

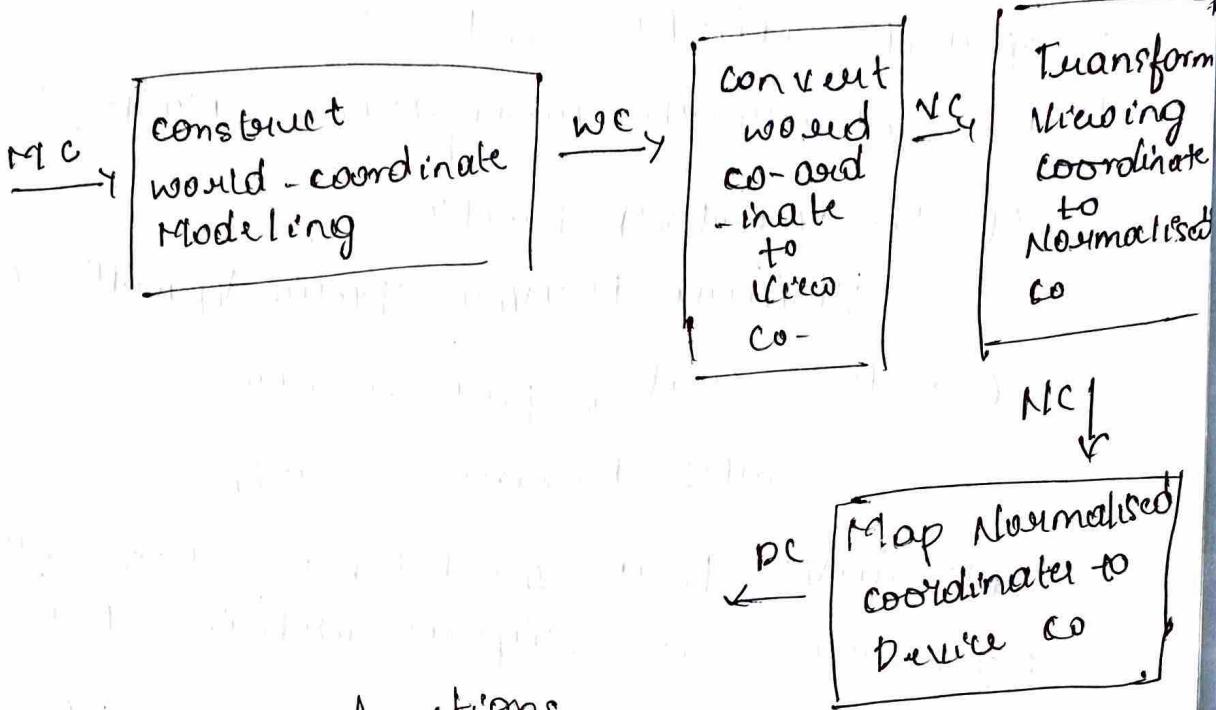
2) ~~NFT~~ NFT? diff b/w  $\rightarrow$  Fungible & nonfungible (Nonfungible)

## CG Assignment

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1. Build a 2D viewing transformation pipeline and also explain OpenGL 2D viewing functions.



### 2D Viewing functions

We can use these two dimensional routines, along with the OpenGL viewport funct,

#### OpenGL Projection Mode

Before we select a clipping window and a viewport in OpenGL, we need to establish an appropriate mode for constructing the matrix to transform from world co., to screen coordinates.

#### glMatrixMode(GL\_PROJECTION)

→ OpenGL wire-frame surface Visibility Method

A wire-frame display of a standard graphical object can be obtained in OpenGL.

diff b/w  $\rightarrow$  Filled & non-filled ren.

gl polygon mode (GL\_FRONT\_AND\_BACK, GL LINE)

$\rightarrow$  if LU clipping window, we can use the OpenGL utility function

gluOrtho2D (xmin, xmax, ymin, ymax);

OpenGL ViewPort Function

gl ViewPort (xmin, ymin, Vp width, Vp height)

Create a glut display window

glutInit (argc, argv);

we have three functions in glut for  
definition a display within the window

$\rightarrow$  setting the glut display - Window Mode & color:  
Various display window Parameters are  
selected with the glut function.

glutInitDisplayMode (mode);

glClearColor (red, green, blue, alpha);

glClearIndex (index);

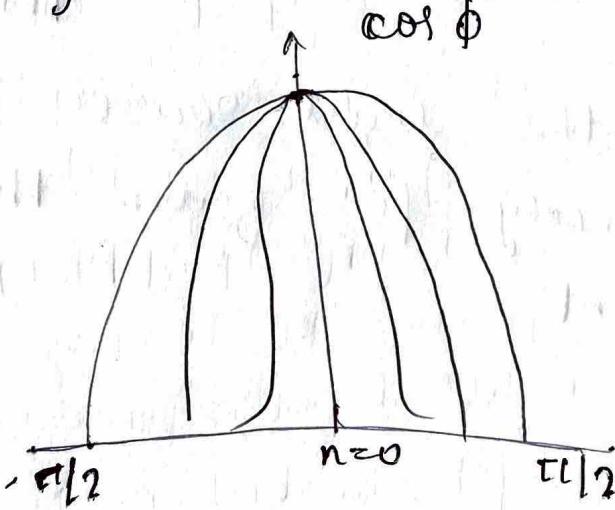
$\rightarrow$  glut display - window identifier  
window ID = glutCreateWindow ( );

$\rightarrow$  Current glut display window

glutSetWindow (windowID);

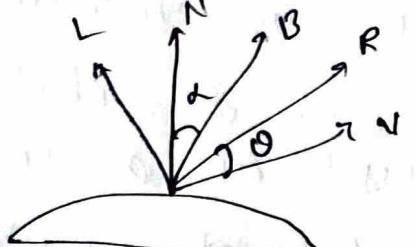
- 2). Build phong lighting Model with equations?

Phong reflection is an empirical model of local illumination. It describes the way a surface reflects light as a combination of the diffuse reflection of rough surfaces, combination of the diffuse with specular reflection of shiny surface. It is based on Phong's informal observation that shiny have small intense specular highlights while dull surfaces have large low highlights that full of more gradually.



If light direction  $L$  and Viewing function direction  $v$  are on the same side of the normal  $N$ , or if  $L$  is behind the surface, specular effects do not exist.

for most opaque materials specular reflection co-efficient is nearly constant

$$I_{\text{specular}} = \begin{cases} K_s L R (1-R)^2, & R \\ 0 & \text{otherwise} \end{cases}$$

$$R = (2N - L)N - L$$

the Normal  $N$  may vary at each point to avoid  $N$  computation angle  $\theta$  is replaced by an angle  $\alpha$  defined by a halfway vector  $H$  between  $L$  and  $V$

$$\text{Efficient } \approx H = \frac{L+V}{|L+V|}$$

If the light source and viewer are relatively far from the object,  $\alpha$  is constant

3)

Apply homogeneous coordinates for translation, rotation & scaling via matrix multiplication.

The three basic 2D transformations are translation, rotation & scaling

$$P' = M_1 + P + M_2$$

$P'$  &  $P$  represents column vectors

Homogeneous coordinates : A standard technique to expand the matrix representation for a 2D coordinate  $(x, y)$  position to a 3-element representation for a 2D coordinate

$(x_h, y_h, h) \rightarrow$  called homogeneous coordinates

$h \rightarrow$  homogeneous coordinate

$(x, y)$  is converted into new coordinate values

$$(x_h, y_h, h) \quad x = \frac{x_h}{h}, \quad y = \frac{y_h}{h} \quad x_h = x \cdot h \\ y_h = y \cdot h$$

Translation:

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & tx \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

This translation operation can be written as  $P' = T(t_x, t_y) \cdot P$

Rotation:

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \Rightarrow P' = R(\theta) \cdot P$$

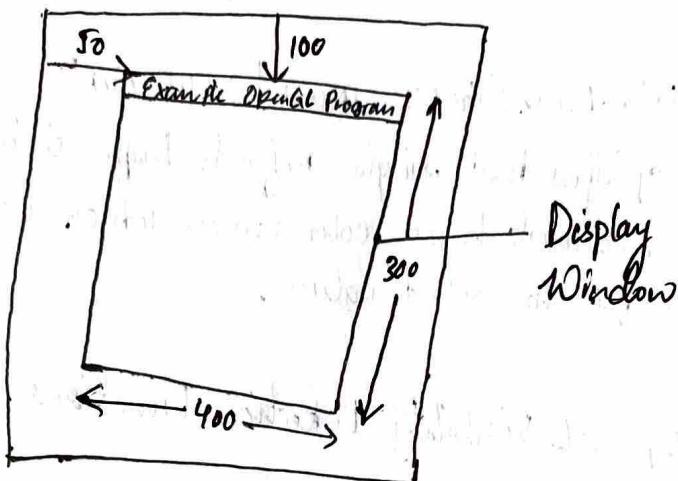
Scaling Matrix

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = P' = S(s_x, s_y) \cdot P$$

## Difference between raster icon & random icon display

Random icon display	Raster icon display
* In random icon display the beam is moved between the end points of graphics primitives	* The beam is moved all over the screen over the screen or scanline at a time, from top to bottom then back to top
* Vector display flickers when the number of primitives in the buffer becomes too large	* The refresh process is independent of complexity of image
* Scan conversion is not required	* Graphics primitives are specified in terms of their endpoints must be scan converted into their corresponding pixels in the frame buffer
* Scan conversion is not required	* Real time dynamics is for more computational & require separate scan conversion hardware
* Vector display derives a continuous & smooth lines	* Icon displays mathematically smooth lines polygons & boundaries of curved primitives only by approximating them with pixels or raster grid
* cost is more	* cost is less
* Vector display only draws lines & characters	* Has ability to display areas filled with solid colors or patterns

- 5) Demonstrate OpenGL functions for displaying window management using GLUT



- We perform the GLUT initialization with the statement  
`glutInit(argc, argv)`
- We can state that a display window is to be created, on the screen with a given caption for title bar.  
`glutCreateWindow("Example OpenGL program")`
- Following function call the line-segment description to the display function  
`glutDisplayFunc(linesegment)`
- `glutMainLoop()`  
It displays the initial graphics and puts the program into an infinite loop that checks the input from devices such as mouse & keyboard.
- `glutWindowPosition(80,100)`  
Specifies that upper-left corner of display window should be placed 80 pixel to the right of left edge of screen and 100 pixels down from top edge of screen

glutWindowSize(400, 300)

function is used to set the initial pixel width/height of display window

• glutInitDisplayMode(GLUT\_SINGLE | GLUT\_RGB)

Command specifies that single refresh buffer is to be used for display windows and convert to use color mode which uses red, green, blue components for to select values.

6) Explain OpenGL Visibility Detection Functions

a) OpenGL Polygon - Culling Functions

Back face removal is accomplished with functions

glEnable(GL\_CULL\_FACE)

glCullFace(mode)

mode is assigned the values GL\_BACK, GL\_FRONT, GL\_FRONT\_AND\_BACK

By default, parameter mode in glCullFace function has value

Culling routine is turned off with glEnable(GL\_CULL\_FACE)

b) OpenGL Depth Buffer Functions

We need to modify the GLUT initialization function for display mode to include a request for depth buffer & refresh buffer

glutInitDisplayMode(GLUT\_SINGLE | GLUT\_RGB | GLUT\_DEPTH)

Depth buffer values can be initialized with

glClear(GL\_DEPTH\_BUFFER\_BIT)

Routines are admitted with following functions

glEnable(GL\_DEPTH\_TEST)

We can also apply depth-buffer testing using some other initial value.  
`glClearDepth(ClearDepth)` can be set b/w 0 & 1

We can adjust normalization values with

`glDepthRange(ClearNormDepth, farNormDepth)`

We specify a test condition for depth buffer routines using

`glDepthFunc(Test cond")`

c)

OpenGL wire-frame surface visibility methods

Wire frame displays of a standard graphics object can be obtained in OpenGL by requesting that only its edges are to generated

`glPolygonMode(GL-FRONT + AND BACK, GL-LINE)`

This displays both visible and hidden edges

d)

OpenGL - DEPTH - Culling Function

We can vary brightness of object as function of its distance from viewing position with `glEnable(GL-FOG)`

`glFog(GL-FOG-MODE, GL-LINEAR)`

Applies linear depth function to object colors using  $dmin = 0.0$  and  $dmax = 1.0$  and we can set different values

`glFogf(GL-FOG-START, minDepth)`

`glFogf(GL-FOG-END, maxDepth)`

7) Write the special cases that we discussed with respect to perspective projection transformation coordinates.

$$x_p = x \left( \frac{z_{pp} - z_{vp}}{z_{pp} - z} \right) + x_{pp} \left( \frac{z_{vp} - z}{z_{pp} - z} \right)$$

$$y_p = y \left( \frac{z_{pp} - z_{vp}}{z_{pp} - z} \right) + y_{pp} \left( \frac{z_{vp} - z}{z_{pp} - z} \right)$$

Special cases :

1)  $z_{pp} = y_{pp} = 0$

$$x_p = x \left( \frac{z_{vp} - z_{vp}}{z_{vp} - z} \right) \quad y_p = y \left( \frac{z_{vp} - z_{vp}}{z_{vp} - z} \right) \rightarrow \textcircled{1}$$

projection reference point is limited to positions along z view axis.

2)  $(x_{pp}, y_{pp}, z_{pp}) = (0, 0, 0)$

$$x_p = x \left( \frac{z_{vp}}{z} \right)$$

$$y_p = y \left( \frac{z_{vp}}{z} \right) \rightarrow \textcircled{2}$$

projection reference point is fixed at coordinate origin.

3)  $z_{vp} = 0$

$$x_p = x \left( \frac{z_{pp}}{z_{pp} - z} \right) - x_{pp} \left( \frac{z}{z_{pp} - z} \right) \rightarrow \textcircled{3a}$$

$$y_p = y \left( \frac{z_{pp}}{z_{pp} - z} \right) - y_{pp} \left( \frac{z}{z_{pp} - z} \right) \rightarrow \textcircled{3b}$$

we get 3a & 3b if the view plane is the uv plane & there are no restrictions on the placement of projections reference point.

$$4) x_{\text{proj}} = y_{\text{proj}} = z_{\text{proj}} = 0$$

$$x_p = x \left( \frac{z_{\text{proj}}}{z_{\text{proj}} - z} \right)$$

$$y_p = y \left( \frac{z_{\text{proj}}}{z_{\text{proj}} - z} \right)$$

we get ④ with the uv plane as the view plane & the projection reference point on the z view axis.

⑧ Explain Beizer curve equation along with its properties.

→ Developed by French engineer Pierre Beizer for use in design of Renault Beizer have a number of properties that make them highly useful for curve & surface design. They are also easy to implement.

Beizer curve section can be filled to any number of control points.

Equations:

$P_k = (x_k, y_k, z_k)$   $P_k$  = General (n+1) control point positions.

$P_u$  = the position vector which describes the path of appropriate Beizer polynomial func-  $P_0$  &  $P_n$ .

$$P(u) = \sum_{k=0}^n P_k B E Z_{k,n}(u), \quad 0 \leq u \leq 1$$

$$B E Z_{k,n}(u) = C(n, k) u^k (1-u)^{n-k} \rightarrow \text{Bernstein polynomial.}$$

where  $C(n, k) = \frac{n!}{k!(n-k)!}$

### Properties :

Basic functions are real

Degree of polynomial defining the curve is one less than number of defining points.

Curve generally follows the shape of defining polygon.

Curve connects the first & last control points thus

$$P[0] = P_0$$

$$P[i] = P_n$$

Curve lies within the convex hull of control points .



$n=3$



$n=4$

9. Explain normalization transformation for an orthogonal projection

We assume that orthogonal projection view volume to be mapped into the symmetric normalization cube within a left-handed reference frame. Also,  $\omega$ -coordinate positions for the near & far places are denoted as  $Z_{\text{near}}$  and  $Z_{\text{far}}$ , respectively, this position  $(x_{\text{min}}, y_{\text{min}}, Z_{\text{near}})$  is mapped to the normalized position  $(-1, -1, -1)$  and position  $(x_{\text{max}}, y_{\text{max}}, Z_{\text{far}})$  is mapped to  $(1, 1, 1)$ .

The normalization transformation for the orthogonal view volume is:

$$M_{\text{ortho, norm}} = \begin{bmatrix} \frac{2}{x_{\text{max}} - x_{\text{min}}} & 0 & 0 & -\frac{x_{\text{max}} + x_{\text{min}}}{x_{\text{max}} - x_{\text{min}}} \\ 0 & \frac{2}{y_{\text{max}} - y_{\text{min}}} & 0 & -\frac{y_{\text{max}} + y_{\text{min}}}{y_{\text{max}} - y_{\text{min}}} \\ 0 & 0 & -\frac{2}{Z_{\text{near}} - Z_{\text{far}}} & \frac{Z_{\text{near}} + Z_{\text{far}}}{Z_{\text{near}} - Z_{\text{far}}} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

The matrix is multiplied on the right by the composite viewing transformation R.T to produce the complete transformation from world coordinates to normalize orthogonal projection coordinates.

10. Explain Cohen-Sutherland line clipping.  
Algorithm.

Every line endpoint in a picture is assigned a 4 digit binary value called a region code and each bit position is used to indicate whether the point is inside or outside of one of the clipping window boundaries.

1001	1000	1010
0001	Clipping window 0000	0010
0101	0100	0110

When the OR operation between 2 endpoints' region codes for a line segment is false (0000), the line is inside the clipping window.

When AND operation between 2 endpoints region codes for a line is true, then the line is completely outside

To determine a boundary intersection for a line segment, the y-coordinate of the intersection point can be obtained by.

$$y = y_0 + m(x - x_0)$$

where,  $x$  is either  $x_{\min}$  or  $x_{\max}$  & slope is

$$m = (y_{\text{end}} - y_0) / (x_{\text{end}} - x_0)$$

for the  $x$ -coordinate,

$$x = x_0 + \left( \frac{y - y_0}{m} \right)$$

=.