

The Grimoire of Programming

Chapter 1

The Trial of Number Theory

```
/* Number theory template :
   Deals with various aspects of integer, division, modulo, etc.
*/
#include <cmath>
#include <complex>
#include <vector>
namespace number {
    /* Basic operation :
       long long inverse (const long long &x, const long long &mod) :
       returns the inverse of x modulo mod.
       i.e.  $x * \text{inv}(x) \% \text{mod} = 1$ .
       int fpm (int x, int n, int mod) :
       returns  $x^n \% \text{mod}$ . i.e. Fast Power with Modulo.
    */
    long long inverse (const long long &x, const long long &mod) {
        if (x == 1) return 1;
        return (mod - mod / x) * inverse (mod % x, mod) % mod;
    }
    int fpm (int x, int n, int mod) {
        register int ans = 1, mul = x;
        while (n) {
            if (n & 1) ans = int (1ll * ans * mul % mod);
            mul = int (1ll * mul * mul % mod);
            n >>= 1;
        }
        return ans;
    }
    /* Discrete Fourier transform :
       int dft::prepare (int n) : readys the transformation with dimension n.
       void dft::main (complex *a, int n, int f) :
       transforms array a with dimension n to its frequency representation.
       transforms back when f = 1.
    */
    struct dft {
        constexpr static int MAXN = 1E6;
        constexpr static double PI = acos (-1);
        typedef std::complex <double> complex;
        complex e[2][MAXN];
        int prepare (int n) {
            int len = 1;
            for (; len <= 2 * n; len <= 1);
            for (int i = 0; i < len; i++) {
                e[0][i] = complex (cos (2 * PI * i / len), sin (2 * PI * i / len));
                e[1][i] = complex (cos (2 * PI * i / len), -sin (2 * PI * i / len));
            }
            return len;
        }
        void main (complex *a, int n, int f) {
            for (int i = 0, j = 0; i < n; i++) {
                if (i > j) std::swap (a[i], a[j]);
                for (int t = n >> 1; (j ^= t) < t; t >>= 1);
            }
            for (int i = 2; i <= n; i <= 1)
                for (int j = 0; j < n; j += i)
                    for (int k = 0; k < (i >> 1); k++) {
                        complex A = a[j + k];
                        complex B = e[f][n / i * k] * a[j + k + (i >> 1)];
                        a[j + k] = A + B;
                        a[j + k + (i >> 1)] = A - B;
                    }
            if (f == 1) {
                for (int i = 0; i < n; i++)
                    a[i] = complex (a[i].real () / n, a[i].imag ());
            }
        }
    };
    /* Number-theoretic transform :
       void ntt::main (int *a, int n, int f, int mod, int prt) :
       converts polynomial  $f(x) = a[0] * x^0 + a[1] * x^1 + \dots + a[n-1] * x^{(n-1)}$ 
       to a vector (f (prt^0), f (prt^1), f (prt^2), ..., f (prt^(n-1))). (module mod)
       Converts back if f = 1.
       Requires specific mod and corresponding prt to work. (given in MOD and PRT)
       int ntt::crt (int *a, int mod) :
       makes up the results a from module 3 primes to a certain module mod.
    */
    struct ntt {
        constexpr static int MAXN = 1E6;
```

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void main (int *a, int n, int f, int mod, int prt) {
    for (register int i = 0, j = 0; i < n; i++) {
        if (i > j) std::swap (a[i], a[j]);
        for (register int t = n >> 1; (j ^ t) < t; t >>= 1);
    }
    for (register int i = 2; i <= n; i <= 1) {
        static int exp[MAXN];
        exp[0] = 1;
        exp[1] = fpm (prt, (mod - 1) / i, mod);
        if (f == 1) exp[1] = fpm (exp[1], mod - 2, mod);
        for (register int k = 2; k < (i >> 1); k++) {
            exp[k] = int (1LL * exp[k - 1] * exp[1] % mod);
        }
        for (register int j = 0; j < n; j += i) {
            for (register int k = 0; k < (i >> 1); k++) {
                register int &pA = a[j + k], &pB = a[j + k + (i >> 1)];
                register int A = pA, B = int (1LL * pB * exp[k] % mod);
                pA = (A + B) % mod;
                pB = (A - B + mod) % mod;
            }
        }
    }
    if (f == 1) {
        register int rev = fpm (n, mod - 2, mod);
        for (register int i = 0; i < n; i++) {
            a[i] = int (1LL * a[i] * rev % mod);
        }
    }
}

constexpr static int MOD[3] = {1045430273, 1051721729, 1053818881}, PRT[3] = {3, 6, 7};
int crt (int *a, int mod) {
    static int inv[3][3];
    for (int i = 0; i < 3; i++)
        for (int j = 0; j < 3; j++)
            inv[i][j] = (int) inverse (MOD[i], MOD[j]);
    static int x[3];
    for (int i = 0; i < 3; i++) {
        x[i] = a[i];
        for (int j = 0; j < i; j++) {
            int t = (x[i] - x[j] + MOD[i]) % MOD[i];
            if (t < 0) t += MOD[i];
            x[i] = int (1LL * t * inv[j][i] % MOD[i]);
        }
    }
    int sum = 1, ret = x[0] % mod;
    for (int i = 1; i < 3; i++) {
        sum = int (1LL * sum * MOD[i - 1] % mod);
        ret += int (1LL * x[i] * sum % mod);
        if (ret >= mod) ret -= mod;
    }
    return ret;
}

/* Chinese Remainder Theroem :
   bool crt::solve (const std::vector <std::pair<long long, long long> > &input,
                   std::pair<long long, long long> &output) :
       solves for an integer set x = output.first + k * output.second
       that satisfies x % input[i].second = input[i].first.
       Returns whether a solution exists.
*/
struct crt {
    void euclid (const long long &a, const long long &b,
                long long &x, long long &y) {
        if (b == 0) x = 1, y = 0;
        else euclid (b, a % b, y, x), y -= a / b * x;
    }
    long long gcd (const long long &a, const long long &b) {
        if (b == 0) return a;
        return gcd (b, a % b);
    }
    long long fix (const long long &a, const long long &b) {
        return (a % b + b) % b;
    }
    bool solve (const std::vector <std::pair<long long, long long> > &input,
                std::pair<long long, long long> &output) {
        output = std::make_pair (1, 1);
        for (int i = 0; i < (int) input.size (); ++i) {
            long long number, useless;
            euclid (output.second, input[i].second, number, useless);
            long long divisor = gcd (output.second, input[i].second);
            if ((input[i].first - output.first) % divisor) {
                return false;
            }
            number *= (input[i].first - output.first) / divisor;
            number = fix (number, input[i].second);
            output.first += output.second * number;
            output.second *= input[i].second / divisor;
            output.first = fix (output.first, output.second);
        }
        return true;
    }
};

#include <cstdio>
int main () {
    return 0;
}

```

Chapter 2

The Trial of Geometry

```
/* Geometry template :
   Most templates of points, lines and circles on a 2D plane.
*/
#include <cmath>
#include <vector>
#include <algorithm>
namespace geometry {
    /* Basic constant & function :
       EPS : fixes the possible error of data.
           i.e.  $x == y$  iff  $|x - y| < EPS$ .
       PI : the value of PI.
       int sgn (const double &x) : returns the sign of x.
       int cmp (const double &x, const double &y) : returns the sign of  $x - y$ .
       double sqr (const double &x) : returns  $x * x$ .
    */
    const double EPS = 1E-8;
    const double PI = acos (-1);
    int sgn (const double &x) { return x < -EPS ? -1 : x > EPS; }
    int cmp (const double &x, const double &y) { return sgn (x - y); }
    double sqr (const double &x) { return x * x; }
    /* struct point : defines a point and its various utility.
       point (const double &x, const double &y) gives a point at (x, y).
       It also represents a vector on a 2D plane.
       point unit () const : returns the unit vector of (x, y).
       point rot90 () const :
           returns a point rotated 90 degrees counter-clockwise with respect to the origin.
       point _rot90 () const : same as above except clockwise.
       point rotate (const double &t) const : returns a point rotated t radian(s) counter-clockwise.
       Operators are mostly vector operations. i.e. vector +, -, *, / and dot/det product.
    */
    struct point {
        double x, y;
        point (const double &x = 0, const double &y = 0) : x (x), y (y) {}
        double norm () const { return sqrt (x * x + y * y); }
        double norm2 () const { return x * x + y * y; }
        point unit () const {
            double l = norm ();
            return point (x / l, y / l);
        }
        point rot90 () const { return point (-y, x); }
        point _rot90 () const { return point (y, -x); }
        point rotate (const double &t) const {
            double c = cos (t), s = sin (t);
            return point (x * c - y * s, x * s + y * c);
        }
    };
    bool operator == (const point &a, const point &b) {
        return cmp (a.x, b.x) == 0 && cmp (a.y, b.y) == 0;
    }
    bool operator != (const point &a, const point &b) {
        return ! (a == b);
    }
    bool operator < (const point &a, const point &b) {
        if (cmp (a.x, b.x) == 0) return cmp (a.y, b.y) < 0;
        return cmp (a.x, b.x) < 0;
    }
    point operator - (const point &a) { return point (-a.x, -a.y); }
    point operator + (const point &a, const point &b) {
        return point (a.x + b.x, a.y + b.y);
    }
    point operator - (const point &a, const point &b) {
        return point (a.x - b.x, a.y - b.y);
    }
    point operator * (const point &a, const double &b) {
        return point (a.x * b, a.y * b);
    }
    point operator / (const point &a, const double &b) {
        return point (a.x / b, a.y / b);
    }
    double dot (const point &a, const point &b) {
        return a.x * b.x + a.y * b.y;
    }
    double det (const point &a, const point &b) {
        return a.x * b.y - a.y * b.x;
    }
}
```

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double dis (const point &a, const point &b) {
    return sqrt (sqr (a.x - b.x) + sqr (a.y - b.y));
}
/* struct line : defines a line (segment) based on two points, s and t.
   line (const point &s, const point &t) gives a basic line from s to t.
   double length () const : returns the length of the segment.
*/
struct line {
    point s, t;
    line (const point &s = point (), const point &t = point ()) : s (s), t (t) {}
    double length () const { return dis (s, t); }
};
/* Point & line interaction :
   bool point_on_line (const point &a, const line &b) : checks if a is on b.
   bool intersect_judgement (const line &a, const line &b) : checks if segment a and b intersect.
   point line_intersect (const line &a, const line &b) : returns the intersection of a and b.
       Fails on colinear or parallel situations.
   double point_to_line (const point &a, const line &b) : returns the distance from a to b.
   double point_to_segment (const point &a, const line &b) : returns the distance from a to b.
       i.e. the minimized length from a to segment b.
   bool in_polygon (const point &p, const std::vector <point> &po) :
       checks if a is in a polygon with vetices po (clockwise or counter-clockwise order).
   double polygon_area (const std::vector <point> &a) :
       returns the signed area of polygon a (positive for counter-clockwise order, and vise-versa).
   point project_to_line (const point &a, const line &b) :
       returns the projection of a on b,
*/
bool point_on_line (const point &a, const line &b) {
    return sgn (det (a - b.s, b.t - b.s)) == 0 && sgn (dot (b.s - a, b.t - a)) <= 0;
}
bool two_side (const point &a, const point &b, const line &c) {
    return sgn (det (a - c.s, c.t - c.s)) * sgn (det (b - c.s, c.t - c.s)) < 0;
}
bool intersect_judgement (const line &a, const line &b) {
    if (point_on_line (b.s, a) || point_on_line (b.t, a)) return true;
    if (point_on_line (a.s, b) || point_on_line (a.t, b)) return true;
    return two_side (a.s, a.t, b) && two_side (b.s, b.t, a);
}
point line_intersect (const line &a, const line &b) {
    double s1 = det (a.t - a.s, b.s - a.s);
    double s2 = det (a.t - a.s, b.t - a.s);
    return (b.s * s2 - b.t * s1) / (s2 - s1);
}
double point_to_line (const point &a, const line &b) {
    return fabs (det (b.t - b.s, a - b.s)) / dis (b.s, b.t);
}
double point_to_segment (const point &a, const line &b) {
    if (sgn (dot (b.s - a, b.t - b.s)) * dot (b.t - a, b.t - b.s)) <= 0)
        return fabs (det (b.t - b.s, a - b.s)) / dis (b.s, b.t);
    return std::min (dis (a, b.s), dis (a, b.t));
}
bool in_polygon (const point &p, const std::vector <point> &po) {
    int n = (int) po.size ();
    int counter = 0;
    for (int i = 0; i < n; ++i) {
        point a = po[i], b = po[(i + 1) % n];
        /*
           The following statement checks if p is on the border of the polygon.
           The boolean returned may be changed if necessary.
           i.e. the algorithm may check if p is strictly in the polygon.
        */
        if (point_on_line (p, line (a, b))) return true;
        int x = sgn (det (p - a, b - a)), y = sgn (a.y - p.y), z = sgn (b.y - p.y);
        if (x > 0 && y <= 0 && z > 0) counter++;
        if (x < 0 && z <= 0 && y > 0) counter--;
    }
    return counter != 0;
}
double polygon_area (const std::vector <point> &a) {
    double ans = 0.0;
    for (int i = 0; i < (int) a.size (); ++i)
        ans += det (a[i], a[(i + 1) % a.size ()]) / 2.0;
    return ans;
}
point project_to_line (const point &a, const line &b) {
    return b.s + (b.t - b.s) * (dot (a - b.s, b.t - b.s) / (b.t - b.s).norm2 ());
}
/* Centers of a triangle :
   returns various centers of a triangle with vertices (a, b, c).
*/
point incenter (const point &a, const point &b, const point &c) {
    double p = dis (a, b) + dis (b, c) + dis (c, a);
    return (a * dis (b, c) + b * dis (c, a) + c * dis (a, b)) / p;
}
point circumcenter (const point &a, const point &b, const point &c) {
    point p = b - a, q = c - a, s (dot (p, p) / 2, dot (q, q) / 2);
    double d = det (p, q);
    return a + point (det (s, point (p.y, q.y)), det (point (p.x, q.x), s)) / d;
}
point orthocenter (const point &a, const point &b, const point &c) {
    return a + b + c - circumcenter (a, b, c) * 2.0;
}
/* Fermat point :
   point fermat_point (const point &a, const point &b, const point &c) :
       returns a point p that minimizes |pa| + |pb| + |pc|.
*/
point fermat_point (const point &a, const point &b, const point &c) {
    if (a == b) return a;
    if (b == c) return b;
}

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    if (c == a) return c;
    double ab = dis (a, b), bc = dis (b, c), ca = dis (c, a);
    double cosa = dot (b - a, c - a) / ab / ca;
    double cosb = dot (a - b, c - b) / ab / bc;
    double cosc = dot (b - c, a - c) / ca / bc;
    double sq3 = PI / 3.0;
    point mid;
    if (sgn (det (b - a, c - a)) < 0) swap (b, c);
    if (sgn (cosa + 0.5) < 0) mid = a;
    else if (sgn (cosb + 0.5) < 0) mid = b;
    else if (sgn (cosc + 0.5) < 0) mid = c;
    else mid = line_intersect (line (a, c + (b - c).rotate (sq3)), line (c, b + (a - b).rotate (sq3)));
    return mid;
}
/* struct circle defines a circle.
   circle (point c, double r) gives a circle with center c and radius r.
*/
struct circle {
    point c;
    double r;
    circle (point c = point (), double r = 0) : c (c), r (r) {}
};
bool operator == (const circle &a, const circle &b) {
    return a.c == b.c && cmp (a.r, b.r) == 0;
}
bool operator != (const circle &a, const circle &b) {
    return ! (a == b);
}
/* Circle interaction :
   bool in_circle (const point &a, const circle &b) : checks if a is in or on b.
   circle make_circle (const point &a, const point &b) :
       generates a circle with diameter ab.
   circle make_circle (const point &a, const point &b, const point &c) :
       generates a circle passing a, b and c.
   std::pair<point, point> line_circle_intersect (const line &a, const circle &b) :
       returns the intersections of a and b.
       Fails if a and b do not intersect.
   std::pair<point, point> circle_circle_intersect (const circle &a, const circle &b) :
       returns the intersections of a and b.
       Fails if a and b do not intersect.
   std::pair<line, line> tangent (const point &a, const circle &b) :
       returns the tangent lines of b passing through a.
       Fails if a is in b.
*/
bool in_circle (const point &a, const circle &b) {
    return cmp (dis (a, b.c), b.r) <= 0;
}
circle make_circle (const point &a, const point &b) {
    return circle ((a + b) / 2, dis (a, b) / 2);
}
circle make_circle (const point &a, const point &b, const point &c) {
    point p = circumcenter (a, b, c);
    return circle (p, dis (p, a));
}
std::pair<point, point> line_circle_intersect (const line &a, const circle &b) {
    double x = sqrt (sqr (b.r) - sqr (point_to_line (b.c, a)));
    return std::make_pair (project_to_line (b.c, a) + (a.s - a.t).unit () * x,
        project_to_line (b.c, a) - (a.s - a.t).unit () * x);
}
point __circle_intersect (const circle &a, const circle &b) {
    point r = (b.c - a.c).unit ();
    double d = dis (a.c, b.c);
    double x = .5 * ((sqr (a.r) - sqr (b.r)) / d + d);
    double h = sqrt (sqr (a.r) - sqr (x));
    return a.c + r * x + r.rot90 () * h;
}
std::pair<point, point> circle_intersect (const circle &a, const circle &b) {
    return std::make_pair (__circle_intersect (a, b), __circle_intersect (b, a));
}
std::pair<line, line> tangent (const point &a, const circle &b) {
    circle p = make_circle (a, b.c);
    return circle_intersect (p, b);
}
/* Convex hull :
   std::vector<point> convex_hull (std::vector<point> a) :
       returns the convex hull of point set a (counter-clockwise).
*/
bool turn_left (const point &a, const point &b, const point &c) {
    return sgn (det (b - a, c - a)) >= 0;
}
bool turn_right (const point &a, const point &b, const point &c) {
    return sgn (det (b - a, c - a)) <= 0;
}
std::vector<point> convex_hull (std::vector<point> a) {
    int n = (int) a.size (), cnt = 0;
    std::sort (a.begin (), a.end ());
    std::vector<point> ret;
    for (int i = 0; i < n; ++i) {
        while (cnt > 1 && turn_left (ret[cnt - 2], a[i], ret[cnt - 1])) {
            --cnt;
            ret.pop_back ();
        }
        ret.push_back (a[i]);
        ++cnt;
    }
    int fixed = cnt;
    for (int i = n - 1; i >= 0; --i) {
        while (cnt > fixed && turn_right (ret[cnt - 2], a[i], ret[cnt - 1])) {
            --cnt;
            ret.pop_back ();
        }
    }
}

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        ret.push_back (a[i]);
        ++cnt;
    }
    ret.pop_back ();
    return ret;
}
/* Minimum circle of a point set :
   circle minimum_circle (std::vector<point> p) : returns the minimum circle of point set p.
*/
circle minimum_circle (std::vector<point> p) {
    circle ret;
    std::random_shuffle (p.begin (), p.end ());
    for (int i = 0; i < (int) p.size (); ++i)
        if (!in_circle (p[i], ret)) {
            ret = circle (p[i], 0);
            for (int j = 0; j < i; ++j)
                if (!in_circle (p[j], ret)) {
                    ret = make_circle (p[j], p[i]);
                    for (int k = 0; k < j; ++k)
                        if (!in_circle (p[k], ret)) ret = make_circle (p[i], p[j], p[k]);
                }
        }
    return ret;
}
/* Online half plane intersection (complexity = O(c.size ())) :
   std::vector<point> cut (const std::vector<point> &c, line p) :
   returns the convex polygon cutting convex polygon c with half plane p.
   (left hand with respect to vector p)
   If such polygon does not exist, returns an empty set.
   e.g.
       static const double BOUND = 1e5;
       convex.clear ();
       convex.push_back (point (-BOUND, -BOUND));
       convex.push_back (point (BOUND, -BOUND));
       convex.push_back (point (BOUND, BOUND));
       convex.push_back (point (-BOUND, BOUND));
       convex = cut (convex, line(point, point));
       if (convex.empty ()) { ... }
*/
std::vector<point> cut (const std::vector<point> &c, line p) {
    std::vector<point> ret;
    if (c.empty ()) return ret;
    for (int i = 0; i < (int) c.size (); ++i) {
        int j = (i + 1) % (int) c.size ();
        if (!turn_right (p.s, p.t, c[i])) ret.push_back (c[i]);
        if (two_side (c[i], c[j], p))
            ret.push_back (line_intersect (p, line (c[i], c[j])));
    }
    return ret;
}
/* Offline half plane intersection (complexity = O(nlogn), n = h.size ()) :
   std::vector<point> half_plane_intersect (std::vector<line> h) :
   returns the intersection of half planes h.
   (left hand with respect to the vector)
   If such polygon does not exist, returns an empty set.
*/
bool turn_left (const line &l, const point &p) {
    return turn_left (l.s, l.t, p);
}
std::vector<point> half_plane_intersect (std::vector<line> h) {
    typedef std::pair<double, line> polar;
    std::vector<polar> g;
    g.resize (h.size ());
    for (int i = 0; i < (int) h.size (); ++i) {
        point v = h[i].t - h[i].s;
        g[i] = std::make_pair (atan2 (v.y, v.x), h[i]);
    }
    sort (g.begin (), g.end (), [] (const polar &a, const polar &b) {
        if (cmp (a.first, b.first) == 0)
            return sgn (det (a.second.t - a.second.s, b.second.t - a.second.s)) < 0;
        else
            return cmp (a.first, b.first) < 0;
    });
    h.resize (std::unique (g.begin (), g.end (), [] (const polar &a, const polar &b) {
        return cmp (a.first, b.first) == 0;
    }) - g.begin ());
    for (int i = 0; i < (int) h.size (); ++i)
        h[i] = g[i].second;
    int fore = 0, rear = -1;
    std::vector<line> ret;
    for (int i = 0; i < (int) h.size (); ++i) {
        while (fore < rear && !turn_left (h[i], line_intersect (ret[rear - 1], ret[rear]))) {
            --rear;
            ret.pop_back ();
        }
        while (fore < rear && !turn_left (h[i], line_intersect (ret[fore], ret[fore + 1])))
            ++fore;
        ret.push_back (h[i]);
    }
    while (rear - fore > 1 && !turn_left (ret[fore], line_intersect (ret[rear - 1], ret[rear]))) {
        --rear;
        ret.pop_back ();
    }
    while (rear - fore > 1 && !turn_left (ret[rear], line_intersect (ret[fore], ret[fore + 1])))
        ++fore;
    if (rear - fore < 2) return std::vector<point> ();
    std::vector<point> ans;
    ans.resize (ret.size ());
    for (int i = 0; i < (int) ret.size (); ++i)
        ans[i] = line_intersect (ret[i], ret[ (i + 1) % ret.size ()]);
    return ans;
}
/* Intersection of a polygon and a circle :

```

```

double polygon_circle_intersect::solve (const std::vector<point> &p, const circle &c) :
    returns the area of intersection of polygon p (vertices in either order) and c.
*/
struct polygon_circle_intersect {
    // The area of the sector with center (0, 0), radius r and segment ab.
    double sector_area (const point &a, const point &b, const double &r) {
        double c = (2.0 * r * r - (a - b).norm2 ()) / (2.0 * r * r);
        double al = acos (c);
        return r * r * al / 2.0;
    }
    // The area of triangle (a, b, (0, 0)) intersecting circle (point (), r).
    double area (const point &a, const point &b, const double &r) {
        double dA = dot (a, a), dB = dot (b, b), dC = point_to_segment (point (), line (a, b)), ans = 0.0;
        if (sgn (dA - r * r) <= 0 && sgn (dB - r * r) <= 0) return det (a, b) / 2.0;
        point tA = a.unit () * r;
        point tB = b.unit () * r;
        if (sgn (dC - r) > 0) return sector_area (tA, tB, r);
        std::pair<point, point> ret = line_circle_intersect (line (a, b), circle (point (), r));
        if (sgn (dA - r * r) > 0 && sgn (dB - r * r) > 0) {
            ans += sector_area (tA, ret.first, r);
            ans += det (ret.first, ret.second) / 2.0;
            ans += sector_area (ret.second, tB, r);
            return ans;
        }
        if (sgn (dA - r * r) > 0)
            return det (ret.first, b) / 2.0 + sector_area (tA, ret.first, r);
        else
            return det (a, ret.second) / 2.0 + sector_area (ret.second, tB, r);
    }
    // Main process.
    double solve (const std::vector<point> &p, const circle &c) {
        double ret = 0.0;
        for (int i = 0; i < (int) p.size (); ++i) {
            int s = sgn (det (p[i] - c.c, p[ (i + 1) % p.size ()] - c.c));
            if (s > 0)
                ret += area (p[i] - c.c, p[ (i + 1) % p.size ()] - c.c, c.r);
            else
                ret -= area (p[ (i + 1) % p.size ()] - c.c, p[i] - c.c, c.r);
        }
        return fabs (ret);
    }
};
/* Union of circles :
   std::vector<double> union_circle::solve (const std::vector<circle> &c) :
   returns the union of circle set c.
   The i-th element is the area covered with at least i circles.
*/
struct union_circle {
    struct cp {
        double x, y, angle;
        int d;
        double r;
        cp (const double &x = 0, const double &y = 0, const double &angle = 0,
            int d = 0, const double &r = 0) : x (x), y (y), angle (angle), d (d), r (r) {}
    };
    double dis (const cp &a, const cp &b) {
        return sqrt (sqr (a.x - b.x) + sqr (a.y - b.y));
    }
    double cross (const cp &p0, const cp &p1, const cp &p2) {
        return (p1.x - p0.x) * (p2.y - p0.y) - (p1.y - p0.y) * (p2.x - p0.x);
    }
    int cir_cross (cp p1, double r1, cp p2, double r2, cp &cp1, cp &cp2) {
        double mx = p2.x - p1.x, sx = p2.x + p1.x, mx2 = mx * mx;
        double my = p2.y - p1.y, sy = p2.y + p1.y, my2 = my * my;
        double sq = mx2 + my2, d = - (sq - sqr (r1 - r2)) * (sq - sqr (r1 + r2));
        if (sgn (d) < 0) return 0;
        if (sgn (d) <= 0) d = 0;
        else d = sqrt (d);
        double x = mx * ((r1 + r2) * (r1 - r2) + mx * sx) + sx * my2;
        double y = my * ((r1 + r2) * (r1 - r2) + my * sy) + sy * mx2;
        double dx = mx * d, dy = my * d;
        sq *= 2;
        cp1.x = (x - dy) / sq;
        cp1.y = (y + dx) / sq;
        cp2.x = (x + dy) / sq;
        cp2.y = (y - dx) / sq;
        if (sgn (d) > 0) return 2;
        else return 1;
    }
    bool circmp (const cp &u, const cp &v) {
        return sgn (u.r - v.r) < 0;
    }
    bool cmp (const cp &u, const cp &v) {
        if (sgn (u.angle - v.angle)) return u.angle < v.angle;
        return u.d > v.d;
    }
    double calc (cp cir, cp cp1, cp cp2) {
        double ans = (cp2.angle - cp1.angle) * sqr (cir.r)
            - cross (cir, cp1, cp2) + cross (cp (0, 0), cp1, cp2);
        return ans / 2;
    }
    std::vector<double> solve (const std::vector<circle> &c) {
        int n = c.size ();
        std::vector<cp> cir, tp;
        std::vector<double> area;
        cir.resize (n);
        tp.resize (2 * n);
        area.resize (n + 1);
        for (int i = 0; i < n; i++)
            cir[i] = cp (c[i].c.x, c[i].c.y, 0, 1, c[i].r);
        cp cp1, cp2;

```



```

std::sort (cir.begin (), cir.end (), circmp);
for (int i = 0; i < n; ++i)
    for (int j = i + 1; j < n; ++j)
        if (sgn (dis (cir[i], cir[j]) + cir[i].r - cir[j].r) <= 0)
            cir[i].d++;
for (int i = 0; i < n; ++i) {
    int tn = 0, cnt = 0;
    for (int j = 0; j < n; ++j) {
        if (i == j) continue;
        if (cir_cross (cir[i], cir[i].r, cir[j], cir[j].r, cp2, cp1) < 2) continue;
        cp1.angle = atan2 (cp1.y - cir[i].y, cp1.x - cir[i].x);
        cp2.angle = atan2 (cp2.y - cir[i].y, cp2.x - cir[i].x);
        cp1.d = 1;
        tp[tn++] = cp1;
        cp2.d = -1;
        tp[tn++] = cp2;
        if (sgn (cp1.angle - cp2.angle) > 0) cnt++;
    }
    tp[tn++] = cp (cir[i].x - cir[i].r, cir[i].y, PI, -cnt);
    tp[tn++] = cp (cir[i].x - cir[i].r, cir[i].y, -PI, cnt);
    std::sort (tp.begin (), tp.begin () + tn, cmp);
    int p, s = cir[i].d + tp[0].d;
    for (int j = 1; j < tn; ++j) {
        p = s;
        s += tp[j].d;
        area[p] += calc (cir[i], tp[j - 1], tp[j]);
    }
}
return area;
};
}
};
}
#include <cstdio>
using namespace geometry;
int main() {
    return 0;
}

```

Chapter 3

The Trial of Graph

```
/* Graph template :
   Most algorithms on a graph.
*/
#include <algorithm>
#include <array>
#include <vector>
#include <queue>
namespace graph {
    /* Edge list:
       Various kinds of edge list.
    */
    const int MAXN = 1E5, MAXM = 1E5;
    struct edge_list {
        int size;
        int begin[MAXN], dest[MAXM], next[MAXM];
        void clear (int n) {
            size = 0;
            for (int i = 0; i < n; i++)
                begin[i] = -1;
        }
        edge_list (int n = MAXN) {
            clear (n);
        }
        void add_edge (int u, int v) {
            dest[size] = v;
            next[size] = begin[u];
            begin[u] = size++;
        }
    };
    struct flow_edge_list {
    };
    /* Hopcroft-Carp algorithm :
       maximum matching with complexity  $O(m * n^{0.5})$ .
       struct hopcroft_carp :
       Initialize : pass n, m as the size of both vertex sets, e as the reference of the edge_list.
       Usage : solve () for maximum matching. The matching is in matchx and matchy.
    */
    struct hopcroft_carp {
        static const int MAXN = 1E5;
        int n, m;
        edge_list &e;
        int matchx[MAXN], matchy[MAXN], level[MAXN];
        bool dfs (int x) {
            for (int i = e.begin[x]; i != -1; i = e.next[i]) {
                int y = e.dest[i];
                int w = matchy[y];
                if (w == -1 || (level[x] + 1 == level[w] && dfs (w))) {
                    matchx[x] = y;
                    matchy[y] = x;
                    return true;
                }
            }
            level[x] = -1;
            return false;
        }
        int solve () {
            std::fill (matchx, matchx + n, -1);
            std::fill (matchy, matchy + m, -1);
            for (int answer = 0; ; ) {
                std::vector <int> queue;
                for (int i = 0; i < n; ++i) {
                    if (matchx[i] == -1) {
                        level[i] = 0;
                        queue.push_back (i);
                    } else {
                        level[i] = -1;
                    }
                }
                for (int head = 0; head < (int) queue.size(); ++head) {
                    int x = queue[head];
                    for (int i = e.begin[x]; i != -1; i = e.next[i]) {
                        int y = e.dest[i];
                        int w = matchy[y];
                        if (w != -1 && level[w] < 0) {
                            level[w] = level[x] + 1;
                            queue.push_back (w);
                        }
                    }
                }
                if (answer == 0) {
                    for (int i = 0; i < n; ++i) {
                        if (matchx[i] == -1) {
                            if (!dfs (i))
                                return answer;
                        }
                    }
                }
                answer++;
            }
        }
    };
}
```

```

    }
    }
    int delta = 0;
    for (int i = 0; i < n; ++i)
        if (matchx[i] == -1 && dfs (i)) delta++;
    if (delta == 0) return answer;
    else answer += delta;
}
}
};

/* Kuhn Munkres algorithm :
   weighted minimum matching algorithm. Complexity O (N^3).
   struct kuhn_munkres :
       Initialize : pass nx, ny as the size of both sets, w as the weight matrix.
       Usage : solve () for the minimum matching. The matching is in link.
*/
struct kuhn_munkres {
    static const int MAXN = 500;
    static const int INF = 1E9;
    int nx, ny;
    int w[MAXN][MAXN];
    int lx[MAXN], ly[MAXN], visx[MAXN], visy[MAXN], slack[MAXN], link[MAXN];
    int dfs (int x) {
        visx[x] = 1;
        for (int y = 0; y < ny; y++) {
            if (visy[y]) continue;
            int t = lx[x] + ly[y] - w[x][y];
            if (t == 0) {
                visy[y] = 1;
                if (link[y] == -1 || dfs (link[y])) {
                    link[y] = x;
                    return 1;
                }
            } else slack[y] = std::min (slack[y], t);
        }
        return 0;
    }
    int solve () {
        int i, j;
        std::fill (link, link + ny, -1);
        std::fill (ly, ly + ny, 0);
        for (i = 0; i < nx; i++)
            for (j = 0; j < ny; j++)
                lx[i] = std::max (lx[i], w[i][j]);
        for (int x = 0; x < nx; x++) {
            for (i = 0; i < ny; i++) slack[i] = INF;
            while (true) {
                std::fill (visx, visx + nx, 0);
                std::fill (visy, visy + ny, 0);
                if (dfs (x)) break;
                int d = INF;
                for (i = 0; i < ny; i++)
                    if (!visy[i] && d > slack[i]) d = slack[i];
                for (i = 0; i < nx; i++)
                    if (visx[i]) lx[i] -= d;
                for (i = 0; i < ny; i++)
                    if (visy[i]) ly[i] += d;
                    else slack[i] -= d;
            }
        }
        int res = 0;
        for (i = 0; i < ny; i++)
            if (link[i] > -1) res += w[link[i]][i];
        return res;
    }
};

/* Weighted matching algorithm :
   maximum match for graphs. Strange hack.
   struct weighted_match :
       Usage : Set k to the size of vertices, w to the weight matrix.
       Note that k has to be even for the algorithm to work.
*/
struct weighted_match {
    static const int MAXN = 500;
    int k;
    long long w[MAXN][MAXN];
    int match[MAXN], path[MAXN], p[MAXN], len;
    long long d[MAXN];
    bool v[MAXN];
    bool dfs (int i) {
        path[len++] = i;
        if (v[i]) return true;
        v[i] = true;
        for (int j = 0; j < k; ++j) {
            if (i != j && match[i] != j && !v[j]) {
                int kok = match[j];
                if (d[kok] < d[i] + w[i][j] - w[j][kok]) {
                    d[kok] = d[i] + w[i][j] - w[j][kok];
                    if (dfs (kok)) return true;
                }
            }
        }
        --len;
        v[i] = false;
        return false;
    }
    long long solve () {
        if (k & 1) ++k;
        for (int i = 0; i < k; ++i) p[i] = i, match[i] = i ^ 1;
        int cnt = 0;

```

```

for (;;) {
    len = 0;
    bool flag = false;
    std::fill (d, d + k, 0);
    std::fill (v, v + k, 0);
    for (int i = 0; i < k; ++i) {
        if (dfs (p[i])) {
            flag = true;
            int t = match[path[len - 1]], j = len - 2;
            while (path[j] != path[len - 1]) {
                match[t] = path[j];
                std::swap (t, match[path[j]]);
                --j;
            }
            match[t] = path[j];
            match[path[j]] = t;
            break;
        }
    }
    if (!flag) {
        if (++cnt >= 1) break;
        std::random_shuffle (p, p + k);
    }
}
long long ans = 0;
for (int i = 0; i < k; ++i)
    ans += w[i][match[i]];
return ans / 2;
}
};

/* Weighted blossom algorithm (vfleaking ver.) :
maximum match for graphs. Complexity O (n^3).
Note that the base index is 1.
struct weighted_blossom :
Usage :
    Set n to the size of the vertices.
    Run init ().
    Set g[][].w to the weight of the edge.
    Run solve ().
    The first result is the answer, the second one is the number of matching pairs.
    Obtain the matching with match[].
*/
struct weighted_blossom {
    const static int INF = INT_MAX;
    const static int MAXN = 500;
    struct edge {
        int u, v, w;
        edge (int u = 0, int v = 0, int w = 0) : u (u), v (v), w (w) {}
    };
    int n, n_x;
    edge g[MAXN * 2 + 1][MAXN * 2 + 1];
    int lab[MAXN * 2 + 1];
    int match[MAXN * 2 + 1], slack[MAXN * 2 + 1], st[MAXN * 2 + 1], pa[MAXN * 2 + 1];
    int flower_from[MAXN * 2 + 1][MAXN + 1], S[MAXN * 2 + 1], vis[MAXN * 2 + 1];
    std::vector<int> flower[MAXN * 2 + 1];
    std::queue<int> q;
    int e_delta (const edge &e) {
        return lab[e.u] + lab[e.v] - g[e.u][e.v].w * 2;
    }
    void update_slack (int u, int x) {
        if (!slack[x] || e_delta (g[u][x]) < e_delta (g[slack[x]][x])) slack[x] = u;
    }
    void set_slack (int x) {
        slack[x] = 0;
        for (int u = 1; u <= n; ++u)
            if (g[u][x].w > 0 && st[u] != x && S[st[u]] == 0) update_slack (u, x);
    }
    void q_push (int x) {
        if (x <= n) q.push (x);
        else for (size_t i = 0; i < flower[x].size(); ++i) q_push (flower[x][i]);
    }
    void set_st (int x, int b) {
        st[x] = b;
        if (x > n) for (size_t i = 0; i < flower[x].size(); ++i)
            set_st (flower[x][i], b);
    }
    int get_pr (int b, int xr) {
        int pr = find (flower[b].begin(), flower[b].end(), xr) - flower[b].begin();
        if (pr % 2 == 1) {
            reverse (flower[b].begin() + 1, flower[b].end());
            return (int)flower[b].size() - pr;
        } else return pr;
    }
    void set_match (int u, int v) {
        match[u] = g[u][v].v;
        if (u > n) {
            edge e = g[u][v];
            int xr = flower_from[u][e.u], pr = get_pr (u, xr);
            for (int i = 0; i < pr; ++i) set_match (flower[u][i], flower[u][i ^ 1]);
            set_match (xr, v);
            rotate (flower[u].begin(), flower[u].begin() + pr, flower[u].end());
        }
    }
    void augment (int u, int v) {
        for (;;) {
            int xnv = st[match[u]];
            set_match (u, v);
            if (!xnv) return;
            set_match (xnv, st[pa[xnv]]);
            u = st[pa[xnv]], v = xnv;
        }
    }
    int get_lca (int u, int v) {
        static int t = 0;

```

```

    for (++t; u || v; std::swap (u, v)) {
        if (u == 0) continue;
        if (vis[u] == t) return u;
        vis[u] = t;
        u = st[match[u]];
        if (u) u = st[pa[u]];
    }
    return 0;
}

void add_blossom (int u, int lca, int v) {
    int b = n + 1;
    while (b <= n_x && st[b]++) ++b;
    if (b > n_x) ++n_x;
    lab[b] = 0, S[b] = 0;
    match[b] = match[lca];
    flower[b].clear();
    flower[b].push_back (lca);
    for (int x = u, y; x != lca; x = st[pa[y]])
        flower[b].push_back (x), flower[b].push_back (y = st[match[x]]), q_push (y);
    reverse (flower[b].begin() + 1, flower[b].end());
    for (int x = v, y; x != lca; x = st[pa[y]])
        flower[b].push_back (x), flower[b].push_back (y = st[match[x]]), q_push (y);
    set_st (b, b);
    for (int x = 1; x <= n_x; ++x) g[b][x].w = g[x][b].w = 0;
    for (int x = 1; x <= n; ++x) flower_from[b][x] = 0;
    for (size_t i = 0; i < flower[b].size(); ++i) {
        int xs = flower[b][i];
        for (int x = 1; x <= n_x; ++x)
            if (g[b][x].w == 0 || e_delta (g[xs][x]) < e_delta (g[b][x]))
                g[b][x] = g[xs][x], g[x][b] = g[x][xs];
        for (int x = 1; x <= n; ++x)
            if (flower_from[xs][x]) flower_from[b][x] = xs;
    }
    set_slack (b);
}

void expand_blossom (int b) {
    for (size_t i = 0; i < flower[b].size(); ++i)
        set_st (flower[b][i], flower[b][i]);
    int xr = flower_from[b][g[b][pa[b]].u], pr = get_pr (b, xr);
    for (int i = 0; i < pr; i += 2) {
        int xs = flower[b][i], xns = flower[b][i + 1];
        pa[xs] = g[xns][xs].u;
        S[xs] = 1, S[xns] = 0;
        slack[xs] = 0, set_slack (xns);
        q_push (xns);
    }
    S[xr] = 1, pa[xr] = pa[b];
    for (size_t i = pr + 1; i < flower[b].size(); ++i) {
        int xs = flower[b][i];
        S[xs] = -1, set_slack (xs);
    }
    st[b] = 0;
}

bool on_found_edge (const edge &e) {
    int u = st[e.u], v = st[e.v];
    if (S[v] == -1) {
        pa[v] = e.u, S[v] = 1;
        int nu = st[match[v]];
        slack[v] = slack[nu] = 0;
        S[nu] = 0, q_push (nu);
    } else if (S[v] == 0) {
        int lca = get_lca (u, v);
        if (!lca) return augment (u, v), augment (v, u), true;
        else add_blossom (u, lca, v);
    }
    return false;
}

bool matching() {
    std::fill (S + 1, S + 1 + n_x, -1);
    std::fill (slack + 1, slack + 1 + n_x, -1);
    q = std::queue<int>();
    for (int x = 1; x <= n_x; ++x)
        if (st[x] == x && !match[x]) pa[x] = 0, S[x] = 0, q_push (x);
    if (q.empty()) return false;
    for (;;) {
        while (q.size()) {
            int u = q.front();
            q.pop();
            if (S[st[u]] == 1) continue;
            for (int v = 1; v <= n; ++v)
                if (g[u][v].w > 0 && st[u] != st[v]) {
                    if (e_delta (g[u][v]) == 0) {
                        if (on_found_edge (g[u][v])) return true;
                    } else update_slack (u, st[v]);
                }
        }
        int d = INF;
        for (int b = n + 1; b <= n_x; ++b)
            if (st[b] == b && S[b] == 1) d = std::min (d, lab[b] / 2);
        for (int x = 1; x <= n_x; ++x)
            if (st[x] == x && slack[x]) {
                if (S[x] == -1) d = std::min (d, e_delta (g[slack[x]][x]));
                else if (S[x] == 0) d = std::min (d, e_delta (g[slack[x]][x]) / 2);
            }
        for (int u = 1; u <= n; ++u) {
            if (S[st[u]] == 0) {
                if (lab[u] <= d) return 0;
                lab[u] -= d;
            } else if (S[st[u]] == 1) lab[u] += d;
        }
        for (int b = n + 1; b <= n_x; ++b)
            if (st[b] == b) {
                if (S[st[b]] == 0) lab[b] += d * 2;
                else if (S[st[b]] == 1) lab[b] -= d * 2;
            }
    }
}

```

```

        q = std::queue<int>();
        for (int x = 1; x <= n_x; ++x)
            if (st[x] == x && slack[x] && st[slack[x]] != x && e_delta (g[slack[x]][x]) == 0)
                if (on_found_edge (g[slack[x]][x])) return true;
        for (int b = n + 1; b <= n_x; ++b)
            if (st[b] == b && S[b] == 1 && lab[b] == 0) expand_blossom (b);
    }
    return false;
}

std::pair<long long, int> solve() {
    std::fill (match + 1, match + n + 1, 0);
    n_x = n;
    int n_matches = 0;
    long long tot_weight = 0;
    for (int u = 0; u <= n; ++u) st[u] = u, flower[u].clear();
    int w_max = 0;
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v) {
            flower_from[u][v] = (u == v ? u : 0);
            w_max = std::max (w_max, g[u][v].w);
        }
    for (int u = 1; u <= n; ++u) lab[u] = w_max;
    while (matching()) ++n_matches;
    for (int u = 1; u <= n; ++u)
        if (match[u] && match[u] < u)
            tot_weight += g[u][match[u]].w;
    return std::make_pair (tot_weight, n_matches);
}

void init () {
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v)
            g[u][v] = edge (u, v, 0);
}

};

}

#include <cstdio>
using namespace graph;
int main () {
    return 0;
}

```

Chapter 4

The Trial of String

```
//string.cpp
#include <string>
#include <vector>
#include <map>
namespace string {
    struct suffix_automaton {
        std::vector <std::map <char, int> > edges; // edges[i] : the labeled edges from node i
        std::vector <int> link; // link[i] : the parent of i
        std::vector <int> length; // length[i] : the length of the longest string in the ith class
        std::vector <int> terminals; // terminals : the terminal state of the automaton
        int last; // the index of the equivalence class of the whole string
        suffix_automaton (std::string s) {
            edges.push_back (std::map <char,int> ());
            link.push_back (-1);
            length.push_back (0);
            last = 0;
            for (int i = 0; i < (int) s.size(); ++i) {
                edges.push_back (std::map <char,int> ());
                length.push_back (i + 1);
                link.push_back (0);
                int r = edges.size() - 1;
                int p = last;
                while (p >= 0 && edges[p].find (s[i]) == edges[p].end ()) {
                    edges[p][s[i]] = r;
                    p = link[p];
                }
                if (p != -1) {
                    int q = edges[p][s[i]];
                    if (length[p] + 1 == length[q]) {
                        link[r] = q;
                    } else {
                        edges.push_back (edges[q]);
                        length.push_back (length[p] + 1);
                        link.push_back (link[q]);
                        int qq = edges.size() - 1;
                        link[q] = qq;
                        link[r] = qq;
                        while (p >= 0 && edges[p][s[i]] == q) {
                            edges[p][s[i]] = qq;
                            p = link[p];
                        }
                    }
                }
                last = r;
            }
            int p = last;
            while (p > 0) {
                terminals.push_back (p);
                p = link[p];
            }
        }
    };
};
#include <cstdio>
int main () {
    return 0;
}
```

Chapter 5

Reference

5.1 vimrc

```
set ruler
set number
set tabstop=4
set softtabstop=4
set shiftwidth=4
set smartindent
set showmatch
set hlsearch
set incsearch
set autoread
set backspace=2
set mouse=a
syntax on
nmap <C-A> ggVG
vmap <C-C> "+y
nmap <C-P> "+p
autocmd FileType cpp set cindent
autocmd FileType cpp map <F3> :vsplit %<.in <CR>
autocmd FileType cpp map <F5> :!time ./%<.exe <CR>
autocmd FileType cpp map <F7> :!gdb ./%<.exe <CR>
autocmd FileType cpp map <F8> :!time ./%<.exe < %<.in <CR>
autocmd FileType cpp map <F9> :!g++ % -o %< -g -std=c++11 -Wall -Wextra -Wconversion && size %<.exe <CR>
autocmd FileType cpp map <F10> :!astyle -A2 -t -C -S -N -O -xd -p -H % <CR>
autocmd FileType java map <F3> :vsplit %<.in <CR>
autocmd FileType java map <F5> :!time java %< <CR>
autocmd FileType java map <F8> :!time java %< < %<.in <CR>
autocmd FileType java map <F9> :!javac % <CR>
autocmd FileType java map <F10> :!astyle -A2 -t -C -S -N -O -xd -p -H % <CR>
autocmd FileType tex map <F9> :!pdflatex % && rm %<.aux && rm %<.log <CR>
autocmd FileType tex map <F8> :!chrome %:h/%<.pdf <CR>
```

5.2 Java Reference

```
/* Java reference :
   References on Java IO, Structures, etc.
*/
import java.io.*;
import java.lang.*;
import java.math.*;
import java.util.*;
/* Regular usage:
   Slower IO :
   Scanner in = new Scanner (System.in));
   Scanner in = new Scanner (new BufferedInputStream (System.in));
   Input :
       in.nextInt () / in.nextBigInteger () / in.nextBigDecimal () / in.nextDouble ()
       in.nextLine () / in.hasNext ()
   Output :
       System.out.print (...);
       System.out.println (...);
       System.out.printf (...);
   Faster IO :
   Shown below.
   BigInteger :
   BigInteger.valueOf (int) : convert to BigInteger.
   abs / negate () / max / min / add / subtract / multiply /
   divide / remainder (BigInteger) : BigInteger algebraic.
   gcd (BigInteger) / modInverse (BigInteger mod) /
   modPow (BigInteger ex, BigInteger mod) / pow (int ex) : Number Theory.
   not () / and / or / xor (BigInteger) / shiftLeft / shiftRight (int) : Bit operation.
   compareTo (BigInteger) : comparison.
   intValue () / longValue () / toString (int radix) : converts to other types.
   isProbablePrime (int certainty) / nextProbablePrime () : checks primitive.
   BigDecimal :
   consists of a BigInteger value and a scale.
   The scale is the number of digits to the right of the decimal point.
   divide (BigDecimal) : exact divide.
   divide (BigDecimal, int scale, RoundingMode roundingMode) :
       divide with roundingMode, which may be:
       CEILING / DOWN / FLOOR / HALF_DOWN / HALF_EVEN / HALF_UP / UNNECESSARY / UP.
   BigDecimal setScale (int newScale, RoundingMode roundingMode) :
       returns a BigDecimal with newScale.
```



```

        doubleValue () / toString () : converts to other types.
Arrays :
    Arrays.sort (T [] a);
    Arrays.sort (T [] a, int fromIndex, int toIndex);
    Arrays.sort (T [] a, int fromIndex, int toIndex, Comparator <? super T> comparator);
LinkedList <E> :
    addFirst / addLast (E) / getFirst / getLast / removeFirst / removeLast () :
        deque implementation.
    clear () / add (int, E) / remove (int) : clear, add & remove.
    size () / contains / removeFirstOccurrence / removeLastOccurrence (E) :
        deque methods.
    ListIterator <E> listIterator (int index) : returns an iterator :
        E next / previous () : accesses and iterates.
        hasNext / hasPrevious () : checks availability.
        nextIndex / previousIndex () : returns the index of a subsequent call.
        add / set (E) / remove () : changes element.
PriorityQueue <E> (int initcap, Comparator <? super E> comparator) :
    add (E) / clear () / iterator () / peek () / poll () / size () :
        priority queue implementations.
TreeMap <K, V> (Comparator <? super K> comparator) :
    Map.Entry <K, V> ceilingEntry / floorEntry / higherEntry / lowerEntry (K):
        getKey / getValue () / setValue (V) : entries.
    clear () / put (K, V) / get (K) / remove (K) : basic operation.
    size () : size.
StringBuilder :
    Mutable string.
    StringBuilder (string) : generates a builder.
    append (int, string, ...) / insert (int offset, ...) : adds objects.
    charAt (int) / setCharAt (int, char) : accesses a char.
    delete (int, int) : removes a substring.
    reverse () : reverses itself.
    length () : returns the length.
    toString () : converts to string.
String :
    Immutable string.
    String.format (String, ...) : formats a string. i.e. sprintf.
    toLowerCase / toUpperCase () : changes the case of letters.
*/
/* Examples on Comparator :
public class Main {
    public static class Point {
        public int x;
        public int y;
        public Point () {
            x = 0;
            y = 0;
        }
        public Point (int xx, int yy) {
            x = xx;
            y = yy;
        }
    };
    public static class Cmp implements Comparator <Point> {
        public int compare (Point a, Point b) {
            if (a.x < b.x) return -1;
            if (a.x == b.x) {
                if (a.y < b.y) return -1;
                if (a.y == b.y) return 0;
            }
            return 1;
        }
    };
    public static void main (String [] args) {
        Cmp c = new Cmp ();
        TreeMap <Point, Point> t = new TreeMap <Point, Point> (c);
        return;
    }
};
*/
/* Another way to implement is to use Comparable.
However, equalTo and hashCode must be rewritten.
Otherwise, containers may fail and give strange answers.
Example :
public static class Point implements Comparable <Point> {
    public int x;
    public int y;
    public Point () {
        x = 0;
        y = 0;
    }
    public Point (int xx, int yy) {
        x = xx;
        y = yy;
    }
    public int compareTo (Point p) {
        if (x < p.x) return -1;
        if (x == p.x) {
            if (y < p.y) return -1;
            if (y == p.y) return 0;
        }
        return 1;
    }
    public boolean equalTo (Point p) {
        return (x == p.x && y == p.y);
    }
    public int hashCode () {
        return x + y;
    }
};
*/
//Faster IO :
public class Main {
    static class InputReader {

```

```

public BufferedReader reader;
public StringTokenizer tokenizer;
public InputReader (InputStream stream) {
    reader = new BufferedReader (new InputStreamReader (stream), 32768);
    tokenizer = null;
}
public String next() {
    while (tokenizer == null || !tokenizer.hasMoreTokens()) {
        try {
            String line = reader.readLine();
            tokenizer = new StringTokenizer (line);
        } catch (IOException e) {
            throw new RuntimeException (e);
        }
    }
    return tokenizer.nextToken();
}
public BigInteger nextBigInteger() {
    return new BigInteger (next (), 10);    // customize the radix here.
}
public int nextInt() {
    return Integer.parseInt (next());
}
public double nextDouble() {
    return Double.parseDouble (next());
}
}
public static void main (String[] args) {
    InputReader in = new InputReader (System.in);
    // Put your code here.
}
}

```

5.3 Hacks

```

/* Hacks :
   unusual codes that may help in contests.
*/
// long long formatting hack :
#ifdef WIN32
#define LL "%I64d"
#else
#define LL "%lld"
#endif
// Optimizing hack :
#pragma GCC optimize ("O3")
#pragma GCC optimize ("whole-program")
// Stack hack :
// C++
#pragma comment(linker, "/STACK:36777216")
// G++
int __size__ = 256 << 20; // 256MB
char *__p__ = (char*)malloc(__size__) + __size__;
__asm__ ("movl $0, %%esp\n" :: "r" (__p__));

```