# Missing Data - Assignment 1

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# 1 Introduction

Alcohol consumption led to 2.8 million deaths in 2016 and accounts for almost 10% of global deaths in people aged 15-49 years. Higher levels of alcohol consumption leads to a higher risk of mortality and the only level of alcohol consumption that minimizes this risk is zero alcohol consumption (study). This means that drinking any alcohol at all increases the risk of mortality. All of this makes it vital to know and understand the factors behind alcohol consumption.

Moore et al. 2005 found that age, sex, ethnicity, marital status, education level and household income were all either negatively or positively associated with alcohol consumption. In Garnett et all. 2022 it was found that the level of depression was negatively associated with alcohol consumption. Considering that the only safe level of alcohol consumption is zero, it is important to understand what factors predict regular consumption of alcohol instead of only looking at the amount of alcohol consumption as in the two studies mentioned above.

The research question of this study is: To what extent can the occurrence of regular alcohol consumption (12 or more in a year) be predicted by the variables: depression level, age, sex, ethnicity, marital status and household income?

It is expected that age and depression level will be negatively correlated with the occurrence of alcohol consumption, whilst household income will be positively correlated (sources). In addition, expectation entails that male (vs female) and white (vs other ethnicities) will be positively correlated with the regular occurrence of alcohol consumption (source). Regarding marital status, it is expected that the married status will be positively associated with the regular occurrence of alcohol consumption compared to other marital statuses. That said, the latter was based on a study where the factor marital status consisted of just married and other (source), while in this study more categories were considered.

# 2 Methodology

#### 2.1 Dataset

The dataset used was a subset of the data collected in the National Health and Nutrition Examination Survey (NHANES). The survey was a part of an annual program that investigated the health and nutrition of a representative sample of people in the United States. The data we used contained information about 525 individuals that were collected for the NHANES 2007-2008 survey. This was a subset of the 12,946 individuals in that years' survey sample, out of which 78.4% were interviewed whilst 75.4% participants were examined in mobile examination centers. The NHANES survey was further subdivided into themed sections - such as the Alcohol Use questionnaire - with each of these sections having separate documentations that will be referred to later on.

The used dataset contained a wide range of variables related to the health of the individuals. We further subsetted the data by only including variables relevant to the study (demographics, alcohol use and answers to depression screener questions). The selected variables are further described in Variables Description (Section 2.2).

#### 2.2 Variables Description

Table 1 lists the variables used in our subset selection, which were utilised for the model in question. The predictor variables [dep1...dep9] were sourced from the same Depression Screener, where respondents of age 18 to 150 were ought to assign a number (1 to 3) regarding their mental and physical state within the last 2 weeks. Multiple signs of depression were measured this way, which can be combined to create an overall depression score.

The demographic variables - that being sex, age, ethnicity, education and income - were taken from the same screening component as well. The variable age was topcoded at the value 80 for the respondents who

Table 1: Variable descriptions

| Role      | Variable                   | Name             | Type        | Characteristics         | Target                     |
|-----------|----------------------------|------------------|-------------|-------------------------|----------------------------|
| Outcome   | Drink regularly            | drink_regularly  | Categorical | Binary, yes and no      | m/f, age 20-150            |
| Predictor | Sex                        | sex              | Categorical | Binary, male and female | m/f, age 0-150             |
| Predictor | Age                        | age              | Numeric     | Discrete                | m/f, age 0-150             |
| Predictor | Ethnicity                  | ethnicity        | Categorical | Nominal, 5 categories   | m/f, age 0-150             |
| Predictor | Education                  | marital          | Categorical | Nominal, 5 categories   | m/f, age 20-150            |
| Predictor | Marital status             | marital          | Categorical | Nominal, 5 categories   | m/f, age 20-150            |
| Predictor | Household income           | household_income | Categorical | Nominal, 12 categories  | m/f, age 0-150             |
| Predictor | No interest in activity    | dep1             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Feeling depressed          | dep2             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Sleeping issues            | dep3             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Feeling tired              | dep4             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Eating issues              | dep5             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Feeling bad about yourself | dep6             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Concentrating issues       | dep7             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Moving and speaking issues | dep8             | Categorical | Ordinal, 1-3 scale      | m/f, age 18-150            |
| Predictor | Suicidial thoughts         | dep9             | Categorical | Ordinal, 1-3 scale      | $\rm m/f,age18\text{-}150$ |

were older than 80 years. Similarly, education was targeted at respondents of age 20 to 150, thus excluding younger participants. This was due to the fact that this question included responses such as AA degree and College Graduate. The variable marital was also targeted at respondents of age 20 to 150. Lastly, the variable income was ordinal, rather than continuous.

As for the remaining demographic variables, namely sex, age, ethnicity and income, these were retrieved from target age 0 to 150.

Finally, the drink\_regularly variable was obtained from an Alcohol Use questionnaire targeted at ages 20 and up.

### 2.3 Software

All of the data cleaning, processing and modeling was performed in R version 4.3.2 (R Core Team 2023). The following packages were used: tidyverse was used for data manipulation (Wickham et al. 2019), the mice (van Buuren and Groothuis-Oudshoorn 2011) and ggmice (Oberman 2024) packaged were used for missing data visualizations and list-wise deletion and mean imputation, the kableExtra package was used for table styling (Zhu 2021), naniar package was used to make the visualization of missing data percentages (Figure 7) (Tierney and Cook 2023), Hmisc was utilized for mode imputation, vtable helped with the summary statistic table in the Appendix (Huntington-Klein 2023) and gtsummary was used to produce the summary tables for the two final models (Sjoberg et al. 2021).

#### 2.4 Data processing

After arriving at the subset dataset, an Exploratory Data Analysis was performed. The distributions of the variables were investigated and the presence of missing data was found in the outcome variable and some of the depression questions. No outliers were found during the EDA. Additionally, the missingness seemed to be more prevalent among younger individuals, which gave a first indication of a lacking MCAR mechanism. The important findings of this step are presented in EDA Results (Section 3).

Following the EDA, the missing data problem was addressed. The extend, distributions and patterns of missingness were investigated. Testing was done to verify the missing data mechanism. This included performing a global test - Little MCAR test (Little 1986) and testing of the dependencies between missing values in one variable vs. observed values of other variables. The latter was done using t-tests for continuous

variables, whilst categorical variables were checked via Chi-squared test and Fisher test (Soetewey, n.d.). The Fisher test with simulated p-values was used to verify outcomes for combinations of variables that included an expected frequency lower than 5, thus not meeting the assumptions of Chi-squared test (Soetewey, n.d.). When the assumptions of MCAR was not met, MAR was assumed.

Two solutions to the missing data problem were implemented: list-wise deletion and mean imputation. These where chosen based on the convenience of implementation. For list-wise deletion, all cases with one or more missing values were excluded from the modeling. The mean imputation method was implemented in the following way: For the missing depression questions, the mean of the observed values within the variable was computed and then the missing values were replaced by said mean value. This approach was taken, since treating ordinal variables on a Likert scale as continuous variables instead was appropriate (Wu, Jia, and Enders 2015). For drink\_regularly - the outcome variable - the mode was computed rather than the mean. This was motivated by the need for a binary outcome variable in the logistic regression model that was utilised to answer the research question. The EDA suggested significantly more "yes" than "no" values in drink\_regularly, hence the missing values were replaces by "yes". Thus, two complete datasets with different missing data treatments were created.

Lastly, following the missing data treatments, the values for the depression questions were summed up to create an overall depression score for each individual case. A sum was used - as opposed to other methods of aggregation (e.g. mean) - as it preserved a convenient interpretation of a unit increase in a depression score. This overall score was used for modeling as opposed to the individual depression levels.

# 2.5 Modelling methodology

Including all of the variables in the two complete data sets was motivated by theoretical findings, since other researchers found a relationship between them and drinking habits. Therefore, verifying the significance of these predictors and their relative importance in the presence of other variables was important. Thus, a decision was made to create two logistical models including all of the variables, instead of a top down or bottom up approach to model building. As opposed to removing the non-significant predictors following the aforementioned model-building methods, it was decided to keep all the predictor variables and therefore have a more complex model. Following model creation, the two logistics models were compared, where the impact of the two different missing data treatments was evaluated. For easier interpretation the model coefficients were exponentiated. Occurrence of regular drinking was considered the "successful" outcome.

### 3 EDA Results

#### 3.1 Descriptive statistics

Table 10 from the appendix shows summary statistics for each of the variables within the dataset; including mean values, standard deviations, IQR statistics and data range values. For categorical variables, a list of possible categories and their respective proportions was provided to replace the continuous summary statistics. Lastly, the column N shows the amount of cases with present data - that being non-NA values. In general, we observed that all variables were interpreted as a factor, excluding age and the multiple depression levels of dep. Table 1 suggested that dep should in fact be categorical ordinal and should therefore be cast as a factor. That said - and as mentioned in Section 2.4 - keeping the levels of dep as a numerical continuous datatype was beneficial for our missing data problem.

The dataset contained a total of 525 observations, each with 17 variables.

Our dichotomous outcome variable drink\_regularly had 307 cases of "yes" and 107 cases of "no", having a outcome balance of 69% and 31% respectively. This outcome ratio could be considered imbalanced, which could affect the accuracy of our logistic regression model. Additionally, the total amount of value entries (N) of 446 suggested that 79 cases contained values outside of the set of possible binary values - most likely being missing values. Table 2 further confirmed this.

Table 2: Drink regularly value distributions

| drink_regularly | n   |
|-----------------|-----|
| no              | 139 |
| yes             | 307 |
| NA              | 79  |

Predictor sex was a dichotomous variable with a balanced frequency distribution across the values "male" and "female", that being 48% and 52% respectively. 525 entries contained one of these values, suggesting that the variable did not contain missing data.

The predictor age was the only continuous variable present within the sub-selected dataset. Although the survey was targeted at respondents of age 0-150 for most variables - the documentation even mentioning the topcoded entries for age 80+ - the dataset seemed to only contain cases of people between the age of 20 and 69. Moreover, Figure 1 suggested a uniform distribution of the age variable. Like sex, age had 525 cases with non-NA values, hence the variable did not contain missing data values.

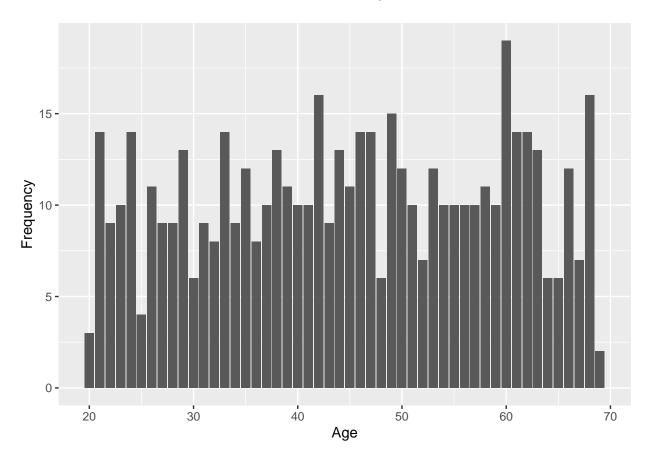


Figure 1: Distribution of age

Predictor ethnicity had 5 categories, with non-hispanic\_white being the most prevalent category with 220 cases (42% of total), all the while other was the most infrequent category with 25 cases (5%). A total of 525 cases contained ethnicity data, once again suggesting no presence of missing data values within this variable.

Predictor education was similar to ethnicity, having 5 categories. That said, the frequencies of said

categories seemed to be less out of proportion, with some\_college being the most frequent category with 155 (30%) cases. Whilst the data was retrieved from respondents of ages 20 and higher, we did not observe any missing data values within the variable. This could be further justified by the fact that the minimum age within our dataset was 20, therefore foregoing possible issues with younger participants being unable to provide data for this specific variable.

The predictor variable marital contained 6 categories. It should be noted that the category value married exceeded the average frequency of other categories (that being 49.2) by a large margin, as can be seen in Figure 2. Specifically, 279 cases (53%) were married, with the other 5 categories making up the remaining 47% of the cases. never\_married was the most frequent among those other 5 categories with 102 (19%) cases, whilst separated was the most infrequent category with only 14 (3%) cases. Furthermore, the meaning of never\_married and living\_with\_partners was ambiguous in the sense that a person specifically living with their (non-married) partner could fall into both these categories.

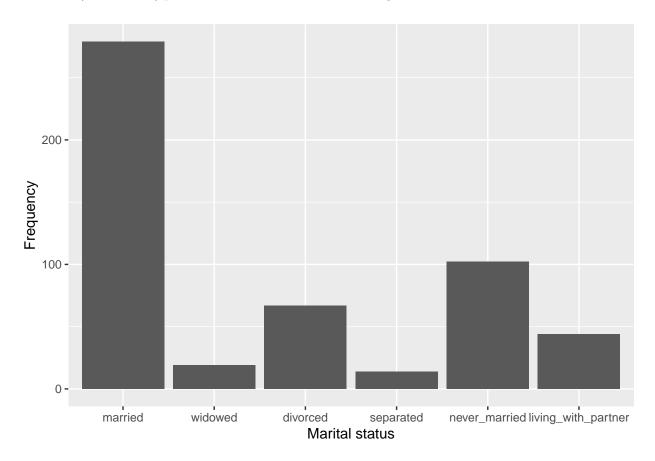


Figure 2: Distribution of marital status categories

Predictor income was a ordinal variable formed by 12 levels, ranging from income values 0 to 100000+. This data, like age, was topcoded at the value 100000. This also explained the highest income category - that being 100000+ - having 76 cases (9%), as can be seen in Figure 3. If we ignore the latter case, the most frequent category was instead 25000:34999, which coincidentally was the mid-range category of our income data.

525 cases contained income data, therefore the variable did not contain missing data values.

The multiple levels of depression all had ranging scores between 0 and 3, with increments of 1 specifically. A higher score indicated an agreement with the signs of depression described in the survey. Only dep1 and dep7 had complete data data, whilst the other levels had varying amounts of missing data. Missing data could possibly be caused by the respondents being reluctant to answers these questions. We also observed

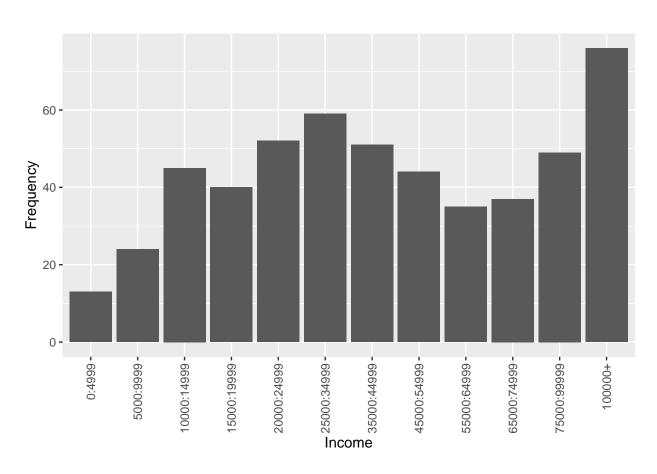


Figure 3: Distribution of income

that dep2, dep3, dep5, dep6 had the same amount of missing data values, hence it was possible that they had a shared cause of missing data. Lastly, dep9 only had 18 cases of scores above 0, whilst also having the lowest mean value out of all depression levels. dep9 described the presence of suicidal thoughts, hence it made sense that this was the lowest average score out of all levels. On the contrary, dep4 (feeling tired) had the highest average score.

Overall, the score distribution were heavily skewed towards the 0 values.

#### 3.2 Outliers

For our only continuous predictor age, a boxplot was utilised to find potential outliers. Figure 4 shows the distribution of age in said boxplot, revealing no possible outliers. This was to be expected, since age was uniformly distributed as was mentioned in Section 3.1.

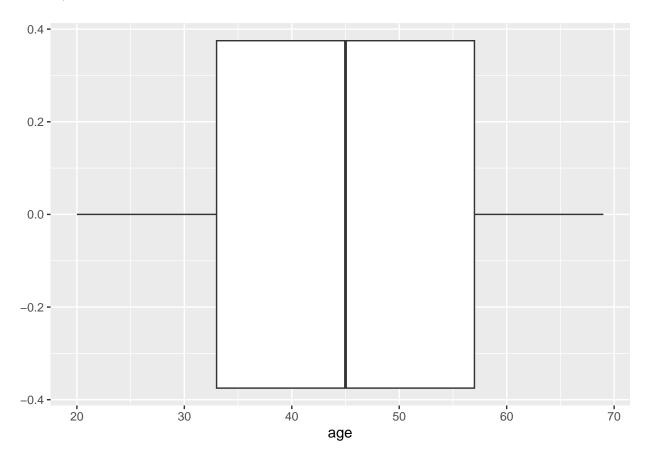


Figure 4: Boxplot of age

Looking at the distributions of the various categorical variables, the marital showed the aforementioned imbalance in frequency distribution, with the category married being overly dominant within the data. We considered combining the other marital categories into one, as their infrequency could allude to being possible outliers. Table 3 shows the interrelations between the martial variable and our outcome drink\_regularly. From this, we concluded that combining the remaining 5 categories - that being widowed, divorced, separated, never\_married and living\_with\_partner - was not feasible, since these relations seemed to differ per category. For example, widowed had more "no" cases compared to "yes", whilst the relation was reversed for separated.

Table 3: Contingency table of marital status vs. drinking regularly

|                         | no | yes |
|-------------------------|----|-----|
| married                 | 81 | 175 |
| widowed                 | 11 | 8   |
| divorced                | 14 | 48  |
| separated               | 4  | 8   |
| never_married           | 23 | 45  |
| $living\_with\_partner$ | 6  | 23  |

# 3.3 Correlations

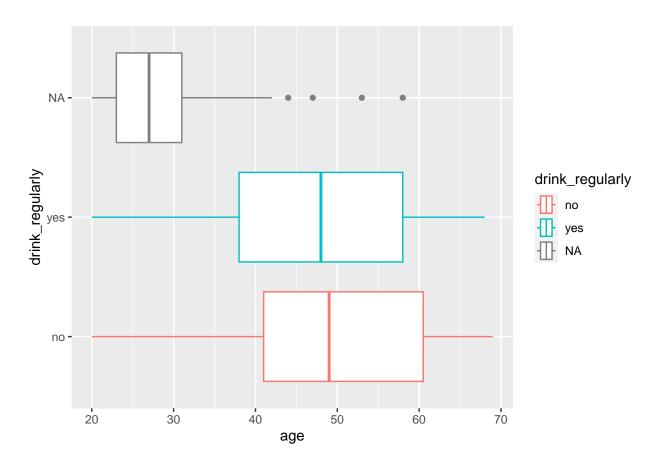


Figure 5: Correlations of age vs. drink regularly

Figure 5 shows the distributions of age over the outcome variable drink\_regularly in a boxplot. Not considering the NA values, age did not seem to be strongly correlated with drink\_regularly, with "no" cases having only slightly higher ages than its counterpart.

It should however be noted that the NA values of drink\_regularly were primarily present in younger participants, therefore possibly attenuating the correlation effect between these two variables. For example, a large amount of missing values belonging to "yes" could shift the distribution of these cases towards lower age values, hence increasing the difference in distributions for each drink\_regularly outcome.

Contingency tables and frequency distribution plots (including NA values) were used to observe the correlation between our categorical predictors and the outcome variable. From this, we observed that <code>sex</code> seemed

to be highly correlated with drink\_regularly; 172 cases of male drank regularly, whilst only 39 didn't. Compared to the 135 cases of female of "yes" and 100 cases of "no", this ratio seemed to differ greatly per sex category. The missingness of drink\_regularly was evenly distributed across both male and female cases.

Likewise, marital showed a similarly strong correlation effect. The category divorced had a significantly higher ratio of respondents who drank regularly, compared to cases of widowed, where respondents were more likely to not drink regularly as can be seen in Figure 6. We also noted that the missing data of drink\_regularly was not evenly distributed across the marital categories. Rather, the missingness was more prevalent in the never\_married and living\_with\_partner cases. This possibly ties back into the fact that more data was missing amongst younger respondents, which can be directly seen in Figure ?? where never\_married and living\_with\_partner have more cases of a younger age as well.

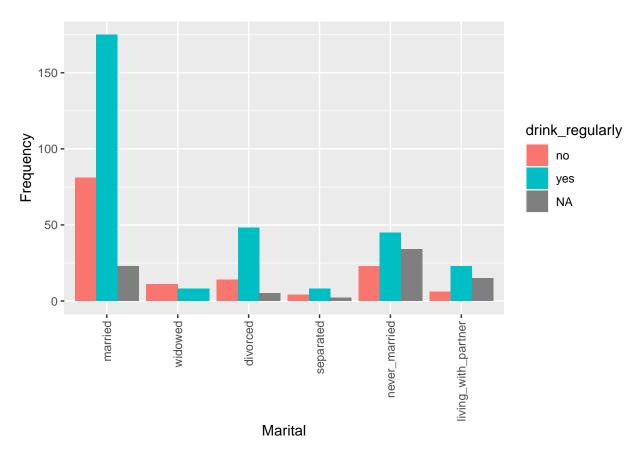


Figure 6: Correlations of marital vs. drink regularly

ethnicity showed a weaker correlation effect with the outcome variable. Only non-hispanic\_black and other showed different frequency distributions compared to the other categories. Missing data of drink\_regularly was present in all categories of ethnicity, though other\_hispanic and other had close to none compared to the remaining categories.

The variable education was considered to have the weakest correlation with drink\_regularly, having similar success ratios across all categories all the while missing data of drink\_regularly was also evenly spread. income was considered to be correlated with the outcome variable. Performing a similar analysis, we observed that respondents with an income up until 24999 were less likely to drink regularly than cases with a higher income. Akin to education, missing data of drink\_regularly seemed to be evenly spread across the income values.

Finally, all levels of depression showed an effect of correlation with drink\_regularly, where higher scores tended to decrease the ratio of "yes" to "no" cases, that is to say that respondents were less likely to drink

regularly if signs of depression were present.

# 4 Missing data problem

#### 4.1 Missing data and response patterns

Firstly, we investigated the overall distribution of missingness within our dataset.

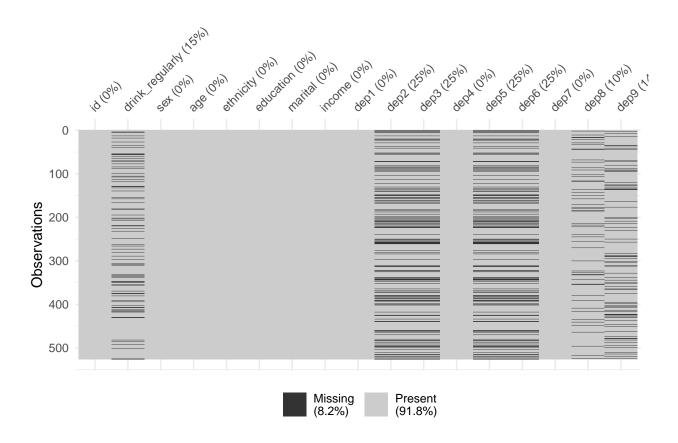


Figure 7: Distribution of missing data in each variable

As can be seen on Figure 7, 8.2% of the data was missing. The missing values occurred in the outcome variable drink\_regularly and in the responses to questions dep2, dep3, dep5, dep6, dep8 and dep9 that created the depression score variable. 15% of responses were missing for the predictor variable. 25% of the responses were missing for the individual depression questions 2, 3, 5 and 6, whilst 10% were missing for question 8. Finally, 14% of data was missing for question 9.

We further investigated the missing data patterns by looking at the response patterns. Figure 8 reveals that there were 13 distinct response patterns in the dataset, with the missingness *not* being monotone. The most frequent pattern is no missing entries, with 263 cases. It is important to note that the depression questions 2, 3, 5 and 6 were always either all present or all missing. It is very probable that the reason for the item non-response regarding these depression leves was the same, since there were no cases with partial missingness in these 4 variables.

Based on the missingness pattern of the depression items, 41% of the overall depression score included at least one missing value.

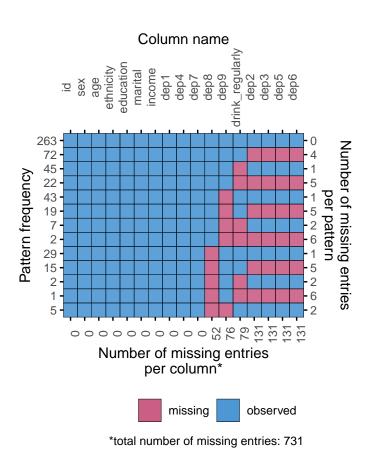


Figure 8: Response patterns and their frequency

### 4.2 Missing data mechanism

Missing completely at random (MCAR) missingness mechanism is often an important assumption for statistical analysis, including this one. To gain some inside whether the data is MCAR or not, we deploy a variety of tests. If missing values of a variable are MCAR then there should be no significant dependency of them with other variables.

Firstly, Little MCAR test was preformed to verify if the missing data is MCAR at a global level, thus for all of the instances of missigness. The test was significant ( $\chi^2(164) = 465.18, p < 0.01$ ), therefore the data may be assumed as not MCAR.

Since the data being MCAR can be questioned following the Little's test, a t-test was performed for all missing values vectors and numerical variables to check which variables are the likely culprit. The test compared the observed means of a given numerical variable within the group of individuals that had an observed value and the group with a missing value for another variable. Effectively testing if there is a significant difference in the continuous variable in the group that answered another question and the group that did not. Since the null hypothesis is no difference in means across the groups, a single significant value for a missingness of a given variable suggests that the missing values in that variable depend on the observed values of another variable. Therefore, it is likely that the missing values are not MCAR. Due to the identical pattern of responses in 'dep2', 'dep3', 'dep5' and 'dep6' it was sufficient to only test once for the dependency of their missing values. By the design of the test it is impossible to test the dependency of missing values and observed values within the same variable, thus these values are missing from the table.

Assuming an alpha of 0.05, it can be observed that missing values of 'drink\_regularly' are dependent on 'age', 'dep2' and 'dep9'. Similarly, 'dep2', 'dep3', 'dep5' and 'dep6' seem to be dependent on 'age' and the remaining depression questions. For missingness in 'dep8' and 'dep9' there are no significant differences across groups in any of the numerical variables. These tests suggest that at least 'drink\_regularly', 'dep2', 'dep3', 'dep5' and 'dep6'are not MCAR, thus MAR will be assumed for them. In Table 4 the exact t-statistic and the p-value are reported.

Table 4: Dependency t-test: mean comparison in numerical variables across missing values and observed values in the other variables

| numerical variable | missing drink_regularly    | missing dep $2/3/5/6$        | missing dep8               | missing dep9                |
|--------------------|----------------------------|------------------------------|----------------------------|-----------------------------|
| age                | t = 19.3, pVal = 3.1e-45   | t = 1.38,  pVal = 0.17       | t = -1.16, $pVal = 0.249$  | t = -0.884,  pVal = 0.379   |
| dep1               | t = 1.39,  pVal = 0.167    | t = -6.72, $pVal = 2.88e-10$ | t = 0.464,  pVal = 0.644   | t = -0.444,  pVal = 0.658   |
| dep2               | t = 3.63,  pVal = 0.000405 | -                            | t = 0.332,  pVal = 0.742   | t = 1.22,  pVal = 0.224     |
| dep3               | t = 0.797, $pVal = 0.428$  | -                            | t = -0.137, $pVal = 0.892$ | t = 0.0545, $pVal = 0.957$  |
| dep4               | t = -0.541,  pVal = 0.59   | t = -7.8, pVal = 6.11e-13    | t = -0.68, pVal = 0.499    | t = -1.28,  pVal = 0.202    |
| dep5               | t = 2.01,  pVal = 0.0466   | _                            | t = -0.605, $pVal = 0.549$ | t = -0.731,  pVal = 0.467   |
| dep6               | t = 0.822,  pVal = 0.414   | -                            | t = 2.3,  pVal = 0.0242    | t = 0.00637, $pVal = 0.995$ |
| dep7               | t = -0.382, $pVal = 0.703$ | t = -8.19, $pVal = 1.24e-13$ | t = -0.239, $pVal = 0.812$ | t = -0.0635, $pVal = 0.949$ |
| dep8               | t = -0.32, pVal = 0.75     | t = -4.26, $pVal = 3.86e-05$ | -                          | t = 0.595,  pVal = 0.553    |
| dep9               | t = 2.48,  pVal = 0.0135   | t = -2.64, $pVal = 0.00947$  | t = -0.295, pVal = 0.769   | -                           |

Table 5: Independency Chi-squared test

| categorical variable | missing drink_regularly          | missing $dep2/3/5/6$             | missing dep8                   | missing dep9                   |
|----------------------|----------------------------------|----------------------------------|--------------------------------|--------------------------------|
| drink_regularly      | -                                | $X^2 = 4.2$ , $pVal = 0.0404$    | $X^2 = 1.52$ , $pVal = 0.218$  | $X^2 = 0.464$ , pVal = 0.496   |
| sex                  | $X^2 = 1.09$ , $pVal = 0.296$    | $X^2 = 5.04$ , $pVal = 0.0248$   | $X^2 = 0.469$ , $pVal = 0.494$ | $X^2 = 0.317$ , pVal = 0.573   |
| ethnicity            | $X^2 = 5.49$ , $pVal = 0.241$    | $X^2 = 1.64$ , $pVal = 0.802$    | $X^2 = 7.74$ , $pVal = 0.102$  | $X^2 = 5.8$ , $pVal = 0.215$   |
| education            | $X^2 = 2.7$ , $pVal = 0.609$     | $X^2 = 5.72$ , $pVal = 0.221$    | $X^2 = 1.63$ , $pVal = 0.803$  | $X^2 = 5.13$ , $pVal = 0.275$  |
| marital              | $X^2 = 55.7$ , pVal = $9.58e-11$ | $X^2 = 22.2$ , $pVal = 0.000477$ | $X^2 = 5.08$ , $pVal = 0.407$  | $X^2 = 3.97$ , $pVal = 0.553$  |
| income               | $X^2 = 2.94$ , $pVal = 0.991$    | $X^2 = 8.84$ , $pVal = 0.636$    | $X^2 = 9.4$ , $pVal = 0.585$   | $X^2 = 17.3$ , $pVal = 0.0995$ |

Since the t-test is not appropriate for categorical variables, we perform the Chi-squared test for them. The null hypothesis of the test is that there is no significant relationship between the categorical variables. The

test compares observed frequencies to expected frequencies if there was no relationship between the variables.

The outcomes of the test are presented in Table 5. However, only 'martial' with missingness of 'drink\_regularly' and 'marital' with missingness of 'dep2', 'dep3', 'dep5' and 'dep6' are significant. Thus, it further supports the non-MCAR nature of missing data in these items.

However, the Chi-squared test has an requirement that the smallest expected frequencies have to be higher than 5. This requirement is not met for some combinations of missing values and categorical variables. Specifically: missing 'dep8/9' and 'ethnicity', 'marital', 'income'; missing 'dep2/3/5/6' and 'marital', 'income'; missing 'drink\_regularly' and 'ethnicity', 'marital', 'income'. Since this assumption is not met for these combination, the pValues might not be correctly estimated. Therefore, the Fischer test, test with the same hypothesis but without the assumption, will be performed for these combinations.

Table 6: Fisher test

| categorical variable | missing drink_regularly | missing $dep2/3/5/6$ | missing dep8  | missing dep9 |
|----------------------|-------------------------|----------------------|---------------|--------------|
| ethnicity            | pVal = 0.232            | -                    | pVal = 0.0804 | pVal = 0.21  |
| marital              | pVal = 1e-05            | pVal = 0.00089       | pVal = 0.399  | pVal = 0.446 |
| income               | pVal = 0.987            | pVal = 0.64          | pVal = 0.561  | pVal = 0.058 |

The outcomes of the FIsher test are presented in Table 6. Like in the case of Chi-squared test, only 'martial' with missingness of 'dep2', 'dep3', 'dep5' and 'dep6' are significant. Therefore, we can conclude the dependence of missingness in these variables on multiple other observed variables and reject MCAR in their case.

In all of the tests above 'dep8' and 'dep9' seem not to be dependent on any of the observed variables. Thus, perhaps MCAR could be assumed. However, since the depression scores will be collapsed into a single depression score ('dep') and other depression questions are MAR, the overall score is also assumed to be MAR.

#### 4.3 Interpretation of the two models

```
##
## iter imp variable
## 1 1 dep2 dep3 dep5 dep6 dep8 dep9
```

Table 7: Mean imputation model

| Characteristic     | OR      | SE    | p-value |
|--------------------|---------|-------|---------|
| (Intercept)        | 6.71    | 1.28  | 0.14    |
| sex                |         |       |         |
| male               | _       | _     |         |
| female             | 0.16*** | 0.350 | < 0.001 |
| age                | 1.00    | 0.013 | 0.8     |
| ethnicity          |         |       |         |
| mexican_american   | _       | _     |         |
| other_hispanic     | 1.49    | 0.594 | 0.5     |
| non-hispanic_white | 1.58    | 0.435 | 0.3     |
| non-hispanic_black | 0.55    | 0.485 | 0.2     |
| other              | 1.04    | 0.792 | > 0.9   |
| education          |         |       |         |
| $no\_high\_school$ | _       | _     |         |

Table 7: Mean imputation model (continued)

| Characteristic                                    | OR      | $\mathbf{SE}$ | p-value |  |
|---|---------|---------------|---------|--|
| some_high_school                                  | 0.82    | 0.582         | 0.7     |  |
| high_school_grad                                  | 1.30    | 0.589         | 0.7     |  |
| some_college                                      | 1.05    | 0.604         | >0.9    |  |
| college_grad                                      | 1.66    | 0.647         | 0.4     |  |
| marital   |         |               |         |  |
| married   | _       | _             |         |  |
| widowed   | 1.37    | 0.711         | 0.7     |  |
| divorced  | 7.37*** | 0.578         | < 0.001 |  |
| separated   | 1.98    | 1.14          | 0.5     |  |
| never_married                                     | 1.34    | 0.435         | 0.5     |  |
| living_with_partner                               | 4.26    | 0.862         | 0.093   |  |
| income  |         |               |         |  |
| 0:4999  | _       |               |         |  |
| 5000:9999   | 0.17    | 1.24          | 0.15    |  |
| 10000:14999                                       | 0.43    | 1.07          | 0.4     |  |
| 15000:19999                                       | 0.43    | 1.05          | 0.4     |  |
| 20000:24999                                       | 0.40    | 1.04          | 0.4     |  |
| 25000:34999                                       | 0.65    | 1.04          | 0.7     |  |
| 35000:44999                                       | 0.79    | 1.07          | 0.8     |  |
| 45000:54999                                       | 0.40    | 1.12          | 0.4     |  |
| 55000:64999                                       | 1.06    | 1.13          | > 0.9   |  |
| 65000:74999                                       | 0.36    | 1.11          | 0.4     |  |
| 75000:99999                                       | 0.56    | 1.13          | 0.6     |  |
| 100000+   | 0.79    | 1.06          | 0.8     |  |
| dep   | 1.03    | 0.051         | 0.6     |  |
| <sup>1</sup> p<0.05; <b>p&lt;0.01;</b> p<0        | 0.001   |               |         |  |
| <sup>2</sup> OR = Odds Ratio, SE = Standard Error |         |               |         |  |

Table 8: Mean imputation model

| Characteristic       | OR      | SE    | p-value |
|----------------------|---------|-------|---------|
| (Intercept)          | 20.5**  | 0.933 | 0.001   |
| sex                  |         |       |         |
| male                 | _       | _     |         |
| female               | 0.24*** | 0.247 | < 0.001 |
| age                  | 0.97*** | 0.009 | < 0.001 |
| ethnicity            |         |       |         |
| mexican_american     | _       | _     |         |
| other_hispanic       | 1.19    | 0.411 | 0.7     |
| non-hispanic_white   | 1.42    | 0.338 | 0.3     |
| non-hispanic_black   | 0.57    | 0.367 | 0.12    |
| other                | 0.59    | 0.543 | 0.3     |
| education            |         |       |         |
| $no\_high\_school$   | _       | _     |         |
| $some\_high\_school$ | 1.16    | 0.428 | 0.7     |
| high_school_grad     | 1.48    | 0.422 | 0.4     |
| $some\_college$      | 1.22    | 0.420 | 0.6     |
| college_grad         | 1.98    | 0.479 | 0.2     |

Table 8: Mean imputation model (continued)

| Characteristic                              | OR                                   | SE    | p-value |  |  |
|---|--------------------------------------|-------|---------|--|--|
| marital                                     |                                      |       |         |  |  |
| married                                     | _                                    | _     |         |  |  |
| widowed                                     | 0.85                                 | 0.547 | 0.8     |  |  |
| divorced                                    | 3.05**                               | 0.385 | 0.004   |  |  |
| separated                                   | 1.36                                 | 0.678 | 0.7     |  |  |
| $never\_married$                            | 1.22                                 | 0.335 | 0.5     |  |  |
| living_with_partner                         | 2.28                                 | 0.508 | 0.10    |  |  |
| income                                      |                                      |       |         |  |  |
| 0:4999                                      | _                                    | _     |         |  |  |
| 5000:9999                                   | 0.64                                 | 0.825 | 0.6     |  |  |
| 10000:14999                                 | 0.92                                 | 0.756 | > 0.9   |  |  |
| 15000:19999                                 | 0.40                                 | 0.738 | 0.2     |  |  |
| 20000:24999                                 | 0.51                                 | 0.732 | 0.4     |  |  |
| 25000:34999                                 | 1.20                                 | 0.752 | 0.8     |  |  |
| 35000:44999                                 | 0.87                                 | 0.753 | 0.9     |  |  |
| 45000:54999                                 | 0.96                                 | 0.791 | > 0.9   |  |  |
| 55000:64999                                 | 0.93                                 | 0.785 | > 0.9   |  |  |
| 65000:74999                                 | 0.60                                 | 0.790 | 0.5     |  |  |
| 75000:99999                                 | 1.19                                 | 0.785 | 0.8     |  |  |
| 100000+                                     | 1.18                                 | 0.752 | 0.8     |  |  |
| dep   | 1.02                                 | 0.035 | 0.6     |  |  |
| <sup>1</sup> p<0.05; <b>p&lt;0.01;</b> p<0  | <sup>1</sup> p<0.05; p<0.01; p<0.001 |       |         |  |  |
| $^{2}$ OR = Odds Ratio, SE = Standard Error |                                      |       |         |  |  |

Table 9: Model fit statistics

| model             | AIC      | BIC      | D        |
|-------------------|----------|----------|----------|
| listwise deletion | 342.6925 | 442.7129 | 286.6925 |
| mean imputation   | 576.6865 | 696.0617 | 520.6865 |

Two logistic models were created, one model with the dataset resulting from using listwise deletion as the method used to treat the missing data and the other model with the dataset resulting from using mean imputation as the method used to treat the missing data. In the interpretation section below only the significant predictors are mentioned as most are non-significant and including them would add an unnecessary amount of text. They are still included in the created models, see table 5 and 6.

Looking at the listwise deletion model, only sex ( p < 0.001) and the marital status divorced (p < 0.001) are significant predictors, all the other predictors and the intercept were insignificant. The odds ratio of females drinking regularly compared to males was  $0.16[0.08,\,0.31]$  meaning they were 0.16 times as likely to drink compared to males ( 0.16 < 1 so it less likely). The odds ratio of people with the marital status divorced compared to people with the marital status married was  $7.37[2.54,\,25.0]$  meaning divorced people were 7.37 times as likely to drink regularly compared to married people.

In the mean imputation model age (p < 0.001) is also a significant predictor next to sex (p < 0.001) and marital status divorced (p < 0.004), the intercept (p < 0.001) is also significant. For a unit increase in age the odds ratio of drinking regularly decreases 0.97[0.95, 0.99] times. The odds ratio of females drinking regularly compared to males was 0.24[0.14, 0.38] meaning they were 0.24 times as likely to drink compared to males. The odds ratio of people with the marital status divorced compared to people with the marital status married was 3.05[1.47, 6.69] meaning divorced people were 3.05 times as likely to drink regularly compared

to married people. If all predictor variables were in their reference state the baseline odds ratio is 20.5[3.40, 136]. Looking at the model fit statistics, it seems like the listwise deletion models seems to fit better with a lower AIC, BIC and D value as show in table 7.

# 4.4 Comparison of the two models in terms the missing data and resulting model

The answer to the research question changes depending on the used method to treat missing data as can be seen in the interpretation section above. The models differ in: the number of significant predictors, the odds ratios, standard errors (these are lower in the mean imputation model, see tables 5 and 6) and the fitness statistics. Both methods used to treat missing data only work correctly if the missingness is MCAR but as the missingness is not MCAR as is explained in section 4, both methods caused bias in the results. In the case of logistic regression (as this study does) listwise deletion could still give unbiased results even if the missingness isn't MCAR if the missing values are either in the predictor variables or in the outcome variable. This isn't the case in the data used in this study, both predictor variables as the outcome variables contain missing values.

When listwise deletion is used on a dataset where the missingness isn't MCAR it will result in bias in the regression coefficients and standard errors that are too large. As the models in this study are logistic regression models the regression coefficients are transformed into odds ratios instead. Another negative of listwise deletion is that it is wasteful, a lot of data goes unused. This is also the case in this study as 41% of the cases are deleted. Which might explain why the listwise deletion model has a lower D value: there is just a lot less data that might not fit in the model. Another consequence of removing so much data from the dataset is that it becomes more difficult to find effects, this is a possible explanation for why the listwise deletion model has less significant predictors.

Using mean imputation on a dataset where the missingness isn't MCAR will give biased results and underestimated standard errors. It is indeed the case that the standard errors in the mean imputation model are lower than those in the listwise deletion model. As listwise deletion usually overestimates the standard errors, the real values are probably somewhere in between.

So as both methods were used when the missingness wasn't MCAR the created models are biased in multiple ways and thus aren't valid.

# 4.5 Conclusion in terms of answering RQ (Nisse)

- go back to papers, reflect hypo
- stuffs

### 5 References

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# A Appendix

Table 10: Summary statistics

| Variable  | N                               | Mean                             | Std. Dev.                          | Min                   | Pctl. 25         | Pctl. 75              | Max              |
|---|---------------------------------|----------------------------------|------------------------------------|-----------------------|------------------|-----------------------|------------------|
| id drink_regularly no yes sex   | 525<br>446<br>139<br>307<br>525 | 46470<br>31%<br>69%              | 2898                               | 41531                 | 43912            | 48934                 | 51610            |
| male female age ethnicity mexican_american  | 254<br>271<br>525<br>525<br>95  | 48%<br>52%<br>45                 | 14                                 | 20                    | 33               | 57                    | 69               |
| <ul><li> other_hispanic</li><li> non-hispanic_white</li><li> non-hispanic_black</li><li> other</li><li>education</li></ul>        | 61<br>220<br>124<br>25<br>525   | 12%<br>42%<br>24%<br>5%          |                                    |                       |                  |                       |                  |
| <ul><li> no_high_school</li><li> some_high_school</li><li> high_school_grad</li><li> some_college</li><li> college_grad</li></ul> | 58<br>101<br>123<br>155<br>88   | 11%<br>19%<br>23%<br>30%<br>17%  |                                    |                       |                  |                       |                  |
| marital married widowed divorced separated  | 525<br>279<br>19<br>67<br>14    | 53%<br>4%<br>13%<br>3%           |                                    |                       |                  |                       |                  |
| never_married living_with_partner income 0:4999 5000:9999   | 102<br>44<br>525<br>13<br>24    | 19%<br>8%<br>2%<br>5%            |                                    |                       |                  |                       |                  |
| 10000:14999<br>15000:19999<br>20000:24999<br>25000:34999<br>35000:44999   | 45<br>40<br>52<br>59<br>51      | 9%<br>8%<br>10%<br>11%<br>10%    |                                    |                       |                  |                       |                  |
| 45000:54999<br>55000:64999<br>65000:74999<br>75000:99999<br>100000+   | 44<br>35<br>37<br>49<br>76      | 8%<br>7%<br>7%<br>9%<br>14%      |                                    |                       |                  |                       |                  |
| dep1<br>dep2<br>dep3<br>dep4<br>dep5  | 525<br>394<br>394<br>525<br>394 | 0.41 $0.28$ $0.53$ $0.76$ $0.31$ | 0.79<br>0.58<br>0.86<br>0.9<br>0.7 | 0<br>0<br>0<br>0<br>0 | 0<br>0<br>0<br>0 | 1<br>0<br>1<br>1<br>0 | 3<br>3<br>3<br>3 |
| dep6<br>dep7<br>dep8<br>dep9  | 394<br>525<br>473<br>449        | 0.2<br>0.32<br>0.2<br>0.067      | 0.56<br>0.71<br>0.59<br>0.379      | 0<br>0<br>0<br>0      | 0<br>0<br>0<br>0 | 0<br>0<br>0<br>0      | 3<br>3<br>3<br>3 |