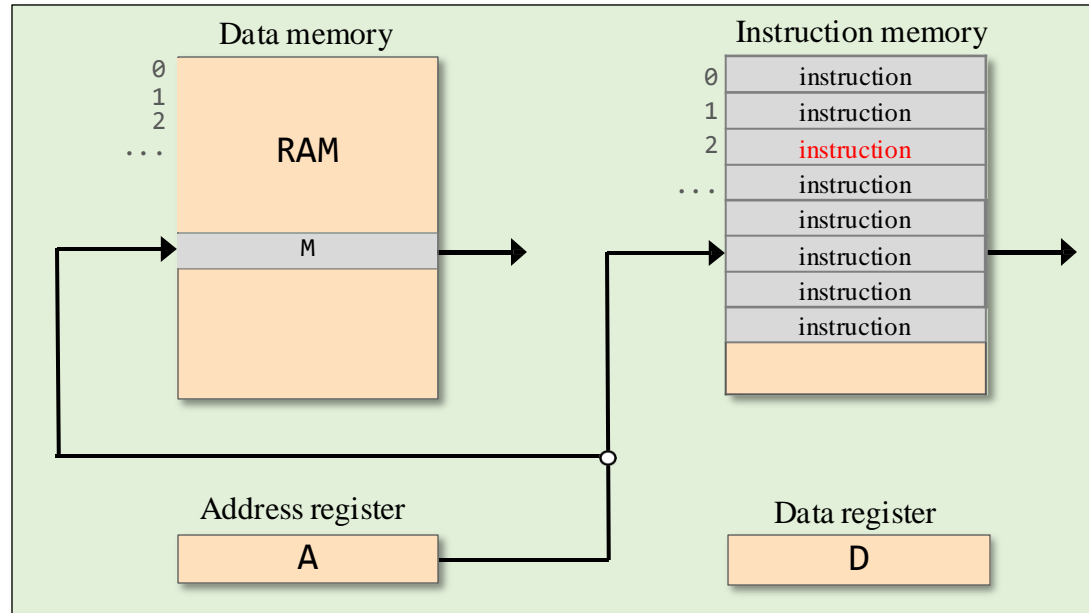
Executing a program



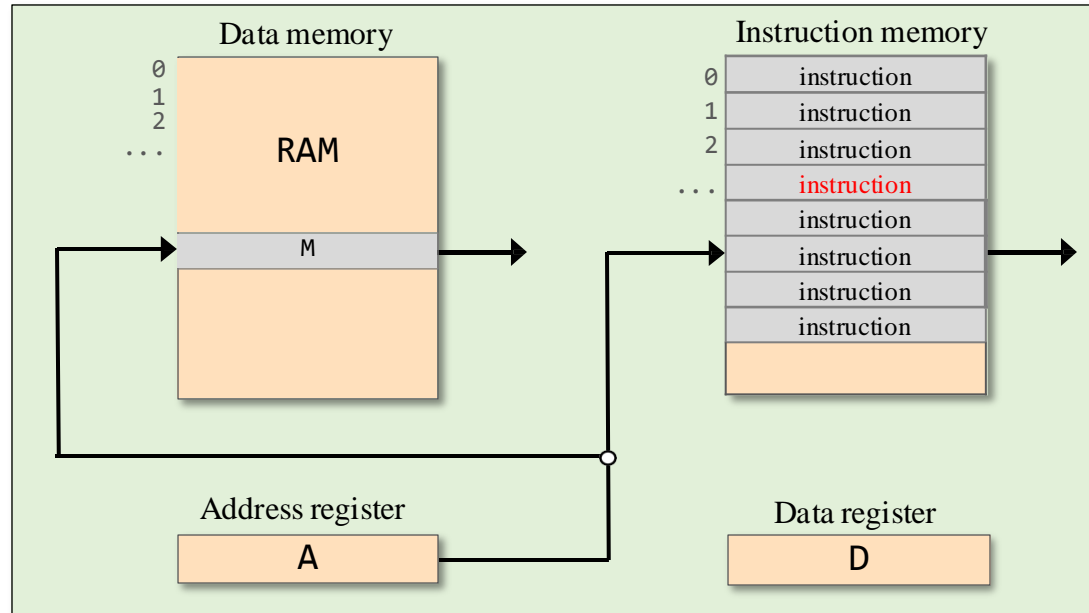
Executing a program



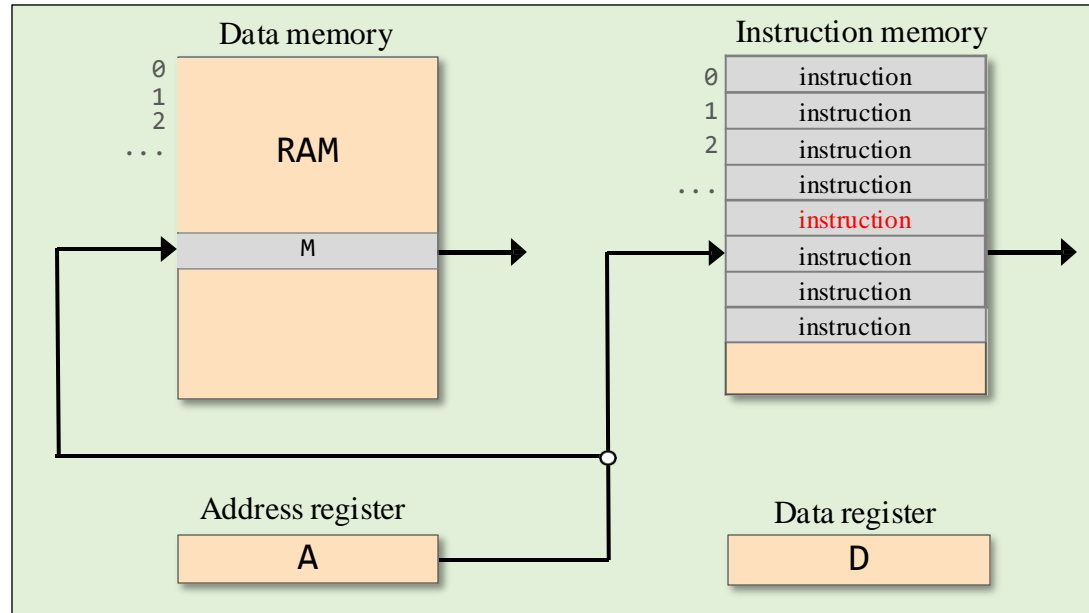
Executing a program



Executing a program

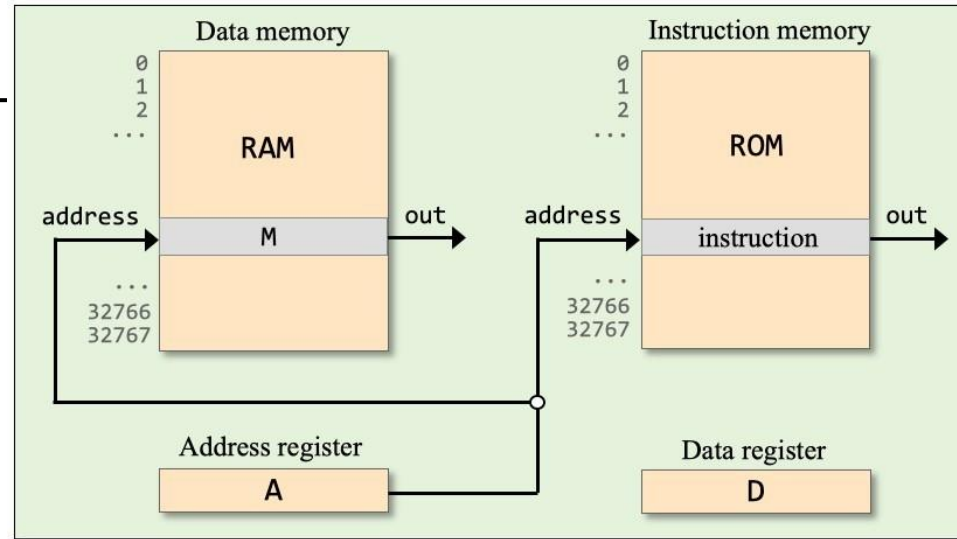


Executing a program



- The default: Execute the next instruction
- Suppose we wish to execute another instruction
- How to specify this *branching*?

Branching



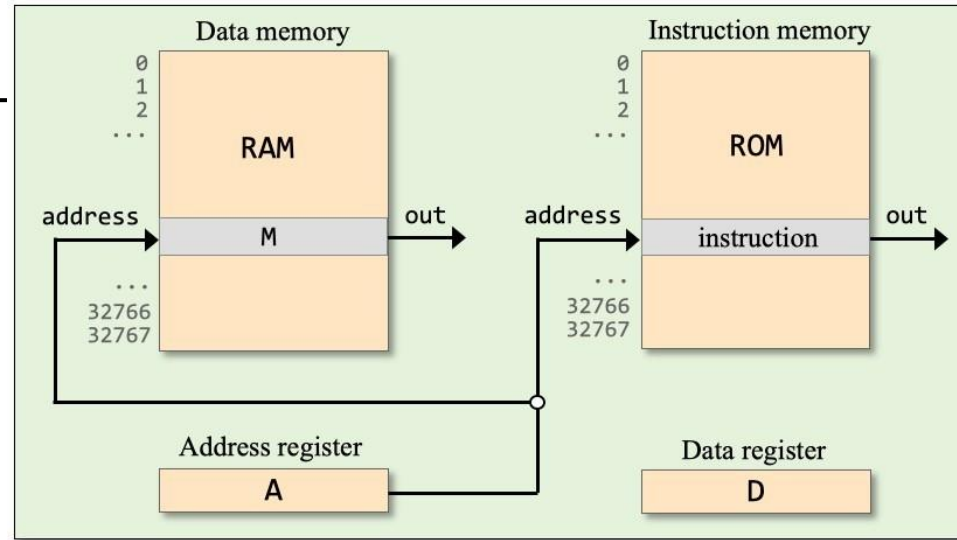
Unconditional branching example (pseudocode)

```
0 instruction
1 instruction
2 instruction
3 instruction
4 goto 7
5 instruction
6 instruction
7 instruction
8 instruction
9 goto 2
10 instruction
11 ...
```

Flow of control:

```
0,1,2,3,4,
7,8,9,
2,3,4,
7,8,9,
2,3,4,
...
```

Branching



Conditional branching example (pseudocode)

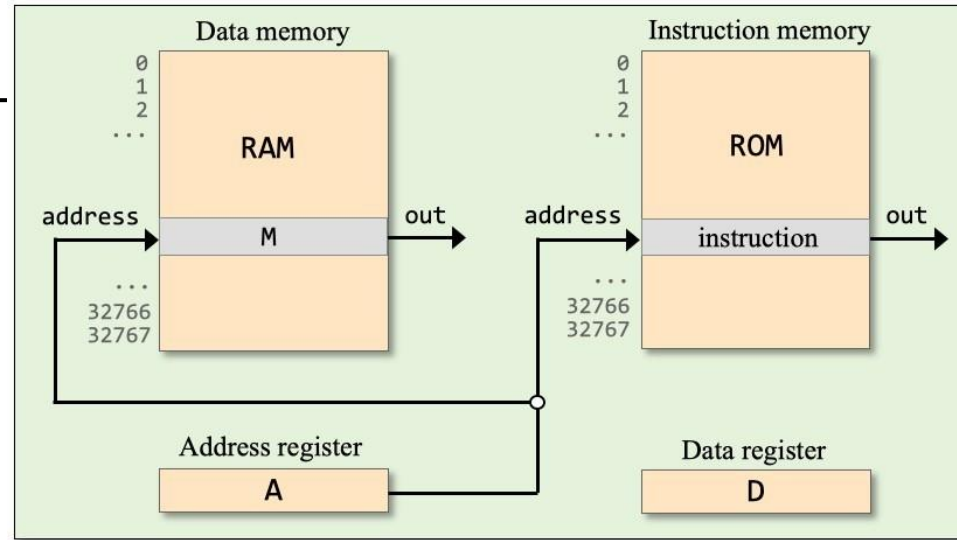
```
0 instruction
1 instruction
2 instruction
3 instruction
4 if (condition) goto 7
5 instruction
6 instruction
7 instruction
8 instruction
9 instruction
... ..
```

Flow of control:

0,1,2,3,4,
if *condition* is true
 7,8,9,...
else
 5,6,7,8,9,...

Branching

Branching in the
Hack language:



Example (Pseudocode):

```
0 instruction
1 instruction
2 goto 6
3 instruction
4 instruction
5 instruction
6 instruction
7 instruction
... ..
```

In Hack:

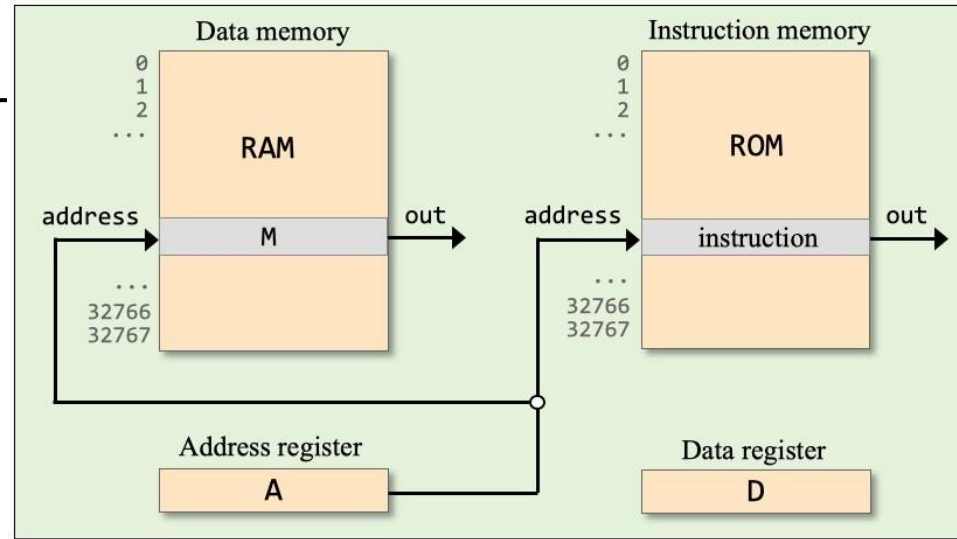
```
...
// goto 6
@6
0; JMP
...
```

Semantics of 0; JMP

Jump to the instruction stored in the register selected by A
(the “0;” prefix will be explained later)

Branching

Branching in the
Hack language:



Example (Pseudocode):

```
1 instruction
2 instruction
3 if (D > 0) goto 6
4 instruction
5 instruction
6 instruction
7 instruction
8 instruction
... ..
```

In Hack:

```
...
// if (D > 0) goto 6
@6
D; JGT
...
```

Typical branching instructions:

```
D; JGT // if D > 0 jump
D; JGE // if D ≥ 0 jump
D; JLT // if D < 0 jump
D; JLE // if D ≤ 0 jump
D; JEQ // if D = 0 jump
D; JNE // if D ≠ 0 jump
0; JMP // jump
```

to the
instruction
stored in
ROM[A]

Branching

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

`A=1`

`D=-1`

`M=0`

`...`

`A=M`

`D=A`

`M=D`

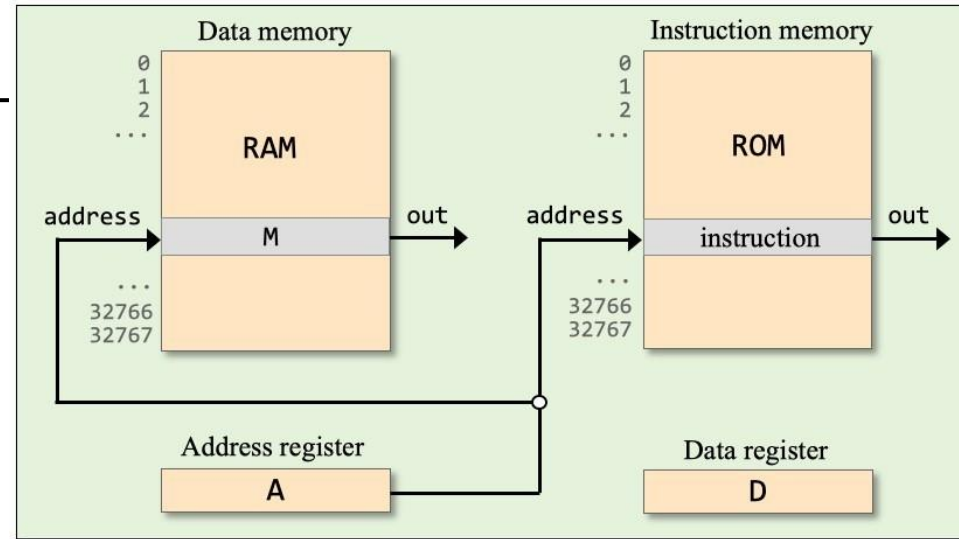
`...`

`D=D-A`

`A=A-1`

`M=D+1`

`...`



`// if (D = 0) goto 300`

?

Use only the instructions shown in the current slide

Typical branching instructions:

`D; JGT // if D > 0 jump`

`D; JGE // if D ≥ 0 jump`

`D; JLT // if D < 0 jump`

`D; JLE // if D ≤ 0 jump`

`D; JEQ // if D = 0 jump`

`D; JNE // if D ≠ 0 jump`

`0; JMP // jump`

to the
instruction
stored in
ROM[A]

Branching

Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

`A=1`

`D=-1`

`M=0`

`...`

`A=M`

`D=A`

`M=D`

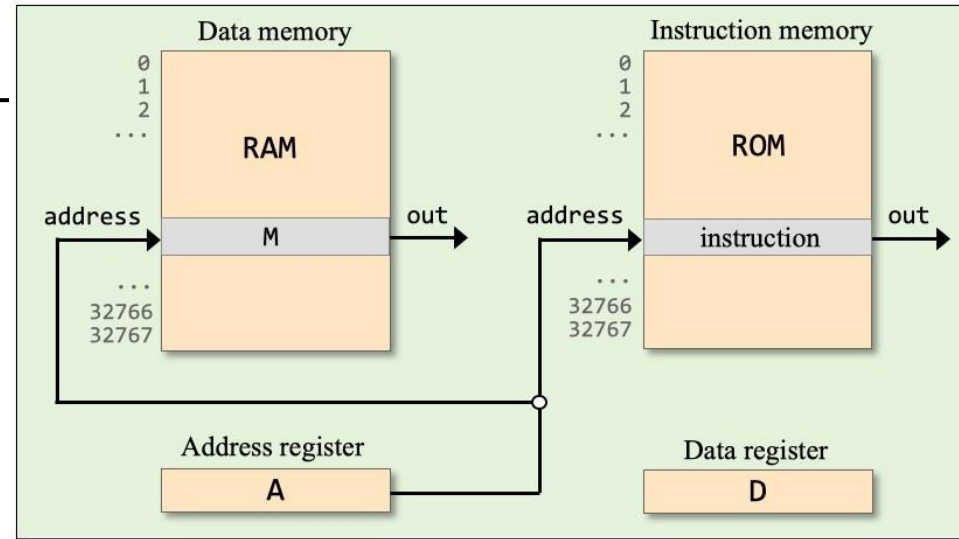
`...`

`D=D-A`

`A=A-1`

`M=D+1`

`...`



`// if (D = 0) goto 300`

`@300`

`D; JEQ`

Use only the instructions shown in the current slide

Typical branching instructions:

`D; JGT // if D > 0 jump`

`D; JGE // if D ≥ 0 jump`

`D; JLT // if D < 0 jump`

`D; JLE // if D ≤ 0 jump`

`D; JEQ // if D = 0 jump`

`D; JNE // if D ≠ 0 jump`

`0; JMP // jump`

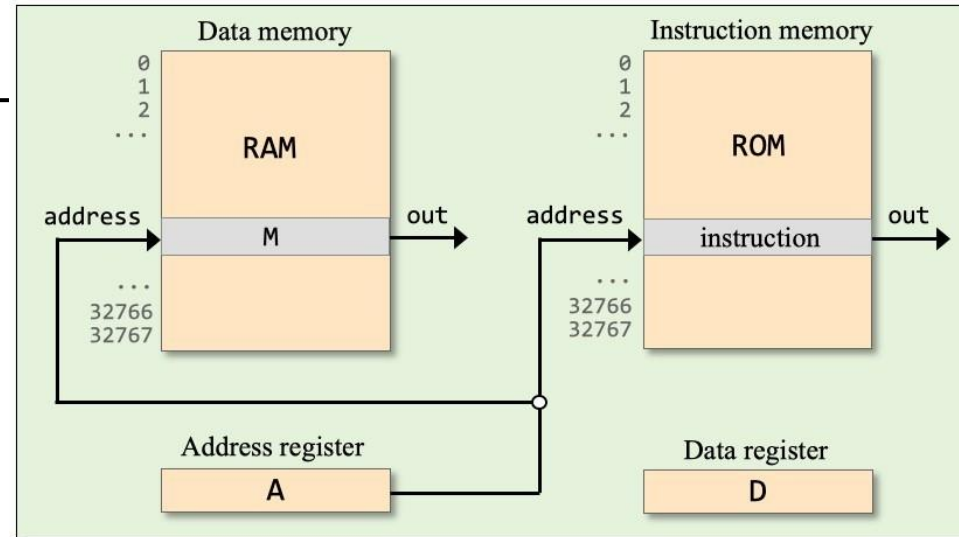
to the instruction stored in ROM[A]

Branching

Typical instructions:

`@ constant` ($A \leftarrow \text{constant}$)

A=1	A=M	D=D-A
D=-1	D=A	A=A-1
M=0	M=D	M=D+1
...



Typical branching instructions:

`// if (RAM[3] < 100) goto 12`

?

`D; JGT // if D > 0 jump`
`D; JGE // if D ≥ 0 jump`
`D; JLT // if D < 0 jump`
`D; JLE // if D ≤ 0 jump`
`D; JEQ // if D = 0 jump`
`D; JNE // if D ≠ 0 jump`
`0; JMP // jump`

to the instruction stored in ROM[A]

Use only the instructions shown in the current slide

Branching

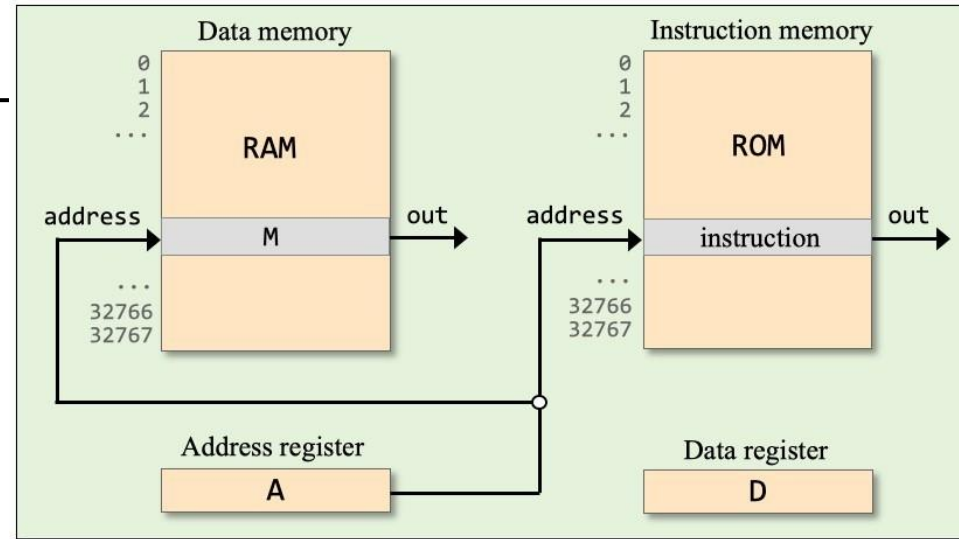
Typical instructions:

`@constant` ($A \leftarrow \text{constant}$)

A=1
D=-1
M=0
...

A=M
D=A
M=D
...

D=D-A
A=A-1
M=D+1
...



Typical branching instructions:

```
// if (RAM[3] < 100) goto 12
// D = RAM[3] - 100
@3
D=M
@100
D=D-A
// if (D < 0) goto 12
@12
D;JLT
```

```
D;JGT // if D > 0 jump
D;JGE // if D ≥ 0 jump
D;JLT // if D < 0 jump
D;JLE // if D ≤ 0 jump
D;JEQ // if D = 0 jump
D;JNE // if D ≠ 0 jump
0;JMP // jump
```

to the
instruction
stored in
ROM[A]

Use only the instructions shown in the current slide

Chapter 4: Machine Language

Overview

- Machine languages
- The Hack computer
- The Hack instruction set
- The Hack CPU Emulator

Low Level Programming

- Basic
- Iteration
- Pointers

Symbolic programming



Control



Variables

- Labels

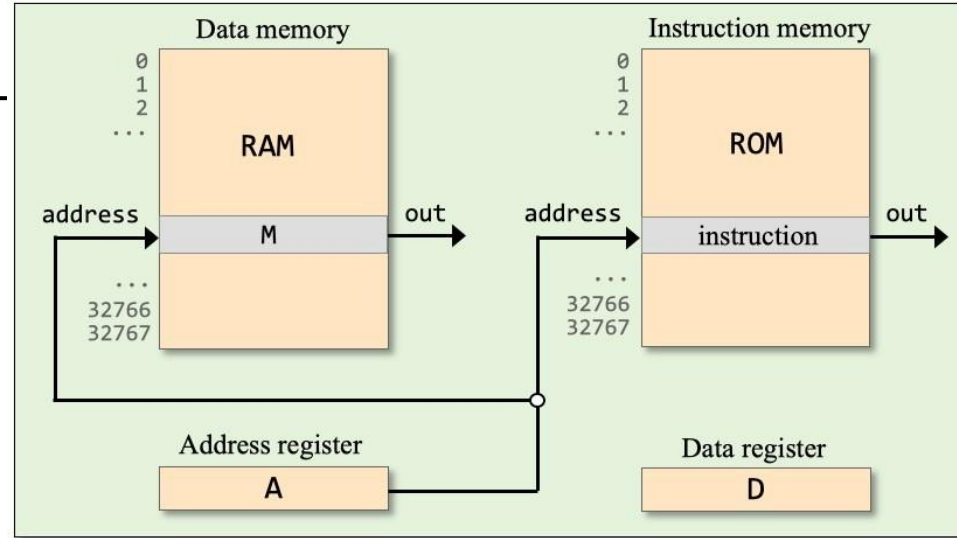
The Hack Language

- Usage
- Specification
- Output
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- Project 4

Hack instructions

➔ A instruction

- C instruction



Syntax:

`@const`

where *const* is a constant

`@sym`

where *sym* is a symbol bound to a constant

Example:

`@19 // A ← 19`

`@x`

For example, if *x* is bound to 21, this instruction will set A to 21

This idiom can be used for realizing:

➔ Variables

- Labels

Variables

Pseudocode (example)

```
...  
i = 1  
sum = 0  
...  
sum = sum + i  
i = i + 1  
...
```

write



Hack assembly

```
...  
// i = 1  
@i  
M=1  
// sum = 0  
@sum  
M=0  
...  
// sum = sum + i  
@i  
D=M  
@sum  
M=D+M  
// i = i + 1  
@i  
M=M+1  
...
```

Symbolic programming

- The code writer is allowed to use symbolic variables, as needed
- We assume that there is an agent who knows how to bind these symbols to selected RAM addresses

This agent is the *assembler*

For example

- If the assembler will bind `i` to 16 and `sum` to 17, every instruction `@i` and `@sum` will end up selecting RAM[16] and RAM[17]
- Should the code writer worry about what is the actual bindings? No
- The result: a low-level model for representing *variables*.

Variables

Typical instructions:

`@ constant` $A \leftarrow \text{constant}$

`@ symbol` $A \leftarrow \text{the constant which is bound to } \textit{symbol}$

D=0
M=1
D=-1
M=0
...

D=M
A=M
M=D
D=A
...

D=D+A
D=A+1
D=D+M
M=M-1
...

// sum = 0

?

// x = 512

?

// n = n - 1

?

// sum = sum + x

?

Use only the instructions
shown in the current slide

Variables

Typical instructions:

`@constant` $A \leftarrow \text{constant}$

`@symbol` $A \leftarrow \text{the constant which is bound to } \textit{symbol}$

```
D=0
M=1
D=-1
M=0
...
```

```
D=M
A=M
M=D
D=A
...
```

```
D=D+A
D=A+1
D=D+M
M=M-1
...
```

```
// sum = 0
@sum
M=0
```

```
// x = 512
@512
D=A
@x
M=D
```

```
// n = n - 1
@n
M=M-1
```

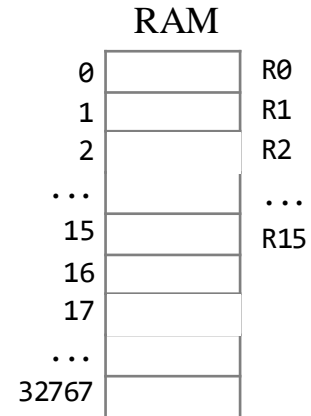
```
// sum = sum + x
@sum
D=M
@x
D=D+M
@sum
M=D
```

Use only the instructions
shown in the current slide

Variables

Pre-defined symbols

<u>symbol</u>	<u>value</u>
R0	0
R1	1
R2	2
...	...
R15	15



- As if you have 16 built-in variables named R0...R15
- We sometimes call them “virtual registers”

Example:

```
// Sets R1 to 2 * R0
// Usage: Enter a value in R0
@R0
D=M
@R1
M=D
M=D+M
```

The use of R0, R1, ... (instead of physical addresses 0, 1, ...) makes it easier to document, write, and debug Hack code.

Chapter 4: Machine Language

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Symbolic programming

- ✓ Control
- ✓ Variables
- ➔ Labels

Low Level Programming

- Basic
- Iteration
- Pointers

The Hack Language

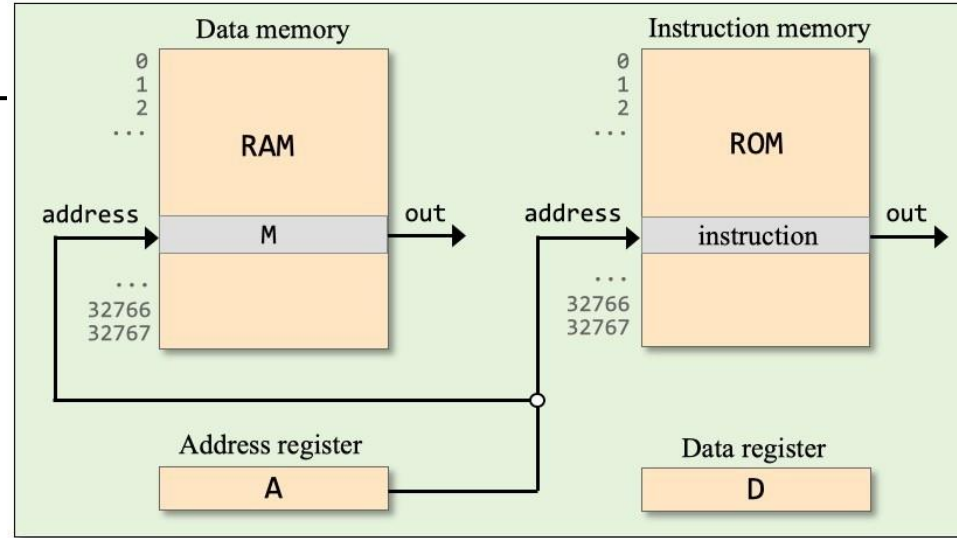
- Usage
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Labels

Typical branching instructions:

D;JGT // if $D > 0$ jump
D;JGE // if $D \geq 0$ jump
D;JLT // if $D < 0$ jump
D;JLE // if $D \leq 0$ jump
D;JEQ // if $D = 0$ jump
D;JNE // if $D \neq 0$ jump
0;JMP // jump

} to ROM[A]



Examples (similar to what we did before):

// goto 48

?

// if ($D > 0$) goto 21

?

// if ($\text{RAM}[100] < 0$) goto 35

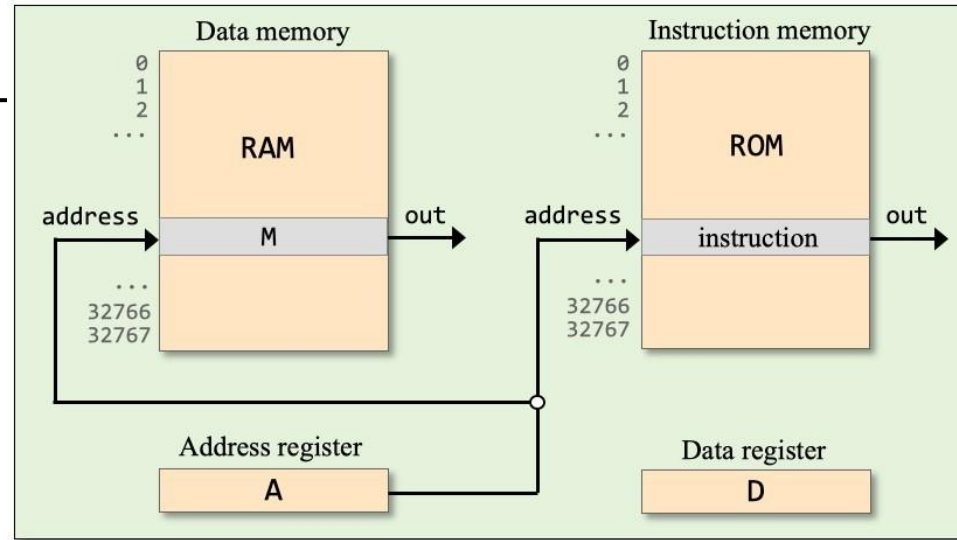
?

Labels

Typical branching instructions:

D;JGT // if $D > 0$ jump
D;JGE // if $D \geq 0$ jump
D;JLT // if $D < 0$ jump
D;JLE // if $D \leq 0$ jump
D;JEQ // if $D = 0$ jump
D;JNE // if $D \neq 0$ jump
0;JMP //jump

to
ROM[A]



Examples (similar to what we did before):

```
// goto 48
@48
0;JMP
```

```
// if (D > 0) goto 21
@21
D;JGT
```

```
// if (RAM[100] < 0) goto 35
@100
D=M
@35
D;JLT
```

Same examples, using *labels*

```
// goto LOOP
@LOOP
0;JMP
```

```
// if (D > 0) goto CONT
@CONT
D;JGT
```

```
// if (x < 0) goto NEG
@x
D=M
@NEG
D;JLT
```

Hack convention:

Variables: lower-case symbols

Labels: upper-case symbols

Labels

Example (pseudocode)

```
...  
LOOP:  
  if (i = 0) goto CONT  
  do this  
  ...  
  goto LOOP  
  
CONT:  
  do that  
  ...
```

write



Hack assembly

```
...  
(LOOP)  
  // if (i = 0) goto CONT  
  @i  
  D=M  
  @CONT  
  D;JEQ  
  do this  
  ...  
  // goto LOOP  
  @LOOP  
  0;JMP  
(CONT)  
  do that  
  ...
```

Hack assembly syntax:

- A label *sym* is declared using (*sym*)
- Any label *sym* declared somewhere in the program can appear in a @*sym* instruction
- The assembler resolves the labels to actual addresses.

Programs that use symbolic labels and variables are...

- Easy to write / translate from pseudocode
- Readable
- Relocatable.

Chapter 4: Machine Language

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Program example 1: Add

Task: $R2 \leftarrow R0 + R1 + 17$

Add.asm

```
// Sets R2 to R0 + R1 + 17
// D = R0
@R0
D=M
// D = D + R1
@R1
D=D+M
// D = D + 17
@17
D=D+A
// R2 = D
@R2
M=D
```

Program example 2: signum

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  if (R0 ≥ 0) goto POS
  R1 = -1
  goto END
POS:
  R1 = 1
END:
```

write



Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  // if R0 >= 0 goto POS
  @R0
  D=M
  @POS
  D; JGE
  // R1 = -1
  @R1
  M=-1
  // goto END
  @END
  0; JMP

(POS)
  // R1 = 1
  @R1
  M=1

(END)
```

Best practice

When writing a (non-trivial) assembly program,
always start with writing pseudocode.

Then translate the pseudo instructions into assembly, line by line.

Program example 2: signum

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
if (R0 ≥ 0) goto POS
R1 = -1
goto END
POS:
R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
// if R0 >= 0 goto POS
@R0
D=M
@POS
D; JGE
// R1 = -1
@R1
M=-1
// goto END
@END
0; JMP

(POS)
// R1 = 1
@R1
M=1
(END)
```

Assembler /
loader

(Note how the
assembler mapped
all the symbols on
physical addresses)

Memory

0	@0
1	D=M
2	@8
3	D; JGE
4	@1
5	M=-1
6	@10
7	0; JMP
8	
9	M=1
10	
11	
12	
13	
14	
...	

Watch out: Security breach

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  if (R0 ≥ 0) goto POS
  R1 = -1
  goto END
POS:
  R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  // if R0 >= 0 goto POS
  @R0
  D=M
  @POS
  D; JGE
  // R1 = -1
  @R1
  M=-1
  // goto END
  @END
  0; JMP

(POS)
  // R1 = 1
  @R1
  M=1
(END)
```

Assembler /
loader

Memory

0	@0
1	D=M
2	@8
3	D; JGE
4	@1
5	M=-1
6	@10
7	0; JMP
8	
9	M=1
10	0111111000111110
11	1010101001011110
12	0100100110011011
13	1110010011111111
14	0101011100110111
...	

The memory is
never empty

Watch out: Security breach

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  if (R0 ≥ 0) goto POS
  R1 = -1
  goto END
POS:
  R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  // if R0 >= 0 goto POS
  @R0
  D=M
  @POS
  D;JGE
  // R1 = -1
  @R1
  M=-1
  // goto END
  @END
  0;JMP

(POS)
  // R1 = 1
  @R1
  M=1
(END)
```

Program
execution:



Memory

0	@0
1	D=M
2	@8
3	D;JGE
4	@1
5	M=-1
6	@10
7	0;JMP
8	
9	M=1
10	0111111000111110
11	1010101001011110
12	Malicious
13	Code
14	0101011100110111
...	

Watch out: Security breach

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  if (R0 ≥ 0) goto POS
  R1 = -1
  goto END
POS:
  R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  // if R0 >= 0 goto POS
  @R0
  D=M
  @POS
  D;JGE
  // R1 = -1
  @R1
  M=-1
  // goto END
  @END
  0;JMP

(POS)
  // R1 = 1
  @R1
  M=1

(END)
```

Program
execution:

Memory

→ 0	@0
→ 1	D=M
→ 2	@8
→ 3	D;JGE
→ 4	@1
→ 5	M=-1
→ 6	@10
→ 7	0;JMP
→ 8	
→ 9	M=1
→ 10	0111111000111110
→ 11	1010101001011110
→ 12	Malicious
→ 13	Code
→ 14	0101011100110111
...	

Terminating programs properly

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  if (R0 ≥ 0) goto POS
  R1 = -1
  goto END
POS:
  R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  // if R0 >= 0 goto POS
  @R0
  D=M
  @POS
  D; JGE
  // R1 = -1
  @R1
  M=-1
  // goto END
  @END
  0; JMP

(POS)
  // R1 = 1
  @R1
  M=1
(END) ←
```

Terminating programs properly

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  if (R0 ≥ 0) goto POS
  R1 = -1
  goto END
POS:
  R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
  // if R0 >= 0 goto POS
  @R0
  D=M
  @POS
  D; JGE
  // R1 = -1
  @R1
  M=-1
  // goto END
  @END
  0; JMP

(POS)
  // R1 = 1
  @R1
  M=1

(END)
  @END
  0; JMP
```



Infinite loop

Terminating programs properly

Pseudocode

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
if (R0 ≥ 0) goto POS
R1 = -1
goto END
POS:
R1 = 1
END:
```

Signum.asm

```
// if R0 >= 0 then R1 = 1
// else R1 = -1
// if R0 >= 0 goto POS
@R0
D=M
@POS
D; JGE
// R1 = -1
@R1
M=-1
// goto END
@END
0; JMP

(POS)
// R1 = 1
@R1
M=1

(END)
@END
0; JMP
```

Memory

0	@0
1	@D=M
2	@8
3	@D; JGE
4	@1
5	@M=-1
6	@10
7	@0; JMP
8	
9	@M=1
10	@10
11	0; JMP
12	0100100110011011
13	1110010011111111
14	0101011100110111
...	

Best practice:

Terminate every assembly program with an infinite loop.

Program example 3: Max

Task: Set $R0$ to $\max(R1, R2)$

Examples: $\max(5,3) = 5$, $\max(2,7) = 7$, $\max(4,4) = 4$

Pseudocode

```
// if (R1 > R2) then R0 = R1  
// else           R0 = R2  
...
```

write



Max2.asm

```
// You do it
```

- Write the pseudocode
- Translate and write the assembly code in a text file named Max2.asm
- Load Max2.asm into the CPU emulator
- Put some values in R1 and R2
- Run the program, one instruction at a time
- Make sure that the program puts the correct value in R0.

Chapter 4: Machine Language

Overview

- Machine languages
- The Hack computer
- The Hack instruction set
- The Hack CPU Emulator

Low Level Programming



Basic



Iteration

- Pointers

Symbolic programming

- Control
- Variables
- Labels

The Hack Language

- Usage
- Specification
- Output
- Input
- Project 4

Iterative processing

Example: Compute $1 + 2 + 3 + \dots + N$

Pseudocode

```
// Program: Sum1ToN (R0 represents N)
// Computes R1 = 1 + 2 + 3 + ... + R0
// Usage: put a value >= 1 in R0
i = 1
sum = 0
LOOP:
  if (i > R0) goto STOP
  sum = sum + i
  i = i + 1
  goto LOOP
STOP:
  R1 = sum
```

Hack assembly

```
// Program: Sum1ToN (R0 represents N)
// Computes R1 = 1 + 2 + 3 + ... + R0
// Usage: put a value >= 1 in R0
// i = 1
@i
M=1
// sum = 0
@sum
M=0
(LLOOP)
// if (i > R0) goto STOP
@i
D=M
@R0
D=D-M
@STOP
D;JGT
// sum = sum + i
@sum
D=M
@i
D=D+M
@sum
M=D
// i = i + 1
@i
M=M+1
// goto LOOP
@LLOOP
0;JMP
```

(code continues here)

```
(STOP)
// R1 = sum
@sum
D=M
@R1
M=D
// infinite loop
(END)
@END
0;JMP
```

Chapter 4: Machine Language

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Basic



Iteration



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The Hack Language

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Pointer-based processing

Example 1: Set the register at address *addr* to -1

Input: $R0$: Holds *addr*

```
// Sets RAM[R0] to -1  
// Usage: Put some non-negative value in R0
```

```
@R0  
A=M  
M=-1
```

The key instruction:

In the Hack machine language, pointer-based processing is realized by setting the address register to the address that we want to access, using the instruction $A = \dots$

RAM		
0	1013	R0
1		R1
2		R2
...		...
15		
16		
17		
...		
255		
256		
...		
1012		
1013	-1	desired result
1014		
1015		
1016		
...		

Pointer-based processing

Example 1: Set the register at address *addr* to -1

Input: R0: Holds *addr*

```
// Sets RAM[R0] to -1
// Usage: Put some non-negative value in R0
@R0
A=M
M=-1
```

Example 2:

```
// Sets RAM[R0] to R1
// Usage: Put some non-negative value in R0,
//         and some value in R1.
@R1
D=M
@R0
A=M
M=D
```

RAM		
0	1015	R0
1	-17	R1
2		R2
...		...
15		
16		
17		
...		
255		
256		
...		
1012		
1013		
1014		
1015		desired result
1016		
...		

Pointer-based processing

Example 3: Get the value of the register at *addr*

Input: R0: Holds *addr*

```
// Gets R1 = RAM[R0]  
// Usage: Put some non-negative value in R0
```

?

RAM		
0	1013	R0
1	75	R1 desired
2		R2 result
...		...
15		
16		
17		
...		
255		
256		
...		
1012	512	
1013	75	
1014	19	
1015		
1016		
...		

Pointer-based processing

Example 3: Get the value of the register at *addr*

Input: R0: Holds *addr*

```
// Gets R1 = RAM[R0]
// Usage: Put some non-negative value in R0

@R0
A=M
D=M

@R1
M=D
```

RAM		
0	1013	R0
1	75	R1 desired
2		R2 result
...		...
15		
16		
17		
...		
255		
256		
...		
1012	512	
1013	75	
1014	19	
1015		
1016		
...		

Pointer-based processing

Example 4: Set the first n entries of the memory block beginning in address $base$ to -1

Inputs: $R0: base$
 $R1: n$

Example: $base = 300, n = 5$

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
```

...

```
// RAM[ R0 + i ] = -1
```

The key operation

?

RAM		
0	300	R0 <i>base</i>
1	5	R1 <i>n</i>
2		R2
...		...
15		R15
16	5	i
17		
...		
255		
256		
...		
300	-1	desired output
301	-1	
302	-1	
303		
304	-1	
305		
...		

Pointer-based processing

Example 4: Set the first n entries of the memory block beginning in address $base$ to -1

Inputs: $R0: base$
 $R1: n$

Example: $base = 300, n = 5$

```
// Program: PointerDemo.asm  
// Starting at the address stored in R0,  
// sets the first R1 words to -1
```

...

```
// RAM[ R0 + i ] = -1
```

The key operation

```
@R0
```

```
D=M
```

```
@i
```

```
A=D+M
```

```
M= -1
```

...

RAM		
0	300	R0 <i>base</i>
1	5	R1 <i>n</i>
2		R2
...		...
15		R15
16	5	i
17		
...		
255		
256		
...		
300	-1	desired output
301	-1	
302	-1	
303		
304	-1	
305		
...		

Pointer-based processing

Pseudocode

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
i = 0
LOOP:
  if (i == R1) goto END
  RAM[R0+i] = -1
  i = i+1
  goto LOOP
END:
```

Assembly code

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
```

?

RAM

0	300	R0
1	5	R1
2		R2
...		...
15		R15
16		i
17		
...		
255		
256		
...		
300	-1	
301	-1	
302	-1	desired
303		output
304	-1	
305		
...		

Pointer-based processing

Pseudocode

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
i = 0
LOOP:
  if (i == R1) goto END
  RAM[R0 + i] = -1
  i = i + 1
  goto LOOP
END:
```

Assembly code

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
    // i = 0
    @i
    M=0
(LLOOP)
    // if (i == R1) goto END
    @i
    D=M
    @R1
    D=D-M
    @END
    D;JEQ
    // RAM[R0 + i] = -1
    @R0
    D=M
    @i
    A=D+M
    M=-1
    // i = i + 1
    @i
    M=M+1
    // goto LOOP
    @LLOOP
    0;JMP
(END)
    @END
    0;JMP
```

RAM

0	300	R0
1	5	R1
2		R2
...		...
15		R15
16		i
17		
...		
255		
256		
...		
300	-1	
301	-1	
302	-1	desired
303		output
304	-1	
305		
...		

Array processing

Pseudocode

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
i = 0
LOOP:
  if (i == R1) goto END
  RAM[R0 + i] = -1
  i = i + 1
  goto LOOP
END:
```

Assembly code

```
// Program: PointerDemo.asm
// Starting at the address stored in R0,
// sets the first R1 words to -1
    // i = 0
    @i
    M=0
(LLOOP)
    // if (i == R1) goto END
    @i
    D=M
    @R1
    D=D-M
    @END
    D;JEQ
    // RAM[R0 + i] = -1
    @R0
    D=M
    @i
    A=D+M
    M=-1
    // i = i + 1
    @i
    M=M+1
    // goto LOOP
    @LLOOP
    0;JMP
(END)
    @END
    0;JMP
```

RAM

0	300	R0
1	5	R1
2		R2
...		...
15		R15
16		i
17		
...		
255		
256		
...		
300	-1	
301	-1	
302	-1	desired
303		output
304	-1	
305		
...		

Array processing

Is done similarly, using pointer-based access to the memory block that represents the array.

Array processing

High-level code (e.g. Java)

```
...  
// Declares variables  
int[] arr = new int[5];  
int sum = 0;  
...  
// Enters some values into the array  
// (code omitted)  
...  
// Sums up the array elements  
for (int j=0; j<5; j++) {  
    sum = sum + arr[j];  
}  
...
```

Memory
state after
executing
this code:

RAM		
0		R0
1		R1
2		R2
...		...
15		R15
16	5034	arr
17		sum
...	4	j
75		
76		
...		
255		
256		
...		
5034	100	
5035	50	
5036	200	
5037		
5038	5	
5036		
...		

Array processing

High-level code (e.g. Java)

```
...  
// Declares variables  
int[] arr = new int[5];  
int sum = 0;  
...  
// Enters some values into the array  
// (code omitted)  
...  
// Sums up the array elements  
for (int j=0; j<5; j++) {  
    sum = sum + arr[j];  
}  
...  
// Increments each array element  
for (int j=0; j<5; j++) {  
    arr[j] = arr[j]+1  
}  
...
```

Compiler

Hack assembly

```
...  
// sum = sum + arr[j]  
@arr  
D=M  
A=D+M  
D=M  
@sum  
M=M+D  
...  
// arr[j] = arr[j] + 1  
@arr  
D=M  
@j  
A=D+M  
M=M+1  
...
```

RAM

0		R0
1		R1
2		R2
...		...
15		R15
16	5034	arr
17		sum
...	4	j
75		
76		
...		
255		
256		
...		
5034	100	
5035	50	
5036	200	
5037		
5038	5	
5036		
...		

Every high-level array access operation involving `arr[expression]` can be compiled into Hack code that realizes the operation using the low-level memory access instruction `A = arr + expression`

Chapter 4: Machine Language

Overview

- Machine languages
- The Hack computer
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- The Hack CPU Emulator

Symbolic programming

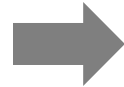
- Control
- Variables
- Labels

Low Level Programming



- Basic
- Iteration
- Pointers

The Hack Language



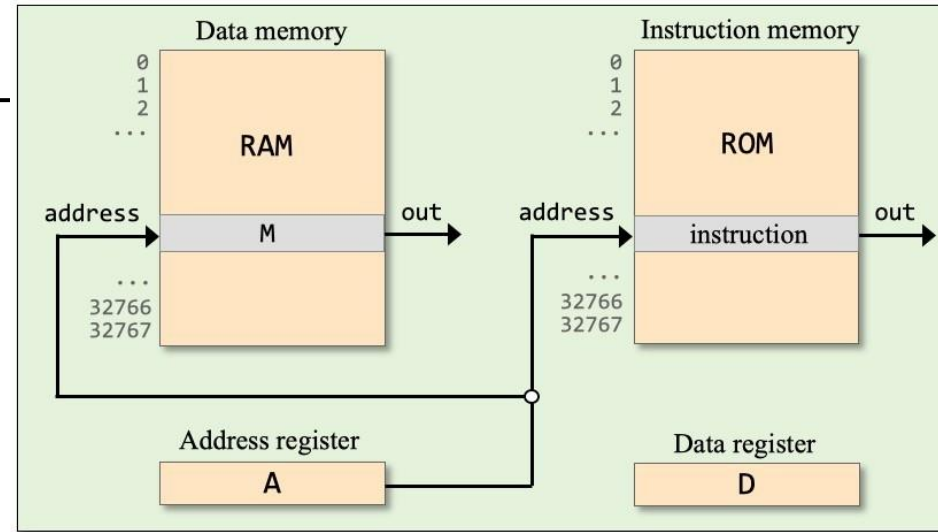
Usage

- Specification
- Output
- Input
- Project 4

The A instruction

Instruction set

- ➔ A instruction
 - C instruction



Syntax:

@value

Where *value* is either:

- ❑ a constant, or
- ❑ a symbol bound to a constant

Semantics:

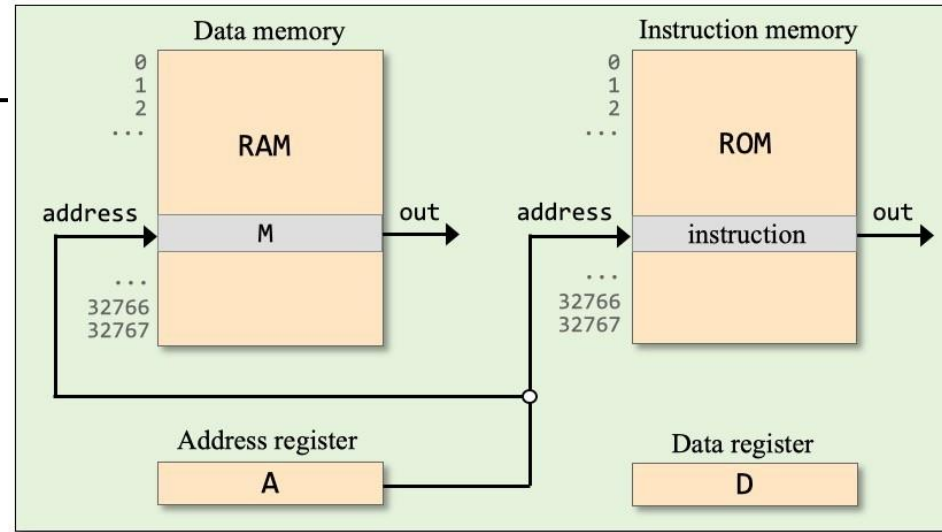
- Sets the A register to the constant
- Side effects:
 - RAM[A] becomes the selected RAM register
 - ROM[A] becomes the selected ROM register

The C instruction

Instruction set

- A instruction

➔ • C instruction



The C instruction

<u>Syntax:</u>	$dest = comp ; jump$	both $dest$ and $jump$ are optional
----------------	----------------------	-------------------------------------

where:

$comp =$	0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D A
	M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D M

<i>dest</i> =	null, M, D, DM, A, AM, AD, ADM	M stands for RAM[A]
---------------	--------------------------------	---------------------

<i>jump</i>	=	null, JGT, JEQ, JGE, JLT, JNE, JLE, JMP
-------------	---	---

Semantics:

Computes the value of *comp* and stores the result in *dest*.

If (*comp jump* 0), jumps to execute ROM[A]

The C instruction

Syntax: `dest = comp ; jump` both *dest* and *jump* are optional

where:

comp = `0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A`
`M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M`

dest = `null, M, D, DM, A, AM, AD, ADM` M stands for RAM[A]

jump = `null, JGT, JEQ, JGE, JLT, JNE, JLE, JMP`

Semantics:

Computes the value of *comp* and stores the result in *dest*.

If (*comp* *jump* 0), jumps to execute ROM[A]

Examples:

```
// Sets the D register to -1
D = -1
```

The C instruction

Syntax: `dest = comp ; jump` both *dest* and *jump* are optional

where:

comp = `0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A`
`M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M`

dest = `null, M, D, DM, A, AM, AD, ADM` M stands for RAM[A]

jump = `null, JGT, JEQ, JGE, JLT, JNE, JLE, JMP`

Semantics:

Computes the value of *comp* and stores the result in *dest*.

If (*comp* *jump* 0), jumps to execute ROM[A]

Examples:

```
// Sets D and M to the value of the D register, plus 1
DM=D+1
```

The C instruction

Syntax: `dest = comp ; jump` both *dest* and *jump* are optional

where:

comp = `0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A`
`M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M`

dest = `null, M, D, DM, A, AM, AD, ADM` M stands for RAM[A]

jump = `null, JGT, JEQ, JGE, JLT, JNE, JLE, JMP`

Semantics:

Computes the value of *comp* and stores the result in *dest*.

If (*comp jump* 0), jumps to execute ROM[A]

Examples:

```
// If (D-1 = 0) jumps to execute the instruction stored in ROM[56]
@56
D-1; JEQ
```

Recap: A instructions and C instructions

They normally come in pairs:

```
// RAM[5] = RAM[5] - 1  
@5  
M=M-1
```

To set up for a C instruction that mentions M,
Use an A instruction that selects the memory address
on which you want to operate

```
// if D=0 goto 100  
@100  
D;JEQ
```

To set up for a C instruction that specifies a jump,
Use an A instruction that selects the memory address
to which you want to jump

Observation: C instructions that include *both* M *and* a jump directive *make no sense*

Best practice rule: Each C instruction should ...

- Either have a reference to M
- Or have a jump directive

But not both.

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The Hack Language



Usage



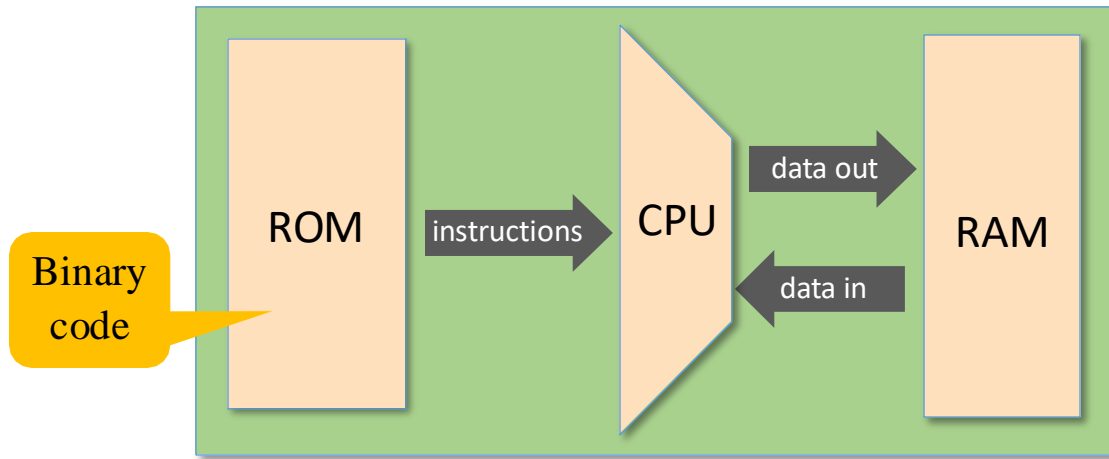
Specification

- Output
- Input
- Project 4

The Hack machine language

So far, we illustrated the Hack language using examples.
We now turn to give a complete language specification.

Hack machine language



The Hack language:

Symbolic: (example)

```
...  
@17  
D;JLE  
...
```

translate

Binary:

```
...  
0000000000010001  
1110001100000110  
...
```

load & execute

- The *binary version* of the language is not essential for low-level programming
- We present it anyway, for completeness
- The binary version will come to play when we'll build the computer architecture (chapter 5) and the assembler (chapter 6)

A instruction

Action: Sets the A register to a constant

Symbolic syntax:

@value

Binary syntax:

0 v v v v v v v v v v v v v v v v

Where *value* is either:

a non-negative decimal
constant ≤ 65535 ($= 2^{16} - 1$)
or a symbol bound to a constant

Where:

0 is the A instruction op-code
v v v ... v is the 15-bit binary
representation of the constant

Example:

Symbolic:

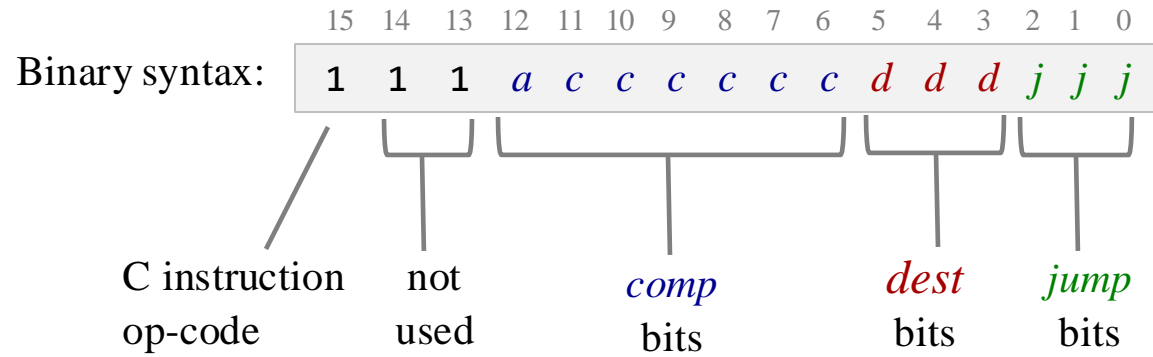
@6

Binary:

00000000000000110

C instruction

Symbolic syntax: *dest* = *comp* ; *jump* *comp* is mandatory.
If *dest* is empty, the = is omitted; If *jump* is empty, the ; is omitted



C instruction

Symbolic syntax: *dest* = *comp* ; *jump* *comp* is mandatory.
If *dest* is empty, the = is omitted; If *jump* is empty, the ; is omitted

Binary syntax:

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	1	1	<i>a</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>j</i>	<i>j</i>	<i>j</i>

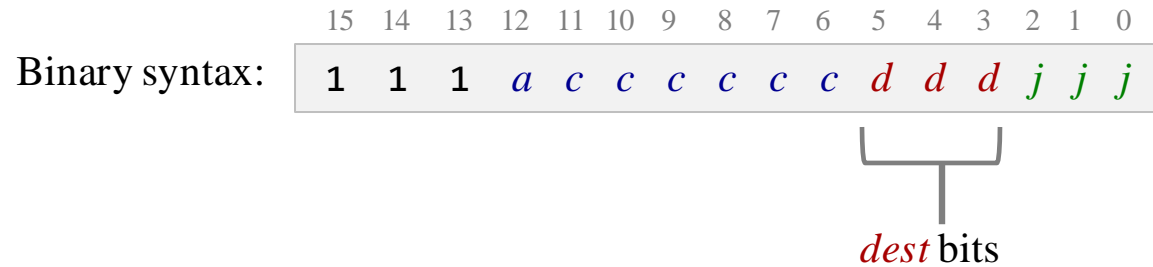
comp bits

<i>comp</i>		<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>
0		1	0	1	0	1	0
1		1	1	1	1	1	1
-1		1	1	1	0	1	0
D		0	0	1	1	0	0
A	M	1	1	0	0	0	0
!D		0	0	1	1	0	1
!A	!M	1	1	0	0	0	1
-D		0	0	1	1	1	1
-A	-M	1	1	0	0	1	1
D+1		0	1	1	1	1	1
A+1	M+1	1	1	0	1	1	1
D-1		0	0	1	1	1	0
A-1	M-1	1	1	0	0	1	0
D+A	D+M	0	0	0	0	1	0
D-A	D-M	0	1	0	0	1	1
A-D	M-D	0	0	0	1	1	1
D&A	D&M	0	0	0	0	0	0
D A	D M	0	1	0	1	0	1

a == 0 *a* == 1

C instruction

Symbolic syntax: *dest* = *comp* ; *jump* *comp* is mandatory.
If *dest* is empty, the = is omitted; If *jump* is empty, the ; is omitted



<i>dest</i>	<i>d</i>	<i>d</i>	<i>d</i>	effect: the value is stored in:
null	0	0	0	the value is not stored
M	0	0	1	RAM[A]
D	0	1	0	D register
DM	0	1	1	D register and RAM[A]
A	1	0	0	A register
AM	1	0	1	A register and RAM[A]
AD	1	1	0	A register and D register
ADM	1	1	1	A register, D register, and RAM[A]

C instruction

Symbolic syntax: *dest* = *comp* ; *jump* *comp* is mandatory.
If *dest* is empty, the = is omitted; If *jump* is empty, the ; is omitted

Binary syntax:

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	1	1	<i>a</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>j</i>	<i>j</i>	<i>j</i>

└───┬───┘
 jump bits

<i>jump</i>	<i>j</i>	<i>j</i>	<i>j</i>	effect:
null	0	0	0	no jump
JGT	0	0	1	if <i>comp</i> > 0 jump
JEQ	0	1	0	if <i>comp</i> = 0 jump
JGE	0	1	1	if <i>comp</i> ≥ 0 jump
JLT	1	0	0	if <i>comp</i> < 0 jump
JNE	1	0	1	if <i>comp</i> ≠ 0 jump
JLE	1	1	0	if <i>comp</i> ≤ 0 jump
JMP	1	1	1	Unconditional jump

The Hack language specification

A instruction Symbolic: $@xxx$ (xxx is a decimal value ranging from 0 to 32767, or a symbol bound to such a decimal value)

Binary: $0\ vvvvvvvvvvvvvvvv$ ($vv \dots v = 15\text{-bit value of } xxx$)

C instruction Symbolic: $dest = comp; jump$ ($comp$ is mandatory.
If $dest$ is empty, the $=$ is omitted;
If $jump$ is empty, the $;$ is omitted)

Binary: $111acccccdddj$

Predefined symbols:

symbol	value
R0	0
R1	1
R2	2
...	...
R15	15
SP	0
LCL	1
ARG	2
THIS	3
THAT	4
SCREEN	16384
KBD	24576

$comp$		c	c	c	c	c	c	$dest$	d	d	d	Effect: store $comp$ in:
0		1	0	1	0	1	0	null	0	0	0	the value is not stored
1		1	1	1	1	1	1	M	0	0	1	RAM[A]
-1		1	1	1	0	1	0	D	0	1	0	D register (reg)
D		0	0	1	1	0	0	DM	0	1	1	RAM[A] and D reg
A	M	1	1	0	0	0	0	A	1	0	0	A reg
!D		0	0	1	1	0	1	AM	1	0	1	A reg and RAM[A]
!A	!M	1	1	0	0	0	1	AD	1	1	0	A reg and D reg
-D		0	0	1	1	1	1	ADM	1	1	1	A reg, D reg, and RAM[A]
-A	-M	1	1	0	0	1	1					
D+1		0	1	1	1	1	1	$jump$	j	j	j	Effect:
A+1	M+1	1	1	0	1	1	1	null	0	0	0	no jump
D-1		0	0	1	1	1	0	JGT	0	0	1	if $comp > 0$ jump
A-1	M-1	1	1	0	0	1	0	JEQ	0	1	0	if $comp = 0$ jump
D+A	D+M	0	0	0	0	1	0	JGE	0	1	1	if $comp \geq 0$ jump
D-A	D-M	0	1	0	0	1	1	JLT	1	0	0	if $comp < 0$ jump
A-D	M-D	0	0	0	1	1	1	JNE	1	0	1	if $comp \neq 0$ jump
D&A	D&M	0	0	0	0	0	0	JLE	1	1	0	if $comp \leq 0$ jump
D A	D M	0	1	0	1	0	1	JMP	1	1	1	unconditional jump

$a == 0$ $a == 1$

Chapter 4: Machine Language



Overview

- Machine languages
- The Hack computer
- The Hack instruction set
- The Hack CPU Emulator



Symbolic programming

- Control
- Variables
- Labels



Low Level Programming

- Basic
- Iteration
- Pointers

The Hack Language



Usage



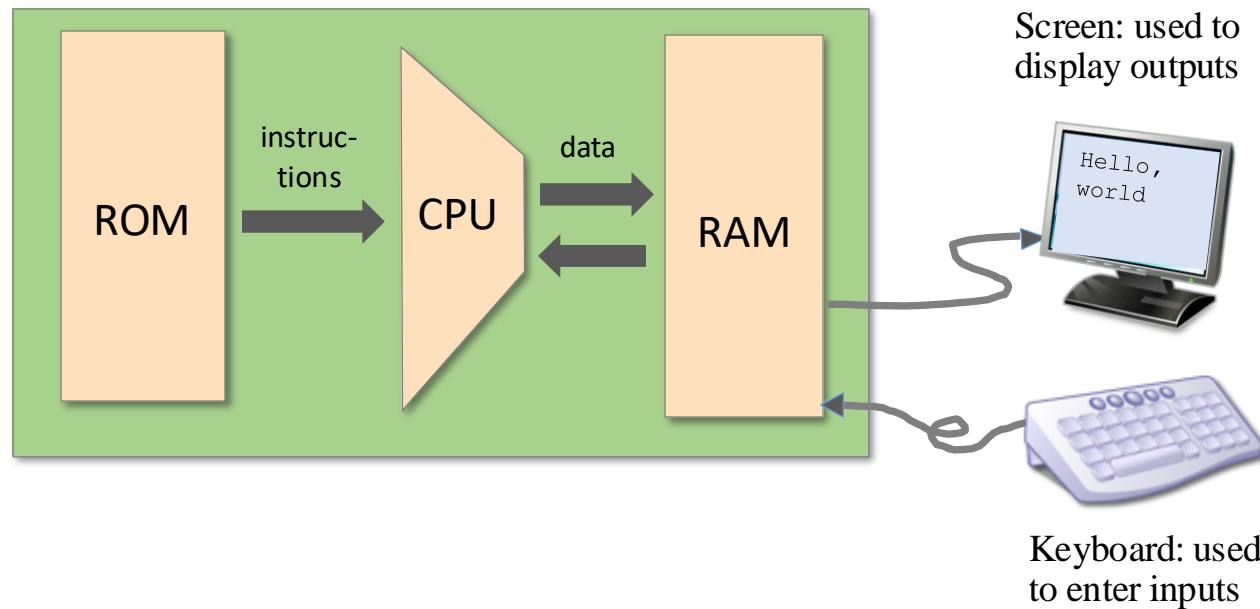
Specification



Output

- Input
- Project 4

Input / output



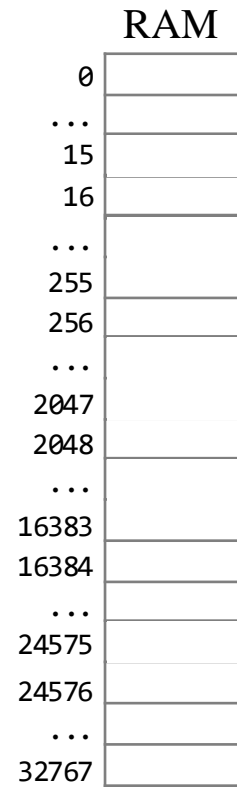
High-level I/O handling:

Software libraries for inputting / outputting text, graphics, audio, video, ...

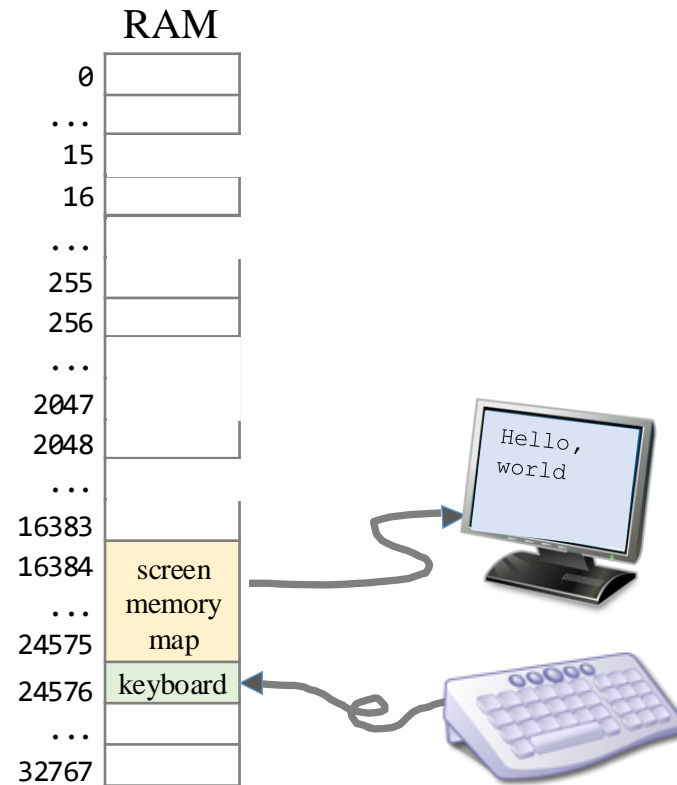
Low-level I/O handling:

Manipulating bits in memory resident *bitmaps*.

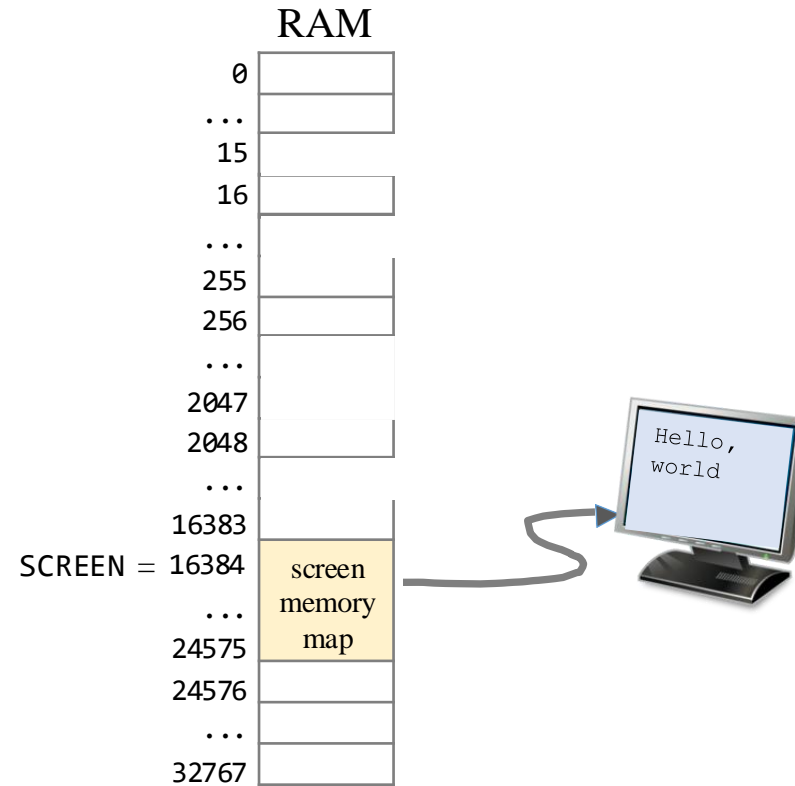
Bitmaps



Bitmaps



Bitmaps



Screen memory map:

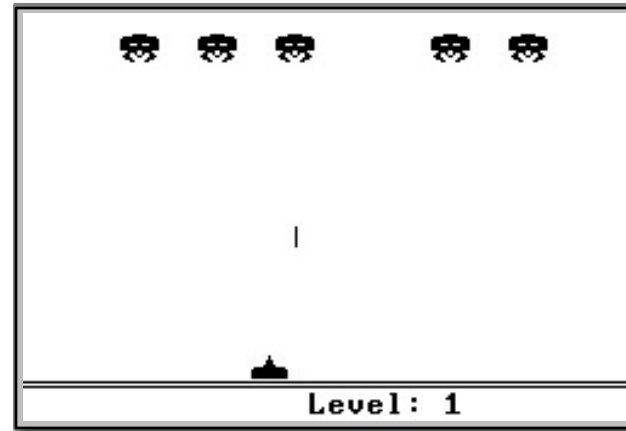
An 8K memory block, dedicated to representing a black-and-white display unit

Base address: SCREEN = 16384 (predefined symbol)

Output is effected by writing bits in the screen memory map.

Bitmaps

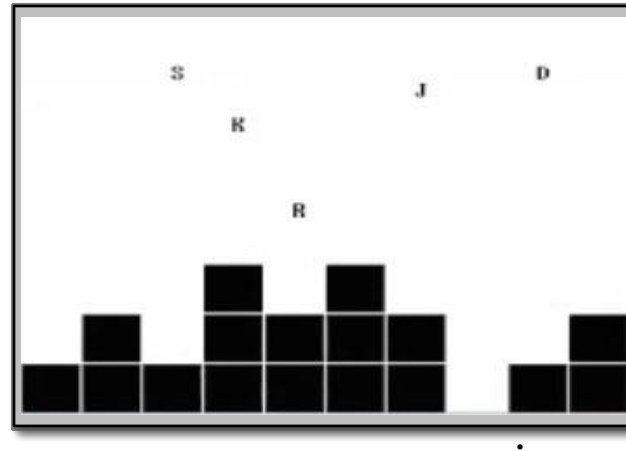
Physical screen



Screen shots of computer games
developed on the Hack computer

Bitmaps

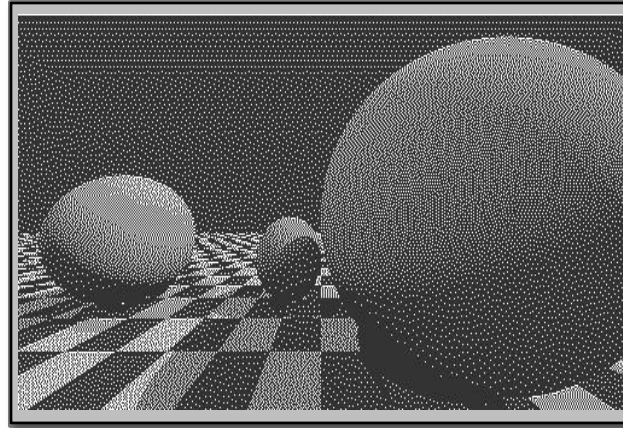
Physical screen



Screen shots of computer games
developed on the Hack computer

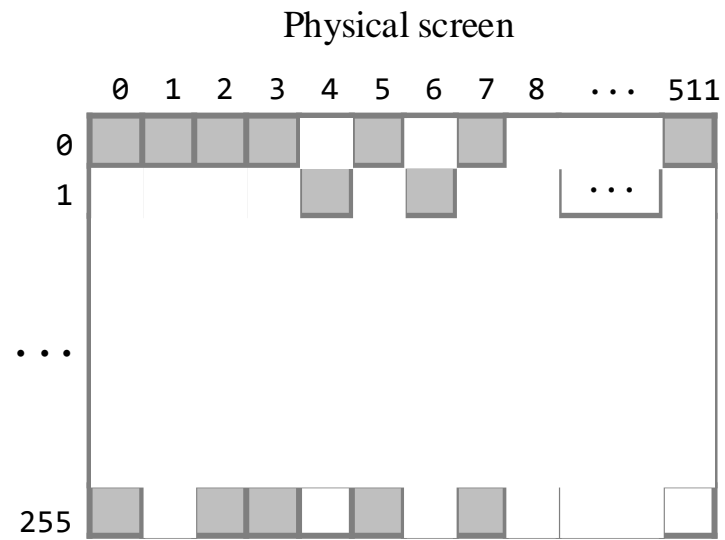
Bitmaps

Physical screen

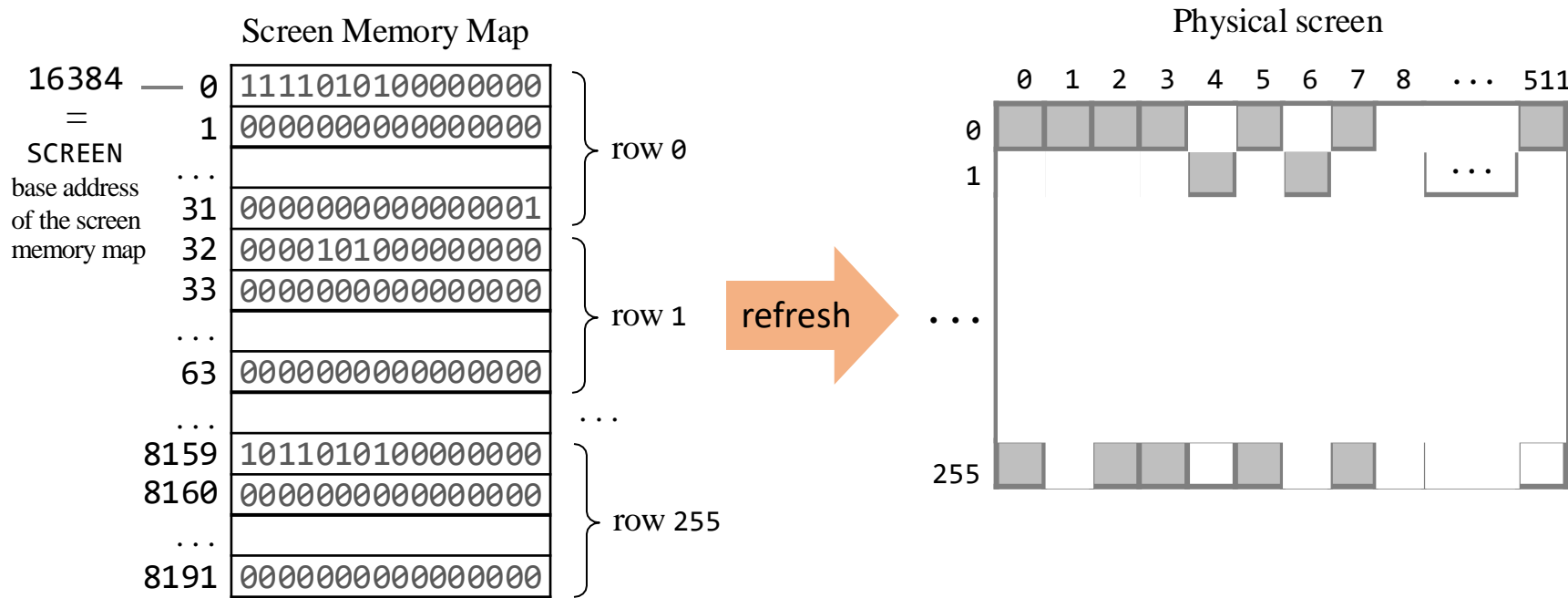


Screen shots of computer games
developed on the Hack computer

Bitmaps



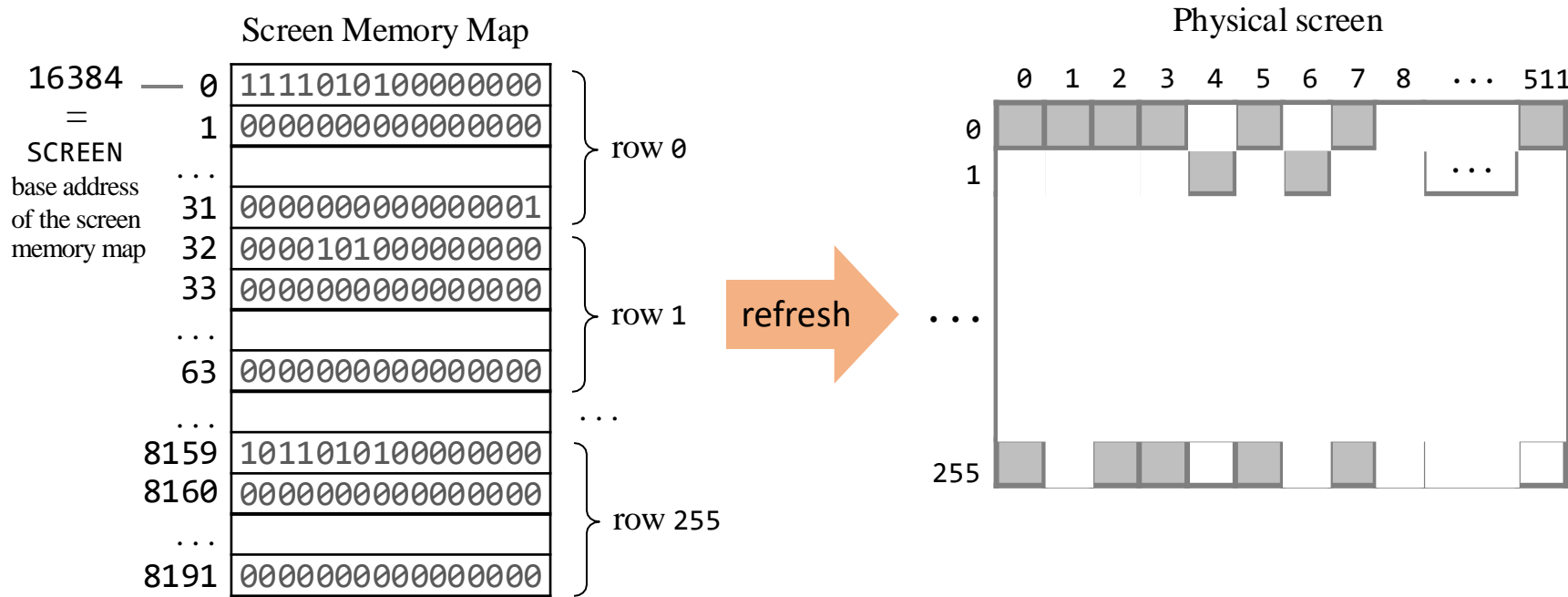
Bitmaps



Mapping:

The pixel in location (row, col) in the physical screen is represented by the $(col \% 16)th$ bit in RAM address $SCREEN + 32 * row + col / 16$

Bitmaps



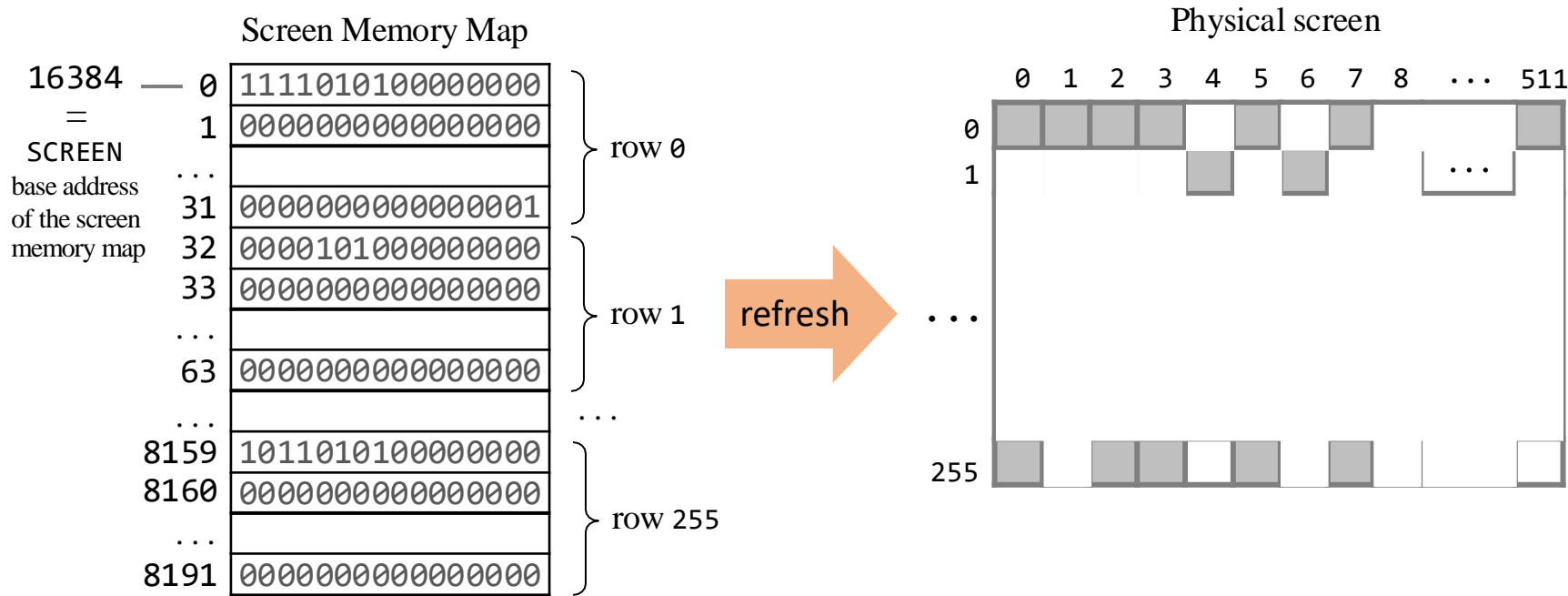
To set pixel (*row*, *col*) to black or white:

- (1) $addr \leftarrow SCREEN + 32 * row + col / 16$
- (2) $word \leftarrow RAM[addr]$
- (3) Set the ($col \% 16$)th bit of *word* to 0 or 1
- (4) $RAM[addr] \leftarrow word$

Not to worry:

Nice workarounds coming up
(Bitmap Editor)

Bitmaps



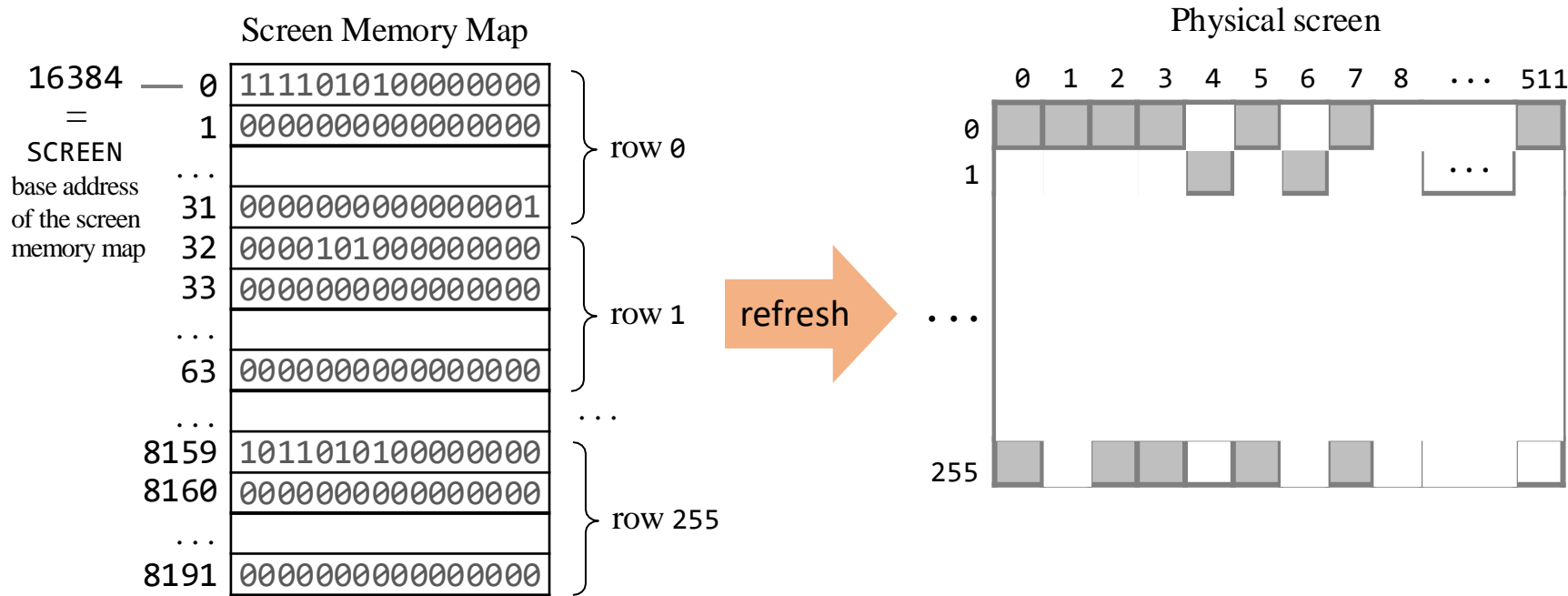
Examples of simple patterns that
can be drawn relatively easily:

```
// Sets the first (left) 16 pixels  
// of the top row to black  
@SCREEN  
M=-1      // -1 = 1111111111111111
```

```
// Sets the first 16 pixels  
// of row 2 to black
```

?

Bitmaps



Examples of simple patterns that can be drawn relatively easily:

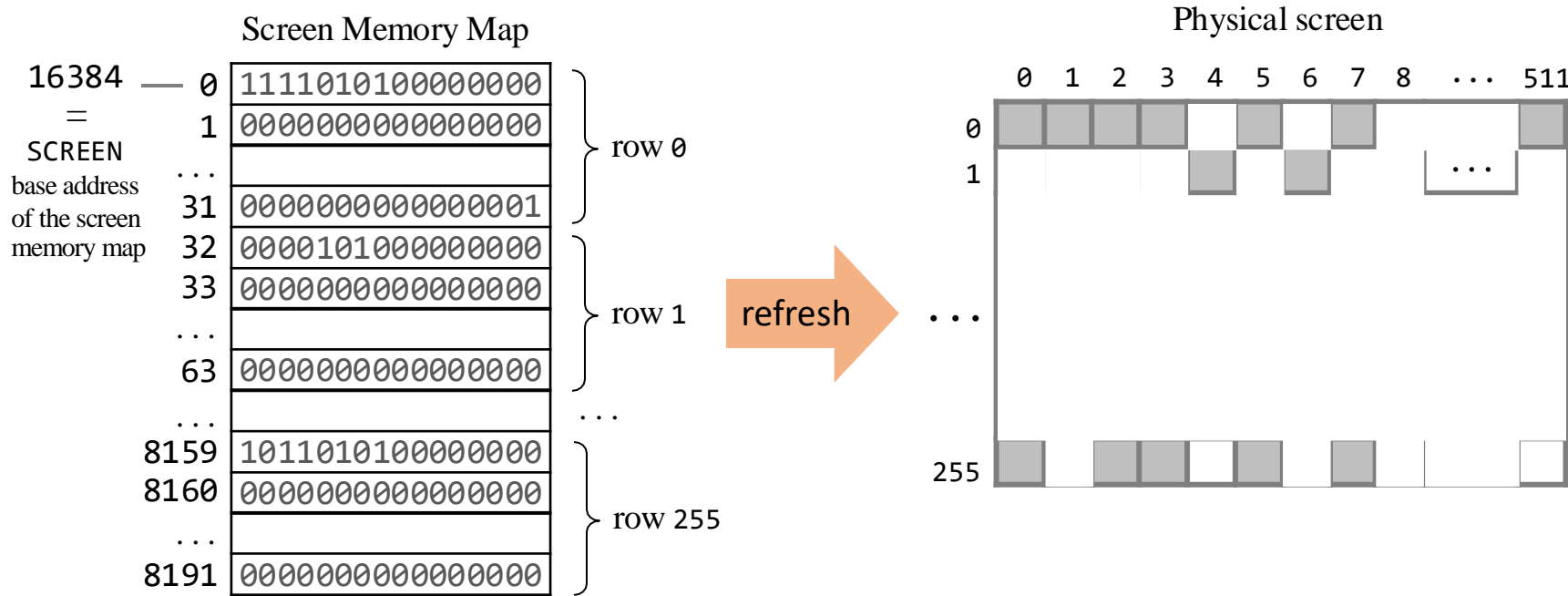
```
// Sets the first (left) 16 pixels
// of the top row to black
@SCREEN
M=-1      // -1 = 1111111111111111
```

```
// Sets the first 16 pixels
// of row 2 to black
@64
D=A
@SCREEN
A=A+D
M=-1
```

```
// Sets the entire screen
// to black / white
```

(Project 4)

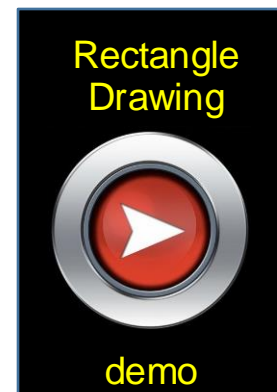
Bitmaps



Examples of simple patterns that can be drawn relatively easily:

```
// Sets the first (left) 16 pixels  
// of the top row to black  
@SCREEN  
M=-1      // -1 = 1111111111111111
```

Simple
graphics
program:



Bitmap Editor

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1																
2																
3																
4																
5																
6																
7																
8																
9																
10																
11																
12																
13																
14																
15																
16																

00001111111100000 = 4064

0001100000110000 = 6192

0001001010010000 = 4752

...

Bitmap editor: A productivity tool for developers.

The developer draws a pixeled image on a 2D grid, and the program generates code that draws the image in the RAM.

The generated code can be copy-pasted into the developer's assembly code.

...

0111111011111100 = 32508

The Nand to Tetris Bitmap Editor is available in this [Git project](#)

Note: The editor generates either Jack code or Hack assembly code – see the radio buttons at the very bottom of the editor's GUI.

Chapter 4: Machine Language

Overview

- Machine languages
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Low Level Programming

- Basic
- Iteration
- Pointers

Symbolic programming

- Control
- Variables
- Labels

The Hack Language

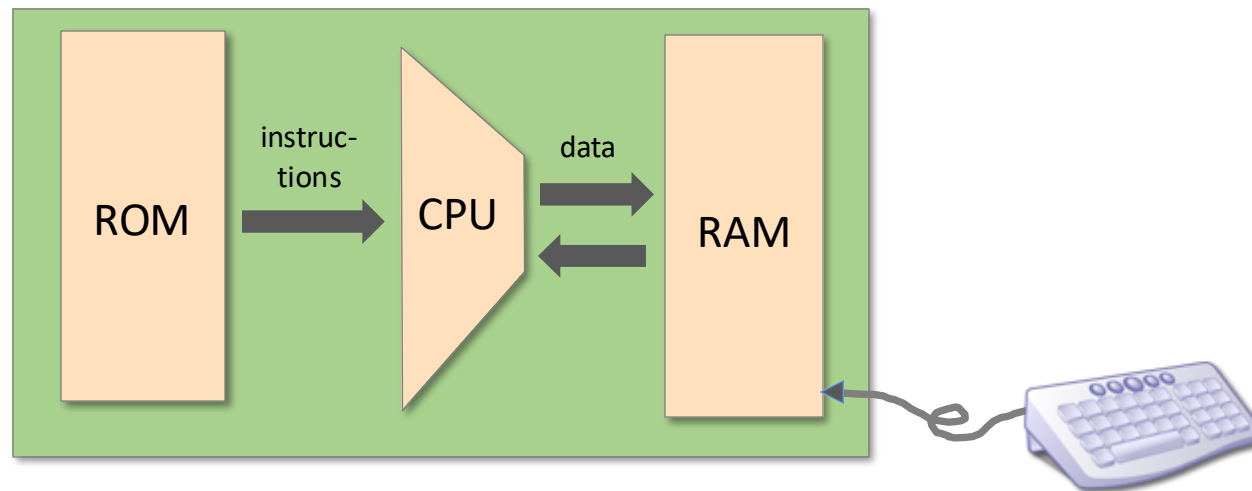
- ✓ Usage
- ✓ Specification
- ✓ Output



Input

- Project 4

Input



Keyboard: used
to enter inputs

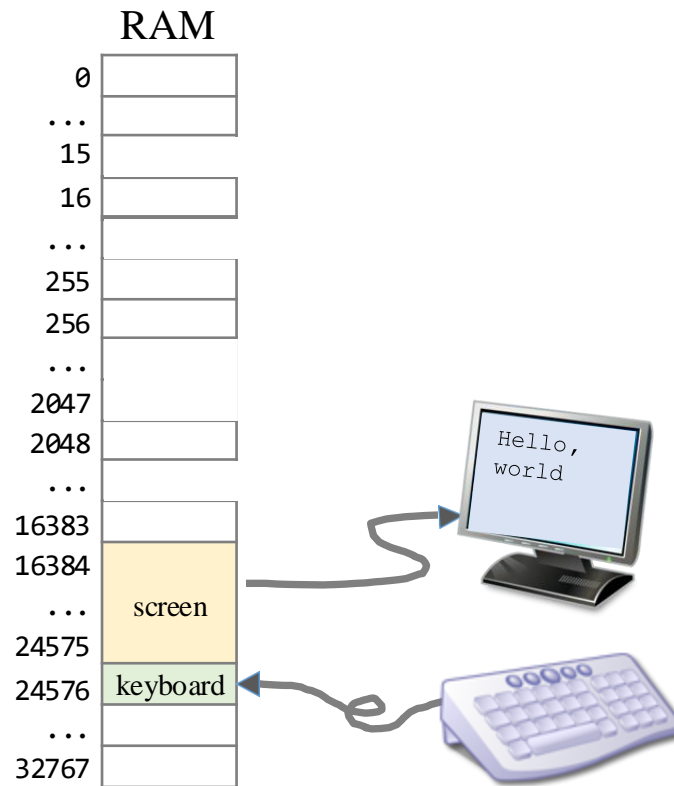
High-level input handling

`readInt`, `readString`, ...

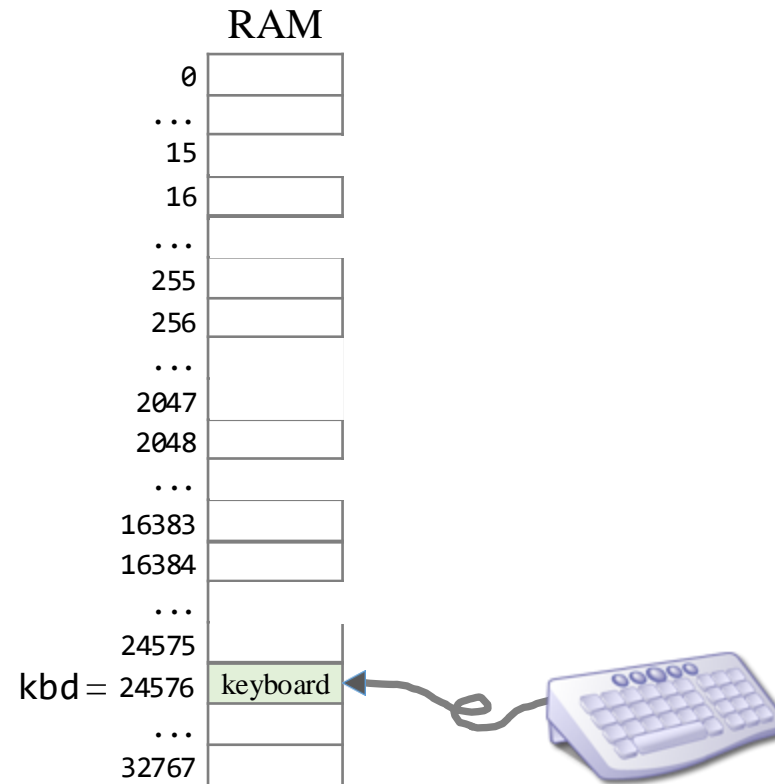
Low-level input handling

Read bits.

Hack RAM



Hack RAM



Keyboard memory map

A single 16-bit register, dedicated to representing the keyboard

Base address: KBD = 24576 (predefined symbol)

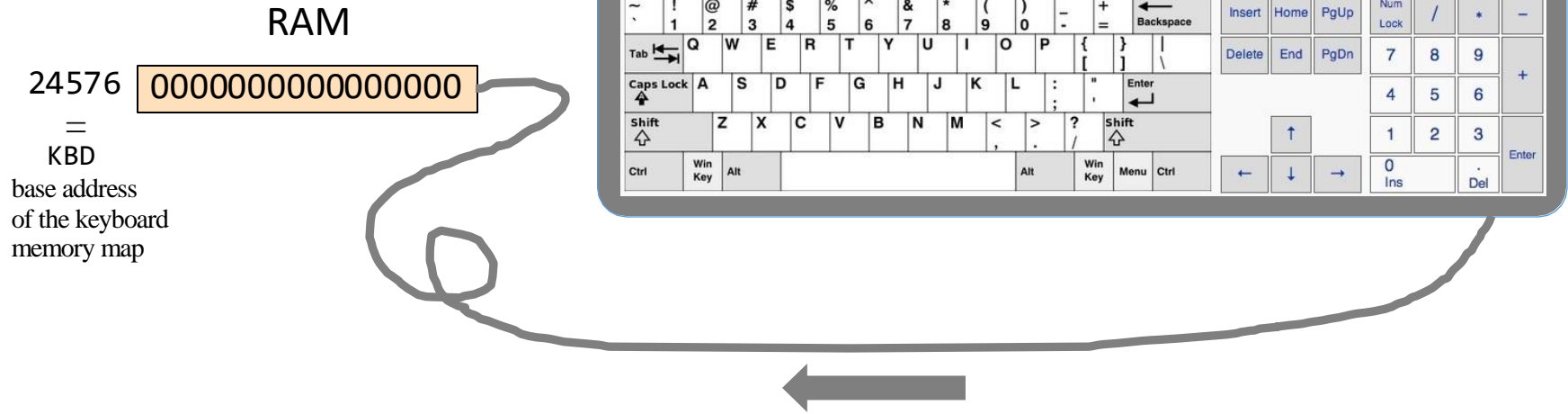
Reading inputs is affected by probing this register.

The Hack character set

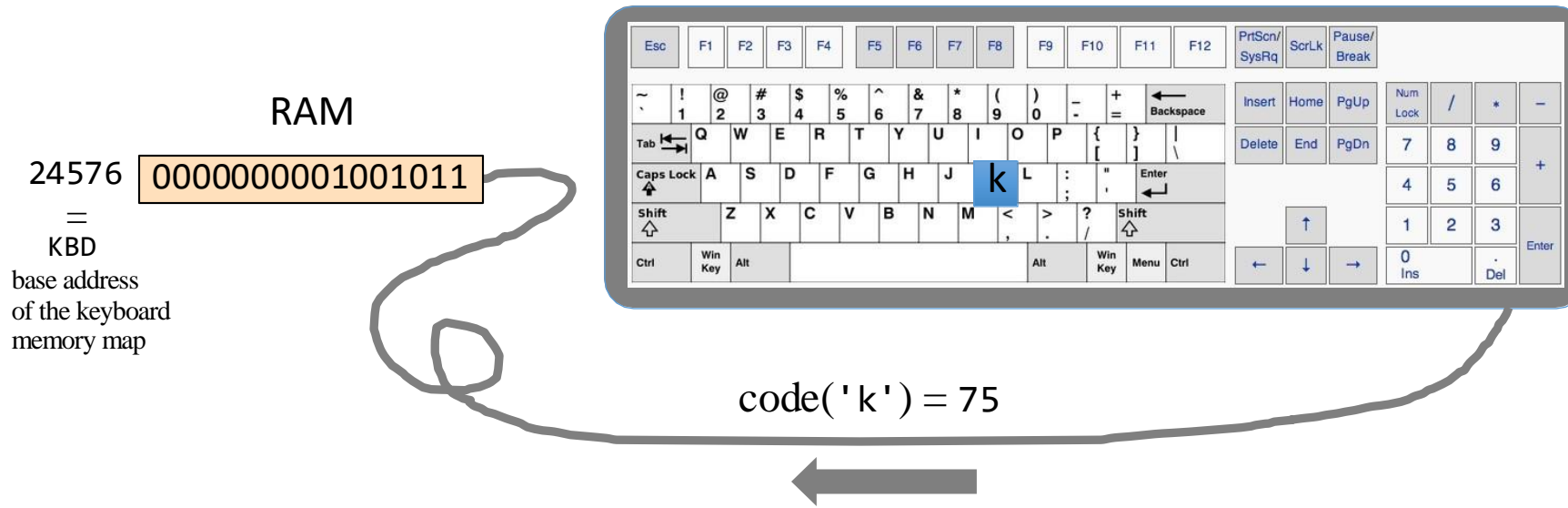
key	code	key	code	key	code	key	code	key	code
(space)	32	0	48	A	65	a	97	newline	128
!	33	1	49	B	66	b	98	backspace	129
“	34	C	...	c	99	left arrow	130
#	35	9	57	up arrow	131
\$	36			Z	90	z	122	right arrow	132
%	37	:	58			{	123	down arrow	133
&	38	;	59	[91		124	home	134
‘	39	<	60	/	92			end	135
(40	=	61]	93	}	125	Page up	136
)	41	>	62	^	94	~	126	Page down	137
*	42	?	63	_	95			insert	138
+	43	@	64	`	96			delete	139
,	44							esc	140
-	45							f1	141
.	46						
/	47							f12	152

(Subset of Unicode)

Memory mapped input

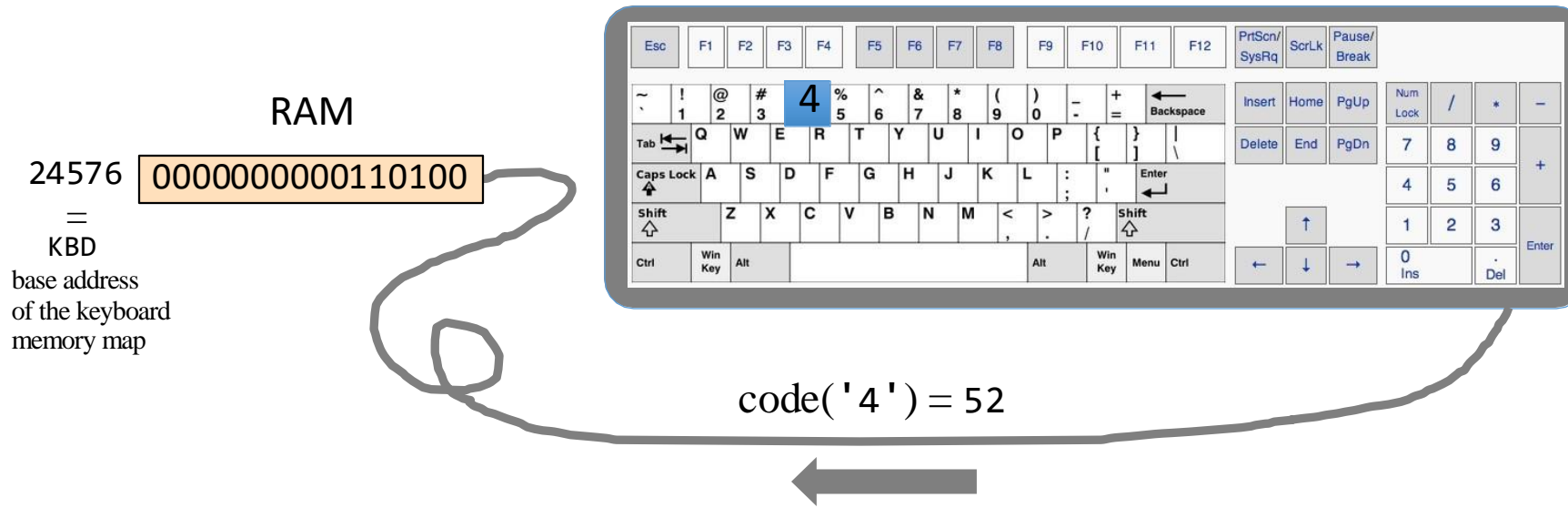


Memory mapped input



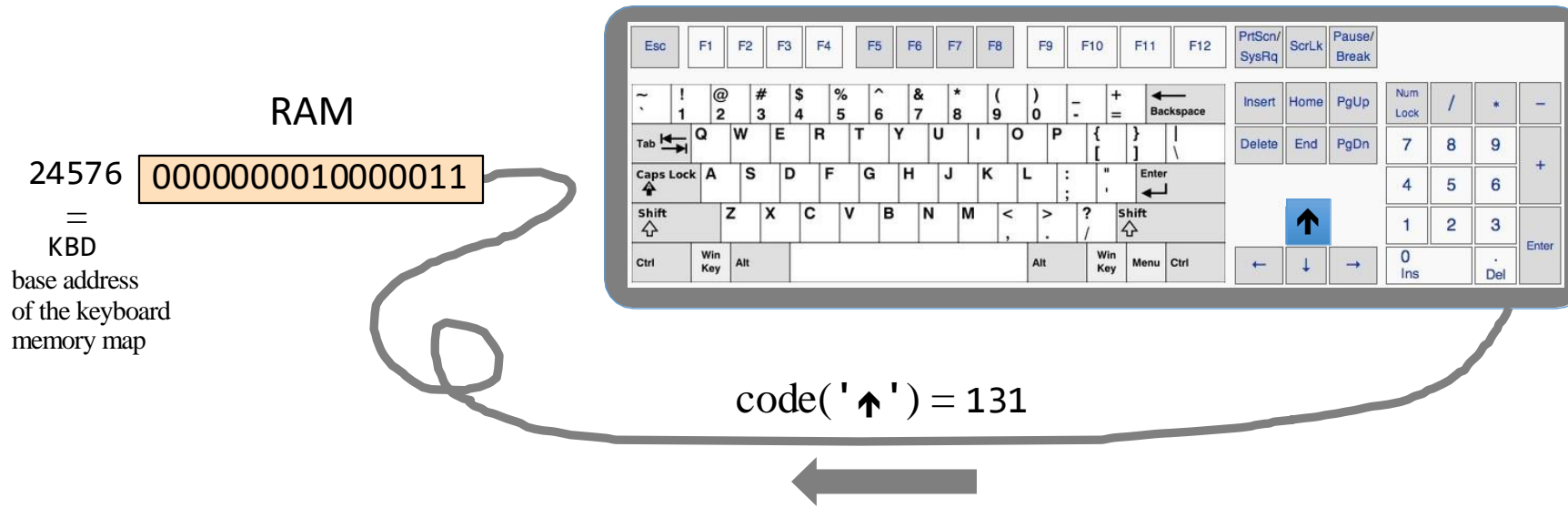
When a key is pressed on the keyboard,
the key's character code appears in the keyboard memory map.

Memory mapped input



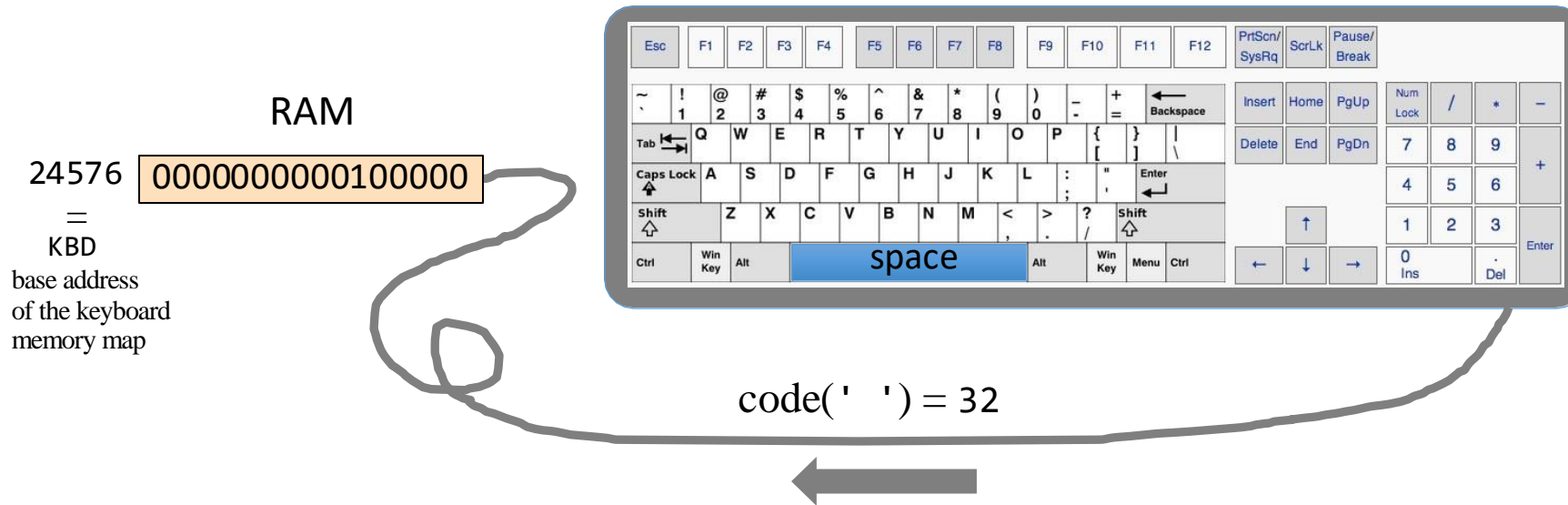
When a key is pressed on the keyboard,
the key's character code appears in the keyboard memory map.

Memory mapped input



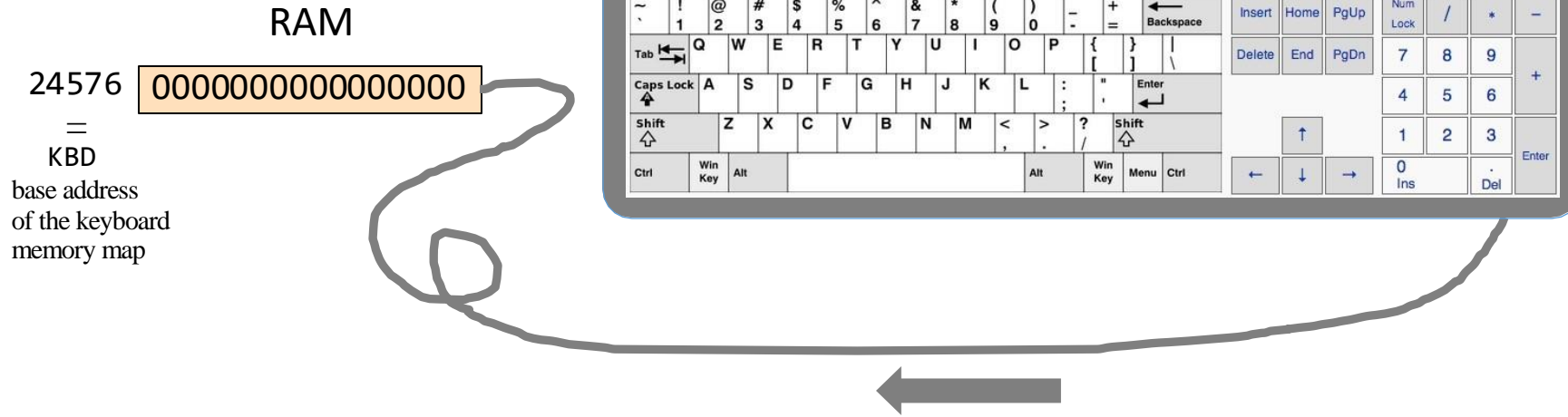
When a key is pressed on the keyboard,
the key's character code appears in the keyboard memory map.

Memory mapped input



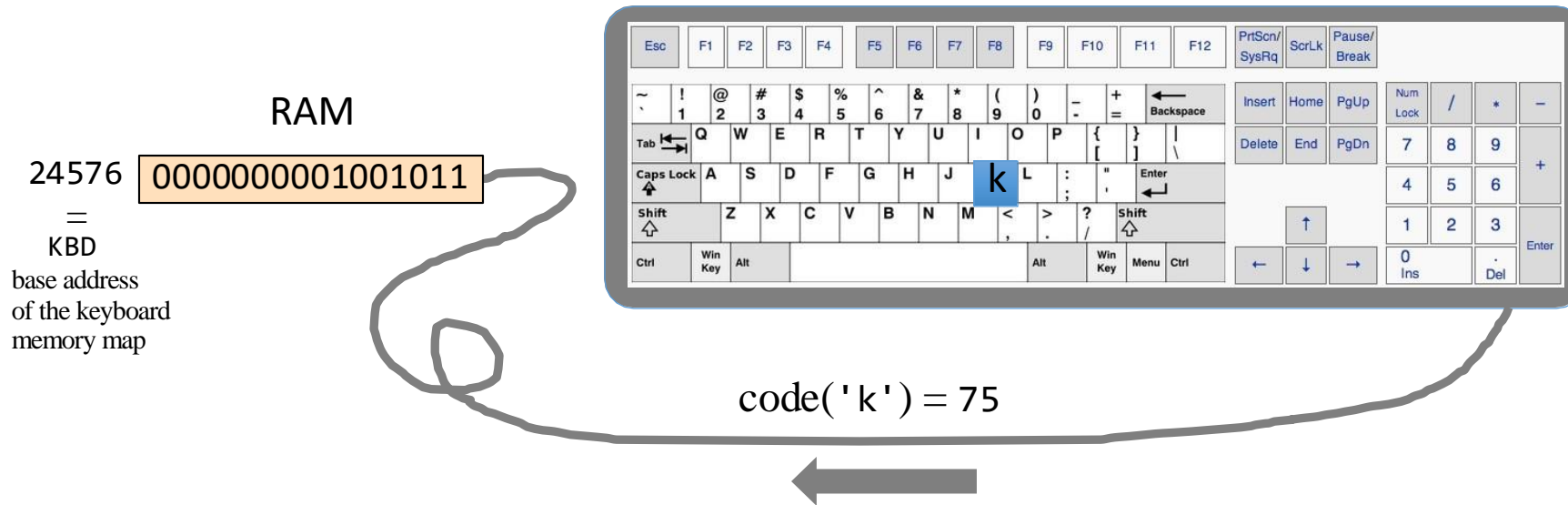
When a key is pressed on the keyboard,
the key's character code appears in the keyboard memory map.

Memory mapped input



When no key is pressed, the resulting code is 0.

Reading inputs



Examples:

```
// Set D to the character code of  
// the currently pressed key  
@KBD  
D=M
```

```
// If the currently pressed key is 'q', goto END  
@KBD  
D=M  
@113 // 'q'  
D=D-A  
@END  
D;JEQ
```

Chapter 4: Machine Language

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Low Level Programming

- Basic
- Iteration
- Pointers

Symbolic programming

- Control
- Variables
- Labels

The Hack Language

- ✓ Usage
- ✓ Specification
- ✓ Output
- ✓ Input



Project 4

Objectives

Gain a hands-on taste of:

- Low-level programming
- Assembly language
- The Hack computer

Tasks

- Write a simple algebraic program: `Mult`
- Write a simple interactive program: `Fill`
- Be creative: Define and write some program of your own.

Mult: a program that computes $R2 = R0 * R1$

CPU Emulator (2.5) - /Users/admin/Dropbox (Slate Team)/hack/project solutions/04/mult/Mult.hack

File View Run Help

Slow Fast Animate: No animation View: Scr... Format: D...

ROM

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	
21	
22	
23	
24	
25	
26	
27	
28	

code not shown

RAM

0	6
1	7
2	42
3	0
4	0
5	0
6	0
7	0
8	0
9	0
10	0
11	0
12	0
13	0
14	0
15	0
16	42
17	-1
18	0
19	0
20	0
21	0
22	0
23	0
24	0
25	0
26	0
27	0
28	0

PC 20 A 20

D 42

ALU

D Input : 42

M/A Input : 20

ALU output : 0

Mult: a program that computes $R2 = R0 * R1$

CPU Emulator (2.5) - /Users/admin/Dropbox (Slate Team)/hack/project solutions/04/mult/Mult.hack

File View Run Help

Slow Fast Animate: No animation View: Scr... Format: D...

ROM

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	
21	
22	
23	
24	
25	
26	
27	
28	

code not shown

RAM

0	6
1	7
2	42
3	0
4	0
5	0
6	0
7	0
8	0
9	0
10	0
11	0
12	0
13	0
14	0
15	0
16	42
17	-1
18	0
19	0
20	0
21	0
22	0
23	0
24	0
25	0
26	0
27	0
28	0

```
set PC 0,  
set RAM[0] 2,  
set RAM[1] 4;  
repeat 150 {  
  ticktock;  
}  
output;  
  
set PC 0,  
set RAM[0] 6,  
set RAM[1] 7;  
repeat 210 {  
  ticktock;  
}  
output;
```

D 42

ALU

D Input: 42

M/A Input: 20

ALU output: 0

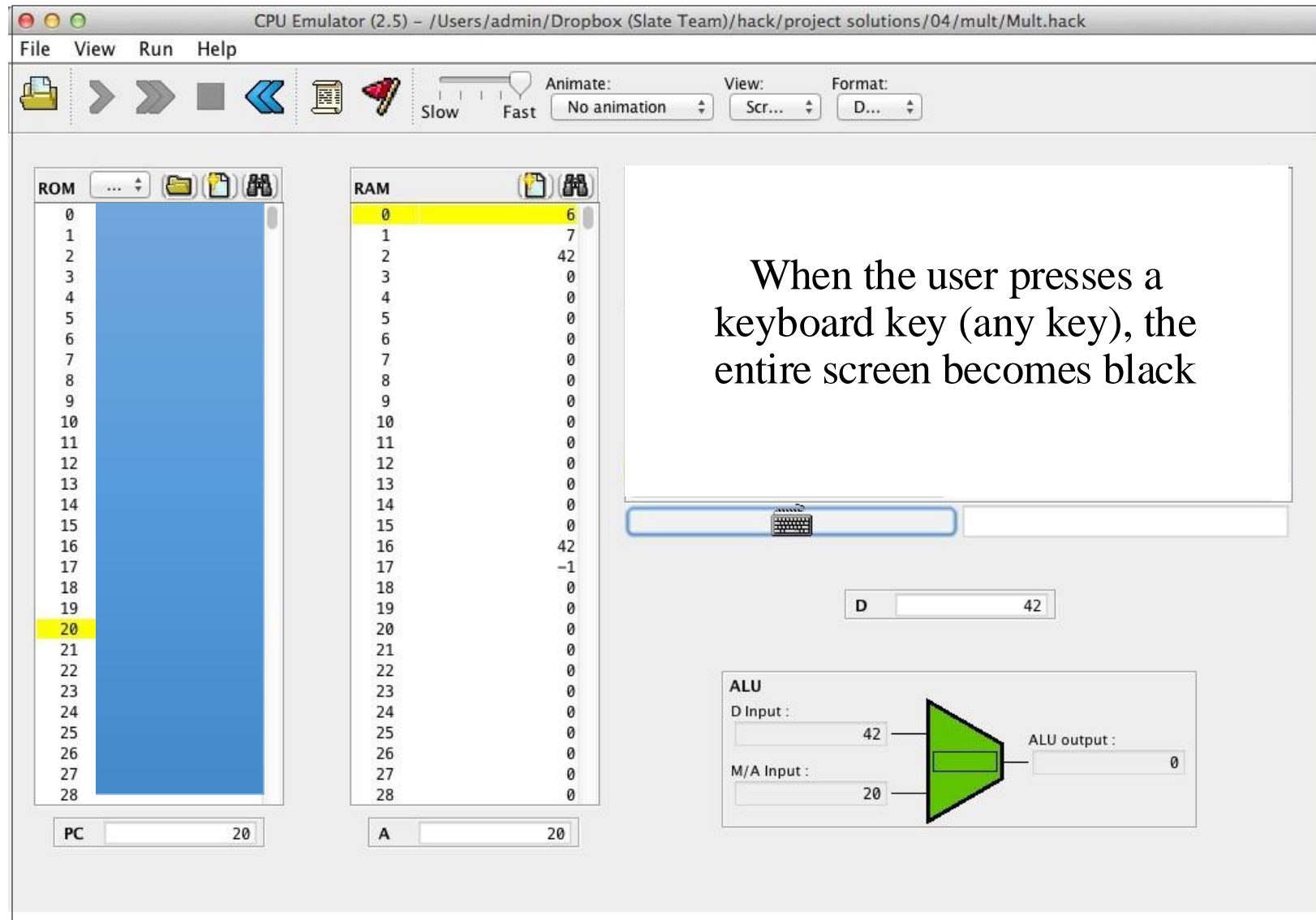
PC 20 A 20

Mult: a program that computes $R2 = R0 * R1$

The screenshot shows a CPU Emulator (2.5) window with the following components:

- ROM:** A list of memory addresses from 0 to 28. Address 20 is highlighted in yellow. The text "code not shown" is displayed in the center of the ROM window.
- RAM:** A list of memory addresses from 0 to 28. Address 0 is highlighted in yellow. The values for RAM are: 0: 6, 1: 7, 2: 42, 3: 0, 4: 0, 5: 0, 6: 0, 7: 0, 8: 0, 9: 0, 10: 0, 11: 0, 12: 0, 13: 0, 14: 0, 15: 0, 16: 42, 17: -1, 18: 0, 19: 0, 20: 0, 21: 0, 22: 0, 23: 0, 24: 0, 25: 0, 26: 0, 27: 0, 28: 0.
- PC (Program Counter):** A register showing the value 20.
- A (Accumulator):** A register showing the value 20.
- D (Data Register):** A register showing the value 42.
- ALU (Arithmetic Logic Unit):** A diagram showing the ALU output. The D Input is 42 and the M/A Input is 20. The ALU output is 0.
- Implementation strategy:** A text box containing the following text:
 - Loop: Repetitive addition
 - Inefficient implementation of multiplication, but OK for the purpose of this project.

Fill: a simple interactive program



Fill: a simple interactive program

CPU Emulator (2.5) - /Users/admin/Dropbox (Slate Team)/hack/project solutions/04/mult/Mult.hack

File View Run Help

Slow Fast Animate: No animation View: Scr... Format: D...

ROM

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	
21	
22	
23	
24	
25	
26	
27	
28	

PC 20

RAM

0	6
1	7
2	42
3	0
4	0
5	0
6	0
7	0
8	0
9	0
10	0
11	0
12	0
13	0
14	0
15	0
16	42
17	-1
18	0
19	0
20	0
21	0
22	0
23	0
24	0
25	0
26	0
27	0
28	0

A 20

The screen remains black as long as the key is pressed.

D 42

ALU

D Input : 42

M/A Input : 20

ALU output : 0

Fill: a simple interactive program

CPU Emulator (2.5) - /Users/admin/Dropbox (Slate Team)/hack/project solutions/04/mult/Mult.hack

File View Run Help

Slow Fast Animate: No animation View: Scr... Format: D...

ROM

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	
21	
22	
23	
24	
25	
26	
27	
28	

PC 20

RAM

0	6
1	7
2	42
3	0
4	0
5	0
6	0
7	0
8	0
9	0
10	0
11	0
12	0
13	0
14	0
15	0
16	42
17	-1
18	0
19	0
20	0
21	0
22	0
23	0
24	0
25	0
26	0
27	0
28	0

A 20

When the user releases the key, the screen is cleared

D 42

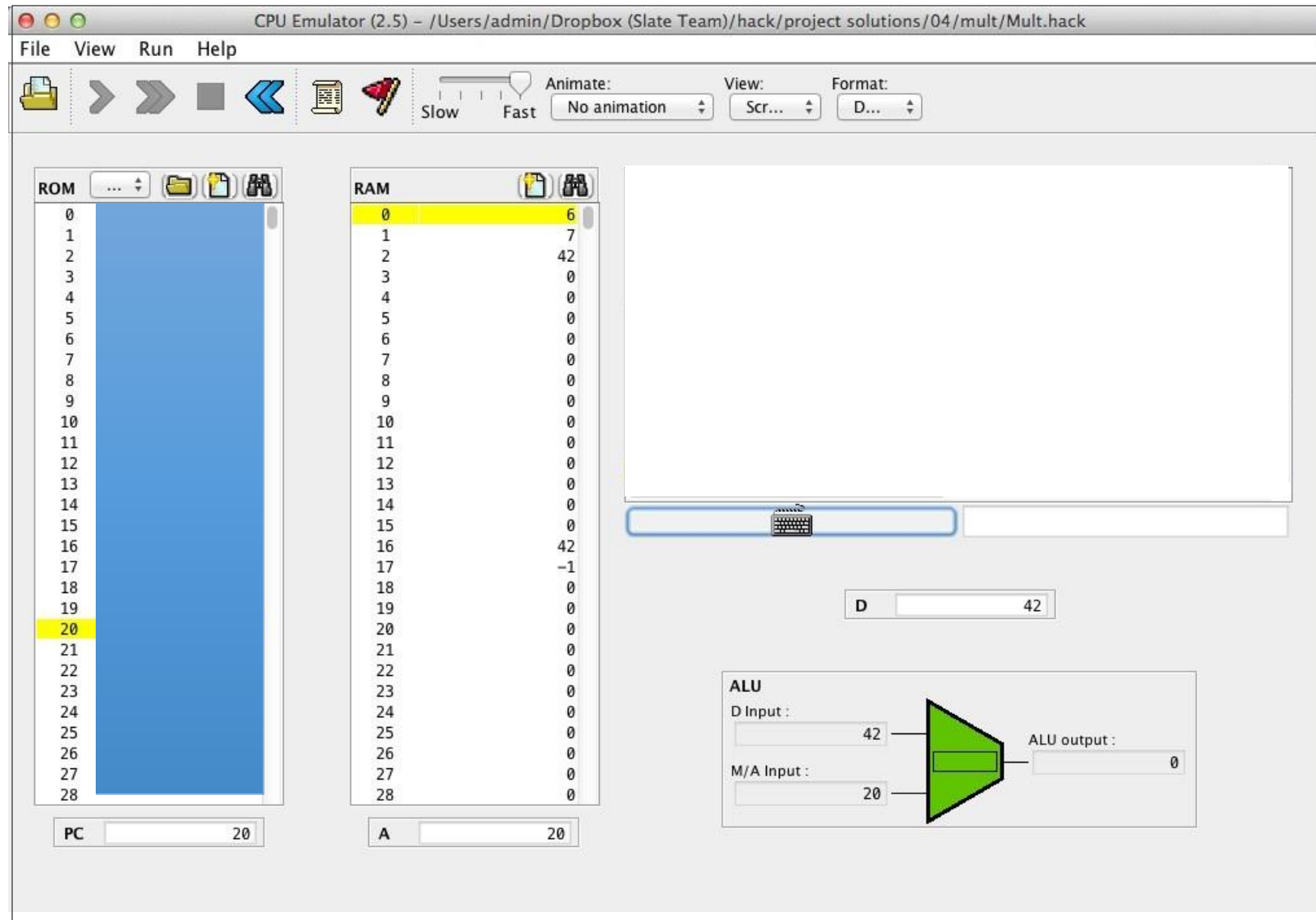
ALU

D Input : 42

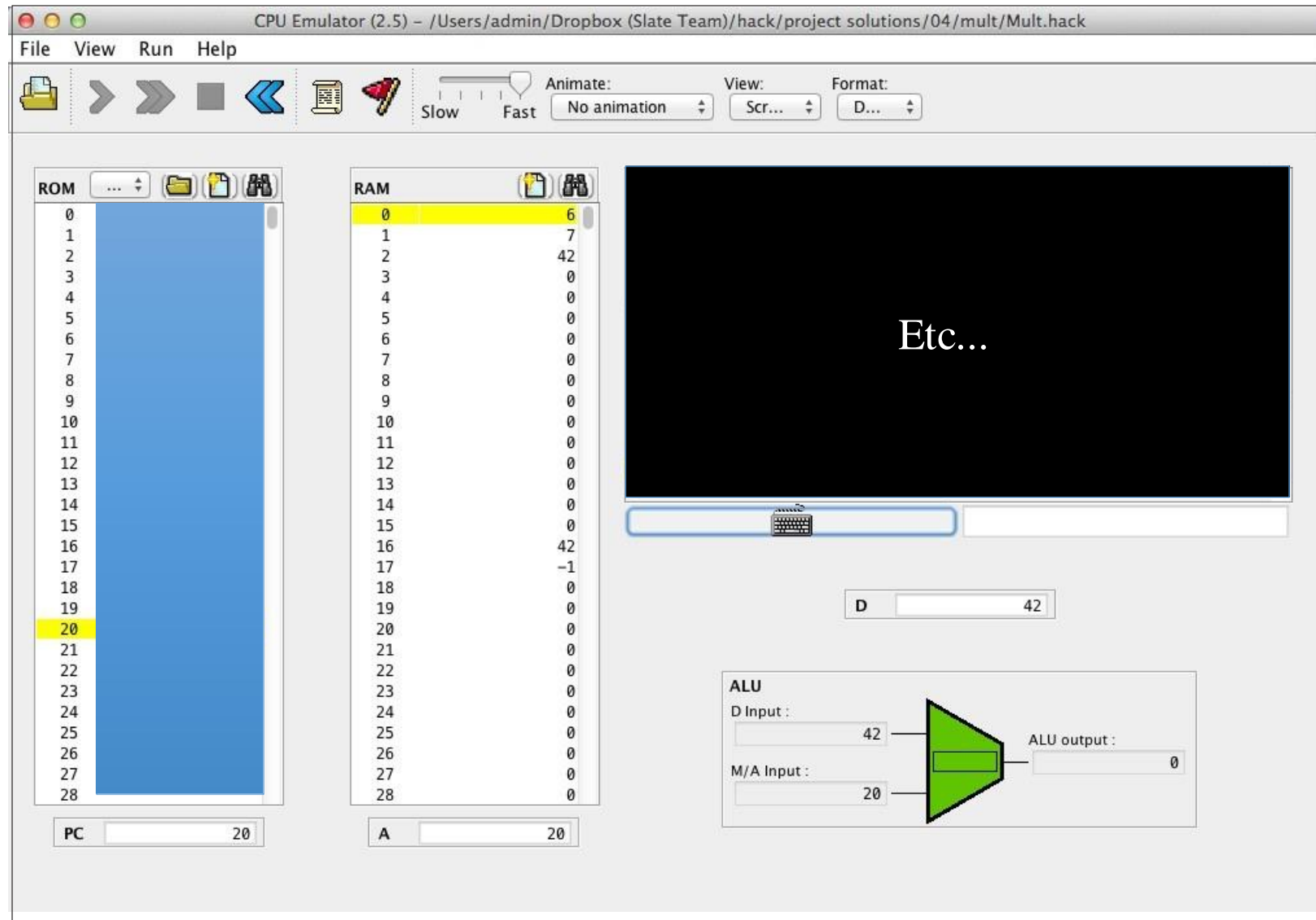
M/A Input : 20

ALU output : 0

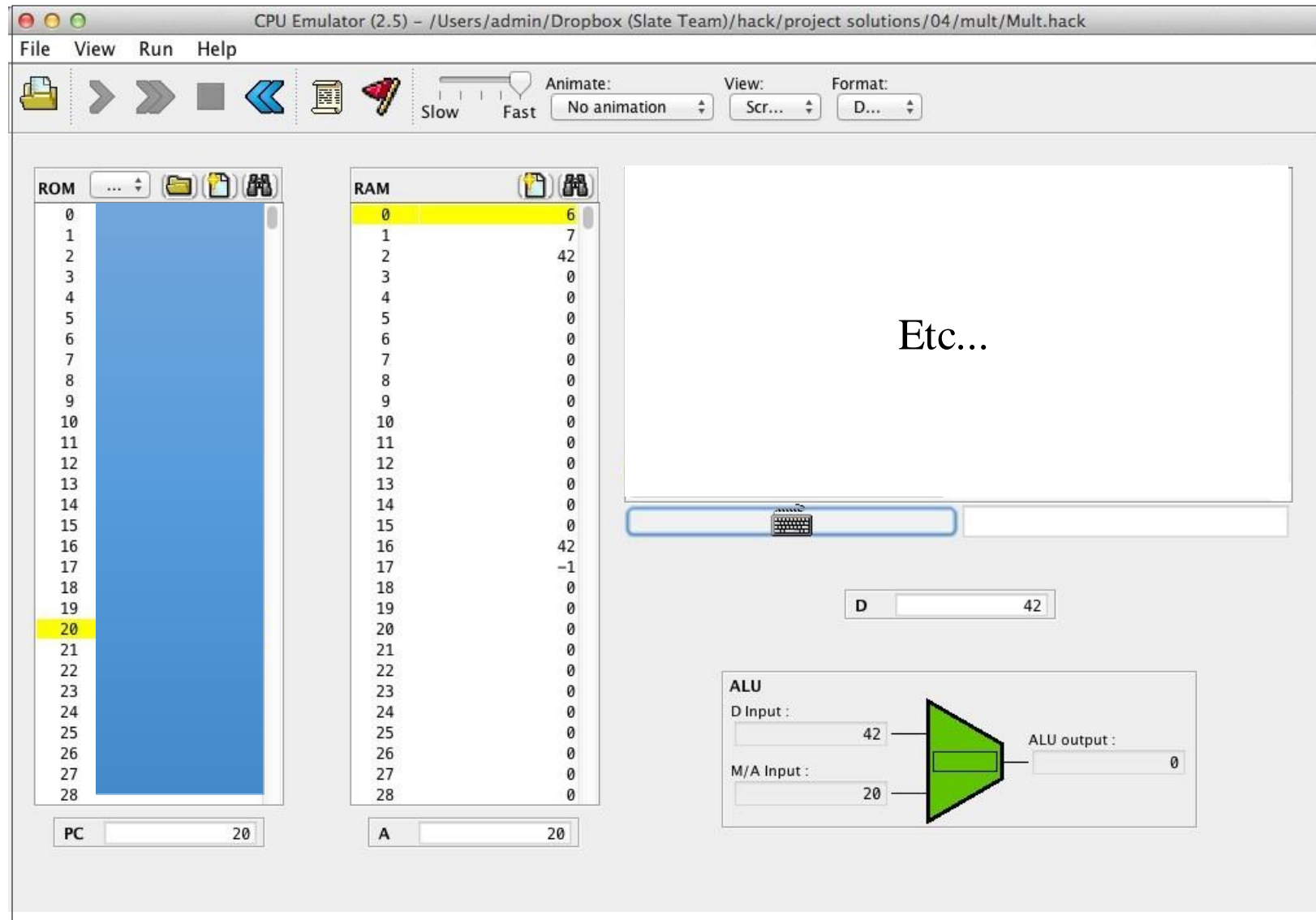
Fill: a simple interactive program



Fill: a simple interactive program



Fill: a simple interactive program



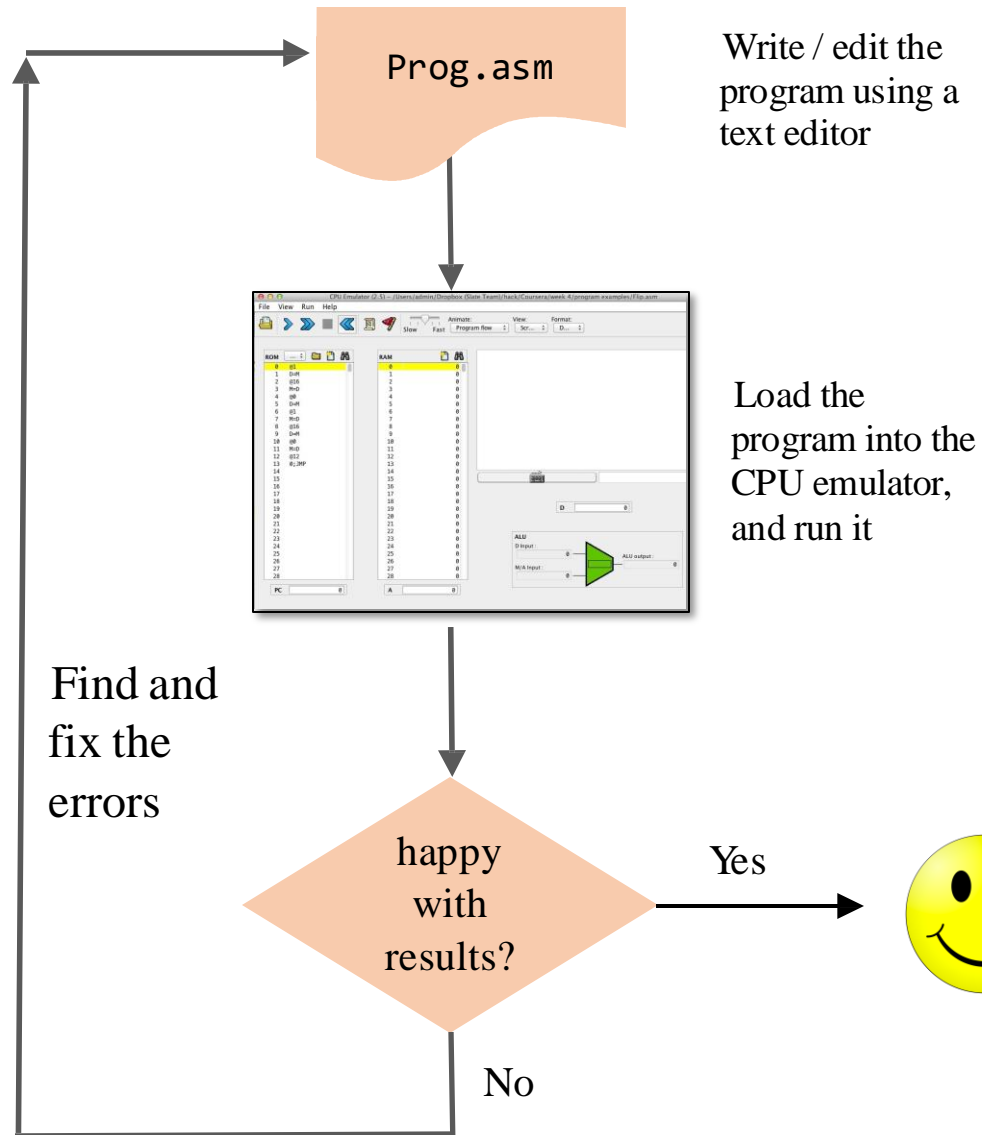
Fill: a simple interactive program

Implementation strategy

- Execute an infinite loop that listens to the keyboard input
- When a key is pressed (any key),
execute code that writes "black" in every pixel
- When no key is pressed, execute code that writes "white" in every pixel

Tip: This program requires working with pointers.

Program development process



Translation options

1. Let the CPU emulator translate into binary code (as seen on the left)

2. Use the supplied assembler:

- Find it on your PC in `nand2tetris/tools`
- See the *Assembler Tutorial* in Project 6 (www.nand2tetris.org)

Implementation notes

Well-written low-level code is

- Compact
- Efficient
- Elegant
- Self-describing

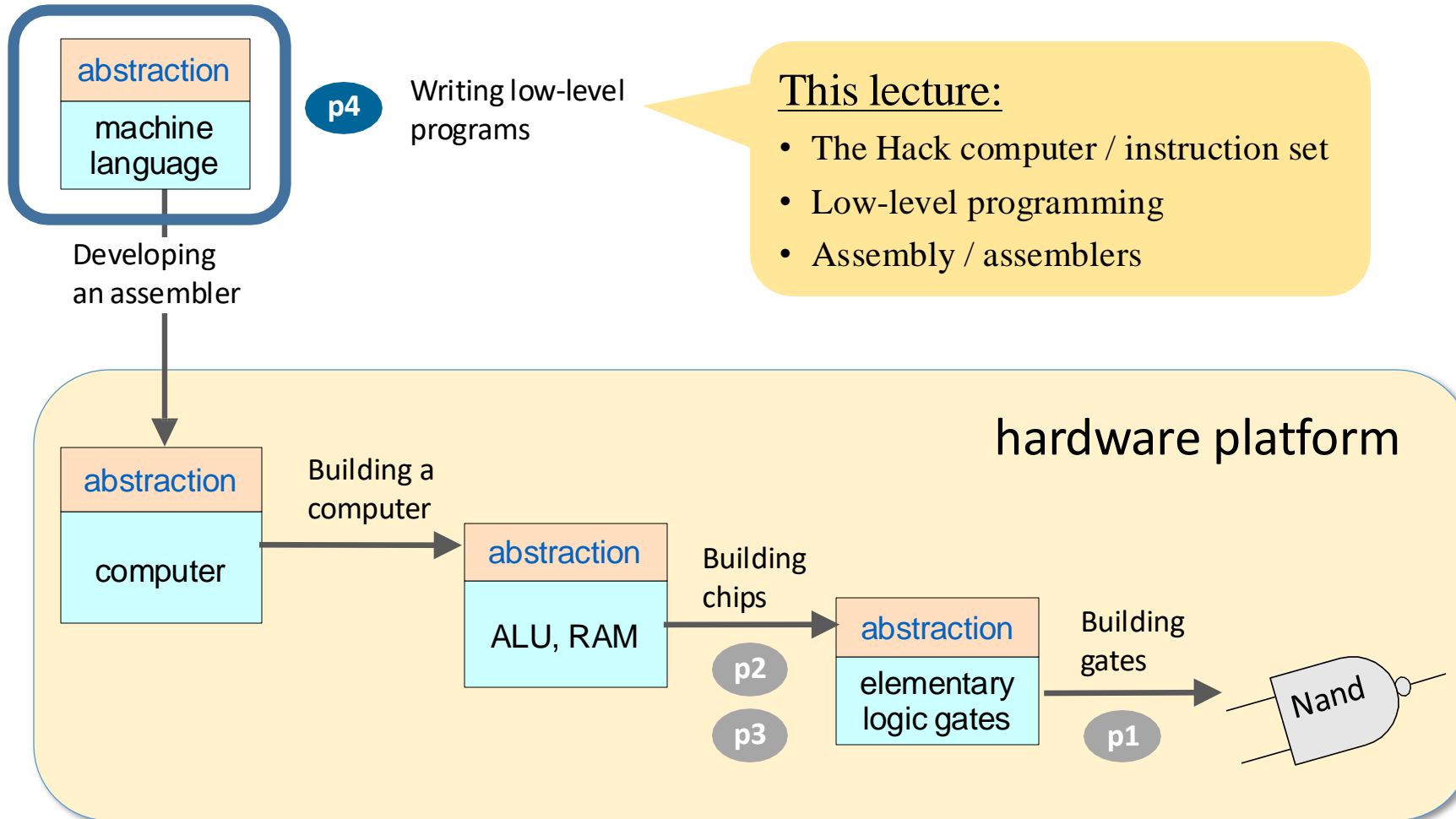
Tips

- Use symbolic variables and labels
- Use sensible variable and label names
- Variables: lower-case
- Labels: upper-case
- Use indentation
- Start by writing pseudocode.

Task 3: Define and write a program of your own

Any ideas?
It's your call!

Nand to Tetris Roadmap (Part I: Hardware)



Nand to Tetris Roadmap (Part I: Hardware)

