

# Overview

Dr. Eva Thomas is an underwater geographer studying mountains and valleys in the Atlantic Ocean. She models mountain and valley ranges using integers whose digits alternate between increasing and decreasing. You have been hired to write a program that, given two integers  $a$  and  $b$ , determines how many numbers model mountain and valley ranges in the range between  $a$  and  $b$ , inclusive.

## Examples:

- An  $n$ -digit integer, for  $n \geq 2$ , with digits  $d_1d_2d_3d_4\dots$  models a mountain range if it has the pattern  $\wedge\dots$ , that is,  $d_1 < d_2$ ,  $d_2 > d_3$ ,  $d_3 < d_4$  etc., and it models a valley range if it has the pattern  $\vee\dots$ , that is  $d_1 > d_2$ ,  $d_2 < d_3$ ,  $d_3 > d_4$ , etc.
  - 1503 has  $1 < 5$ ,  $5 > 0$ , and  $0 < 3$ , so it models a mountain range.
  - 7120 has  $7 > 1$ ,  $1 < 2$ , and  $2 > 0$ , so it models a valley range.
  - 7113 has consecutive 1s, so it models neither.
- For  $a = 15$  and  $b = 25$ , the answer is **8 mountain ranges** and **2 valley ranges**.
  - The numbers 15, 16, 17, 18, 19, 23, 24, and 25 are mountain ranges.
  - The numbers 20 and 21 are valley ranges.
  - The number 22 is neither a mountain nor a valley range.
- For  $a = 1234$  and  $b = 4321$ , the answer is **753 mountain ranges** and **351 valley ranges**.
- For  $a = 10$  and  $b = 1000$ , the answer is **276 mountain ranges** and **330 valley ranges**.

See the following how we got the solution for  $a = 15$ , and  $b = 25$ , and how to handle 2, 3 or 4 digits:

## 2 Digit Value

Mountain (M): if  $d_1 < d_2$

Valley (V): if  $d_1 > d_2$

Neither (N)

Count	Value	d1	d2	Result
1	15	1	5	M

2	16	1	6	M
3	17	1	7	M
4	18	1	8	M
5	19	1	9	M
6	20	2	0	V
7	21	2	1	V
8	22	2	2	N
9	23	2	3	M
10	24	2	4	M
11	25	2	5	M

### 3 Digit Value

Mountain (M): if  $d1 < d2$ ,  $d2 > d3$

Valley (V): if  $d1 > d2$ ,  $d2 < d3$

Neither (N)

Count	Value	d1	d2	d3	Result
1	123	1	2	3	N
2	124	1	2	4	N
3	125	1	2	5	N
4	126	1	2	6	N

5	127	1	2	7	N
6	128	1	2	8	N
7	129	1	2	9	N
8	130	1	3	0	M
9	131	1	3	1	M
10	132	1	3	2	M
11	133	1	3	3	N
12	134	1	3	4	N

## 4 Digit Value

Mountain (M): if  $d1 < d2$ ,  $d2 > d3$ ,  $d3 < d4$

Valley (V): if  $d1 > d2$ ,  $d2 < d3$ ,  $d3 > d4$

Neither (N)

Count	Value	d1	d2	d3	d4	Result
1	7623	7	6	2	3	N
2	7624	7	6	2	4	N
3	7625	7	6	2	5	N
4	7626	7	6	2	6	N
5	7627	7	6	2	7	N
6	7628	7	6	2	8	N
7	7629	7	6	2	9	N

8	7630	7	6	3	0	N
9	7631	7	6	3	1	N
10	7632	7	6	3	2	N
11	7633	7	6	3	3	N
12	7634	7	6	3	4	N

# Requirements

When developing your solution to this problem, ensure that your program conforms to the following requirements and assumptions:

1. Name the source file containing the main function `mountains_valleys.cpp`. Name the source file containing the function declarations `functions.h`. Name the source file containing the function definitions `functions.cpp`. These files already exist in the starter code.
2. Implementation is written such that it is readable by other programmers. Use descriptive variable identifiers and comments where appropriate (comments should explain things that are not obvious from the code).
3. You cannot use the `string` class in this assignment. Neither can you use data structures not yet covered in this course such as `vector` or functions from the `<algorithms>` library. You could use an array, but you shouldn't.
4. The input/output format should be exactly as follows. The expected input to the program is given by two integers `a` and `b` such that  $10 \leq a \leq b < 10000$ .

Required i/o format (user input in **bold red**; everything else is output):

Enter numbers  $10 \leq a \leq b < 10000$ : **15 25**↵

There are 8 mountain ranges and 2 valley ranges between 15 and 25.↵

Enter numbers  $10 \leq a \leq b < 10000$ : **1234 4321**↵

There are 753 mountain ranges and 351 valley ranges between 1234 and 4321.↵

Enter numbers  $10 \leq a \leq b < 10000$ : 10 1000↵

There are 276 mountain ranges and 330 valley ranges between 10 and 1000.↵

Enter numbers  $10 \leq a \leq b < 10000$ : -7 10↵

Invalid Input↵

Enter numbers  $10 \leq a \leq b < 10000$ : 12 100230↵

Invalid Input↵

Enter numbers  $10 \leq a \leq b < 10000$ : 110 115↵

There are 0 mountain ranges and 0 valley ranges between 110 and 115.↵

5. Your code should check if the input is valid: the numbers are positive integers, the second one is greater than or equal to the first, and so on. If the input does not meet the requirements, the output should be “Invalid Input”, followed by a re-prompt for input. The program should terminate after providing the result for valid input (see the test cases on Mimir).

6. Your program must define and use the following functions:

**bool is\_valid\_range(int a, int b):** This function returns the boolean value true if and only if inputs a and b satisfy the constraint that  $10 \leq a \leq b < 10000$ .

**is\_valid\_range(12, 34)** should return true.

**is\_valid\_range(34, 12)** should return false.

**char classify\_mv\_range\_type(int number):** This function returns the char value ‘M’ if number models a mountain range, ‘V’ if number models a valley range, and ‘N’ if number does not model either. The input is **not** constrained by the range in Requirement 4.

**classify\_mv\_range\_type(1503)** should return ‘M’.

**classify\_mv\_range\_type(7120)** should return ‘V’.

**classify\_mv\_range\_type(7113)** should return ‘N’.

**void count\_valid\_mv\_numbers(int a, int b):** This function prints out how many numbers in the range  $[a, b]$  (i.e.,  $a \leq \text{number} \leq b$ ) are mountain ranges and valley ranges using the definition in the Overview. This function is **not** constrained by the range specified in Requirement 4.

These functions must be defined (and, therefore, submitted) in a separate file `functions.cpp` along with the corresponding header file `functions.h` which contains the declarations of these functions. This header file must be included at the beginning of `mountains_valleys.cpp` and `functions.cpp`. For example, `mountains_valleys.cpp` should begin with:

```
#include <iostream>

#include "functions.h"
```

This is already done for you in the starter code.

A convenient way to compile multiple source files (in this case the two files: `functions.cpp` and `mountains_valleys.cpp`) is to put all the source and header files in a directory (for example, `hw_mountains_valleys`) and run `g++` on all source files in this directory:

1. Download the starter code from Mimir.
2. Make a directory named `hw_mountains_valleys`.
3. Put the starter code in `hw_mountains_valleys`.
4. In a terminal (assuming you are in the parent directory of `hw_mountains_valleys`):

```
$ cd hw_mountains_valleys
$ ls
mountains_valleys.cpp  functions.cpp  functions.h
$ g++ -std=c++17 -Wall -Wextra -pedantic -Werror *.cpp
```

The `*` symbol is a wildcard that matches any valid character in an identifier. So, `*.cpp` means all files in the current directory whose name ends in `.cpp` (i.e. all C++ source files).

7. Your program must compile without errors or warnings.

## Number Peeling

You might like to know of this interesting technique called "number peeling". Given a decimal (base-10) number like 8675309, we can read each digit, one-by-one as follows:

```
1. number <-- 8675309
2. while number is not 0 do
3.   digit <-- remainder after dividing number by 10
4.   number <-- number divided by 10
5. end
```

If you trace this algorithm, you will see that *digit* takes on the values 9, 0, 3, 5, 7, 6, 8, in that order (i.e. the digits in the number as read from right to left, what you might call reverse order). You can peel numbers in any base by simply changing the divisor and modulus, e.g. to peel in base 7, take remainder after division by 7 and divide by 7 at each step.