

Frequency Count method :-

This Method is useful for finding the time complexity of algorithms.

ex: algorithm $\text{sum}(A, n)$

A	1	1	2	3	2
	0	1	2	3	4

$A = \text{array}$
 $n = 5$

$\text{sum}(A, n)$
 $S = 0 \rightarrow 1$

$i < n$

$i = 0$
 $i = 1$
 $i = 2$
 $i = 3$
 $i = 4$

$n+1$
times
executing

for $(i = 0; i < n; i++)$
 $\{$
② $n+1$
③ $\text{time} \leftarrow S = S + A[i];$
 $\}$

④ $\text{return } S; \rightarrow 1$
 $\}$

$n+1$

n

1

$$(2n + 3) = f(n) \rightarrow$$

$$\underline{O(n)}$$

Space & variable

$A \rightarrow n$

$n \rightarrow 1$

$s \rightarrow 1$

$i \rightarrow 1$

$$S(n) = \underline{\underline{n+3}}$$

\Rightarrow polynomial $O(n)$

ex: (2) finding the sum of two matrices

Algorithm Add(A, B, n)

{ for ($i=0$; $i < n$; $i++$) \rightarrow $(n+1)$

whatever
inside a for
loop runs
 (n) times

{ for ($j=0$; $j < n$; $j++$) \rightarrow (n)

{ same
inside
for loop
 (n) times

$$C[i, j] = A[i, j] + B[i, j]$$

$(n+1)$

$n \times (n+1)$
 $n \times n$

time complexity $f(n) = 2n^2 + 2n + 1 \Rightarrow O(n^2)$

Space Complexity :- Variables are used in code.

A, B, C

A, B, C, n, i, j

They are matrices

They are two dimensional 2D array

$$\begin{aligned} A &= n^2 & n &= 1 & n \times n \\ B &= n^2 & i &= 1 \\ C &= n^2 & j &= 1 \end{aligned}$$

n, i, j

They are scalar variable,
simple variables

$$\begin{aligned} A &= n^2 \\ B &= n^2 \\ C &= n^2 \\ n &= 1 \\ i &= 1 \\ j &= 1 \end{aligned}$$

Space function $S(n) = 3n^2 + 3 \rightarrow$ degree for n
 $O(n^2)$

Time

and

Space

Complexity for this

code is

$$\text{Time} = O(n^2)$$

$$\text{Space} = O(n^2)$$

Algorithm multiply (A, B, n)

```

{
  for (i=0; i<n; i++) → n+1
  {
    for (j=0; j<n; j++) → n+1
    {
      C[i, j] = 0; → n*n
      for (k=0; k<n; k++) → n+1
      {
        C[i, j] = C[i, j] + A[i, k] *
          B[k, j];
        → n*n*n
      }
    }
  }
}

```

Time Complexity :

Space Complexity :

Variables

A ⇒ n^2

B ⇒ n^2

C ⇒ n^2

n ⇒ 1

i ⇒ 1

j ⇒ 1

k ⇒ 1

T/C = $O(n^3)$

S/C = $O(n^2)$

$3n^2 + 4$

$O(n^2)$ space

T/C ⇒ $O(n^3)$
degree

n+1
n * (n+1)

n * n

n * n * (n+1)

n * n * n

$2n^3 + 3n^2 + 2n + 4$