

Algorithm + Data Structure = program

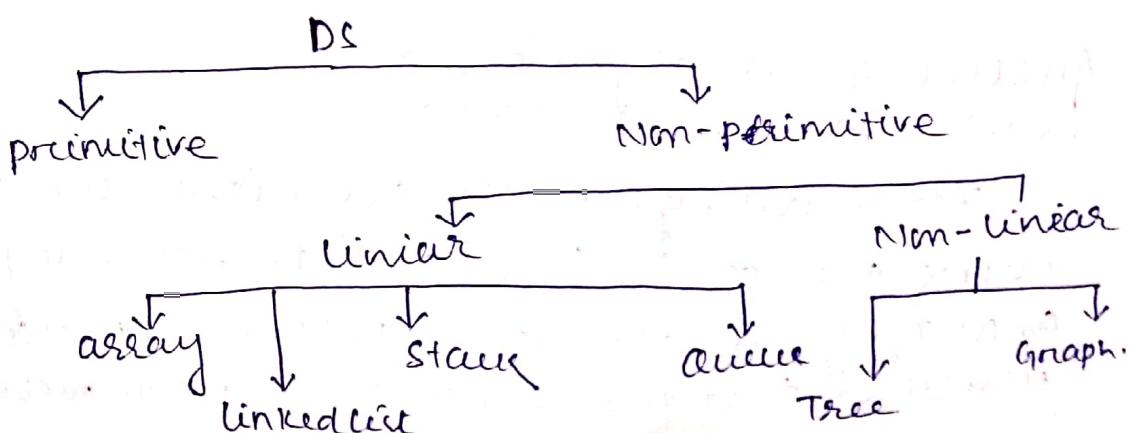
- The organised collection of data is called data structure. The data are organised in the logical manner so that processing of data will be easier.
- Data may be organised in different ways. The logical or mathematical model of a particular organisation is called data structure.

DS = organised data + operation

Different types of operations:-

- Retrieval/ Traversing.
- Insertion.
- Deletion.
- Modification.
- Sorting.
- Searching.
- Merging.

Classification of Data Structure:-



Algorithm:

→ It is a well defined set of steps for

solving a particular problem.

→ An algorithm is a sequence of computational steps that transforms inputs into outputs.

Criterial conditions:

1) Input:- 0 or more.

For any operation input either 1 or 2.

For print anything ("Hello world") input is zero.

2) Output:- one or more output ~~one~~ most should be three.

3) Definiteness:- Every step must be clear and be clear and unambiguous.

4) Finiteness:- The algorithm must terminate after a finite time.

5) Effectiveness:- Every step must be basic, so that algorithm is possible.

Analyzing an algorithm:-

After designing an algorithm we have to check the correctness and its efficiency.

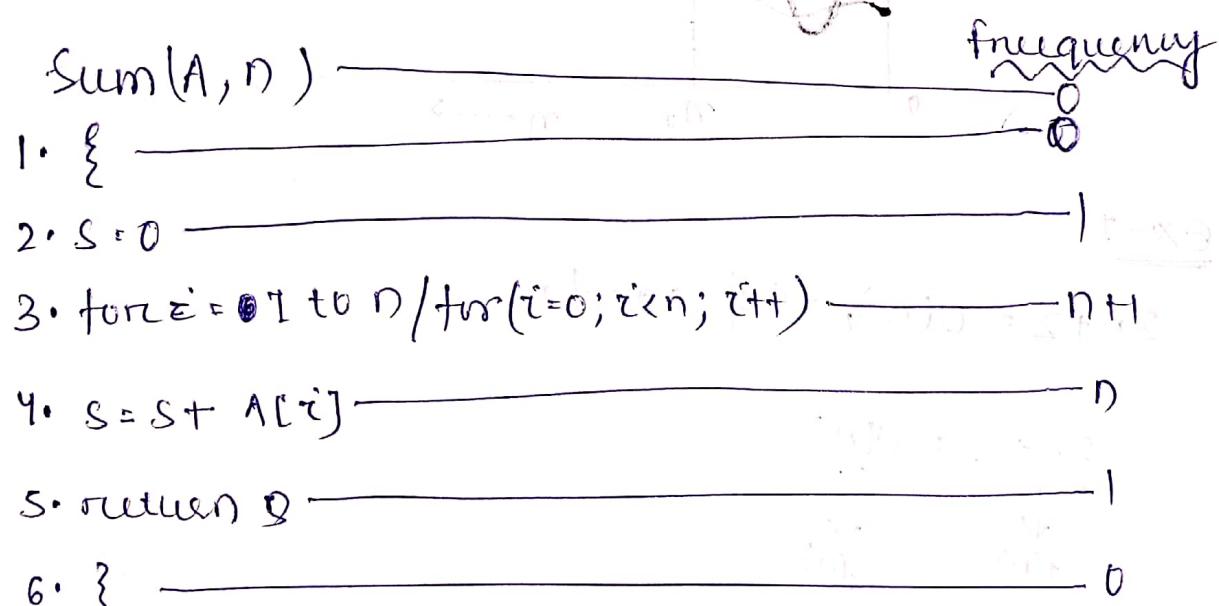
Analysing an algorithm means predicting the resources that the algorithm requires.

- while designing an algorithm for a program we must consider:
- 1) Time complexity.
 - 2) Space complexity.

Time complexity:- Amount of computer time it required.

Space complexity:- Amount of memory it requires.

* Time complexity or running time of an algorithm on a particular input number of primitive operations or steps enacted



$$T(n) = 2n + 1$$

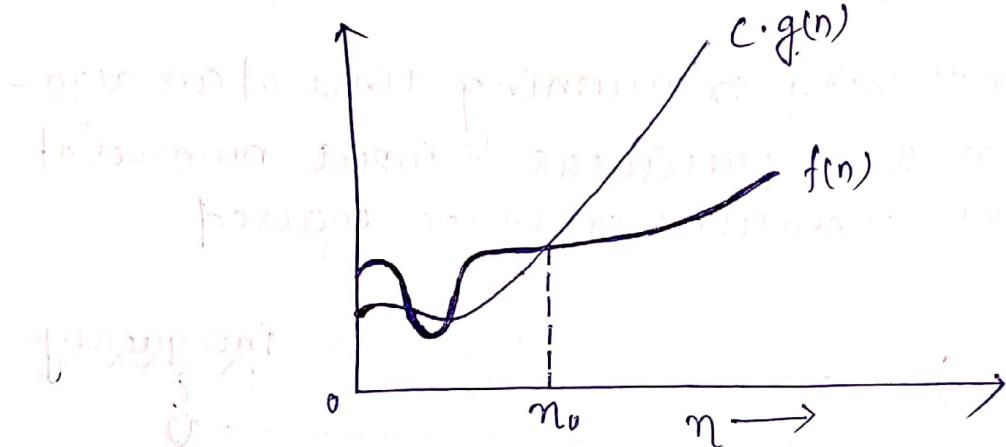
→ When the size of a problem increases it will increase the number of operations (T_n). In what order the total number of operation increased is known as rate of growth. So when we increase the input size (n), the running time of the algorithm $T(n)$ also increases.

To know the order $T(n)$ we use some notation known as "Asymptotic notation". ($O, \Omega, \Theta, o, \omega$)

* O -Notation ("Big-oh" notation):

$$f(n) = O(g(n))$$

$O(g(n)) = \{ f(n) \mid \text{There exists positive constant } c \text{ and } n_0 \text{ such that } 0 \leq f(n) \leq c \cdot g(n) \text{ for all } n \geq n_0 \}$



Ex-1

$$3n+2 = O(n), \text{ find } c \text{ and } n_0$$

$$\frac{3n+2}{\downarrow} = \underline{\underline{O(n)}} \quad \frac{\downarrow}{f(n)} \quad \frac{\downarrow}{g(n)}$$

$$3n+2 \leq c \cdot n$$

$$\text{ut, } \boxed{c=4}$$

$$3n+2 \leq 4n$$

$$\Rightarrow \text{at } \boxed{n=2}$$

$$\boxed{8 \leq 8}$$

$$\boxed{\text{so, } c=4 \text{ and } n_0=2}$$

(Ans).

* Asymptotic Notation:-

Dt:- 13/01/2020.

Ex:- prove that;

$$2n^2 + 3n + 4 = O(n^2)$$

Here, $f(n) = 2n^2 + 3n + 4$ and $g(n) = n^2$

$$\text{so, } 2n^2 + 3n + 4 \leq cn^2$$

$$\begin{cases} c = 9 \\ n_0 = 1 \end{cases}$$

$$\begin{cases} c = 3 \\ n_0 = 4 \end{cases}$$

Ex:- $3n + 2 = O(n)$

Here, $f(n) = 3n + 2$, $g(n) = n$

$$\begin{cases} c = 5 \\ n_0 = 1 \end{cases}$$

Ex:- $2n^2 + 3n + 2 = O(n)$

Here, $f(n) = 2n^2 + 3n + 2$, $g(n) = n$

$$\begin{cases} c = 7 \\ n_0 = 1 \end{cases}$$

$$2n^2 + 3n + 2 \not\leq c(n)$$

(It can't be a big-oh notation.)

for($i=0$; $i < m$; $i++$) $\underbrace{\hspace{10em}}$ $m+1$

{ for($j=0$; $j < n$; $j++$) $\underbrace{\hspace{10em}}$ $n+1$

{ printf("%d", $i * j$); $\underbrace{\hspace{10em}}$ $m * n$

}

$$\begin{aligned} T(n) &= \underline{(m+1) + (m+1)} + m * n \\ &= O(m * n) \approx O(m^2) \\ &\quad (\text{or}) O(n^2) \end{aligned}$$

Ex:-

1. $i = 1;$

frequency

1

2. while ($i \leq n$)

$n+1$

3. {

4. $x = x + 1;$

n

5. $i = i + 1;$

n

6. }

$$T(n) = 3n + 2$$

$$T(n) = O(n)$$

Ex:-

int f(int n)

{

 if ($n == 1$)

{

 return 1;

}

 }

 else

{

 return $n + f(n-1);$

}

$$T(n) = 1; \text{ if } n=1$$

$$= n + T(n-1) \text{ if } n > 0$$

$$T(n) = n + T(n-1)$$

$$T(n) = n + (n-1) + T(n-2)$$

$$T(n) = n + (n-1) + (n-2) + T(n-3)$$

$$\Rightarrow T(n+1) = n + (n-1) + (n-2) + \dots + 3 + 2 + 1 \quad (\because T(1) = 1)$$

$$\Rightarrow T(n) = \frac{n(n+1)}{2}$$

$$\Rightarrow T(n) = \frac{n^2 + n}{2}$$

$$\Rightarrow \boxed{T(n) = O(n^2)}$$

Assignment:-

1. $4n^3 + 6n + 5 = O(n^3)$ (prove that)

2. $2n^5 + 100n + 6 = O(n^5)$

3. $2^n + 3n^5 + 5 = O(2^n)$

4. Factorial of a number;

$$T(n) = 1 \text{ for } n=1$$

$$= n * T(n-1) \quad \text{for } n \geq 2$$

5. Fibonacci

$$T(n) = 0 \quad \text{if } n=1$$

$$= 1 \quad \text{if } n=1$$

$$= T(n-1) + T(n-2) \quad n \geq 2$$

Have to submit
on (25/01/2020)

Dt:- 25/01/2020

* Abstract Data type (ADT) :-

The ADT consist of a set of definition, that allow programmers to use the functions while hiding the implementation.

With an ADT users are not concerned with how the task is done rather they need to be concerned only what it can do?

An ADT is a datatype declaration packaged together with the operations that are meaningful on the datatype.

Array:-

2D - array :-

`int a[3][2];`

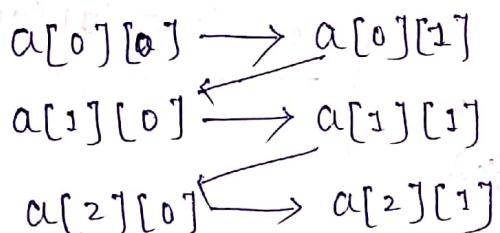
Representation

Row-major order.

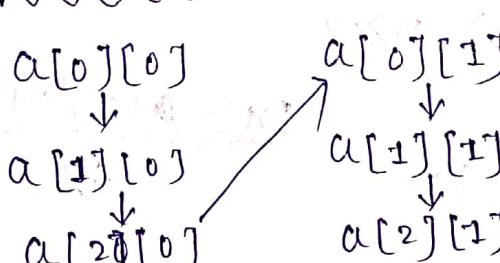
Column-major order.

$$\begin{bmatrix} a[0][0] & a[0][1] \\ a[1][0] & a[1][1] \\ a[2][0] & a[2][1] \end{bmatrix}$$

(a) Row-major order:-



(b) Column-major order:-



Address calculation:-

(a) Row-major order:-

Let, $a[u_1][u_2]$ be a 2-D array.

$$\text{addr}(a[u_1][u_2]) = b + (i * u_2 * j) * w$$

$b \leftarrow$ Base address.

$w \leftarrow$ width of the data.

(b) column major order :-

$$\text{add}(a[m][n][j]) = b + (j * u_1 + i) * w$$

Ex:- consider the array with $u_1 = 10$ and $u_2 = 15$ and b is the address of $a[0][0]$ and $w = 2$

$$\text{add}(a[9][8]) = ?$$

(a) Row-major :-

$$= b + 226$$

(b) column-major :-

$$= b + 174$$

Ex:- If the address of $A[1][1]$ and $A[2][1]$ is 1000 and 1016 respectively and each element occupies 2 bytes. Then the array have been stored in which order.

Q2:- Assume 4 bytes of storage required to store each element of an array $A[10][20]$ which is stored in row-major order. Let the element $A[0][3]$ is at the location 1012 in memory. Find out the address of the element $A[8][15]$

Ans:- $A[10][20]$

$$w = 4$$

$$\text{add}(A[0][3]) = 1012$$

$$\text{add}(A[8][15]) = ?$$

$$\Rightarrow b + (8 * 20 + 15) * 4$$

$$\Rightarrow b + (160 + 15) * 4$$

$$\Rightarrow b + 700$$

$$\Rightarrow 1000 + 700 = 1700$$

Q.1 (Ans):-

$$\text{Add}[A[1][1]] = 1000$$

$$\text{Add}[A[2][1]] = 1010$$

w:2

Sparse Matrix:-

A $m \times n$ matrix, is called sparse matrix, if it consists of more number of '0's as compare to non-zero elements. A matrix which is not sparse is called dense matrix.

$$A = \begin{bmatrix} 1 & 0 & 0 & 0 & -2 & 0 \\ 0 & 0 & 3 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 4 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

6x6 matrix for 2000, A = 100

$$6 \times 6 \times 4 = 144 \text{ bytes}$$

Alternate approach:-

No. of rows	No. of columns	No. of Non-zero
-	-	-
-	-	-
-	-	-
-	-	8 (10)

$$\Rightarrow \text{Alt} \rightarrow A \Rightarrow \begin{bmatrix} 6 & 6 & 5 \\ 0 & 0 & 1 \\ 0 & 4 & -2 \\ 1 & 2 & 3 \\ 2 & 2 & -1 \\ 4 & 2 & 4 \end{bmatrix}$$

$6 \times 3 \times 4 = 72 \text{ bytes.}$

* Two types of n-square space matrix:-

1) Triangular space matrix.

2) Tridiagonal space matrix.

1) Triangular space matrix:-

All entries above the main diagonal are zero.

Ex:-

$$\begin{bmatrix} 5 & 0 & 0 & 0 & 0 \\ 2 & 3 & 0 & 0 & 0 \\ 1 & 2 & 4 & 0 & 0 \\ 2 & 1 & 2 & 3 & 0 \\ 4 & 5 & 6 & 3 & 2 \end{bmatrix} (5 \times 5)$$

2) Tridiagonal space matrix:-

Non-zero entries can occur on the diagonal or on elements immediately above or below the diagonal.

$$\begin{bmatrix} 1 & 2 & 0 & 0 & 0 & 0 \\ 4 & 3 & 5 & 0 & 0 & 0 \\ 0 & 6 & 4 & 7 & 0 & 0 \\ 0 & 0 & 8 & 9 & 2 & 0 \\ 0 & 0 & 0 & 3 & 1 & 6 \\ 0 & 0 & 0 & 0 & 2 & 3 \end{bmatrix} (6 \times 6)$$

Position of a particular elements in an array:-

1) Triangular:

$$\begin{bmatrix} 5 & 0 & 0 \\ 2 & 3 & 0 \\ 1 & 2 & 4 \\ 2 & 1 & 2 & 3 \\ 4 & 5 & 6 & 3 & 2 \end{bmatrix} 5 \times 5$$

$$\Rightarrow \begin{array}{cccccccccc} 11 & 21 & 22 & 31 & 32 & 33 & 41 & 42 & 43 & 44 \\ | & | & | & | & | & | & | & | & | & | \\ 5 & 2 & 3 & 1 & 2 & 4 & 2 & 1 & 2 & 3 \\ | & | & | & | & | & | & | & | & | & | \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \end{array}$$

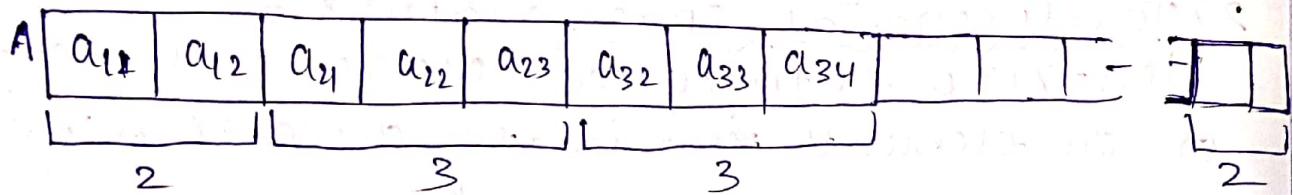
$$\text{pos}[a_{ij}] = 1 + 2 + 3 + \dots + (i-1) + (j-1) + 1 \\ = \frac{i(i-1)}{2} + j$$

Ex:-
 $\text{pos}[a_{43}] = \frac{4 \times 3 + 3}{2} = 19$

Tridiagonal:

$$\begin{bmatrix} 1 & 2 & & & & & \\ 3 & 4 & 5 & & & & \\ & 6 & 7 & 8 & 9 & 2 & \\ & & 1 & 2 & 3 & 1 & 6 \\ & & & 3 & 1 & 2 & 3 \end{bmatrix} \quad (6 \times 6)$$

↓ (1-D array)



$$P(a_{ij}) = 2+3+3+\dots+3+1$$

→ DD: 17/01/2020

*

$$A = \begin{bmatrix} 5 & 0 & 0 & 0 \\ 0 & 9 & 0 & 0 \\ 2 & 0 & 0 & 0 \end{bmatrix} \xrightarrow{\text{Triplets}} (B) = \begin{bmatrix} 3 & 4 & 3 \\ 0 & 0 & 5 \\ 1 & 1 & 9 \\ 2 & 0 & 2 \end{bmatrix}$$



$$A^T = \begin{bmatrix} 5 & 0 & 2 \\ 0 & 9 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \xrightarrow{\text{Triplets}} (C) = \begin{bmatrix} 4 & 3 & 3 \\ 0 & 0 & 5 \\ 0 & 2 & 2 \\ 1 & 1 & 9 \end{bmatrix}$$

1) convert sparse matrix to triplet form.

```
void triplet(int A[ ][10], int B[ ][3], int n, int c)
{
    int cnt = 0;
    B[0][0] = n; B[0][0] = c;
    for (i=0; i<n; i++)
    {
        for (j=0; j<c; j++)
        {
            if (A[i][j] != 0)
            {
                cnt++;
                B[cnt][0] = i;
                B[cnt][1] = j;
                B[cnt][2] = A[i][j];
            }
        }
    }
    B[0][2] = cnt++;
}
```

$$\left\{ \begin{array}{l} T(n) = O(n^2) \\ \text{Due to nested loop} \end{array} \right\}$$

2) Find out the transpose of a sparse matrix which is represented in triplet matrix form.

```
void Triplet_Transpose(int B[ ][3]; int C[ ][3])
{
    C[0][0] = B[0][0]; C[0][1] = B[0][0]; C[0][2] = B[0][0];
    m = 1;
    for (i=0; i<B[0][1]; i++)
    {
        for (j=1; j<=B[0][2]; j++)
        {
            if (i == B[j][0])

```

$c[m][0] = B[j][1];$

$c[m][1] = B[j][0];$

$c[m][2] = B[j][2];$

$m++$

}

}

}

}

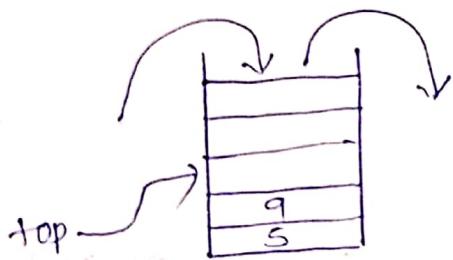
STACK :- { }

IDT :- 22/01/2020

↓

→ Stack is a linear data structure in which insertions and deletion of element will take place at one end called top of the stack.

→ Stack follows last-in-first-out (LIFO).



~~Insert an element on the stack from it's top.~~

Operation:- Push (s, i) & Pop (s)

1) $\text{push}(s, i)$: Insert an element (i) to the top of the stack.

2) $\text{pop}(s)$: Delete the top element of the stack.

Implementation of Stack:-

- Array (static allocation)
- linked-list (Dynamic allocation.)

1) Array Implementation of Stack:-

In the array implementation, we will use an array and an element "top" which holds the index of the "top" element of the array. The limitation of this technique, ~~is~~ is we have to declare the size of the array, before start the operation.

* push operation:-

```
#define maxsize 5
```

```
int s[maxsize];
```

```
int top=-1; /* stack is empty */
```

```
void push(int s[maxsize], int i)
```

```
{ if (top == maxsize-1)
```

```
{ printf("stack is full");
```

```
exit(1);
```

```
}
```

```
else
```

```
{
```

```
top = top + 1; / top++; / top+=1;
```

```
s[top] = i;
```

```
}
```

```
}
```

* pop operation:-

```
# define maxsize(5)
int s[maxsize]; int top=-1;
int pop( int s[maxsize])
{
    if (top == -1)
        printf("Stack is empty\n");
    else
        ele = *s[top];
    pop--;
    return ele;
}
```

STACK-operation:-

```
# include <stdio.h>
# include <stdlib.h>
# define maxsize 10
int s[maxsize];
int top=-1;
void push( int [maxsize], int );
int pop( int [maxsize] );
void display( int [maxsize] );
```

Dt:- 23/01/2020

```

int main()
{
    int choice, ele,
        while (1)
    {
        printf("1 for push\n");
        printf("2 for pop\n");
        printf("3 for display\n");
        printf("4 for quit\n");
        printf("Enter your choice\n");
        scanf("%d", &choice);
        switch(choice)
        {
            case 1:
                printf("Enter an element\n");
                scanf("%d", &ele);
                push(s, ele);
                break;
            case 2:
                x = pop(s);
                printf("%d is deleted\n", x);
                break;
            case 3:
                printf("The stack is :-\n");
                display(s);
                break;
            case 4:
                exit(0);
            default:
                printf("Wrong option\n");
                break;
        }
    }
}

```

Applications of stack:-

- Implementation of recursion.
- Evaluation of arithmetic expression.
 - (i) infix to postfix expression.
 - (ii) infix to prefix expression.
 - (iii) evaluation postfix expression.
 - (iv) evaluation of prefix expression.
 - (v) check for balanced parenthesis.

→ Reversing a string.

IDt:- 24/01/2020

* Arithmetic operation:-

Infix expression (real expression) = A + B.

Postfix expression = AB +

Prefix expression = + AB.

$$\text{Ex:- } ((A+B) * (C-D)) = (AB+) * (CD-)$$

$$= AB + CD - *$$

(i) infix to postfix expression:-

void infix_to_postfix(E,P)

{

push(s,c);

while (stack is not empty \n)

{ item = E, search();

if (item = = operand)

else if (item = = '(')

else if (item = = ')')

{

```

x = pop(s);
while (x != 'c')
{
    add top();
    x = pop(s);
}
else
{
    x = pop(s);
    while (precedence(x) > precedence(item))
    {
        add top();
        x = pop(s);
    }
    pnum(s, x);
    pnum(s, item);
}
while (x = pop(s) != 'c')
{
    add top();
}

```

Ex:- ~~After scanning with it, parenthesis will be removed.~~
E: A + (B * C - (D / E ^ F) * G) } * H

<u>Symbol Scanned</u>	<u>Stack(s)</u>	<u>Postfix(p)</u>
1 A.	C	A
2 +	(A
3 ((+	A
4 B	(+ C	AB
5 *	(+ C *	AB
6 C	(+ C *	ABC
7 -	(+ C -	ABC*
8 ((+ C - (ABC*
9 D	(+ C - (ABC*D
10 /	(+ C - (/	ABC*D
11 E	(+ C - (/	ABC*D E
12 ^	(+ C - (/ ^	ABC*D E
13 F	(+ C - (/ ^	ABC*D E F
14)	(+ C -	ABC*D E F A
15 *	(+ C - *	ABC*D E F A
16 G	(+ C - *	ABC*D E F A G
17)	(+	ABC*D E F A G *
18 *	(+ *	ABC*D E F A G *
19 H	(+ *	ABC*D E F A G * - H
20)	—	ABC*D E F A G * - H * +

Q Convert the following Infix expression into Postfix expression (using STACK). - $5 * (6+2) - 12 / 4$

(a) 5 * (6 + 2) - 12 / 4

5 6 2 12 4

*

(

+

6

2

3 4

5 * 6

7 8 9 10

6 * 7 8

9 * 10 11

3 6 * 4 5

7 8 9 10

11 12 13

14 15 16

17 18 19

20 21 22

23 24 25

26 27 28

29 30 31

32 33 34

35 36 37

38 39 40

41 42 43

44 45 46

47 48 49

50 51 52

53 54 55

56 57 58

59 60 61

62 63 64

65 66 67

68 69 70

71 72 73

74 75 76

(b) 5 * (6 + 2) - 12 / 4

5 6 2 12 4

*

(

+

6

2

3 4

5 * 6

7 8 9 10

6 * 7 8

9 * 10 11

3 6 * 4 5

7 8 9 10

11 12 13

14 15 16

17 18 19

20 21 22

23 24 25

26 27 28

29 30 31

32 33 34

35 36 37

38 39 40

41 42 43

44 45 46

47 48 49

50 51 52

53 54 55

56 57 58

59 60 61

62 63 64

65 66 67

68 69 70

71 72 73

74 75 76

(c) 5 * (6 + 2) - 12 / 4

5 6 2 12 4

*

(

+

6

2

3 4

5 * 6

7 8 9 10

6 * 7 8

9 * 10 11

3 6 * 4 5

7 8 9 10

11 12 13

14 15 16

17 18 19

20 21 22

23 24 25

26 27 28

29 30 31

32 33 34

35 36 37

38 39 40

41 42 43

44 45 46

47 48 49

50 51 52

53 54 55

56 57 58

59 60 61

62 63 64

65 66 67

68 69 70

71 72 73

74 75 76

Postfix - Evaluation

Symbol
Scanned

1. 5

2. 6

3. 2

4. +

5. *

6. 12

7. 4

8. /

9. -

A(A+B)

B

A(B+C)

C

A(B+C)

B

A(B+C)

C

A(B+C)

B

A(B+C)

C

A(B+C)

B

A(B+C)

C

A(B+C)

B

A(B+C)

C

Stack(S)

5

5, 6

5, 6, 2

5, 8

40

40, 12

40, 12, 4

40, 3

37

```

int pointer eval(char p[])
{
    int op1, op2;
    while (p[0] != '\0')
    {
        if (operand)
        {
            push(s, p[0]);
        }
        else
        {
            op1 = pop(s);
            op2 = pop(s);
            switch(p[0])
            {
                case '+':
                    r = op2 + op1;
                    break;
                case '-':
                    r = op2 - op1;
                    break;
                case '*':
                    r = op2 * op1;
                    break;
                case '/':
                    r = op2 / op1;
                    break;
                case '^':
                    r = op2 ^ op1;
                    break;
            }
            push(s, r);
            i++;
        }
    }
    return pop(s);
}

```

Assignment:- (Submission date:- 31/01/2020)

1) Convert infix to postfix using stack.

a) $A + [(B + C) + (D + E) * F] / G$

b) $(A + B) * C / D + E * F / G$ (here, $\$ = \wedge$)

c) $A - B / (C * D \$ E)$

d) $(A - B / C) * (D * E - F)$

e) $(C - D) + (E \$ F) + F / (H + W) * A \$ B$

2) Post-fix evaluation:-

4, 2, \$, 3, *, 3 -, 8, 4, 1, 7, 7, +, 1, +

* Queue:-

→ A queue is a linear Data-structure, in which elements are added at one end and known as "rear" and remove from other end "front".

→ It follows First in first out (FIFO)

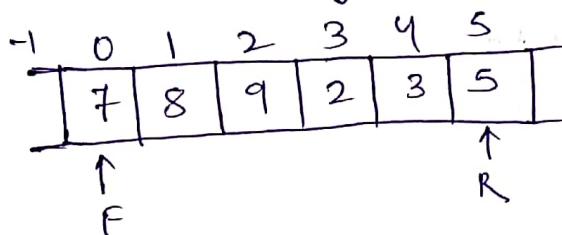
Operations:-

→ Insert(Q, n) { Insert n into Queue(Q) at rear end }

→ Delete(Q) { Delete an element from the front-end. }

array Implementation:-

- During initialisation of "Q" front = 0
rear = -1
- On each addition (insert an new element) of Q rear is incremented by 1.
- On each delete operation front is incremented by 1.



maxsize = 6

front = 0

rear = -1

Insert (int Q[maxsize], int n)

{

if (rear == maxsize - 1)

{

printf("Queue full");

exit(0);

}

else

{

rear = rear + 1;

Q[rear] = n;

}

else

{

Q[rear] = n; // If rear is 0, then front = rear

}

else

{

Q[rear] = n; // If rear is 0, then front = rear

}

```

int delete (int Q[maxsize])
{
    if (front > rear)
    {
        printf ("Queue is Empty\n");
        exit(0);
    }
    else
    {
        n = Q[front];
        front = front + 1;
    }
    return n;
}

```

display (int Q[maxsize])

```

for (i=front; i<=rear; i++)

```

```

{
    printf ("%d", Q[i]);
}

```

Q write a menu driven program, to ~~find~~ implement of Queue.

Q Assume that there is a queue having maxsize = 5, the following operations;

Insert(10), Insert(20), Insert 30, Delete(),

Insert(40), Insert(50), Delete(), find the final ~~value~~ result of Queue as well as value of front and rear.

Ans; Result:- 30, 40, 50

rear :- ~~40~~ 4.

front :- 2.

Again, insert(60)

Result: 30, 40, 50, 60

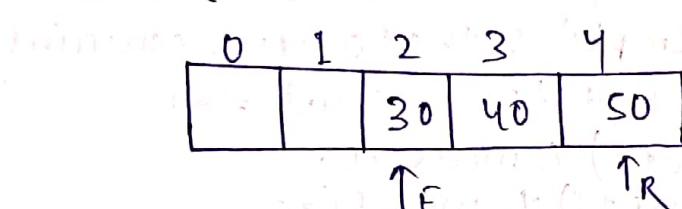
front = 2

rear = 5

Q consider a linear Queue with MAXSIZE = 5. After performing the following operations, what will be result of the queue.

Insert(10), Insert(20), Insert(30), Delete, Delete, Insert(40)

Insert(50), Insert(60)



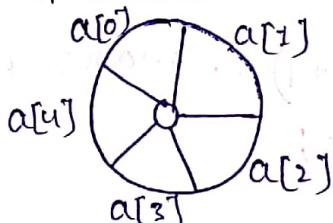
front = 2
rear = 4

* Circular Queue:

A circular is one in which insertion of a new element is done at the very first location of the queue if the last location of the queue is filled. ~~front == rear~~

That is, for the queue of n elements after inserting an element at the location of array, for a queue of n elements the next element will be inserted at very first location

It is possible if these locations are empty



Assumption:-

- 1) front will always point to the first element i.e., $front = -1 \Rightarrow$ queue is empty

$front = rear = -1$

2) Each time a new element is inserted into the queue.

$$\text{rear} = \text{rear} + 1$$

3) Each time an element is deleted from the queue.

$$\text{front} = \text{front} + 1$$

4) If ($\text{front} == \text{rear}$) \Rightarrow queue contains only one element except $\text{front} = \text{rear} = -1$.

5) If $\text{front} = \text{rear}$, it implies that queue contains only one element except $\text{front} = \text{rear} = -1$

$$\rightarrow \text{rear} = (\text{rear} + 1) \% \text{maxsize};$$

$$\rightarrow \text{front} = (\text{front} + 1) \% \text{maxsize}$$

For insertion:-

```
int front = -1, rear = -1;
```

```
void insert(int Q[], int ele);
```

```
{ if (front == (front + 1) \% maxsize)
```

```
for
```

```
printf("Queue is full");
```

```
exit(0);
```

```
} else if (front == -1) /* Empty Queue */
```

```
front = rear = 0; /* Initialize front and rear to 0 */
```

```
else /* Inserting element */
```

```
{ rear = (rear + 1) \% maxsize;
```

```
Q[rear] = ele;
```

```
}
```

```
else /* Inserting element at position greater than maxsize */
```

```
printf("Overflow");
```

```
for display:-  
void display()  
{  
    if(front <= rear) {  
        for(i = front; i <= rear; i++) {  
            printf("%d", Q[i]);  
        }  
    }  
    else {  
        for(i = front; i <= maxsize - 1; i++) {  
            printf("%d", Q[i]);  
        }  
        for(j = 0; j <= rear; j++) {  
            printf("%d", Q[j]);  
        }  
    }  
}
```

Application of Lienier Queue:

a) simulation of traffic control system.

b) CPU scheduling in multiprogramming.

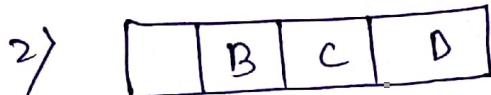
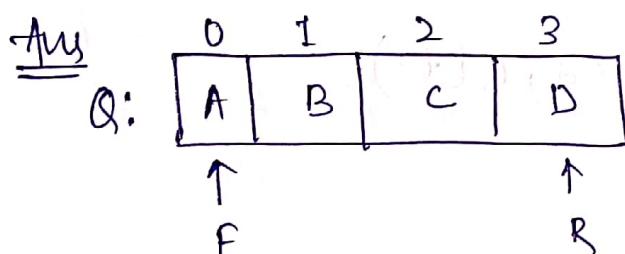
c) Round-Robin scheduling.

Q. Consider a circular queue implemented on an array of size 4. The front is pointing to element A and the rear is pointing to element D. Perform the following operations and show the content of circular queue after each operation.

1) Insert(F), 2) Delete(e), 3) Delete()

4) Insert(K), 5) Insert(L), 6) Insert(M)

Ans



* Dqueue (Double-ended Queue) :-

A Dqueue is a linear list in which elements can be added or removed at either end, but not in the middle.

Types:-

(a) Input restricted queue.

(b) Output restricted queue.

(a) Input restricted queue:-

An input restricted queue is a Dqueue which allows insertion at only one end of the list but allows deletion at both ends of the list.

(b) Output restricted queue:-

An output restricted Dqueue is a Dqueue which allows deletion operation at any one end of the list, but allows insertion at both the ends.

* Operations of the D-Queue:-

- 1) Insertion of an element at the rear end.
- 2) Deletion of an element at the front end.
- 3) Insertion of an element at the front end.
- 4) Deletion of an element at the rear end.

* Priority Queue:-

It is a collection of elements such that each element has been assigned a priority and the order in which elements are deleted and possessed comes from the following rules.

- 1) The element of an higher priority is possessed before lower priority elements.
- 2) Two elements with same priority are processed according to the order in which they were added to the queue.

Applications:-

- Jobs waiting to use printer on an LAN.
- For checking the balanced parentheses, an expression is valid if it satisfies two conditions:-
 - (a) Number of left parentheses should equal to the total number of right parentheses in the equation.
 - (b) For every right parenthesis, there should be a left parenthesis of the same type.

* Algorithm:-

- 1) Scan the symbols of expression from left to right.
- 2) If the symbol is a left parenthesis then push into the stack.

3) If the symbol is right parenthesis, then,
if the stack is empty then,
valid = False.

else pop the element from the stack. with

If the popped parenthesis does not match, the
parenthesis being seen then,

valid = False.

4) After scanning all symbols if the stack is not
empty then,

valid = False.

* Reverse of a string:-

main()

{

char str[10];

printf("Enter any string data\n");

gets(str);

for(i=0; i< strlen(str); i++)

{

push(str[i]);

}

for(i=0; i< strlen(str); i++)

{

str[i] = pop();

}

printf("Reverse string is : \n");

puts(str);

}

* Tower of Hanoi
* conversion

→ Tower of Hanoi.

→ conversion of decimal to binary. } (function)

- Q) consider a stack with maxsize = 4.
perform the following operations:
push(1), push(2), push(3), push(4), push(5),
what is the output?

What is the output for the following program?

int main() {
 int a[5];
 a[0] = 1;
 a[1] = 2;
 a[2] = 3;
 a[3] = 4;
 a[4] = 5;
 cout << a[0] << endl;
 cout << a[1] << endl;
 cout << a[2] << endl;
 cout << a[3] << endl;
 cout << a[4] << endl;
}

What is the output for the following program?

int main() {
 int a[5];
 a[0] = 1;
 a[1] = 2;
 a[2] = 3;
 a[3] = 4;
 a[4] = 5;
 cout << a[0] << endl;
 cout << a[1] << endl;
 cout << a[2] << endl;
 cout << a[3] << endl;
 cout << a[4] << endl;
}

What is the output for the following program?

int main() {
 int a[5];
 a[0] = 1;
 a[1] = 2;
 a[2] = 3;
 a[3] = 4;
 a[4] = 5;
 cout << a[0] << endl;
 cout << a[1] << endl;
 cout << a[2] << endl;
 cout << a[3] << endl;
 cout << a[4] << endl;
}

What is the output for the following program?

int main() {
 int a[5];
 a[0] = 1;
 a[1] = 2;
 a[2] = 3;
 a[3] = 4;
 a[4] = 5;
 cout << a[0] << endl;
 cout << a[1] << endl;
 cout << a[2] << endl;
 cout << a[3] << endl;
 cout << a[4] << endl;
}

Linked - List

array

- It contains fixed memory location.
- Easy to implement.
- It has random access.
- Chances of wastage of memory.
- It has continuous memory location.

Linked - list

- It is of variable length.
- Little bit complex to implement.
- It has sequential access.
- According to requirement memory is allocated so, no chance of ~~waste~~ waste of memory.
- memory is allocated randomly, sometimes it may contain contiguous location.

Dynamic memory allocation

- Dynamic memory management techniques allow to allocate additional memory space or to release unwanted storage at run-time. They optimize the user storage space.
- The memory management functions that can be used for allocation and freeing memory in program execution are:-

 - (i) malloc():- Allocates required size of bytes.
 - (ii) calloc():- Allocates array of specified number of elements of a given size.
 - (iii) realloc:- Modifies the previously allocated space.

(iv) Free():- Relieve a previously allocated space.

* Allocating a block of memory:-

→ The malloc() function can be used to allocate a block of memory. It reserves a specified size of memory and returns a pointer of type void.

• Syntax:-

```
ptr = (type cast *) malloc (byte (size));
```

Ex:- `ptr = (int *) malloc (100 * sizeof(int));`

* Linked List:

It is an ordered collection of data in which each element contains the location of the next element.

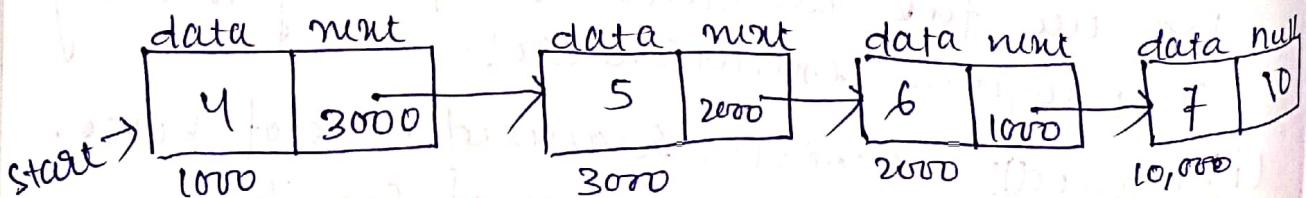
(or),

It is a collection of nodes in which each node has 2 parts:-

i) Data Part, ii) Next-Part.

Eg:- A

4	5	6	7
---	---	---	---



→ Self Referential Structure:-

The nodes in the linked-list are called "self referential structures".

In this, each instance of the structure contains a pointer ~~refers to~~ to another instance of the same structural type.

1) Single Linked-List:

Operation:-

a) Create Linked-List.

b) Insertion Operation.

→ Insertion of a node at the beginning of linked-list.

→ Insertion of a node at the end of linked-list.

→ Insertion of a node at a specification location.

c) Deletion Operation:-

→ Delete the first node.

→ Delete the last node.

→ Delete a node at specific location.

→ Traversing operation.

→ Searching operation.

→ Sorting operation.

→ Merging operation.

→ A "single linked-list" is a dynamic data structure and is a linear collection of data elements called "nodes" where each node is divided into two parts:-

1) Data Part

2) Next Part

A linked-list is created using structures, pointers and dynamic memory allocation functions e.g., malloc().

* Node-declaration

struct node

{

```
    int data;  
    struct node *next;
```

}

struct node *start;

[or]

```
typedef struct node NODE;  
NODE *start;
```

```
start = (struct node *) malloc(sizeof(struct node));  
NODE
```

```
scanf("%d", &start->data);
```

```
start->next = NULL;
```

Q create a single linked-list and display all nodes.

```
#include<malloc.h>
```

struct link

{

```
    int info;  
    struct link *next;
```

}

```
void create L(struct link *);
```

```
void display (struct link *);
```

struct link

{ int data;

```
    struct link next;
```

}

```

int main()
{
    struct link *node, *start;
    node = (struct link*) malloc(sizeof(struct link));
    if (start == node);
    if (node == NULL)
    {
        printf("out of memory\n");
        exit(0);
    }
    printf("Enter the data\n");
    scanf("%d", &node->data);
    node->next = NULL;
    create_L(node);
    display(node);
}

```

```
void create_L(struct link *node)
```

```

{
    char ch;
    printf("Enter the data\n");
    scanf("%d", &node->data);
    node->next = NULL;
    printf("Enter 'n' to exit else any key to
           continue\n");
    ch = getchar();
    while(ch != 'n')
    {
        node->next = (struct link*).malloc
                      (sizeof(struct link));
        if (node->next == NULL)
        {
            printf("out of memory\n");
            exit(0);
        }
    }
}
```

```

node = node->next;
printf("Enter the data\n");
scanf("%d", &node->data);
node->next = NULL;
printf("Enter 'n' to exit else any key to
continue\n");
ch = getch();
}
}

void display(struct link *node)
{
while (node != NULL)
{
printf("%d\t", node->data);
node = node->next;
}
}

```

* Insertion of a node in a single linked list:-

→ The insertion operation is used to add an element in an existing linked list.

→ points to be remembered before make a insertion operation:-

- (a) create a new node.
- (b) If the list is empty, insert the node as the first node.
- (c) If the node to be inserted at the beginning, insert the node and adjust the next pointer till.
- (d) Insert the node at the desired place in the list.

* various position where node can be inserted!:-

1) Insert at beginning.

2) Insertion at the end.

3) Insertion at specific location.

4) Insert a node after a given node.

1) Insertion of a node at the beginning!:-

* Algorithm:-

→ start holds the address of the first node.

→ curr holds the address of current node.

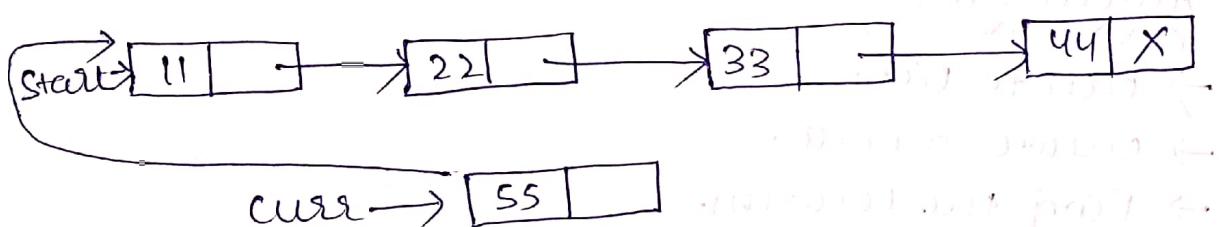
→ create a node named curr.

→ If (curr == NULL), print("out of memory\n") and exit.

→ set curr → data = x.

→ set curr → next = start.

→ set start = curr.



Pseudo code!:-

```
void Insert_B (struct Link *node)
{
    struct Link *curr;
    curr = (struct Link *) malloc(sizeof(struct Link));
    if (curr == NULL)
    {
        printf("out of memory\n");
        exit(0);
    }
    scanf("%d", &curr->data);
    curr->next = node;
    start = curr;
}
```

2) Insert of a node at the end:-

* Pseudo code:-

* Algorithm:-

- Create a node named curr.
- If (curr == NULL), print ("out of memory\n"); and exit.
- Set curr → data = x.
- Set curr → next = NULL.
- While (node → next != NULL)

 - node = node → next.

- node → next = curr;
- Exit.

3) Insert of a node at Specific location:-

* Algorithm:-

- Create list.
- Create a node.
- Find the location.
- Assign the data.
- Find the previous node.
- Update the pointer.

* Pseudo code:-

```
void insert(struct link *node)
```

```
{
```

```
    int loc, r=1;
```

```
    struct link *curr *prev;
```

```
    curr = (struct link *) malloc(sizeof(struct link));
```

```

if (curr == NULL)
{
    printf("out of memory\n");
    exit(0);
}

printf("Enter the position\n");
scanf("%d", &loc);

printf("Input the value\n");
scanf("%d", &curr->data);

while (i < loc)
{
    if (curr->next == NULL)
        break;
    prev = node;
    node = node->next;
    i++;
}

prev->next = curr;
curr->next = node;
}

```

4) Insert a node after a given node:-

```

void insert (struct link *node)
{
    int n;
    printf("Enter the element after which element  
to be inserted\n");
    scanf("%d", &n);

    while (node != NULL)
    {
        if (node->data == n)
        {
            break;
        }
    }
}

```

```

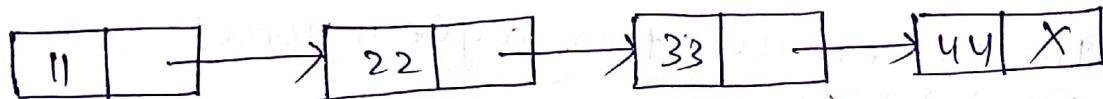
else
{
    node = node->next;
}

if (node == NULL)
{
    cout << "Element not found" << endl;
    exit(0);
}

curr = (struct Link *)malloc(sizeof(struct Link));
printf("Enter the value\n");
scanf("%d", &curr->data);
curr->next = node->next;
node->next = curr;
}
}

```

* Deletion of a Node:-



- 1) Delete first node.
- 2) Delete last node.
- 3) Delete specific location node.
- 4) Delete a node after a given data.

1) Deletion of first node:-

```

void delete_B(struct Link *node)
{
    node = node->next;
}

```

```
if (node->next == NULL)
{
    struct = NULL;
    start = node->next;
    free(node);
}
```

2) Deletion of ~~node~~ last node:-

```
void deleteL (struct Link *node)
```

```
{
    struct Link *prev;
    if (node->next == NULL)
    {
        start = NULL;
        free(node);
        return;
    }
    while (node->next != NULL)
    {
        prev = node;
        node = node->next;
    }
    prev->next = NULL;
    free(node);
}
```

3) Deletion of a node at Specific position:-

```
void deleteS (struct Link *node)
{
    int i, loc;
    i = 1;
    struct Link *prev;
```

```

printf("Enter the location of the element  

      to be deleted \n");
scanf("%d", &loc);
while(r<loc)
{
    prev = node;
    node = node->next;
    r++;
}
prev->next = node->next;
free(node);
}

```

4) Deletion of a node after a given data:-

What is meant by
deletion of node
after a given data?

(Data deletion from linked list)

What is meant by
deletion of node
after a given data?

What is meant by
deletion of node
after a given data?

What is meant by deletion of node after a given data?
Delete the node which contains the data which is greater than
the data which is given to us for deletion.

(Data deletion)

{i=1}

ANUJ KUMAR

(minimum and maximum) position of array

start node

last node or end node

length of array

Date:- 19/02/2020

* Operations of Single Linked List Operation:-

1) Inserting.

2) Sorting.

3) Reverse.

4) merging.

2) Sorting:-



(a) Algorithm:-

Let start is pointing to the first node.

1) Let node = start.

2) Repeat steps 3 to 10 while node->next!=NULL

3) set pptr= node->next.

4) Repeat step 5 to 9 until pptr!=NULL.

5) if (node->data > pptr->data)

6) set temp = node->data.

7) set node->data = pptr->data.

8) pptr->data = temp.

a) $\text{ptrc} = \text{ptrc} \rightarrow \text{next}$.

b) $\text{node} = \text{node} \rightarrow \text{next}$.

Code:-

```
void sorting (struct link *node)
```

```
{
```

```
    int temp;
```

```
    struct link *ptrc;
```

```
    node = start;
```

```
    ptrc = node → next;
```

```
    while (node → next != NULL)
```

```
{
```

```
        while (ptrc != NULL)
```

```
{
```

```
            if (node → data > ptrc → data)
```

```
{
```

```
                temp = node → data;
```

```
                node → data = ptrc → data;
```

```
                ptrc → data = temp;
```

```
}
```

```
            ptrc = ptrc → next;
```

```
}
```

```
        node = node → next;
```

```
}
```

```
{
```

```
    }
```

```
    }
```

```
    }
```

```
    }
```

q) Merging :-

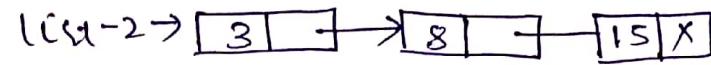
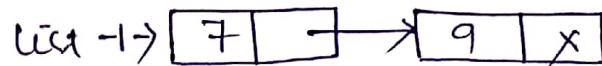
Algorithm :-

1. list3 = list1

2. while (list → next != NULL)

3. list = list → next;

4. list → next = list2.



Algorithm :-
Step 1 : Initialize list1 and list2
Step 2 : If list1 > list2 then
 list = list1
 list → next = list2
Step 3 : If list1 < list2 then
 list = list2
 list → next = list1
Step 4 : If list1 == list2 then
 list = list1
 list → next = list2
Step 5 : If list1 < list2 then
 list = list1
 list → next = list2
Step 6 : If list1 > list2 then
 list = list2
 list → next = list1
Step 7 : If list1 == list2 then
 list = list1
 list → next = list2

3) Reverse:-

* Algorithm:-

Start will be pointing to the 1st node.

1) Set curr = start.

2) If curr → next == NULL then return.

3) prev = curr → next;

4) curr → next = NULL.

5) Repeat step 6 to 9 while (prev → next != NULL)

6) ptrc = prev → next.

7) prev → next = curr.

8) curr = prev.

9) prev = ptrc.

10) prev → next = curr.

11) start = ptrc.

* Double Linked-list:-

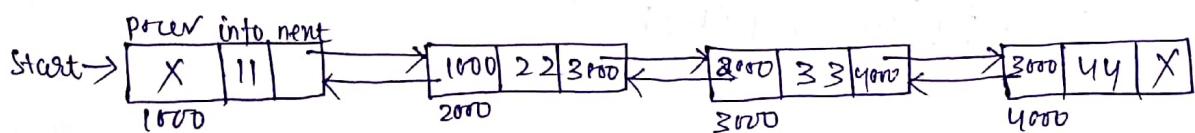
In single-linked-list one can move starting from the first node to any node in one direction only in left to right, that is why it is termed as one-way list. On other hand a double linked-list is a two way list one can move in either direction, either from left to right or from right to left.

A two way list is a linear collection of data elements called nodes, where each node is divided into three parts.

1) Info (Information / data) field.

2) Next pointer (contains the ~~address~~ ^{address} of next pointer)

3) Previous pointer (contains the address of prev-pointer)



struct d-link
{

IMPLEMENTATION OF DOUBLE LINKED-LIST

11

struct dlink *prev;
int data;
struct dlink *next;

}

void createdouble(struct dlink *)

void display(struct dlink *)

int main()

{

struct dlink *node;

node = (struct dlink *)malloc(sizeof(struct dlink));

if (node == NULL)

{

printf("Out of memory\n");

exit(0);

}

create_double(node);

display(node);

}

void create_double(struct dlink *node)

{

printf("Enter the data for the node\n");

scanf("%d", &node->data);

struct dlink *curr;

node->prev = NULL;

node->next = NULL;

printf("Enter N to exit\n");

scanf("%c", &ch);

```

while(ch != 'n')
{
    curr = (struct dlink*)malloc(sizeof(struct dlink));
    if(curr == NULL)
    {
        printf("Out of memory\n");
        exit(0);
    }
    node->next = curr;
    curr->prev = node;
    node = node->next;
    printf("Enter the data for node\n");
    scanf("%d", node->data);
    node->next = NULL;
    printf("Enter 'n' to exit\n");
    scanf("%d", &ch);
}
}

void display(struct dlink *node)
{
    printf("The list is in the forward direction\n");
    struct dlink *p;
    while(node != NULL)
    {
        p = node;
        printf("%d\t", node->data);
        node = node->next;
    }
    printf("The list is in the backward direction\n");
    while(p != NULL)
    {
        printf("%d\t", p->data);
        p = p->prev;
    }
}

```