

The Trial of Number Theory

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Number theory template:
Deals with various aspects of integer, division, modulo, etc.
#include <cstdlib>
#include <cmath>
#include <complex>
#include <vector>
namespace number {
      const double PI = acos (-1);
       /* Basic operation :
                     long long inverse (const long long &x, const long long &mod) :
                    long long abs (const long long &x) { return x > 0 ? x : -x; }
       long long inverse (const long long &x, const long long &mod) {
   if (x == 1) return 1;
   return (mod - mod / x) * inverse (mod % x, mod) % mod;
      int fpm (int x, int n, int mod) {
    register int ans = 1, mul = x;
    while (n) {
        if (n & 1) ans = int (111 * ans * mul % mod);
        mul = int (111 * mul * mul % mod);
        n >>= 1;
}
      long long gcd (const long long &a, const long long &b) {
   if (b == 0) return a;
   return gcd (b, a % b);
      long long mul_mod (const long long &a, const long long &b, const long long &mod) {
  long long ans = 0, add = a, k = b;
  while (k) {
    if (k & 1) ans = (ans + add) % mod;
    add = (add + add) % mod;
    k >>= 1;
              }
return ans;
       long long llfpm (const long long &x, const long long &n, const long long &mod) {
   long long ans = 1, mul = x, k = n;
   while (k) {
      if (k & 1) ans = mul_mod (ans, mul, mod);
      mul = mul_mod (mul, mul, mod);
      k >>= 1;
}
              }
return ans;
       /* Discrete Fourier transform :
    int dft::prepare (int n) : readys the transformation with dimension n.
    void dft::main (complex *a, int n, int f) :
        transforms array a with dimension n to its frequency representation.
        transforms back when f = 1.
       template <int MAXN = 1E6>
struct dft {
   typedef std::complex <double> complex;
              complex e[2][MAXN];
              int prepare (int n) {
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int len = 1;
for (; len <= 2 * n; len <<= 1);
for (int i = 0; i < len; i++) {
    e[0][i] = complex (cos (2 * PI * i / len), sin (2 * PI * i / len));
    e[1][i] = complex (cos (2 * PI * i / len), -sin (2 * PI * i / len));</pre>
                       }
return len;
           1
          void main (complex *a, int n, int f) {
    for (int i = 0, j = 0; i < n; i++) {
        if (i > j) std::swap (a[i], a[j]);
        for (int t = n >> 1; (j ^= t) < t; t >>= 1);
                      for (int i = 2; i <= n; i <<= 1)
    for (int j = 0; j < n; j += i)
        for (int k = 0; k < (i >> 1); k++) {
            complex A = a[j + k];
            complex B = e[f][n / i * k] * a[j + k + (i >> 1)];
            a i i + kl = A + B;
                                                        a[j + k] = A + B;

a[j + k + (i >> 1)] = A - B;
                     if (f == 1) {
   for (int i = 0; i < n; i++)
       a[i] = complex (a[i].real () / n, a[i].imag ());</pre>
};
//
/* Number-theoretic transform :
    void ntt::main (int *a, int n, int f, int mod, int prt) :
        converts polynominal f (x) = a[0] * x^0 + a[1] * x^1 + ... + a[n - 1] * x^(n - 1)
            to a vector (f (prt^0), f (prt^1), f (prt^2), ..., f (prt^(n - 1))). (module mod)
        Converts back if f = 1.
        Requries specific mod and corresponding prt to work. (given in MOD and PRT)
    int ntt::crt (int *a, int mod) :
        makes up the results a from module 3 primes to a certain module mod.
template <int MAXN = 1E6>
struct ntt {
          void main (int *a, int n, int f, int mod, int prt) {
    for (register int i = 0, j = 0; i < n; i++) {
        if (i > j) std::swap (a[i], a[j]);
        for (register int t = n >> 1; (j ^= t) < t; t >>= 1);
                      }
for (register int i = 2; i <= n; i <<= 1) {
    static int exp[MAXN];
    exp[0] = 1;
    exp[1] = fpm (prt, (mod - 1) / i, mod);
    if (f == 1) exp[1] = fpm (exp[1], mod - 2, mod);
    for (register int k = 2; k < (i >> 1); k++) {
        exp[k] = int (111 * exp[k - 1] * exp[1] % mod);
}
                                 for (register int j = 0; j < n; j += i) {
   for (register int k = 0; k < (i >> 1); k++) {
      register int &pA = a[j + k], &pB = a[j + k + (i >> 1)];
      register int A = pA, B = int (111 * pB * exp[k] % mod);
      pA = (A + B) % mod;
      pB = (A - B + mod) % mod;
}
                                 }
                      }
if (f == 1) {
    register int rev = fpm (n, mod - 2, mod);
    for (register int i = 0; i < n; i++) {
        a[i] = int (111 * a[i] * rev % mod);
}</pre>
            int MOD[3] = {1045430273, 1051721729, 1053818881}, PRT[3] = {3, 6, 7};
          int MOD[3] = {10494302/3, 1051/21/3, 1
int crt (int *a, int mod) {
    static int inv[3][3];
    for (int i = 0; i < 3; i++)
        for (int j = 0; j < 3; j++)
            inv[i][j] = (int) inverse (MOD[i], MOD[j]);
    static int x[3]:</pre>
                     inv[i][j] = (inc, incert),
static int x[3];
for (int i = 0; i < 3; i++) {
    x[i] = a[i];
    for (int j = 0; j < i; j++) {
        int t = (x[i] - x[j] + MOD[i]) % MOD[i];
        if (t < 0) t += MOD[i];
        x[i] = int (1LL * t * inv[j][i] % MOD[i]);
}</pre>
                      for (int i = 1; i < 3; i ++) {
    sum = int (1LL * sum * MOD[i - 1] % mod);
    ret += int (1LL * x[i] * sum % mod);
    if (ret >= mod) ret -= mod;
}
                       return ret;
           }
};
       Returns whether a solution exists.
struct crt {
          long long fix (const long long &a, const long long &b) {
   return (a % b + b) % b;
           bool solve (const std::vector <std::pair <long long, long long> > &input,
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std::pair <long long, long long> &output) {
output = std::make_pair (1, 1);
for (int i = 0; i < (int) input.size (); ++i) {
   long long number, useless;
   euclid (output.second, input[i].second, number, useless);
   long long divisor = gcd (output.second, input[i].second);
   if ((input[i].first - output.first) % divisor) {
      return false;
   }</pre>
                                         number *= (input[i].first - output.first) / divisor;
number = fix (number, input[i].second);
output.first += output.second * number;
output.second *= input[i].second / divisor;
output.first = fix (output.first, output.second);
                               return true;
                    }
           };
                    Miller Rabin :
    Checks whether a certain integer is prime.
    Usage : bool miller_rabin::solve (const long long &).
           */
           struct miller_rabin {
                     int BASE[12] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
                    int BASE[12] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
bool check (const long long &prime, const long long &base) {
    long long number = prime - 1;
    for (; "number & 1; number >>= 1);
    long long result = llfpm (base, number, prime);
    for (; number != prime - 1 && result != 1 && result != prime - 1; number <<= 1)
        result = mul_mod (result, result, prime);
    return result == prime - 1 || (number & 1) == 1;</pre>
                    bool solve (const long long &number) {
    if (number < 2) return false;
    if (number < 4) return true;
    if ("number & 1) return false;
    for (int i = 0; i < 12 && BASE[i] < number; ++i)
        if (!check (number, BASE[i]))
            return false;
    return true;
}</pre>
                    }
           };
                    Pollard Rho :
                               Factorizes an integer.
Usage : void pollard_rho::solve (const long long &, std::vector <long long> &).
           struct pollard_rho {
                    miller_rabin is_prime;
                    long long factorize (const long long &number, const long long &seed) {
  long long x = rand() % (number - 1) + 1, y = x;
  for (int head = 1, tail = 2; ; ) {
    x = mul_mod (x, x, number);
    x = (x + seed) % number;
    if (x == y)
        return number:
                                         return number;
long long answer = gcd (abs (x - y), number);
if (answer > 1 && answer < number)
    return answer;
if (++head == tail) {
    y = x;
    tail <<= 1;
}</pre>
                              }
                     void solve (const long long &number, std::vector<long long> &divisor) {
                               if (number > 1) {
                               }
          };
#include <cstdio>
using namespace number;
int main () {
    return 0;
```

The Trial of Geometry

```
#include <cmath>
#include <vector>
#include <algorithm>
namespace geometry {
         /* Basic constant & function
                          EPS : fixes the possible error of data
                                 i.e. x == y \text{ iff } |x - y| < EPS.
                          PI : the value of PI.
int sgn (const double &x) : returns the sign of x.
int cmp (const double &x, const double &y) : returns the sign of x - y.
double sqr (const double &x) : returns x * x.
         const double EPS = 1E-8;
const double PI = acos (-1);
        int sgn (const double &x) { return x < -EPS ? -1 : x > EPS; } int cmp (const double &x, const double &y) { return sgn (x - y); } double sqr (const double &x) { return x * x; }
         /* struct point : defines a point and its various utility.
    point (const double &x, const double &y) gives a point at (x, y).
    It also represents a vector on a 2D plane.
    point unit () const : returns the unit vector of (x, y).
    point rot90 () const :
                          returns a point rotated 90 degrees counter-clockwise with respect to the origin.

point _rot () const : same as above except clockwise.

point rotate (const double &t) const : returns a point rotated t radian(s) counter-clockwise.

Operators are mostly vector operations. i.e. vector +, -, *, / and dot/det product.
       */
struct point {
    double x, y;
    point (const double &x = 0, const double &y = 0) : x (x), y (y) {}
    double norm () const { return sqrt (x * x + y * y); }
    double norm2 () const { return x * x + y * y; }
    point unit () const {
        double 1 = norm ();
        return point (x / 1, y / 1);
}
                 point rot90 () const {return point (-y, x); }
point _rot90 () const {return point (y, -x); }
point rotate (const double &t) const {
    double c = cos (t), s = sin (t);
    return point (x * c - y * s, x * s + y * c);
}
        bool operator == (const point &a, const point &b) {
   return cmp (a.x, b.x) == 0 && cmp (a.y, b.y) == 0;
        bool operator != (const point &a, const point &b) {
    return ! (a == b);
        bool operator < (const point &a, const point &b) {
   if (cmp (a.x, b.x) == 0) return cmp (a.y, b.y) < 0;
   return cmp (a.x, b.x) < 0;</pre>
         point operator - (const point &a) { return point (-a.x, -a.y); }
        point operator + (const point &a, const point &b) {
   return point (a.x + b.x, a.y + b.y);
        point operator - (const point &a, const point &b) {
   return point (a.x - b.x, a.y - b.y);
        point operator * (const point &a, const double &b) {
   return point (a.x * b, a.y * b);
        point operator / (const point &a, const double &b) {
   return point (a.x / b, a.y / b);
         double dot (const point &a, const point &b) {
    return a.x * b.x + a.y * b.y;
        double det (const point &a, const point &b) {
   return a.x * b.y - a.y * b.x;
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double dis (const point &a, const point &b) {
   return sqrt (sqr (a.x - b.x) + sqr (a.y - b.y));
         struct line : defines a line (segment) based on two points, s and t.
    line (const point &s, const point &t) gives a basic line from s to t.
    double length () const : returns the length of the segment.
struct line {
         point s, t;
line (const point &s = point (), const point &t = point ()) : s (s), t (t) {}
double length () const { return dis (s, t); }
/* Point & line interaction :
    bool point_on_line (const point &a, const line &b) : checks if a is on b.
    bool intersect_judgement (const line &a, const line &b) : checks if segment a and b intersect.
    point line_intersect (const line &a, const line &b) : returns the intersection of a and b.
        Fails on colinear or parallel situations.
    double point_to_line (const point &a, const line &b) : returns the distance from a to b.
    double point_to_segment (const point &a, const lint &b) : returns the distance from a to b.
    i.e. the minimized length from a to segment b.
    bool in polvgon (const point &p, const std::vector <point> &po) :
                   1.e. the minimized length from a to segment b.
bool in_polygon (const point &p, const std::vector <point> &po):
    checks if a is in a polygon with vetices po (clockwise or counter-clockwise order).
double polygon_area (const std::vector <point> &a):
    returns the signed area of polygon a (positive for counter-clockwise order, and vise-versa).
point project_to_line (const point &a, const line &b):
    returns the projection of a on b,
bool point_on_line (const point &a, const line &b) {
   return sgn (det (a - b.s, b.t - b.s)) == 0 && sgn (dot (b.s - a, b.t - a)) <= 0;</pre>
bool two_side (const point &a, const point &b, const line &c) {
   return sgn (det (a - c.s, c.t - c.s)) * sgn (det (b - c.s, c.t - c.s)) < 0;</pre>
bool intersect_judgement (const line &a, const line &b) {
         if (point_on_line (b.s, a) || point_on_line (b.t, a)) return true;
if (point_on_line (a.s, b) || point_on_line (a.t, b)) return true;
return two_side (a.s, a.t, b) && two_side (b.s, b.t, a);
point line_intersect (const line &a, const line &b) {
    double s1 = det (a.t - a.s, b.s - a.s);
    double s2 = det (a.t - a.s, b.t - a.s);
    return (b.s * s2 - b.t * s1) / (s2 - s1);
double point_to_line (const point &a, const line &b) {
   return fabs (det (b.t - b.s, a - b.s)) / dis (b.s, b.t);
double point_to_segment (const point &a, const line &b) {
   if (sgn (dot (b.s - a, b.t - b.s) * dot (b.t - a, b.t - b.s)) <= 0)
      return fabs (det (b.t - b.s, a - b.s)) / dis (b.s, b.t);
   return std::min (dis (a, b.s), dis (a, b.t));</pre>
bool in_polygon (const point &p, const std::vector <point> & po) {
         #/
if (point_on_line (p, line (a, b))) return true;
int x = sgn (det (p - a, b - a)), y = sgn (a.y - p.y), z = sgn (b.y - p.y);
if (x > 0 && y <= 0 && z > 0) counter++;
if (x < 0 && z <= 0 && y > 0) counter--;
          return counter != 0;
double polygon_area (const std::vector <point> &a) {
    double ans = 0.0;
    for (int i = 0; i < (int) a.size (); ++i)
        ans += det (a[i], a[ (i + 1) % a.size ()]) / 2.0;
    return ans;</pre>
point project_to_line (const point &a, const line &b) {
    return b.s + (b.t - b.s) * (dot (a - b.s, b.t - b.s) / (b.t - b.s).norm2 ());
/*
         Centers of a triangle :
    returns various centers of a triangle with vertices (a, b, c).
point incenter (const point &a, const point &b, const point &c) {
   double p = dis (a, b) + dis (b, c) + dis (c, a);
   return (a * dis (b, c) + b * dis (c, a) + c * dis (a, b)) / p;
point circumcenter (const point &a, const point &b, const point &c) {
   point p = b - a, q = c - a, s (dot (p, p) / 2, dot (q, q) / 2);
   double d = det (p, q);
   return a + point (det (s, point (p.y, q.y)), det (point (p.x, q.x), s)) / d;
point orthocenter (const point &a, const point &b, const point &c) {
   return a + b + c - circumcenter (a, b, c) * 2.0;
/* Fermat point :
                 point fermat_point (const point &a, const point &b, const point &c) :
    returns a point p that minimizes |pa| + |pb| + |pc|.
point fermat_point (const point &a, const point &b, const point &c) {
   if (a == b) return a;
   if (b == c) return b;
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```
if (c == a) return c;
double ab = dis (a, b), bc = dis (b, c), ca = dis (c, a);
double cosa = dot (b - a, c - a) / ab / ca;
double cosb = dot (a - b, c - b) / ab / bc;
double cosc = dot (b - c, a - c) / ca / bc;
double sq3 = PI / 3.0;
         double sq3 = F1 / 3.0;
point mid;
if (sgn (det (b - a, c - a)) < 0) swap (b, c);
if (sgn (cosa + 0.5) < 0) mid = a;
else if (sgn (cosb + 0.5) < 0) mid = b;
else if (sgn (cosc + 0.5) < 0) mid = c;
else mid = line_intersect (line (a, c + (b - c).rotate (sq3)), line (c, b + (a - b).rotate (sq3)));</pre>
          return mid;
 /* struct circle defines a circle.
circle (point c, double r) gives a circle with center c and radius r.
 struct circle
         point c;
double r;
circle (point c = point (), double r = 0) : c (c), r (r) {}
bool operator == (const circle &a, const circle &b) {
   return a.c == b.c && cmp (a.r, b.r) == 0;
bool operator != (const circle &a, const circle &b) {
   return ! (a == b);
/* Circle interaction :
    bool in_circle (const point &a, const circle &b) : checks if a is in or on b.
    circle make_circle (const point &a, const point &b) :
        generates a circle with diameter ab.
    circle make_circle (const point &a, const point &b, const point &c) :
        generates a circle passing a, b and c.
    std::pair <point, point> line_circle_intersect (const line &a, const circle &b) :
        returns the intersections of a and b.
        Fails if a and b do not intersect.
    std::pair <point, point> circle_intersect (const circle &a, const circle &b):
        returns the intersections of a and b.
        Fails if a and b do not intersect.
    std::pair std::pair sine> tangent (const point &a, const circle &b) :
        returns the tangent lines of b passing through a.
        Fails if a is in b.
bool in_circle (const point &a, const circle &b) {
   return cmp (dis (a, b.c), b.r) <= 0;</pre>
 circle make_circle (const point &a, const point &b) {
   return circle ((a + b) / 2, dis (a, b) / 2);
 circle make_circle (const point &a, const point &b, const point &c) {
   point p = circumcenter (a, b, c);
   return circle (p, dis (p, a));
 nt __circle_intersect (const circle &a, const circle &b) {
point r = (b.c - a.c).unit ();
double d = dis (a.c, b.c);
double x = .5 * ((sqr (a.r) - sqr (b.r)) / d + d);
double h = sqrt (sqr (a.r) - sqr (x));
return a.c + r * x + r.rot90 () * h;
point
 std::pair <point, point> circle_intersect (const circle &a, const circle &b) {
    return std::make_pair (__circle_intersect (a, b), __circle_intersect (b, a));
 std::pair <line, line> tangent (const point &a, const circle &b) {
    circle p = make_circle (a, b.c);
    return circle_intersect (p, b);
                  std::vector <point> convex_hull (std::vector <point> a) :
    returns the convex hull of point set a (counter-clockwise).
bool turn_left (const point &a, const point &b, const point &c) {
    return sgn (det (b - a, c - a)) >= 0;
bool turn_right (const point &a, const point &b, const point &c) {
    return sgn (det (b - a, c - a)) <= 0;</pre>
ret.pop_back ();
                   ret.push_back (a[i]); ++cnt;
```

```
ret.push_back (a[i]);
++cnt;
       ret.pop_back ();
return ret;
       Minimum circle of a point set : circle minimum_circle (std::vector <point> p) : returns the minimum circle of point set p.
circle minimum_circle (std::vector <point> p) {
       circle ret;
       }
return ret;
      Online half plane intersection (complexity = O(c.size ())) :
    std::vector <point> cut (const std::vector<point> &c, line p) :
        returns the convex polygon cutting convex polygon c with half plane p.
        (left hand with respect to vector p)
        If such polygon does not exist, returns an empty set.
                      If such polygon goes not end;
e.g.
static const double BOUND = 1e5;
convex.clear ();
convex.push_back (point (-BOUND, -BOUND));
convex.push_back (point (BOUND, -BOUND));
convex.push_back (point (BOUND, BOUND));
convex.push_back (point (-BOUND, BOUND));
convex = cut (convex, line(point, point));
if (convex.empty ()) { ... }
return ret;
}
       Offline half plane intersection (complexity = O(nlogn), n = h.size ()) : std::vector <point> half_plane_intersect (std::vector <line> h) : returns the intersection of half planes h. (left hand with respect to the vector)
/*
                       If such polygon does not exist, returns an empty set.
bool turn_left (const line &1, const point &p) {
    return turn_left (1.s, 1.t, p);
std::vector <point> half_plane_intersect (std::vector <line> h) {
    typedef std::pair <double, line> polar;
    std::vector <polar> g;
    g.resize (h.size ());
    for (int i = 0; i < (int) h.size (); ++i) {
        point v = h[i].t - h[i].s;
        g[i] = std::make_pair (atan2 (v.y, v.x), h[i]);
}</pre>
        sort (g.begin (), g.end (), [] (const polar &a, const polar &b) {
   if (cmp (a.first, b.first) == 0)
      return sgn (det (a.second.t - a.second.s, b.second.t - a.second.s)) < 0;</pre>
                       return cmp (a.first, b.first) < 0;
       });
h.resize (std::unique (g.begin (), g.end (), [] (const polar &a, const polar &b) {
    return cmp (a.first, b.first) == 0;
}) - g.begin ());
for (int i = 0; i < (int) h.size (); ++i)
    h[i] = g[i].second;
int fore = 0, rear = -1;
std::vector <line> ret;
for (int i = 0; i < (int) h.size (); ++i) {
    while (fore < rear && !turn_left (h[i], line_intersect (ret[rear - 1], ret[rear]))) {
        --rear;
        ret.pop back ();
}</pre>
                      ret.pop_back ();
               ret.push_back (h[i]);
       ret.pop_back ();
                   (rear - fore > 1 && !turn_left (ret[rear], line_intersect (ret[fore], ret[fore + 1])))
        ++fore;
if (rear - fore < 2) return std::vector <point> ();
       ir (rear - fore < 2) return std::vector <point> ();
std::vector <point> ans;
ans.resize (ret.size ());
for (int i = 0; i < (int) ret.size (); ++i)
    ans[i] = line_intersect (ret[i], ret[ (i + 1) % ret.size ()]);
return ans;</pre>
      Intersection of a polygon and a circle :
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```
double polygon_circle_intersect::solve (const std::vector <point> &p, const circle &c) :
    returns the area of intersection of polygon p (vertices in either order) and c.
struct polygon_circle_intersect {
         // The area of the sector with center (0, 0), radius r and segment ab.
         double sector_area (const point &a, const point &b, const double &r) {
   double c = (2.0 * r * r - (a - b).norm2 ()) / (2.0 * r * r);
   double al = acos (c);
   return r * r * al / 2.0;
         // The area of triangle (a, b, (0, 0)) intersecting circle (point (), r).
        // The area of triangle (a, b, (0, 0)) intersecting circle (point (), r).
double area (const point &a, const point &b, const double &r) {
   double dA = dot (a, a), dB = dot (b, b), dC = point_to_segment (point (), line (a, b)), ans = 0.0;
   if (sgn (dA - r * r) <= 0 && sgn (dB - r * r) <= 0) return det (a, b) / 2.0;
   point tA = a.unit () * r;
   point tB = b.unit () * r;
   if (sgn (dC - r) > 0) return sector_area (tA, tB, r);
   std::pair <point, point> ret = line_circle_intersect (line (a, b), circle (point (), r));
   if (sgn (dA - r * r) > 0 && sgn (dB - r * r) > 0) {
      ans += sector_area (tA, ret.first, r);
      ans += det (ret.first, ret.second) / 2.0;
      ans += sector_area (ret.second, tB, r);
      return ans;
}
                   if (sgn (dA - r * r) > 0)
    return det (ret.first, b) / 2.0 + sector_area (tA, ret.first, r);
                   else return det (a, ret.second) / 2.0 + sector_area (ret.second, tB, r);
         // Main process.
        double solve (const std::vector <point> &p, const circle &c) {
    double ret = 0.0;
    for (int i = 0; i < (int) p.size (); ++i) {
        int s = sgn (det (p[i] - c.c, p[ (i + 1) % p.size ()] - c.c));
        if (s > 0)
                                       ret += area (p[i] - c.c, p[ (i + 1) % p.size ()] - c.c, c.r);
                                      ret -= area (p[ (i + 1) % p.size ()] - c.c, p[i] - c.c, c.r);
                   return fabs (ret);
         }
};
        Union of circles:
    std::vector <double> union_circle::solve (const std::vector <circle> &c) :
        returns the union of circle set c.
        The i-th element is the area covered with at least i circles.
struct union_circle {
         struct cp {
    double x, y, angle;
                  double x, y, angle,
int d;
double r;
cp (const double &x = 0, const double &y = 0, const double &angle = 0,
    int d = 0, const double &r = 0) : x (x), y (y), angle (angle), d (d), r (r) {}
         double dis (const cp &a, const cp &b) {
   return sqrt (sqr (a.x - b.x) + sqr (a.y - b.y));
         double cross (const cp &p0, const cp &p1, const cp &p2) {
    return (p1.x - p0.x) * (p2.y - p0.y) - (p1.y - p0.y) * (p2.x - p0.x);
                  cir_cross (cp p1, double r1, cp p2, double r2, cp &cp1, cp &cp2) {
    double mx = p2.x - p1.x, sx = p2.x + p1.x, mx2 = mx * mx;
    double my = p2.y - p1.y, sy = p2.y + p1.y, my2 = my * my;
    double sq = mx2 + my2, d = - (sq - sqr (r1 - r2)) * (sq - sqr (r1 + r2));
    if (sgn (d) < 0) return 0;
    if (sgn (d) <= 0) d = 0;
    else d = sqrt (d);
    double x = mx * ((r1 + r2) * (r1 - r2) + mx * sx) + sx * my2;
    double y = my * ((r1 + r2) * (r1 - r2) + my * sy) + sy * mx2;
    double dx = mx * d, dy = my * d;
    sq *= 2;
    cp1.x = (x - dy) / sq;
    cp2.x = (x + dy) / sq;
    cp2.y = (y + dx) / sq;
    if (sgn (d) > 0) return 2;
    else return 1;
        bool circmp (const cp &u, const cp &v) {
   return sgn (u.r - v.r) < 0;</pre>
         bool cmp (const cp &u, const cp &v) {
    if (sgn (u.angle - v.angle)) return u.angle < v.angle;
    return u.d > v.d;
         std::vector <double> solve (const std::vector <circle> &c) {
  int n = c.size ();
  std::vector <cp> cir, tp;
  std::vector <double> area;
                  std::vector <double> area;
cir.resize (n);
tp.resize (2 * n);
area.resize (n + 1);
for (int i = 0; i < n; i++)
    cir[i] = cp (c[i].c.x, c[i].c.y, 0, 1, c[i].r);</pre>
                   cp cp1, cp2;
```

The Trial of Graph

```
/* Graph template
              Most algorithms on a graph.
#include <algorithm>
#include <array>
#include <queue>
#include <vector>
namespace graph {
   const int INF = 1E9;
       /* Edge list:
                     Various kinds of edge list.
       template <int MAXN = 1E5, int MAXM = 1E5>
       struct edge_list {
              int size;
int begin[MAXN], dest[MAXM], next[MAXM];
              void clear (int n) {
    size = 0;
    std::fill (begin, begin + n, -1);
              edge_list (int n = MAXN) {
    clear (n);
              void add_edge (int u, int v) {
   dest[size] = v; next[size] = begin[u]; begin[u] = size++;
       template <int MAXN = 1E5, int MAXM = 1E5>
       struct flow_edge_list {
              int size;
int begin[MAXN], dest[MAXM], next[MAXM], flow[MAXM], inv[MAXM];
              void clear (int n) {
    size = 0;
                     std::fill (begin, begin + n, -1);
              flow_edge_list (int n = MAXN) {
    clear (n);
              void add_edge (int u, int v, int f) {
    dest[size] = v; next[size] = begin[u]; flow[size] = f; inv[size] = size + 1; begin[u] = size++;
    dest[size] = u; next[size] = begin[v]; flow[size] = 0; inv[size] = size - 1; begin[v] = size++;
       };
       template <int MAXN = 1E5, int MAXM = 1E5>
struct cost_flow_edge_list {
              int size;
int begin[MAXN], dest[MAXM], next[MAXM], cost[MAXM], flow[MAXM], inv[MAXM];
void clear (int n) {
    size = 0;
    std::fill (begin, begin + n, -1);
}
              cost_flow_edge_list (int n = MAXN) {
    clear (n);
              void add_edge (int u, int v, int c, int f) {
    dest[size] = v; next[size] = begin[u]; cost[size] = c;
    flow[size] = f; inv[size] = size + 1; begin[u] = size++;
    dest[size] = u; next[size] = begin[v]; cost[size] = c;
    flow[size] = 0; inv[size] = size - 1; begin[v] = size++;
}
              Hopcoft-Carp algorithm
                     maximum matching with complexity O (m * n^0.5).
struct hopcoft_carp:
Initialize: pass n, m as the size of both vertex sets, e as the reference of the edge_list.
Usage: solve() for maximum matching. The matching is in matchx and matchy.
       template <int MAXN = 1E5, int MAXM = 1E5>
       struct hopcoft_carp {
              int n, m;
edge_list <MAXN, MAXM> &e;
              int matchx[MAXN], matchy[MAXN], level[MAXN];
              bool dfs (int x) {
    for (int i = e.begin[x]; ~i; i = e.next[i]) {
        int y = e.dest[i];
        int w = matchy[y];
}
```

```
if (w == -1 \mid | (level[x] + 1 == level[w] && dfs (w))) {
                                        matchx[x] = y;
matchy[y] = x;
return true;
                               }
                    level[x] = -1;
return false;
        } else {
   level[i] = -1;
                              for (int head = 0; head < (int) queue.size(); ++head) {
   int x = queue[head];
   for (int i = e.begin[x]; ~i; i = e.next[i]) {
      int y = e.dest[i];
      int w = matchy[y];
      if (w != -1 && level[w] < 0) {
            level[w] = level[x] + 1;
            queue.push_back (w);
      }
}</pre>
                                        }
                              int delta = 0;
for (int i = 0; i < n; ++i)
    if (matchx[i] == -1 && dfs (i)) delta++;
if (delta == 0) return answer;
else answer += delta;</pre>
         }
};
         Kuhn Munkres algorithm :
    weighted maximum matching algorithm. Complexity O (N^3).
                     struct kuhn_munkres :
                              Initialize: pass nx, ny as the size of both sets, w as the weight matrix. Usage: solve () for the minimum matching. The matching is in link.
*/
template <int MAXN = 500>
struct kuhn_munkres {
         int nx, ny;
int w[MAXN][MAXN];
          int lx[MAXN], ly[MAXN], visx[MAXN], visy[MAXN], slack[MAXN], link[MAXN];
         if (link[y] == -1 || dfs (link[y])) {
    link[y] = x;
    return 1;
                               } else slack[y] = std::max (slack[y], t);
                    return 0;
                  solve () {
int i, j;
std::fill (link, link + ny, -1);
std::fill (ly, ly + ny, 0);
for (i = 0; i < nx; i++)
    for (j = 0, lx[i] = INF; j < ny; j++)
        lx[i] = std::min (lx[i], w[i][j]);

for (int x = 0; x < nx; x++) {
    for (i = 0; i < ny; i++) slack[i] = -INF;
    while (true) {
        std::fill (visx, visx + nx, 0);
        std::fill (visy, visy + ny, 0);
        if (dfs (x)) break;
        int d = INF;
        for (i = 0; i < ny; i++)
              if (!visy[i] && d < slack[i]) d = slack[i];
        for (i = 0; i < nx; i++)
              if (visx[i]) lx[i] -= d;
        for (i = 0; i < ny; i++)
              if (visy[i]) ly[i] += d;
              else slack[i] -= d;
}</pre>
          int solve () {
                    int res = 0;
for (i = 0; i < ny; i ++)
    if (link[i] > -1) res += w[link[i]][i];
return res;
         }
};
         Weighted matching algorithm :
    maximum match for graphs. Not stable.
    struct weighted_match :
        Usage : Set k to the size of vertices, w to the weight matrix.
        Note that k has to be even for the algorithm to work.
*/
```

```
template <int MAXN = 500>
struct weighted_match {
         int k;
long long w[MAXN][MAXN];
int match[MAXN], path[MAXN], p[MAXN], long long d[MAXN];
bool v[MAXN];
       }
--len;
v[i] = false;
return false;
         long long solve () {
   if (k & 1) ++k;
   for (int i = 0; i < k; ++i) p[i] = i, match[i] = i ^ 1;
   int cnt = 0;
   for (;;) {
      len = 0;
   }
}</pre>
                            len'='0;
bool flag = false;
std::fill (d, d + k, 0);
std::fill (v, v + k, 0);
for (int i = 0; i < k; ++i) {
    if (dfs (p[i])) {
        flag = true;
        int t = match[path[len - 1]], j = len - 2;
        while (path[j] != path[len - 1]) {
            match[t] = path[j];
            std::swap (t, match[path[j]]);
            --i;
                                                 match[t] = path[j];
match[path[j]] = t;
                                       }
                             if (!flag) {
   if (++cnt >= 1) break;
   std::random_shuffle (p, p + k);
                   forg long ans = 0;
for (int i = 0; i < k; ++i)
    ans += w[i][match[i]];
return ans / 2;</pre>
         }
};
         Weighted blossom algorithm (vfleaking ver.) :
   maximum match for graphs. Complexity O (n^3).
   Note that the base index is 1.
   struct weighted_blossom :
                    struct weig
Usage :
                                       ge:
Set n to the size of the vertices.
Run init ().
Set g[][].w to the weight of the edge.
Run solve ().
The first result is the answer, the second one is the number of matching pairs.
Obtain the matching with match[].
template <int MAXN = 500>
struct weighted_blossom {
         struct edge {
   int u, v, w;
   edge (int u = 0, int v = 0, int w = 0): u (u), v (v), w (w) {}
       edge (inc =
};
int n, n_x;
edge g[MAXN * 2 + 1][MAXN * 2 + 1];
int lab[MAXN * 2 + 1], slack[MAXN * 2 + 1], st[MAXN * 2 + 1], pa[MAXN * 2 + 1];
int match[MAXN * 2 + 1] [MAXN * 1], s[MAXN * 2 + 1], vis[MAXN * 2 + 1];
int flower_from[MAXN * 2 + 1][MAXN + 1], s[MAXN * 2 + 1], vis[MAXN * 2 + 1];
std::vector<int> flower[MAXN * 2 + 1];
std::queue<int> q;
int e_delta (const edge &e) {
    return lab[e.u] + lab[e.v] - g[e.u][e.v].w * 2;
}
          void set_slack (int x) {
    slack[x] = 0;
    for (int u = 1; u <= n; ++u)
        if (g[u][x].w > 0 && st[u] != x && S[st[u]] == 0)update_slack (u, x);
          }
void q_push (int x) {
    if (x <= n)q.push (x);
    else for (size_t i = 0; i < flower[x].size(); i++)q_push (flower[x][i]);
}</pre>
         }
void set_st (int x, int b) {
    st[x] = b;
    if (x > n) for (size_t i = 0; i < flower[x].size(); ++i)
        set_st (flower[x][i], b);</pre>
          int get_pr (int b, int xr) {
```

```
int pr = find (flower[b].begin(), flower[b].end(), xr) - flower[b].begin();
if (pr % 2 == 1) {
    reverse (flower[b].begin() + 1, flower[b].end());
                    return (int) flower[b].size() - pr;
} else return pr;

}
void set_match (int u, int v) {
    match[u] = g[u][v].v;
    if (u > n) {
        edge e = g[u][v];
        int xr = flower_from[u][e.u], pr = get_pr (u, xr);
        for (int i = 0; i < pr; ++i)set_match (flower[u][i], flower[u][i ^ 1]);
        set_match (xr, v);
        rotate (flower[u].begin(), flower[u].begin() + pr, flower[u].end());
}
</pre>

}
void augment (int u, int v) {
    for (;;) {
        int xnv = st[match[u]];
        set_match (u, v);
        if (!xnv) return;
        set_match (xnv, st[pa[xnv]]);
        u = st[pa[xnv]], v = xnv;
}

}
int get_lca (int u, int v) {
    static int t = 0;
    for (++t; u || v; std::swap (u, v)) {
        if (u == 0) continue;
        if (vis[u] == t) return u;
        vis[u] = t;
        u = st[match[u]];
        if (u)u = st[pa[u]];
                                      if (u) u = st[pa[u]];
                     return 0;
return 0;
}
void add_blossom (int u, int lca, int v) {
    int b = n + 1;
    while (b <= n_x && st[b])++b;
    if (b > n_x)++n_x;
    lab[b] = 0, S[b] = 0;
    match[b] = match[lca];
    flower[b].clear();
    flower[b].push_back (lca);
    for (int x = u, y; x != lca; x = st[pa[y]])
        flower[b].push_back (x), flower[b].push_back (y = st[match[x]]), q_push (y);
    reverse (flower[b].begin() + 1, flower[b].end());
    for (int x = v, y; x != lca; x = st[pa[y]])
        flower[b].push_back (x), flower[b].push_back (y = st[match[x]]), q_push (y);
    set_st (b, b);
                   flower[b].push_back (x), flower[b].push_back (y = st[match[x]]),
set_st (b, b);
for (int x = 1; x <= n_x; ++x)g[b][x].w = g[x][b].w = 0;
for (int x = 1; x <= n; ++x)flower_from[b][x] = 0;
for (size_t i = 0; i < flower[b].size(); ++i) {
   int xs = flower[b][i];
   for (int x = 1; x <= n_x; ++x)
        if (g[b][x].w == 0 || e_delta (g[xs][x]) < e_delta (g[b][x]))
            g[b][x] = g[xs][x], g[x][b] = g[x][xs];
   for (int x = 1; x <= n; ++x)
        if (flower_from[xs][x])flower_from[b][x] = xs;
}</pre>
                     }
set_slack (b);
set_slack (b),
}
void expand_blossom (int b) {
    for (size_t i = 0; i < flower[b].size(); ++i)
        set_st (flower[b][i], flower[b][i]);
    int xr = flower_from[b][g[b][pa[b]].u], pr = get_pr (b, xr);
    for (int i = 0; i < pr; i += 2) {
        int xs = flower[b][i], xns = flower[b][i + 1];
        pa[xs] = g[xns][xs].u;
        S[xs] = 1, S[xns] = 0;
        slack[xs] = 0, set_slack (xns);
        q_push (xns);
}</pre>
                    }
S[xr] = 1, pa[xr] = pa[b];
for (size_t i = pr + 1; i < flower[b].size(); ++i) {
   int xs = flower[b][i];
   S[xs] = -1, set_slack (xs);</pre>
                     st[b] = 0;
  bool on_found_edge (const edge &e) {
                   l on_found_edge (const edge &e) {
int u = st[e.u], v = st[e.v];
if (S[v] == -1) {
    pa[v] = e.u, S[v] = 1;
    int nu = st[match[v]];
    slack[v] = slack[nu] = 0;
    S[nu] = 0, q push (nu);
} else if (S[v] == 0) {
    int lca = get_lca (u, v);
    if (!lca)return augment (u, v), augment (v, u), true;
    else add_blossom (u, lca, v);
}
                     return false:
bool matching() {
    std::fill (S + 1, S + 1 + n_x, -1);
    std::fill (slack + 1, slack + 1 + n_x, -1);
    q = std::queue<int>();
    for (int x = 1; x <= n_x; ++x)
        if (st[x] == x && !match[x])pa[x] = 0, S[x] = 0, q_push (x);
    if (q.empty())return false;
    for (;;) {
        while (q.size()) {
            int u = q.front();
        }
    }
}</pre>
```

```
if (S[st[u]] == 1) continue;
for (int v = 1; v <= n; ++v)
   if (g[u][v].w > 0 && st[u] != st[v]) {
      if (e_delta (g[u][v]) == 0) {
         if (on_found_edge (g[u][v])) return true;
      } else update_slack (u, st[v]);

}
int d = INF;
for (int b = n + 1; b <= n_x; ++b)
    if (st[b] == b && S[b] == 1)d = std::min (d, lab[b] / 2);
for (int x = 1; x <= n_x; ++x)
    if (st[x] == x && slack[x]) {
        if (S[x] == -1)d = std::min (d, e_delta (g[slack[x]][x]));
        else if (S[x] == 0)d = std::min (d, e_delta (g[slack[x]][x]) / 2);
}
</pre>
                                 for (int u = 1; u <= n; ++u) {
   if (S[st[u]] == 0) {
      if (lab[u] <= d) return 0;
      lab[u] -= d;
   } else if (S[st[u]] == 1) lab[u] += d;
}</pre>
                                 for (int b = n + 1; b <= n_x; ++b)
   if (st[b] == b) {
      if (S[st[b]] == 0)lab[b] += d * 2;
      else if (S[st[b]] == 1)lab[b] -= d * 2;</pre>
                                 g = std::queue<int>();
for (int x = 1; x <= n_x; ++x)
    if (st[x] == x && slack[x] && st[slack[x]] != x && e_delta (g[slack[x]][x]) == 0)
    if (on_found_edge (g[slack[x]][x]))return true;
for (int b = n + 1; b <= n_x; ++b)
    if (st[b] == b && S[b] == 1 && lab[b] == 0)expand_blossom (b);</pre>
                      return false;
          }
std::pair <long long, int> solve () {
    std::fill (match + 1, match + n + 1, 0);
    n_x = n;
    int n_matches = 0;
    int n_matches = 0;
}
                     int n_matches = 0;
long long tot_weight = 0;
for (int u = 0; u <= n; ++u)st[u] = u, flower[u].clear();
int w_max = 0;
for (int u = 1; u <= n; ++u)
    for (int v = 1; v <= n; ++v) {
        flower_from[u][v] = (u == v ? u : 0);
        w_max = std::max (w_max, g[u][v].w);
}</pre>
                     for (int u = 1; u <= n; ++u)lab[u] = w_max;
while (matching())++n_matches;
for (int u = 1; u <= n; ++u)
    if (match[u] && match[u] < u)
        tot_weight += g[u][match[u]].w;
return std::make_pair (tot_weight, n_matches);</pre>
          }
void init () {
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v)
        g[u][v] = edge (u, v, 0);</pre>
};
          Sparse graph maximum flow :
                      int isap::solve (flow_edge_list &e, int n, int s, int t) :
    e : edge list.
                                 n : vertex size.
s : source.
t : sink.
template <int MAXN = 1E3, int MAXM = 1E5>
struct isap {
          int pre[MAXN], d[MAXN], gap[MAXN], cur[MAXN];
          gap[v] = n,
int u = pre[s] = s, v, maxflow = 0;
while (d[s] < n) {
    v = n;</pre>
                                  v = n;
for (int i = cur[u]; ~i; i = e.next[i])
   if (e.flow[i] && d[u] == d[e.dest[i]] + 1) {
      v = e.dest[i];
      cur[u] = i;
      break;
}
                                  if (v < n) {
    pre[v] = u;
    u = v;</pre>
                                           pu='v;
if (v == t) {
    int dflow = INF, p = t;
    u = s;
    while (p != s) {
        p = pre[p];
        dflow = std::min (dflow, e.flow[cur[p]]);
        .
                                                        maxflow += dflow;
p = t;
while (p != s) {
    p = pre[p];
    e.flow[cur[p]] -= dflow;
    e.flow[e.inv[cur[p]]] += dflow;
                                 } else {
  int mindist = n + 1;
```

```
for (int i = e.begin[u]; ~i; i = e.next[i])
    if (e.flow[i] && mindist > d[e.dest[i]]) {
        mindist = d[e.dest[i]];
        cur[u] = i;
                              if (!--gap[d[u]]) return maxflow;
gap[d[u] = mindist + 1]++;
u = pre[u];
               return maxflow;
       }
};
       Dense graph maximum flow :
    int dinic::solve (flow_edge_list &e, int n, int s, int t) :
/*
                       e : edge list
                       n : vertex size.
s : source.
t : sink.
template <int MAXN = 1E3, int MAXM = 1E5>
struct dinic {
       flow_edge_list <MAXN, MAXM> &e;
       int n, s, t;
       int d[MAXN], w[MAXN], q[MAXN];
       int bfs() {
    for (int i = 0; i < n; i ++) d[i] = -1;
    int 1, r;
    q[1 = r = 0] = s, d[s] = 0;
    for (; 1 <= r; 1 ++)
        for (int k = e.begin[q[1]]; k > -1; k = e.next[k])
        if (d[e.dest[k]] == -1 && e.flow[k] > 0) d[e.dest[k]] = d[q[1]] + 1, q[++r] = e.dest[k];
    return d[t] > -1 ? 1 : 0;
}
      }
               if (k == -1) d[u] = -1;
return ret;
       void solve (flow_edge_list <MAXN, MAXM> &e, int n, int s, int t) {
    dinic::e = e; dinic::n = n; dinic::s = s; dinic::t = t;
    while (bfs ()) {
        for (int i = 0; i < n; i ++) w[i] = e.begin[i];
        dfs (s, INF);
}</pre>
       }
     Sparse graph minimum cost flow :
               e : edge list.
n : vertex size.
s : source.
t : sink
                       t : sink. returns the flow and the cost respectively.
template <int MAXN = 1E3, int MAXM = 1E5>
struct minimum_cost_flow {
       cost_flow_edge_list <MAXN, MAXM> &e;
int n, source, target;
int prev[MAXN];
int dist[MAXN], occur[MAXN];
      int x = queue[head];
for (int i = e.begin[x]; ~i; i = e.next[i]) {
    int y = e.dest[i];
    if (e.flow[i] && dist[y] > dist[x] + e.cost[i]) {
        dist[y] = dist[x] + e.cost[i];
        prev[y] = i;
        if (!occur[y]) {
            occur[y] = true;
            queue.push_back (y);
    }
                              }
                       occur[x] = false;
               return dist[target] < INT_MAX;</pre>
       ,
std::pair <int, int> solve (cost_flow_edge_list <MAXN, MAXM> &e, int n, int s, int t) {
    minimum_cost_flow::e = e; minimum_cost_flow::n = n;
    source = s; target = t;
    std::pair <int, int> answer = std::make_pair (0, 0);
    while (augment()) {
        int number = INT_MAX;
    }
}
        }
```

```
for (int i = target; i != source; i = e.dest[e.inv[prev[i]]]) {
   number = std::min (number, e.flow[prev[i]]);
                                  answer.first += number;
for (int i = target; i != source; i = e.dest[e.inv[prev[i]]]) {
    e.flow[prev[i]] -= number;
    e.flow[e.inv[prev[i]]] += number;
    answer.second += number * e.cost[prev[i]];
                          return answer;
                 }
        };
                Dense graph minimum cost flow :
    std::pair <int, int> zkw_flow::solve (cost_flow_edge_list &e,
                                                                                                           int \overline{n}, int \overline{s}, int \overline{t}):
                                  e : edge list.
                                  n : vertex size.
s : source.
t : sink.
                                  returns the flow and the cost respectively.
         template <int MAXN = 1E3, int MAXM = 1E5>
         struct zkw_flow {
                 cost_flow_edge_list <MAXN, MAXM> &e;
int n, s, t, totFlow, totCost;
int dis[MAXN], slack[MAXN], visit[MAXN];
                int dis[FHANI, case]
int modlable() {
   int delta = INF;
   for (int i = 0; i < n; i++) {
      if (!visit[i] && slack[i] < delta) delta = slack[i];
      slack[i] = INF;
}</pre>
                          if (delta == INF) return 1;
for (int i = 0; i < n; i++) if (visit[i]) dis[i] += delta;
return 0;</pre>
                int dfs (int x, int flow) {
   if (x == t) {
      totFlow += flow;
      totCost += flow * (dis[s] - dis[t]);
      return flow;
}
                       return :::.,
}
visit[x] = 1;
int left = flow;
for (int i = e.begin[x]; ~i; i = e.next[i])
    if (e.flow[i] > 0 && !visit[e.dest[i]]) {
        int y = e.dest[i];
        if (dis[y] + e.cost[i] == dis[x]) {
            int delta = dfs (y, std::min (left, e.flow[i]));
            e.flow[i] -= delta;
            e.flow[e.inv[i]] += delta;
            left -= delta;
            if (!left) { visit[x] = false; return flow; }
} else
                                                    slack[y] = std::min (slack[y], dis[y] + e.cost[i] - dis[x]);
                          return flow - left;
                ,
std::pair <int, int> solve (cost_flow_edge_list <MAXN, MAXM> &e, int n, int s, int t) {
    zkw_flow::e = e; zkw_flow::n = n; zkw_flow::s = s; zkw_flow::t = t;
    totFlow = 0; totCost = 0;
    std::fill (dis + 1, dis + t + 1, 0);
    do {
                         return std::make_pair (totFlow, totCost);
                 }
        };
#include <cstdio>
using namespace graph;
int main () {
    return 0;
```

The Trial of String

Reference

5.1 vimrc

```
set ruler
set tabstop=4
set softtabstop=4
set softtabstop=4
set siftwidth=4
set smartindent
set showmatch
set hlsearch
set autoread
set backspace=2
set set autoread
set backspace=2
syntax on
nmap <C-A> ggVG
vmap <C-P> "+p
autocmd FileType cpp map <F3> :vsplit %<.in <CR>
autocmd FileType cpp map <F3> :!time ./%<.exe <CR>
autocmd FileType cpp map <F>:!time ./%<.exe <<CR>
autocmd FileType cpp map <F>:!time ./%<.exe <<CR>
autocmd FileType cpp map <F>:!time ./%<.exe <<.in <CR>
autocmd FileType pdp map <F>:!style -A2 -t -C -S -N -O -xd -p -H % <CR>
autocmd FileType java map <F8> :!time java %< <CR>
autocmd FileType java map <F8> :!time java %< <CR>
autocmd FileType java map <F9> :!java %< CR>
autocmd FileType tex map <F9> :!java %< CR>
autocmd FileType tex map <F9> :!java istyle -A2 -t -C -S -N -O -xd -p -H % <CR>
autocmd FileType tex map <F9> :!java %< CR>
autocmd FileType tex map <F9> :!pdflatex % && rm %<.aux && rm %<.log <CR>
autocmd FileType tex map <F9> :!pdflatex % && rm %<.aux && rm %<.log <CR>
autocmd FileType tex map <F9> :!pdflatex % && rm %<.aux && rm %<.log <CR>
autocmd FileType tex map <F9> :!pdflatex % && rm %<.aux && rm %<.log <CR>
autocmd FileType tex map <F9> :!pdflatex % && rm %<.aux && rm %<.log <CR>
autocmd FileType tex map <F8> :!chrome %:p:h/%<.pdf <CR>
```

5.2 Java Reference

```
doubleValue () / toPlainString () : converts to other types.
                       Arrays:
Arrays.sort (T [] a);
Arrays.sort (T [] a, int fromIndex, int toIndex);
Arrays.sort (T [] a, int fromIndex, int toIndex, Comperator <? super T> comperator);

**TabedTiet <E>:

**TabedTiet <E>:

**TabedTiet / GetLast / removeFirst / removeLast () :
                        LinkedList <E>:
   addFirst / addLast (E) / getFirst / getLast / removeFirst / removeLast ():
   deque implementation.
   clear () / add (int, E) / remove (int): clear, add & remove.
   size () / contains / removeFirstOccurrence / removeLastOccurrence (E):
   deque methods.
                      deque methods.

ListIterator <E> listIterator (int index) : returns an iterator :
    E next / previous () : accesses and iterates.
    hasNext / hasPrevious () : checks availablity.
    nextIndex / previousIndex () : returns the index of a subsequent call.
    add / set (E) / remove () : changes element.

PriorityQueue <E> (int initcap, Comparator <? super E> comparator) :
    add (E) / clear () / iterator () / peek () / poll () / size () :
        priority queue implementations.

TreeMap <K, V> (Comparator <? super K> comparator) :
    Map.Entry <K, V> ceilingEntry / floorEntry / higherEntry / lowerEntry (K):
        getKey / getValue () / setValue (V) : entries.
    clear () / put (K, V) / get (K) / remove (K) : basic operation.
    size () : size.

StringBuilder :
                       clear () / put (K, V) / get (K) / remove (K) : basic operation.
    size () : size.
StringBuilder :
    Mutable string.
    StringBuilder (string) : generates a builder.
    append (int, string, ...) / insert (int offset, ...) : adds objects.
    charAt (int) / setCharAt (int, char) : accesses a char.
    delete (int, int) : removes a substring.
    reverse () : reverses itself.
    length () : returns the length.
    toString () : converts to string.
                         String :
                                    Immutable string.

String.format (String, ...) : formats a string. i.e. sprintf. toLowerCase / toUpperCase () : changes the case of letters.
/* Examples on Comparator :
public class Main {
           public static class Point {
                        public int x;
public int y;
                        public Point () {
                                   x = 0;

y = 0;
                        public Point (int xx, int yy) {
    x = xx;
    y = yy;
            1;
           public static class Cmp implements Comparator <Point> {
   public int compare (Point a, Point b) {
      if (a.x < b.x) return -1;
      if (a.x == b.x) {
        if (a.y < b.y) return -1;
        if (a.y == b.y) return 0;
   }</pre>
                                    return 1:
                        }
            1;
           public static void main (String [] args) {
   Cmp c = new Cmp ();
   TreeMap <Point, Point> t = new TreeMap <Point, Point> (c);
            1
};
            Another way to implement is to use Comparable. However, equalTo and hashCode must be rewritten. Otherwise, containers may fail and give strange answers.
            Example :
           public static class Point implements Comparable <Point> {
                        public int x;
public int y;
public Point () {
                                   x = 0;

y = 0;
                        public Point (int xx, int yy) {
    x = xx;
    y = yy;
                        public int compareTo (Point p) {
    if (x < p.x) return -1;
    if (x == p.x) {
        if (y < p.y) return -1;
        if (y == p.y) return 0;
    }
}</pre>
                                    return 1;
                        public boolean equalTo (Point p) {
    return (x == p.x && y == p.y);
                        public int hashCode () {
    return x + y;
           };
//Faster IO :
public class Main {
            static class InputReader {
```

5.3 Operator Precedence

A Subscript Subscript	Precedence	Operator	Description	Associativity
2	1	::	Scope resolution	
2	2	a++ a	Suffix/postfix increment and decrement	Left-to-right
2 a () Function call Subscript > Member access		type() type{}	Functional cast	
		a()	Function call	
++aa		a[]	Subscript	
+a -a Unary plus and minus Costyle cast Costyle cast Right-to-left		>	Member access	
1	3	++aa	Prefix increment and decrement	Right-to-left
C-style cast		+a -a	Unary plus and minus	
3 *a Indirection (dereference) Right-to-left &a Address-of Size-of new new[] Dynamic memory allocation delete delete[] Dynamic memory deallocation 4 .* ->* Pointer-to-member 5 a*b a/b a*b Multiplication, division, and remainder 6 a*b a-b Addition and subtraction 7 << >> Bitwise left shift and right shift 8 < <=		! ~	Logical NOT and bitwise NOT	
Sa Sizeof Size-of Size-of Size-of Size-of Dynamic memory allocation Dynamic memory deallocation Dynamic memory deallocation		(type)	C-style cast	
Size-of Dynamic memory allocation Dynamic memory allocation Dynamic memory deallocation		*a	Indirection (dereference)	
Dynamic memory allocation		&a	Address-of	
delete delete[] Dynamic memory deallocation		sizeof	Size-of	
16		new new[]	Dynamic memory allocation	
5 a*b a/b a%b Multiplication, division, and remainder 6 a+b a-b Addition and subtraction 7 << >> Bitwise left shift and right shift 8 <<= For relational operators < and ≤ respectively 9 == != For relational operators > and ≥ respectively 10 a&b Bitwise AND 11		delete delete[]	Dynamic memory deallocation	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4	.* ->*	Pointer-to-member	- Left-to-right
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	5	a*b a/b a%b		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		a+b a-b		
For relational operators $>$ and \ge respectively 9	7	<< >>		
For relational operators $>$ and \ge respectively $=$ $=$ $!$ $=$ For relational operators $=$ and \ne respectively $=$ $=$ $!$ $=$ For relational operators $=$ and \ne respectively $=$ $=$ $=$ $=$ Bitwise AND $=$ Bitwise VOR (exclusive or) $=$ Bitwise OR (inclusive or) $=$ Logical AND $=$ Logical OR $=$ Ternary conditional $=$ throw operator $=$ Direct assignment $=$ Compound assignment by arithmetic operation $=$ Compound assignment by bitwise shift $=$ Compound assignment by bitwise AND, XOR, and OR $=$ Compound assignment by bitwise AND, XOR, and OR		< <=		
9 == != For relational operators = and \neq respectively 10 a&b Bitwise AND 11		> >=		
11		== !=		
Bitwise XOR (exclusive or) 12				
13 & && Logical AND 14 Logical OR a?b:c Ternary conditional throw perator birect assignment += -= *= /= %= Compound assignment by arithmetic operation		^		
14			,	
a?b:c Ternary conditional throw operator $= Direct assignment \\ += -= *= /= %= Compound assignment by arithmetic operation \\ <<= >>= Compound assignment by bitwise shift \\ &= ^= = Compound assignment by bitwise AND, XOR, and OR $ Left to right		& &		
throw throw operator Direct assignment $+=-= *=/= %=$ Compound assignment by arithmetic operation $<<=>>=$ Compound assignment by bitwise shift $&=$ $&=$ Compound assignment by bitwise AND, XOR, and OR Compound assignment by bitwise AND, XOR, and OR	14			
15 = Direct assignment Right-to-left $+=-=*=/=%=$ Compound assignment by arithmetic operation Compound assignment by bitwise shift $&=-*=/=%=$ Compound assignment by bitwise AND, XOR, and OR 16 Compound assignment Compound assignment by bitwise AND, XOR, and OR 17 Compound assignment Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 19 Compound assignment by bitwise AND, XOR, and OR 10 Compound assignment by bitwise AND, XOR, and OR 11 Compound assignment by bitwise AND, XOR, and OR 12 Compound assignment by bitwise AND, XOR, and OR 13 Compound assignment by bitwise AND, XOR, and OR 14 Compound assignment by bitwise AND, XOR, and OR 15 Compound assignment by bitwise AND, XOR, and OR 16 Compound assignment by bitwise AND, XOR, and OR 17 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 19 Compound assignment by bitwise AND, XOR, and OR 10 Compound assignment by bitwise AND, XOR, and OR 10 Compound assignment by bitwise AND, XOR, and OR 11 Compound assignment by bitwise AND, XOR, and OR 12 Compound assignment by bitwise AND, XOR, and OR 13 Compound assignment by bitwise AND, XOR, and OR 14 Compound assignment by bitwise AND, XOR, and OR 15 Compound assignment by bitwise AND, XOR, and OR 16 Compound assignment by bitwise AND, XOR, and OR 16 Compound assignment by bitwise AND, XOR, and OR 17 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18 Compound assignment by bitwise AND, XOR, and OR 18	15	a?b:c	, and the second	Right-to-left
+= -= *= /= %= Compound assignment by arithmetic operation		throw	_	
Compound assignment by arithmetic operation $<<=>>=$ $&=$ $&=$ $&=$ $&=$ $&=$ $&=$ $&=$ $&=$ Compound assignment by bitwise shift Compound assignment by bitwise AND, XOR, and OR Compound assignment by bitwise AND, XOR, and OR		=		
&= = = Compound assignment by bitwise AND, XOR, and OR		, ,		
16 Comma Left to right				
16 , Comma Left-to-right		&= ^= =		
	16	,	Comma	Left-to-right

5.4 Hacks

```
*/
// long long formatting hack :
#ifdef WIN32
    #define LL "%164d"
#else
    #define LL "%lld"
#endif
// Optimizing hack :
#pragma GCC optimize ("03")
#pragma GCC optimize ("whole-program")
// Stack hack :
// C++
#pragma comment(linker, "/STACK:36777216")
// G++
int __size__ = 256 << 20; // 256MB
char *_p_ = (char*)malloc(_size__) + __size__;
__asm__("mov1_%0,_%%esp\n" :: "r"(_p__));</pre>
```