Missing Data - Assignment A

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1 Introduction

Alcohol consumption led to 2.8 million deaths in 2016 and accounts for almost 10% of global deaths in people aged 15-49 years. Higher levels of alcohol consumption leads to a higher risk of mortality and the only level of alcohol consumption that minimizes this risk is zero alcohol consumption (GBD 2016 Alcohol Collaborators 2018). This means that drinking any alcohol at all increases the risk of mortality. All of this makes it vital to know and understand the factors behind alcohol consumption.

Moore et al. 2005 found that age, sex, ethnicity, marital status, education level and household income were all either negatively or positively associated with alcohol consumption. In Garnett et all. 2022 it was found that the level of depression was negatively associated with alcohol consumption. Considering that the only safe level of alcohol consumption is zero, it is important to understand what factors predict regular consumption of alcohol instead of only looking at the amount of alcohol consumption as in the two studies mentioned above.

The research question of this study is: To what extent can the occurrence of regular alcohol consumption (12 or more in a year) be predicted by the variables: depression level, age, sex, ethnicity, marital status and household income?

It is expected that age and depression level will be negatively correlated with the occurrence of alcohol consumption, whilst household income will be positively correlated (Garnett et al. 2022; Moore et al. 2005). In addition, expectation entails that male (vs female) and white (vs other ethnicities) will be positively correlated with the regular occurrence of alcohol consumption (Moore et al. 2005). Regarding marital status, it is expected that the married status will be positively associated with the regular occurrence of alcohol consumption compared to other marital statuses. That said, the latter was based on a study where the factor marital status consisted of just married and other (Moore et al. 2005), while in this study more categories were considered.

2 Methodology

2.1 Dataset

The dataset used was a subset of the data collected in the National Health and Nutrition Examination Survey (NHANES). The survey was a part of an annual program that investigated the health and nutrition of a representative sample of people in the United States. The data used contained information about 525 individuals that were collected for the NHANES 2007-2008 survey. This was a subset of the 12,946 individuals in that years' survey sample, out of which 78.4% were interviewed whilst 75.4% participants were examined in mobile examination centers. The NHANES survey was further subdivided into themed sections - such as the Alcohol Use questionnaire - with each of these sections having separate documentations that will be referred to later on.

The "full" dataset contained a wide range of variables related to the health of the individuals. This "full" dataset excluding the 'id' variable was used for the multiple imputation and stochastic regression missing data treatments. For the remaining data processing, analysis and modeling the data was further subsetted to only include variables relevant to the study (demographics, alcohol use and answers to depression screener questions). The selected variables are further described in Variables Description (Section 2.2).

2.2 Variables Description

Table 1 lists the variables used in the subset selection, which were utilized for the model in question. The table for the "full" dataset can be found in the Appendix B. The predictor variables [dep1...dep9] were sourced from the same Depression Screener, where respondents of age 18 to 150 were ought to assign a number (1)

Table 1: Variable descriptions

Role	Variable	Name	Type	Characteristics	Target
Outcome	Drink regularly	drink_regularly	Categorical	Binary, yes and no	m/f, age 20-150
Predictor	Sex	sex	Categorical	Binary, male and female	m/f, age 0-150
Predictor	Age	age	Numeric	Discrete	m/f, age 0-150
Predictor	Ethnicity	ethnicity	Categorical	Nominal, 5 categories	m/f, age 0-150
Predictor	Education	marital	Categorical	Nominal, 5 categories	m/f, age 20-150
Predictor	Marital status	marital	Categorical	Nominal, 5 categories	m/f, age 20-150
Predictor	Household income	household_income	Categorical	Nominal, 12 categories	m/f, age 0-150
Predictor	No interest in activity	dep1	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Feeling depressed	dep2	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Sleeping issues	dep3	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Feeling tired	dep4	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Eating issues	dep5	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Feeling bad about yourself	dep6	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Concentrating issues	dep7	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Moving and speaking issues	dep8	Categorical	Ordinal, 1-3 scale	m/f, age 18-150
Predictor	Suicidial thoughts	dep9	Categorical	Ordinal, 1-3 scale	m/f, age 18-150

to 3) regarding their mental and physical state within the last 2 weeks. Multiple signs of depression were measured this way, which can be combined to create an overall depression score.

The demographic variables - that being sex, age, ethnicity, education and income - were taken from the same screening component as well. The original authors of the dataset topcoded the variable age was at the value 80 for the respondents who were older than 80 years. Similarly, education was targeted at respondents of age 20 to 150, thus excluding younger participants. This was due to the fact that this question included responses such as AA degree and College Graduate. The variable marital was also targeted at respondents of age 20 to 150. Lastly, the variable income was ordinal, rather than continuous. As for the remaining demographic variables, namely sex, age, ethnicity and income, these were retrieved from target age 0 to 150. Finally, the drink_regularly variable was obtained from an Alcohol Use questionnaire targeted at ages 20 and up.

2.3 Software

All of the data cleaning, processing and modeling was performed in R version 4.3.2 (R Core Team 2023). The following packages were used: tidyverse was used for data manipulation (Wickham et al. 2019), the mice (van Buuren and Groothuis-Oudshoorn 2011) and ggmice (Oberman 2024) packaged were used for missing data visualizations and list-wise deletion and mean imputation, the kableExtra package was used for table styling (Zhu 2021), naniar package was used to make the visualization of missing data percentages (Figure 8) (Tierney and Cook 2023), Hmisc was utilized for mode imputation, vtable helped with the summary statistic table in the Appendix (Huntington-Klein 2023) and gtsummary was used to produce the summary tables for the two final models (Sjoberg et al. 2021).

2.4 Data processing

After arriving at the subset dataset, an Exploratory Data Analysis was performed. The distributions of the variables were investigated and the presence of missing data was found in the outcome variable and some of the depression questions. No outliers were found during the EDA. Additionally, the missingness seemed to be more prevalent among younger individuals, which gave a first indication of a lacking MCAR mechanism. The important findings of this step are presented in EDA Results (Section 3).

Following the EDA, the missing data problem was addressed. The extend, distributions and patterns of missingness were investigated. Testing was done to verify the missing data mechanism. This included performing a global test - Little MCAR test (Little 1986) and testing of the dependencies between missing values in one variable against observed values of other variables. The latter was done using t-tests for continuous variables, whilst categorical variables were checked via Chi-squared test and Fisher test (Soetewey, n.d.). The Fisher test with simulated p-values was used to verify outcomes for combinations of variables that included an expected frequency lower than 5, thus not meeting the assumptions of Chi-squared test (Soetewey, n.d.). When the assumptions of MCAR was not met, MAR was assumed.

Four solutions to the missing data problem were implemented: list-wise deletion, mean imputation, stochastic regression imputation and multiple imputation.

For list-wise deletion, all cases with one or more missing values were excluded from the modeling. Thus, the dateset was reduced by half to 263 observation.

The mean imputation method was implemented in the following way: For the missing depression questions, the mean of the observed values within the variable was computed and then the missing values were replaced by said mean value. This approach was taken, since treating ordinal variables on a Likert scale as continuous variables instead was appropriate (Wu, Jia, and Enders 2015). As found in the EDA (Section 3.1), all of the depression item distributions are heavily skewed towards 0. Because of that, '0.28', '0.53', '0.31', '0.20', '0.20' and '0.067' were imputed for 'dep2', 'dep3', 'dep5', 'dep6', 'dep8' and 'dep9' respectively. In turn, these low means even further skewed the distribution towards lower values. For drink_regularly - the outcome variable - the mode was computed rather than the mean. This was motivated by the need for a binary outcome variable in the logistic regression model that was utilized to answer the research question. The EDA suggested significantly more "yes" than "no" values in drink_regularly, hence the missing values were replaces by "yes". The 'drink_regularly' variable went from '397' 'yes' answers to '476', with '139' 'no' answers remaining unchanged. Therefore, after this data treatment the outcome ratio of the logistic regression was even more imbalanced, which could negatively affect the accuracy of the model.

Stochastic regression imputation

Multiple imputation

Following each missing data treatment, the values for the depression questions were summed up to create an overall depression score for each individual case. A sum was used - as opposed to other methods of aggregation (e.g. mean) - as it preserved a convenient interpretation of a unit increase in a depression score. This overall score was used for modeling as opposed to the individual depression levels.

To conclude, the different missing data treatments created three complete datasets and a single MIDS object that were then used for statistical analysis.

2.5 Modelling methodology

Including all of the variables in the two complete data sets was motivated by theoretical findings, since other researchers found a relationship between them and drinking habits. Therefore, verifying the significance of these predictors and their relative importance in the presence of other variables was important. Thus, a decision was made to create two logistical models including all of the variables, instead of a top down or bottom up approach to model building. As opposed to removing the non-significant predictors following the aforementioned model-building methods, it was decided to keep all the predictor variables and therefore have a more complex model. Following model creation, the two logistics models were compared, where the impact of the two different missing data treatments was evaluated. For easier interpretation the model coefficients were exponentiated. Occurrence of regular drinking was considered the "successful" outcome.

3 EDA Results

3.1 Descriptive statistics

Table 12 in Appendix A shows summary statistics for each of the variables within the dataset; including mean values, standard deviations, IQR statistics and data range values. For categorical variables, a list of possible categories and their respective proportions was provided to replace the continuous summary statistics. Lastly, the column N shows the amount of cases with present data - that being non-NA values.

In general, it was observed that all variables were interpreted as a factor, excluding age and the multiple depression levels of dep. Table 1 suggested that dep should in fact be categorical ordinal and should therefore be cast as a factor. That said - and as mentioned in Section 2.4 - keeping the levels of dep as a numerical continuous datatype was beneficial for the missing data problem.

The dataset contained a total of 525 observations, each with 17 variables.

The dichotomous outcome variable drink_regularly had 307 cases of "yes" and 107 cases of "no", having a outcome balance of 69% and 31% respectively. This outcome ratio could be considered imbalanced, which could affect the accuracy of the logistic regression model. Additionally, the total amount of value entries (N) of 446 suggested that 79 cases contained values outside of the set of possible binary values - most likely being missing values. Table 2 further confirmed this.

Table 2: Drink regularly value distributions

drink_regularly	n
no	139
yes	307
NA	79

Predictor sex was a dichotomous variable with a balanced frequency distribution across the values "male" and "female", that being 48% and 52% respectively. 525 entries contained one of these values, suggesting that the variable did not contain missing data.

The predictor age was the only continuous variable present within the sub-selected dataset. Although the survey was targeted at respondents of age 0-150 for most variables - the documentation even mentioning the topcoded entries for age 80+ - the dataset seemed to only contain cases of people between the age of 20 and 69. Moreover, Figure 1 suggested a uniform distribution of the age variable. Like sex, age had 525 cases of non-NA values, hence the variable did not contain missing data values.

Predictor ethnicity had 5 categories, with non-hispanic_white being the most prevalent category with 220 cases (42% of total), all the while other was the most infrequent category with 25 cases (5%). A total of 525 cases contained ethnicity data, once again suggesting no presence of missing data values within this variable.

Predictor education was similar to ethnicity, having 5 categories. That said, the frequencies of said categories seemed to be less out of proportion, with some_college being the most frequent category with 155 (30%) cases. Whilst the data was retrieved from respondents of ages 20 and higher, no missing data values were observed within the variable. This could be further justified by the fact that the minimum age within the used dataset was 20, therefore foregoing possible issues with younger participants being unable to provide data for this specific variable.

The predictor variable marital contained 6 categories. It should be noted that the category value married exceeded the average frequency of other categories (that being 49.2) by a large margin, as can be seen in Figure 2. Specifically, 279 cases (53%) were married, with the other 5 categories making up the remaining 47% of the cases. never_married was the most frequent among those other 5 categories with 102 (19%) cases, whilst separated was the most infrequent category with only 14 (3%) cases. Furthermore, the meaning

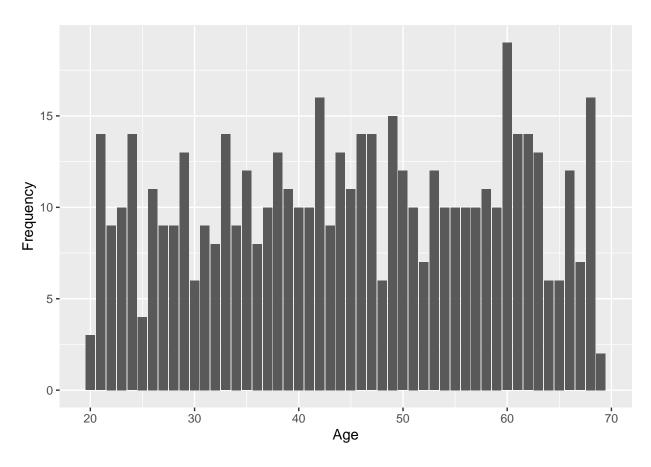


Figure 1: Distribution of age

of never_married and living_with_partners was ambiguous in the sense that a person specifically living with their (non-married) partner could fall into both these categories.

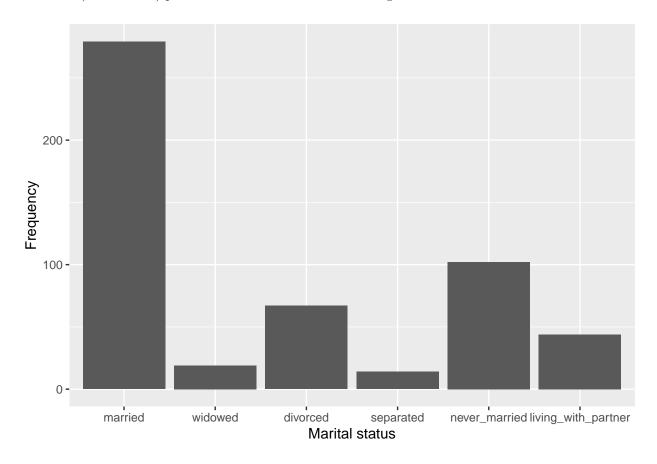


Figure 2: Distribution of marital status categories

Predictor income was an ordinal variable formed by 12 levels, ranging from income values 0 to 100000+. This data, like age, was topcoded at the value 100000. This also explained the highest income category - that being 100000+ - having 76 cases (9%), as can be seen in Figure 3. If the latter case is ignored, the most frequent category was instead 25000:34999, which coincidentally was the mid-range category of income data. 525 cases contained only observed income data, therefore the variable did not contain missing data values.

The multiple levels of depression all had ranging scores between 0 and 3, with increments of 1 specifically. A higher score indicated an agreement with the signs of depression described in the survey. Only dep1 and dep7 had complete data data, whilst the other levels had varying amounts of missing data. Missing data could possibly be caused by the respondents being reluctant to answers these questions. It was also observed that dep2, dep3, dep5, dep6 had the same amount of missing data values, hence it was possible that they had a shared cause of missing data. Lastly, dep9 only had 18 cases of scores above 0, whilst also having the lowest mean value out of all depression levels. dep9 described the presence of suicidal thoughts, hence it made sense that this was the lowest average score out of all levels. On the contrary, dep4 (feeling tired) had the highest average score. Overall, the score distribution were heavily skewed towards the 0 values.

3.2 Outliers

For the only continuous predictor age, a boxplot was utilised to find potential outliers . Figure 4 shows the distribution of age in said boxplot, revealing no possible outliers. This was to be expected, since age was

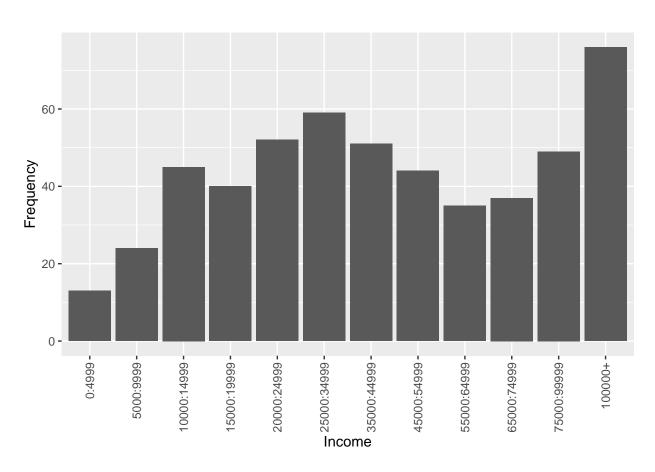


Figure 3: Distribution of income

uniformly distributed as was mentioned in Section 3.1.

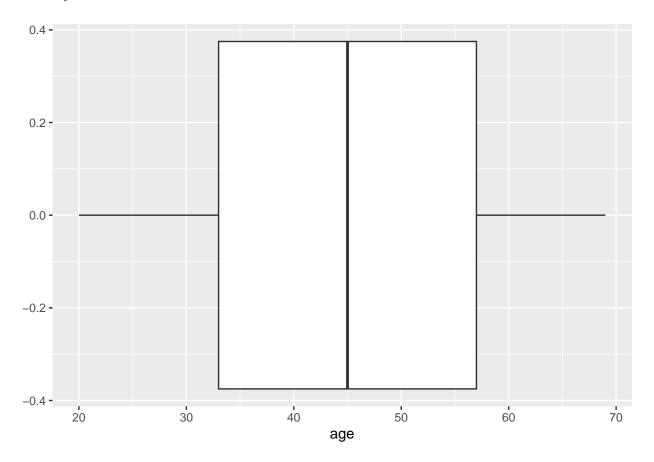


Figure 4: Boxplot of age

Looking at the distributions of the various categorical variables, the marital showed the aforementioned imbalance in frequency distribution, with the category married being overly dominant within the data. It was considered combining the other marital categories into one, as their infrequency could allude to being possible outliers. Table 3 shows the interrelations between the martial variable and the outcome drink_regularly. From this, it was concluded that combining the remaining 5 categories - that being widowed, divorced, separated, never_married and living_with_partner - was not feasible, since these relations seemed to differ per category. For example, widowed had more "no" cases compared to "yes", whilst the relation was reversed for separated.

Table 3: Contingency table of marital status vs. drinking regularly

	no	yes
married	81	175
widowed	11	8
divorced	14	48
separated	4	8
never_married	23	45
living_with_partner	6	23

3.3 Correlations

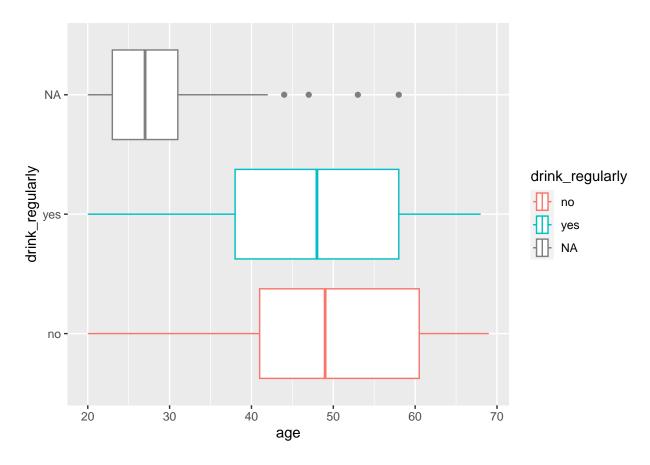


Figure 5: Correlations of age vs. drink regularly

Figure 5 shows the distributions of age over the outcome variable drink_regularly in a boxplot. Not considering the NA values, age did not seem to be strongly correlated with drink_regularly, with "no" cases having only slightly higher ages than its counterpart. It should however be noted that the NA values of drink_regularly were primarily present in younger participants, therefore possibly attenuating the correlation effect between these two variables. For example, a large amount of missing values belonging to "yes" could shift the distribution of these cases towards lower age values, hence increasing the difference in distributions for each drink_regularly outcome.

Contingency tables and frequency distribution plots (including NA values) were used to observe the correlation between the categorical predictors and the outcome variable. From these, it was observed that sex seemed to be highly correlated with drink_regularly; 172 cases of male drank regularly, whilst only 39 didn't. Compared to the 135 cases of female of "yes" and 100 cases of "no", this ratio seemed to differ greatly per sex category. The missingness of drink_regularly was evenly distributed across both male and female cases.

Likewise, marital showed a similarly strong correlation effect. The category divorced had a significantly higher ratio of respondents who drank regularly, compared to cases of widowed, where respondents were more likely to not drink regularly as can be seen in Figure 6. It was also noted that the missing data of drink_regularly was not evenly distributed across the marital categories. Rather, the missingness was more prevalent in the never_married and living_with_partner cases. This possibly ties back into the fact that more data was missing amongst younger respondents, which can be directly seen in Figure 7 where never_married and living_with_partner have more cases of a younger age as well.

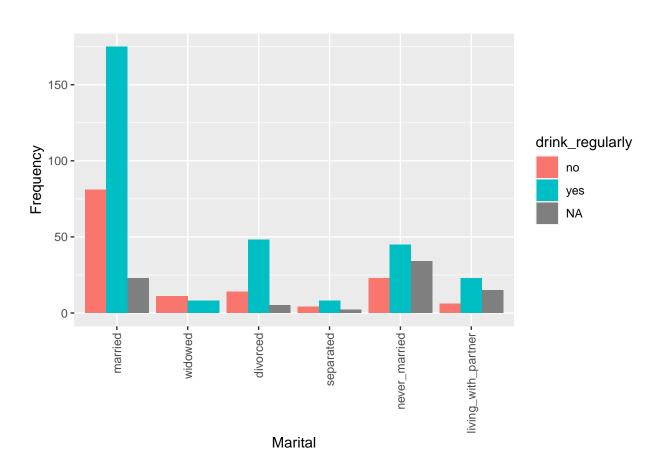


Figure 6: Correlations of marital vs. drink regularly

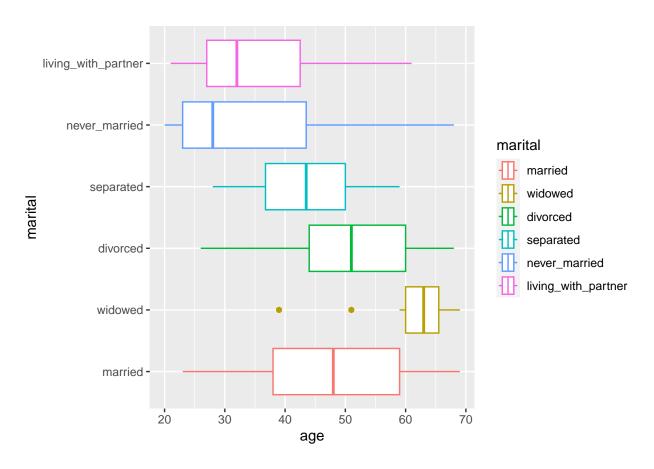


Figure 7: Age distributions over marital statuses

Ethnicity showed a weaker correlation effect with the outcome variable. Only non-hispanic_black and other showed different frequency distributions compared to the other categories. Missing data of drink_regularly was present in all categories of ethnicity, though other_hispanic and other had close to none compared to the remaining categories. The variable education was considered to have the weakest correlation with drink_regularly, having similar success ratios across all categories all the while missing data of drink_regularly was also evenly spread.

income was considered to be correlated with the outcome variable. Performing a similar analysis, it was observed that respondents with an income up until 24999 were less likely to drink regularly than cases with a higher income. Akin to education, missing data of drink_regularly seemed to be evenly spread across the income values.

Finally, all levels of depression showed an effect of correlation with drink_regularly, where higher scores tended to decrease the ratio of "yes" to "no" cases, that is to say that respondents were less likely to drink regularly if signs of depression were present.

4 Missing data problem

4.1 Missing data and response patterns

Firstly, the overall distribution of missingness within the dataset was investigated.

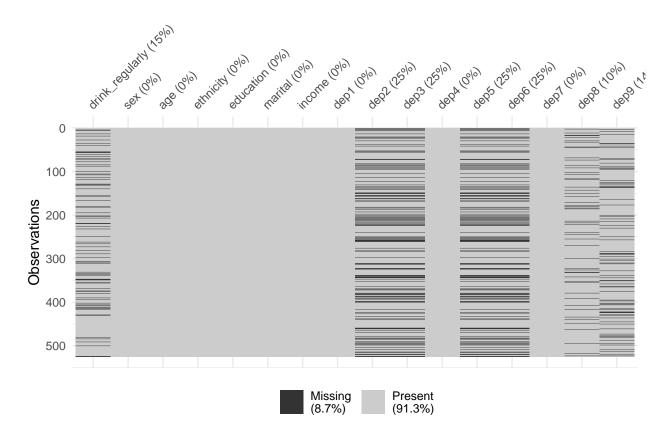


Figure 8: Distribution of missing data in each variable

As can be seen on Figure 8, 8.2% of the data was missing. The missing values occurred in the outcome variable drink_regularly and in the responses to questions dep2, dep3, dep5, dep6, dep8 and dep9 that

created the depression score variable. 15% of responses were missing for the predictor variable. 25% of the responses were missing for the individual depression questions 2, 3, 5 and 6, whilst 10% were missing for question 8. Finally, 14% of data was missing for question 9.

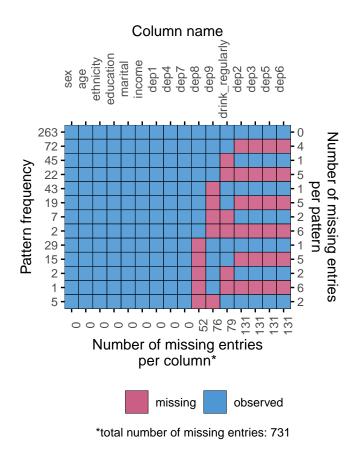


Figure 9: Response patterns and their frequency

The missing data patterns were further investigated by looking at the response patterns. Figure 9 reveals that there were 13 distinct response patterns in the dataset, with the missingness *not* being monotone. The most frequent pattern was no missing entries, with 263 cases. It is important to note that the depression questions 2, 3, 5 and 6 were always either all present or all missing. It is very probable that the reason for the item non-response regarding these depression levels was the same, since there were no cases with partial missingness in these 4 variables.

Based on the missingness pattern of the depression items, 41% of the overall depression score included at least one missing value.

4.2 Missing data mechanism

Missing completely at random (MCAR) missingness mechanism is often an important assumption for statistical analysis, including this one. To gain some inside whether the data was MCAR or not, we deployed a variety of tests. If missing values of a variable was MCAR, said variable should not have a significant dependency with other (observed) variables.

Firstly, Little MCAR test was performed to verify if the missing data was MCAR at a global level, thus for all of the instances of missingess. The test was significant ($\chi^2(164) = 465.18, p < 0.01$), therefore the data was assumed to *not* be MCAR.

Since the data being MCAR can be questioned following the Little's test, a t-test was performed for all missing values vectors and numerical variables to check which variables were the likely culprit. The test compared the observed means of a given numerical variable within the group of individuals that had an observed value and the group with a missing value for another variable. Effectively testing if there is a significant difference in the continuous variable in the group that answered another question and the group that did not. Since the null hypothesis suggests no difference in means across the groups, a single significant value for a missingness of a given variable suggests that the missing values in that variable depend on the observed values of another variable. Therefore, it is likely that the missing values are not MCAR. Due to the identical pattern of responses in dep2, dep3, dep5 and dep6 it was sufficient to only test once for the dependency of their missing values. By the design of the test, it was impossible to test the dependency of missing values and observed values within the same variable, thus these values were missing from the table.

Assuming an alpha of 0.05, it was observed that missing values of drink_regularly were dependent on age, dep2 and dep9. Similarly, dep2, dep3, dep5 and dep6 seemed to be dependent on age and the remaining depression questions. For missingness in dep8 and dep9, there were no significant differences across groups in any of the numerical variables. These tests suggested that at least drink_regularly, dep2, dep3, dep5 and dep6 were not MCAR, thus MAR was assumed for them. In Table 4 the exact t-statistic and the p-value are reported.

Table 4: Dependency t-test: mean comparison in numerical variables across missing values and observed values in the other variables

numerical variable	missing drink_regularly	missing $dep2/3/5/6$	missing dep8	missing dep9
age	t = 19.3, pVal = 3.1e-45	t = 1.38, pVal = 0.17	t = -1.16, $pVal = 0.249$	t = -0.884, pVal = 0.379
dep1	t = 1.39, pVal = 0.167	t = -6.72, $pVal = 2.88e-10$	t = 0.464, pVal = 0.644	t = -0.444, pVal = 0.658
dep2	t = 3.63, pVal = 0.000405	-	t = 0.332, pVal = 0.742	t = 1.22, pVal = 0.224
dep3	t = 0.797, $pVal = 0.428$	-	t = -0.137, $pVal = 0.892$	t = 0.0545, $pVal = 0.957$
dep4	t = -0.541, pVal = 0.59	t = -7.8, $pVal = 6.11e-13$	t = -0.68, pVal = 0.499	t = -1.28, pVal = 0.202
dep5	t = 2.01, pVal = 0.0466	-	t = -0.605, $pVal = 0.549$	t = -0.731, pVal = 0.467
dep6	t = 0.822, pVal = 0.414	-	t = 2.3, pVal = 0.0242	t = 0.00637, $pVal = 0.995$
dep7	t = -0.382, pVal = 0.703	t = -8.19, $pVal = 1.24e-13$	t = -0.239, $pVal = 0.812$	t = -0.0635, $pVal = 0.949$
dep8	t = -0.32, pVal = 0.75	t = -4.26, $pVal = 3.86e-05$	-	t = 0.595, pVal = 0.553
dep9	t = 2.48, pVal = 0.0135	t = -2.64, pVal = 0.00947	t = -0.295, pVal = 0.769	-

Table 5: Independency Chi-squared test

categorical variable	missing drink_regularly	missing $dep2/3/5/6$	missing dep8	missing dep9
drink_regularly	-	$X^2 = 4.2$, $pVal = 0.0404$	$X^2 = 1.52$, $pVal = 0.218$	$X^2 = 0.464$, $pVal = 0.496$
sex	$X^2 = 1.09$, $pVal = 0.296$	$X^2 = 5.04$, $pVal = 0.0248$	$X^2 = 0.469$, $pVal = 0.494$	$X^2 = 0.317$, pVal = 0.573
ethnicity	$X^2 = 5.49$, $pVal = 0.241$	$X^2 = 1.64$, $pVal = 0.802$	$X^2 = 7.74$, $pVal = 0.102$	$X^2 = 5.8$, $pVal = 0.215$
education	$X^2 = 2.7$, $pVal = 0.609$	$X^2 = 5.72$, $pVal = 0.221$	$X^2 = 1.63$, $pVal = 0.803$	$X^2 = 5.13$, $pVal = 0.275$
marital	$X^2 = 55.7$, $pVal = 9.58e-11$	$X^2 = 22.2$, $pVal = 0.000477$	$X^2 = 5.08$, $pVal = 0.407$	$X^2 = 3.97$, pVal = 0.553
income	$X^2 = 2.94$, pVal = 0.991	$X^2 = 8.84$, $pVal = 0.636$	$X^2 = 9.4$, pVal = 0.585	$X^2 = 17.3$, $pVal = 0.0995$

Since the t-test was not appropriate for categorical variables, we performed the Chi-squared test for said variables. The null hypothesis of the tests entailed no significant relationships between the categorical variables. The test compared observed frequencies to expected frequencies, if there was no relationship between the variables.

The outcomes of the test are presented in Table 5. However, only martial with missingness of drink_regularly and marital with missingness of dep2, dep3, dep5 and dep6 were significant. Thus, it further supported the non-MCAR behaviour of missing data in these items.

However, the Chi-squared test had an requirement that the smallest expected frequencies had to be higher than 5. This requirement was not met for some combinations of missing values and categorical variables. Specifically: missing dep8/9 and ethnicity, marital, income; missing dep2/3/5/6 and marital, income; missing drink_regularly and ethnicity, marital, income. Since this assumption was not met for these

combination, the p-values might not have been correctly estimated. Therefore, the Fischer test - which has the same hypothesis, but not the same assumption - was performed for these combinations.

Table 6: Fisher test

categorical variable	missing drink_regularly	missing dep $2/3/5/6$	missing dep8	missing dep9
ethnicity	pVal = 0.232	-	pVal = 0.0804	pVal = 0.21
marital	pVal = 1e-05	pVal = 0.00089	pVal = 0.399	pVal = 0.446
income	pVal = 0.987	pVal = 0.64	pVal = 0.561	pVal = 0.058

The outcomes of the Fisher test are presented in Table 6. Like in the case of Chi-squared test, only martial with missingness of dep2, dep3, dep5 and dep6 were significant. Therefore, it was concluded the dependence of missingness in these variables on multiple other observed variables and rejected MCAR in their case.

In all of the tests above, dep8 and dep9 did not seem to be dependent on any of the observed variables. Thus, perhaps MCAR could be assumed for these variables. However, since the depression scores will be collapsed into a single depression score ('dep') and other depression questions were MAR, the overall score was also assumed to be MAR.

5 Imputation results

Four imputed datasets were created for the analysis models. The imputed values of interest were drink_regularly, dep2, dep3, dep5, dep6, dep8, dep9.

5.1 List-wise deletion

The data before applying list-wise deletion had 525 cases. After performing the deletion-based treatment, the resulting dataset had 263 cases left. The ratio of "yes" to "no" cases in the outcome variable drink_regularly changed from 2.21 to 1.86, hence decreasing by -15.84%.

Table 7 shows the means of the multiple depression levels in the original data set and the resulting dataset from list-wise deletion. It was observed that the mean values of dep8 and dep9 decreased by half in the resulting dataset, suggesting that this missing data treatment deleted cases with higher dep8 and dep9 values due to missing values in either drink_regularly or the depression levels. The mean values of the remaining levels stayed roughly the same, showing no significant increase or decrease.

Table 7: Depression means for list-wise deletion

data	dep2	dep3	dep5	dep6	dep8	dep9
original result				$0.201 \\ 0.217$		

Table 8 shows the change of variance across the multiple depression levels. Similar to the affect on mean values, variances of depression only showed significant changes in dep8 and dep9, furthermore suggesting that missing data was present in other variables for particular dep8 and dep9 values respectively. The other depression levels showed only small increases or decrease in variance, which is due to the sampling variability as a consequence of list-wise deletion. Although dep8 and dep9 were assumed to be MCAR in Section 4.2, these did in fact show the most substantial changes in their distribution.

TODO: explain the above, why?!

Table 8: Depression variance for list-wise deletion

data	dep2	dep3	dep5	dep6	dep8	dep9
original	0.34	0.733	0.494	0.318	0.344	0.138
result	0.38	0.677	0.487	0.331	0.196	0.053

Lastly, the depression values were still discrete - the values ranged from 0 to 3. This was expected, since this missing data treatment didn't change / impute the values of the dataset.

5.2 Mean imputation

Mode imputation was applied to the missing values in drink_regularly. As mentioned in Section 2.4, "yes" was the most occurring case in the outcome variable, therefore missing values were replaced by "yes". This resulted in the ratio of "yes" to "no" cases changing from 2.21 to 2.78, increasing by 25.79%. It is worthy to note that this is a 41.63% total increase compared to the ratio of list-wise deletion mentioned in Section 5.1. As for the depression levels, mean imputation did not change the mean values. The overall variance of the depression levels decreased, which is an expected result of mean imputation - imputing missing data with the same value attenuates the variance of the variable.

5.3 Stochastic regression

The 3rd imputation method utilised a single stochastic regression model to treat the missing. The ratio of "yes" to "no" cases in the outcome variable drink_regularly showed minimal change when observing the imputed data, with the original and imputed data having a ratio of 2.21 and 2.26 respectively.

Due to the nature of the stochastic regression model, the range of 0 to 3 with increments of 1 no longer held. To illustrate, dep2 had a minimum value of -1.03 and a maximum value of 3.61, with values other than 0, 1, 2 or 3 existing within the variable. This also caused the variance of the assumed MAR depression levels to increase, as can be seen in Table 10. The assumed MCAR depression variables - namely dep8 and dep9 - showed non-substantial increases in their variance. The proportional change in the mean values was also only present in dep2, dep3, dep5 and dep6, whilst the assumed MCAR levels once again showed minimal change, as shown in Table 9.

Table 9: Depression means for stochastic regression

data	dep2	dep3	dep5	dep6	dep8	dep9
original	0.282	0.533	0.310	0.201	0.203	0.067
result	0.426	0.706	0.407	0.365	0.198	0.057

Table 10: Depression variance for stochastic regression

data	dep2	dep3	dep5	dep6	dep8	dep9
original result			0.494 0.556			

The density plots of Figure 10 were used to evaluate the imputation results. It was observed that the assumed MCAR (dep8 and dep9) depression levels had very similar distributions to the observed data, more so than the assumed MAR levels that clearly showed higher variances and mean values. This is how the imputed values should behave, and therefore the resulting imputations were accepted.

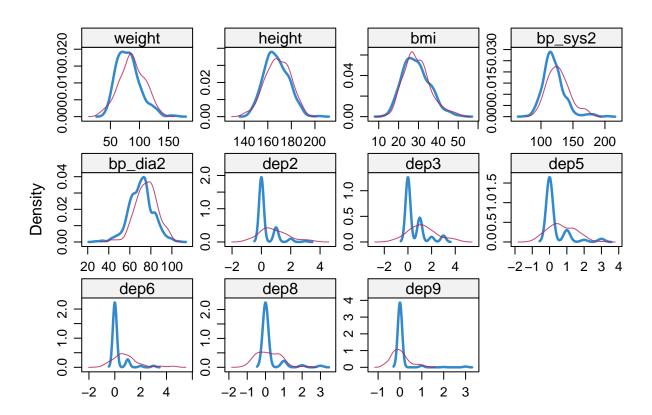
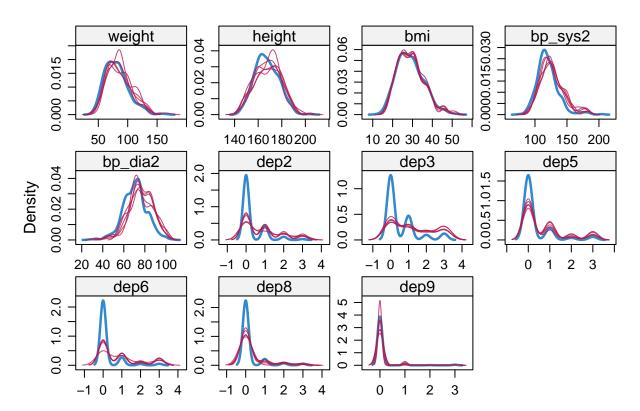
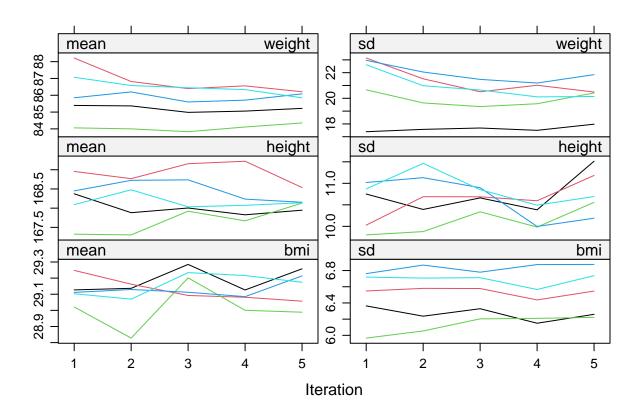


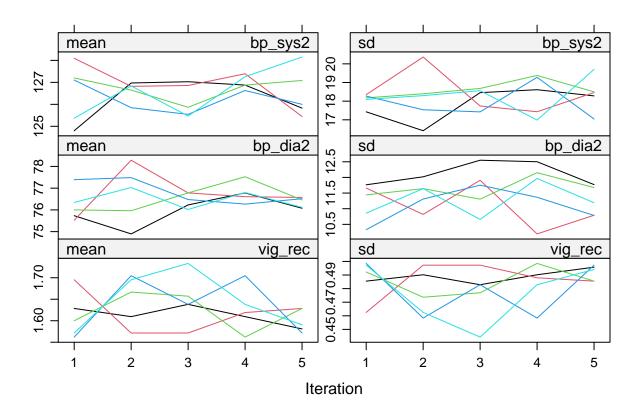
Figure 10: Density plots for single stochastic regression

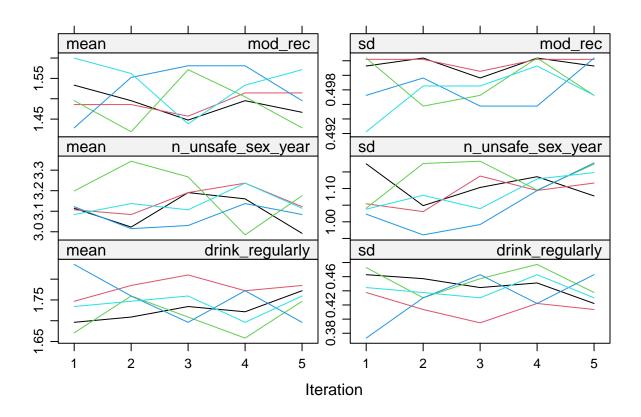
5.4 Multiple imputation

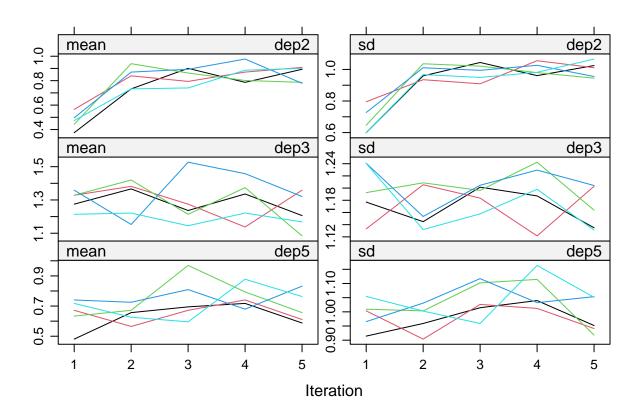
. . .

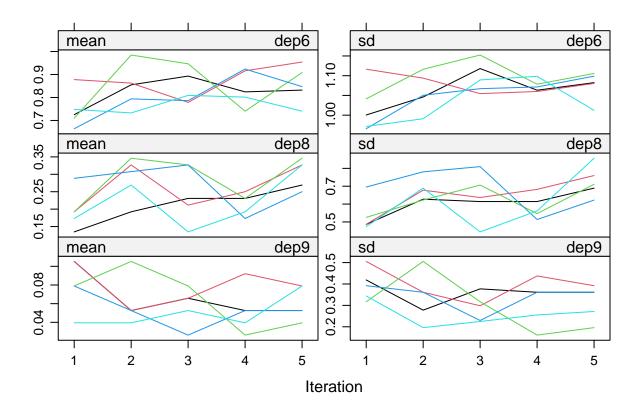




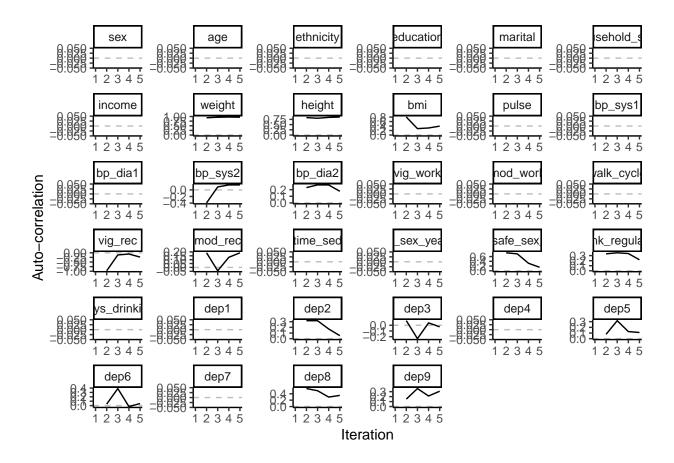








Warning: Removed 36 rows containing missing values ('geom_line()').



6 Modelling

6.1 Interpretation of the two models

Table 11: Model fit statistics

model	AIC	BIC	Residual_Deviance
listwise deletion	342.6925	442.7129	286.6925
mean imputation	576.6865	696.0617	520.6865

Two logistic models were created, one for each of the imputed datasets that resulted from both the adhoc mean imputation and listwise deletion missing data methods. The interpretation below only includes significant predictors, since most of the model's predictors were non-significant. That said, they are still reported in the model summary tables, as can be seen Table 13 and Table 14 in Appendix A.

Looking at the listwise deletion model, only sex (p < 0.001) and the marital category divorced (p < 0.001) were significant predictors, whilst all the other predictors (including the intercept) were insignificant. The odds ratio of females drinking regularly compared to males was 0.16[0.08, 0.31], meaning they were 0.16 times as likely to drink regularly compared to males. The odds ratio of divorced respondents compared to those who were married was 7.37[2.54, 25.0], meaning divorced people were 7.37 times as likely to drink regularly compared to married people.

In the mean imputation model, age (p < 0.001) was also a significant predictor. This was in addition to sex (p < 0.001) and marital status divorced (p < 0.004). Moreover, the intercept (p < 0.001) was also

significant. For a unit increase in age the odds ratio of drinking regularly decreases 0.97[0.95, 0.99] times. The odds ratio of females drinking regularly compared to males was 0.24[0.14, 0.38], meaning they were 0.24 times as likely to drink compared to males. The odds ratio of people with the marital status divorced compared to people with the marital status married was 3.05[1.47, 6.69], meaning divorced people were 3.05 times as likely to drink regularly compared to married people. If all predictor variables were in their reference state, the baseline odds ratio was 20.5[3.40, 136]. Looking at the model fit statistics, the listwise deletion model performed better with a lower AIC, BIC and residual deviance value, as is shown in Table 11.

6.2 Results comparison ad-hoc methods

Following Section 6.1, the answer to the research question will differ depending on the ad-hoc method used to treat the missing data. Said difference is comprised of: the number of significant predictors, the odds ratios, standard errors and the fitness statistics. The SE of the mean imputation model was lower than the listwise deletion model, which can be see in Table 14 and 13.

It was concluded that the missing data treating methods caused biased results within each model, since these methods assume the missingness to be MCAR. This assumption does not hold, in case the data is assumed to be MAR - as was described in Section 4.2. In the specific case of logistic regression - which was utilised in this study - listwise deletion could still give unbiased results even if the missingness isn't MCAR, but only if the missing values are either in the predictor variables or in the outcome variable. From the EDA and missing data specification it was observed that both predictor and outcome variables contained missing data, hence the results were biased as well.

When listwise deletion is used on a dataset where the missingness isn't MCAR, it will result in a bias in the regression coefficients, with standard errors that are too large. As the models in this study were logistic regression models, the regression coefficients were transformed into odds ratios instead. Another negative of listwise deletion is that it is wasteful, a lot of data goes unused. This is also the case in this study, as 263 out of a total of 525 cases were deleted or in other words only half the cases were used. This might explain why the listwise deletion model has a lower D value; there is just a lot less data that might not fit in the model. Another consequence of removing so much data from the dataset is that it becomes more difficult to find effects, this is a possible explanation for why the listwise deletion model had less significant predictors.

Using mean imputation on a dataset where the missingness isn't MCAR will give biased results and underestimated standard errors. It is indeed the case that the standard errors in the mean imputation model are lower than those in the listwise deletion model. As listwise deletion usually overestimates the standard errors, the real values are probably somewhere in between.

So as both methods were used on data where the missingness wasn't MCAR, the created models were biased in multiple ways.

7 Conclusion

The research question was To what extent can the occurrence of regular alcohol consumption (12 or more in a year) be predicted by the variables: depression level, age, sex, ethnicity, marital status and household income? Here, it was expected that sex male, ethnicity non-hispanic_white and marital status married would exhibit a positive relation with drinking regularly, whilst age and depression would have a negative relation with said outcome variable.

The resulting listwise deletion model - using a logistic regression approach - only had sex and marital status divorced (in reference to married) as significant predictors. Using this ad-hoc method, no significant relation between the predictors depression and ethnicity and the outcome variable drink_regularly could be deduced. Additionally, divorced was positively related to drinking regularly, which goes against the expectation of categories other than married exhibiting a negative relation with the outcome. The

model did suggest that male respondents are more likely to drink regularly than female participants, and can therefore be used to predict alcohol consumption.

As for the mean imputation model, the results similarly suggested non-significant predictors for ethnicity and depression. age was significant, as opposed to in the listwise deletion model - this was in addition to the other significant predictors, those being the married status divorced and sex. Once again, the model aligned with expectations of male respondents drinking more regularly. age also showed a negative relation with the outcome, albeit a small decrease per unit change of age. Similar to the previous model, divorced showed an unexected positive behaviour with the outcome variable.

Overall, it was concluded from both models that depression and ethnicity cannot be used to predict whether a case is drinking regularly. Marital status is a valid predictor, although its relation does not align with research previously done by others. Whether age can be used as a predictor, depends on the ad-hoc method used to treat missing data. Lastly, the coefficients of significant predictors in both models differed greatly. The coefficient of divorced in the listwise deletion model exceeded the mean imputation variant twofold.

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A Appendix

Table 12: Summary statistics

Variable	N	Mean	Std. Dev.	Min	Pctl. 25	Pctl. 75	Max
drink_regularly no yes sex male	446 139 307 525 254	31% 69% 48%					
 femaleageethnicity mexican_american other_hispanic	271 525 525 95 61	52% 45 18% 12%	14	20	33	57	69
non-hispanic_white non-hispanic_black other education no_high_school	220 124 25 525 58	42% 24% 5% 11%					
some_high_school high_school_grad some_college college_grad marital	101 123 155 88 525	19% 23% 30% 17%					
 married widowed divorced separated never_married	279 19 67 14 102	53% 4% 13% 3% 19%					
living_with_partner income 0:4999 5000:9999 10000:14999	44 525 13 24 45	8% 2% 5% 9%					
15000:19999 20000:24999 25000:34999 35000:44999 45000:54999	40 52 59 51 44	8% 10% 11% 10% 8%					
55000:64999 65000:74999 75000:99999 100000+ dep1	35 37 49 76 525	7% 7% 9% 14% 0.41	0.79	0	0	1	3
dep2 dep3 dep4 dep5 dep6	394 394 525 394 394	0.28 0.53 0.76 0.31 0.2	0.58 0.86 0.9 0.7 0.56	0 0 0 0	0 0 0 0	0 1 1 0 0	3 3 3 3
dep7 dep8 dep9	525 473 449	0.32 0.2 0.067	0.71 0.59 0.37	0 0 0	0 0 0	0 0 0	3 3 3

Table 13: Listwise deletion model

Characteristic	\mathbf{OR}	\mathbf{SE}	p-value
(Intercept)	6.71	1.28	0.14
sex			
male	_	_	
female	0.16***	0.350	< 0.001
age	1.00	0.013	0.8
ethnicity			
mexican_american	_		
$other_hispanic$	1.49	0.594	0.5
non-hispanic_white	1.58	0.435	0.3
non-hispanic_black	0.55	0.485	0.2
other	1.04	0.792	> 0.9
education			
no_high_school	_	_	
$some_high_school$	0.82	0.582	0.7
high_school_grad	1.30	0.589	0.7
some_college	1.05	0.604	> 0.9
$college_grad$	1.66	0.647	0.4
marital			
married	_	_	
widowed	1.37	0.711	0.7
divorced	7.37***	0.578	< 0.001
separated	1.98	1.14	0.5
never_married	1.34	0.435	0.5
living_with_partner	4.26	0.862	0.093
income			
0:4999	_	_	
5000:9999	0.17	1.24	0.15
10000:14999	0.43	1.07	0.4
15000:19999	0.43	1.05	0.4
20000:24999	0.40	1.04	0.4
25000:34999	0.65	1.04	0.7
35000:44999	0.79	1.07	0.8
45000:54999	0.40	1.12	0.4
55000:64999	1.06	1.13	> 0.9
65000:74999	0.36	1.11	0.4
75000:99999	0.56	1.13	0.6
100000+	0.79	1.06	0.8
dep	1.03	0.051	0.6
¹ p<0.05; p<0.01; p<0			

Table 14: Mean imputation model

Characteristic	OR	\mathbf{SE}	p-value
(Intercept)	20.5**	0.933	0.001
sex			
male	_	_	
female	0.24***	0.247	< 0.001
age	0.97***	0.009	< 0.001
ethnicity			
mexican_american	_	_	
other_hispanic	1.19	0.411	0.7
non-hispanic_white	1.42	0.338	0.3
non-hispanic_black	0.57	0.367	0.12
other	0.59	0.543	0.3
education			
no_high_school	_	_	
$some_high_school$	1.16	0.428	0.7
high_school_grad	1.48	0.422	0.4
some_college	1.22	0.420	0.6
college_grad	1.98	0.479	0.2
marital			
married	_	_	
widowed	0.85	0.547	0.8
divorced	3.05**	0.385	0.004
separated	1.36	0.678	0.7
never_married	1.22	0.335	0.5
living_with_partner	2.28	0.508	0.10
income			
0:4999	_	_	
5000:9999	0.64	0.825	0.6
10000:14999	0.92	0.756	> 0.9
15000:19999	0.40	0.738	0.2
20000:24999	0.51	0.732	0.4
25000:34999	1.20	0.752	0.8
35000:44999	0.87	0.753	0.9
45000:54999	0.96	0.791	> 0.9
55000:64999	0.93	0.785	>0.9
65000:74999	0.60	0.790	0.5
75000:99999	1.19	0.785	0.8
100000+	1.18	0.752	0.8
dep	1.02	0.035	0.6
¹ p<0.05; p<0.01; p<0	0.001		
2 OR = Odds Ratio, SE		rd Error	•

 $^{^{2}}$ OR = Odds Ratio, SE = Standard Error

B Appendix

Table 15: Variable descriptions

Role	Variable	riable Further.Description		Type	Characteristics	Target	
Outcome	Drink regularly	at least 12 drinks in a year	drink_regularly	Categorical	Binary, yes and no	m/f, age 20-150	
Predictor	Sex		sex	Categorical	Binary, male and female	m/f, age 0-150	
Predictor	Age	years at screening	age	Numeric	Discrete	m/f, age 0-150	
Predictor	Ethnicity		ethnicity	Categorical	Nominal, 5 categories	m/f, age 0-150	
Predictor	Education		marital	Categorical	Nominal, 5 categories	m/f, age 20-150	
Predictor	Marital status		marital	Categorical	Nominal, 5 categories	m/f, age 20-150	
Predictor	household income	annual in USD	household_income	Categorical	Nominal, 12 categories	m/f, age 0-150	
Predictor	No interest in activity		dep1	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Feeling depressed		dep2	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Sleeping issues		dep3	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Feeling tired		dep4	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Eating issues		dep5	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Feeling bad about yourself		dep6	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Concentrating issues		dep7	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Moving and speaking issues		dep8	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Predictor	Suicidial thoughts		dep9	Categorical	Ordinal, 1-3 scale	m/f, age 18-150	
Imputation	Household size	number of people	household_size	Numeric	Discrete	m/f, age 0-150	
Imputation	Weight	in kg	weight	Numeric	Continious	m/f, age 0-150	
Imputation	Height	standing in cm	height	Numeric	Continious	m/f, age 2-150	
${\bf Imputation}$	Body Mass Index	in kg/m^2	bmi	Numeric	Continious	m/f, age 2-150	
Imputation	Pulse	beats per minute	pulse	Numeric	Discrete	m/f, age 8-150	
Imputation	Systolic blood pressure	1st reading, in mm Hg	bp sys1	Numeric	Discrete	m/f, age 8-150	
Imputation	Diastolic blood pressure	1st reading, in mm Hg	bp dia1	Numeric	Discrete	m/f, age 8-150	
Imputation	Systolic blood pressure	2nd reading, in mm Hg	bp_sys2	Numeric	Discrete	m/f, age 8-150	
Imputation	Diastolic blood pressure	2nd reading, in mm Hg	bp_dia2	Numeric	Discrete	m/f, age $8-150$	
Imputation	Vigorous work activity		vig work	Categorical	Binary, yes and no	m/f, age 12-150	
Imputation	Moderate work activity		mod work	Categorical	Binary, yes and no	m/f, age 12-150	
Imputation	Walking or cycling		walk cycle	Categorical	Binary, yes and no	m/f, age 12-150	
Imputation	Vigorous sport activity		vig rec	Categorical	Binary, yes and no	m/f, age 12-150	
Imputation	Moderate sport activity		mod_rec	Categorical	Binary, yes and no	m/f, age 12-150	
Imputation	Sedentary activity	in minutes	time sed	Numeric	Discrete	m/f, age 12-150	
Imputation	Number of sex	in a year	n sex year	Categorical	Nominal, 7 categories	m/f, age 20-59	
Imputation	Frequency of unsafe sex	in a year	n unsafe sex year	Categorical	Nominal, 5 categories	m/f, age 20-59	
Imputation	Number of days drinking aclohol	v	days drinking	Numeric	Discrete	m/f, age 20-150	