

Computer Architecture:-Digital Assignment-2

① Express the following number in IEEE 32-bit floating point format

a) -1.5

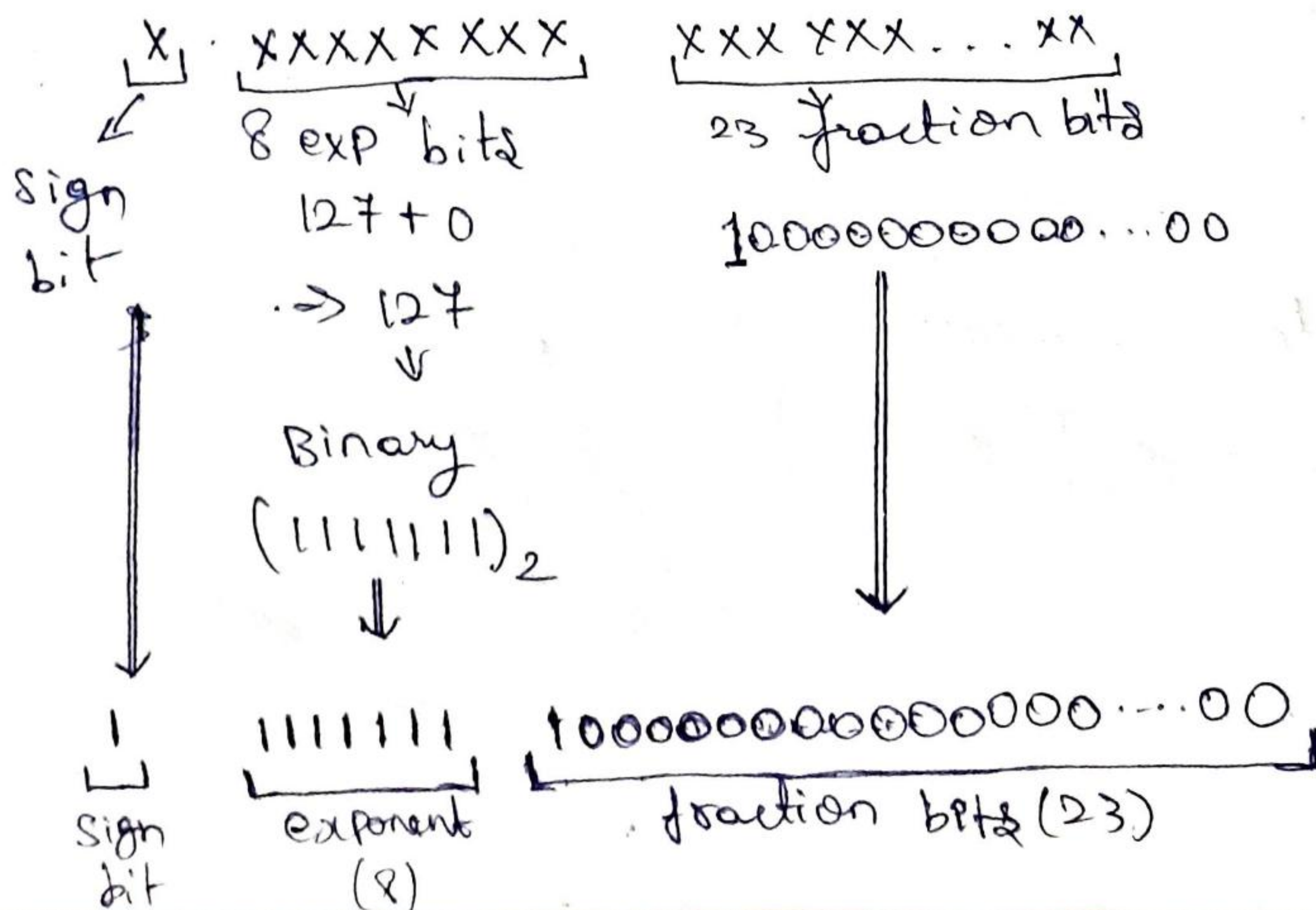
Ans

$-1.5 \rightarrow \text{Binary } (-1.1)_2$

Sign bit | mantissa $\Rightarrow 7$
 $8 = 1$ | $E = 0$

<u>decimal</u>	<u>Binary</u>
1	01
0.5	.1
1.5	$\rightarrow 1.1$
exp bias = 127	

-1.1 \rightarrow it doesn't need normalization.



⑥ $(\underline{384})_{10}$

4

Binary $(1100000000)_2$

Normalize

$$1.100000000 \times 2^8$$

Sign bit

$$S = 0$$

man tissa

$$M = 10000000$$

sign
bit

8 exponent
bits

23 fraction bits:-

X

X X X X X X X

XXXXXX XX XX XX ... XX

10

10000111

10 oooooooooooooo...oo

② The following numbers use the IEEE 32 bit floating point format. What is the equivalent decimal value?

or

100000011

fraction bits (23)

Sign (S) = 1 bit

$$E = (10000011)_2 \Rightarrow (131)_{10}$$

$E_{bias} = 127$ for 32-bit

exp
bias : 127 for 32bit

Exponent(E): 8

$E' = 8 + \exp bias$

$$E' = 8 + 127$$

$$11' = 135$$

$$(135)_{10} \rightarrow (10000111)_2$$

$$E = 137 - 127$$

$$\Rightarrow 10$$

$$\boxed{\text{Exponent} = 10}$$

$$1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + \dots$$

$$\boxed{11000000 \dots 00}$$

Mantissa (M)

$$\Rightarrow 1 + 2^{-1} + 1 \times 2^{-2} \Rightarrow 2^{-1} + 2^{-2}$$

$$\boxed{\text{Mantissa} \rightarrow 0.75}$$

$$\boxed{(-1)^s \times (1+m) \times 2^e}$$

$$\Rightarrow (-1)^0 \times (1+0.75) \times 2^4$$

$$\Rightarrow (1) \times (1.75) \times 2^4 \Rightarrow 28$$

$$\boxed{\text{Equivalent decimal value} = (28)_{10}}$$

⑥

$$\begin{array}{ccc} \boxed{0} & \boxed{01111110} & \boxed{101000000000000000000000} \\ \downarrow & \text{Exponent} & \text{fraction bit (23)} \\ \text{Sign} & \text{bit} & \\ \text{bit} & (8) & \end{array}$$

$$E = (01111110)_2 \rightarrow 126$$

$$\boxed{\text{Sign bit} = 0}$$

$$\underline{\text{exp bias for 32 bit } E_{\text{bias}} = 127}$$

$$E' = E - E_{\text{bias}}$$

$$E' = 126 - 127$$

$$\boxed{E' = -1}$$

$$\begin{array}{c} \text{mantissa} \\ \downarrow \\ \boxed{10100000 \dots 00} \\ \swarrow \quad \downarrow \quad \searrow \\ 1 \times 2^{-1} \quad 0 \times 2^{-2} \quad 1 \times 2^{-3} \end{array}$$

$$2^{-1} + 2^{-3} \Rightarrow 0.625$$

$$\boxed{\text{Mantissa} = 0.625}$$

$$\boxed{(-1)^s \times (1+m) \times 2^e} \Rightarrow \text{equivalent formula (decimal)}$$

$$\Rightarrow (-1)^0 \times (1+0.625) \times 2^{-1} \Rightarrow 0.8125$$

\therefore The equivalent decimal value for the given binary 32 bit format $\Rightarrow 0.8125$

③ show step by step process using sing magnitude multiplication algorithm and both multiplication algorithm for the following numbers:-

a) 7×3

Multiplicand (B) = $(7)_{10} \rightarrow (0111)_2$ $7 \times 3 = 21$

Multiplier (Q) = $(3)_{10} \rightarrow (0011)_2$

Comment	SE	A	Q	SC
$Q_n = 1; A \leftarrow A + B$	0	$\begin{array}{r} 0000 \\ +B \ 0111 \\ \hline 0111 \end{array}$	0011	4
$\text{shr } EAQ$ $SC \leftarrow SC - 1$	0	$\begin{array}{r} 0111 \\ \hline 0111 \end{array}$		
	0	0011	1001	3
$Q_n = 1; A \leftarrow A + B$	0	$\begin{array}{r} 0111 \\ +B \ 0111 \\ \hline 1010 \end{array}$		
$\text{shr } EAQ$ $SC \leftarrow SC - 1$	0	0101	0100	2
$\text{shr } EAQ \quad Q_n = 0$	0	0010	1010	1
$Q_n = 0 \text{ shr } EAQ$	0	0001	0101	0

$$7 \times 3 = 21 = 010101$$

① +7 +3

Booth multiplication algorithm

Multiplicand (BR) = $(+7)_{10} \rightarrow (0111)_2$

Multiplier (QR) = $(+3)_{10} \rightarrow (0011)_2$

$\bar{B}R + 1 \Rightarrow 1001$

Comment	AC	QB	Q _{n+1}	SC
QR = 1 and Q _{n+1} = 0 AC ← AC + $\bar{B}R + 1$	0000 1001 ----- 1001	0011	0	4
Ashr (AC & QR) SC ← SC - 1	1100	1001	1	3
QR = 1 & Q _{n+1} = 1 Ashr (AC & QR) SC ← SC - 1	1110 +BR 0111 ----- 0101	0100	1	2
QR = 0 & Q _{n+1} = 1 AC ← AC + BR Ashr (AC & QR) SC ← SC - 1	0010	1010	0	1
Ashr (AC & QR) QR = 0 Q _{n+1} = 0	0001	0101	0	0

00010101 $\Rightarrow +21$

1x16 1x4 1x1

16+4+1 = 21

using Booth multiplication

algorithm:-

we get final

result as +21

Q6

-7 * 3

Booth multiplication Algorithm

$$QR = 3 = 0011$$

$$BR = -7 = 1001$$

$$\overline{BR} + 1 = 0111$$

$$-(7) = 0111$$

$$12 \quad 1000$$

$$+1$$

$$1001$$

$$1011$$

$$0100$$

$$0101$$

$$1001$$

$$15 \quad 0110$$

$$+1$$

$$0111$$

Comment	AC	QR	Q _{n-1}	SC
QR = 1 Q _{n-1} = 0 AC ← AC - BR	0000 0111 ----- 0111	0011	0	4
Ashr	0011	1001	1	3
QR = 1 Q _{n-1} = 1 Ashr	0001 1001 ----- 1001	1100	1	2
QR = 0 Q _{n-1} = 1 SC ← SC - 1	1010 1101 ----- 1101	0110	0	1
Ashr	1110	1011	0	0

AC

QR

$$1110 \quad 1011 \Rightarrow 1's \rightarrow 00010100 \Rightarrow -21$$

$$2's \rightarrow 00010101$$

$$16 + 4 + 1 \Rightarrow 21$$

$$11101011$$

$$00010100$$

- 13

3b) Sign magnitude
multiplicand (B) \rightarrow $-(7) \Rightarrow (0111)_2$

The sign bit of (B) and (Q) are store in

B_s and Q_s , $B_s = 1$ $Q_s = 0$ $B_s \oplus Q_s = 1$

multiplier (Q) = $(3)_{10} \Rightarrow (0011)_2$

Comment	E	A	Q	SC
$Q_n = 1; E$ $EA \leftarrow A + B$ $\text{shr } EAQ$ $SC \leftarrow SC - 1$	0	0000 $+B \ 0111$ 0111	0011	4
$Q_n = 1; EA \leftarrow A + B$ $\text{shr } EAQ$ $SC \leftarrow SC - 1$	0	0011 $+B \ 0111$ 1010	1001	3
$Q_n = 1; EA \leftarrow A + B$ $\text{shr } EAQ$ $SC \leftarrow SC - 1$	0	1010 $+B \ 0111$ 0101	0100	2
$\text{shr } EAQ$	0	0010	1010	1
$Q_n = 0 \text{ shr } EAQ$	0	0001	0101	0

$$B_s \oplus Q_s = 1$$

$$1 \oplus 0 = 1$$

sign bit = 1

$$1 \ 0010101 \Rightarrow -(21)_{10}$$

Using sign magnitude the we obtain
 $-(21)_{10}$

(4)

Address	Value	Instruction	Addressing mode	Value in R ₀
PC	100	Load R ₀ , #200	Immediate	200
R ₀	200	load R ₀ , 200	Direct	500
R ₁	300	load R ₀ , (200)	Indirect	700
100	200	load R ₀ , R ₁	Register	300
104	300	load R ₀ , [R ₁]	Register Indirect	600
108	400	Load R ₀ - 100[R ₁]	Based	500
200	500	Load R ₀ , 200[PC]	Relative	600
300	600			
500	700			

⑤ Write a short note on different types of memory?

Memory:-

- Complete programs and data sets are held in memory external to the processor.
- Two fundamental types:-

Main memory:-

- ✧ main memory is sometimes called volatile because it loses its information when power is removed.

* Secondary memory is usually nonvolatile because it retains its information when power is removed. (1)

* Main memory is sometimes called main storage.

* Main memory sometimes called RAM.

RAM stands for Random Access Memory.

"Random" means means that the memory cells can be accessed in any order.

Secondary Memory:-

→ Secondary memory is where programs and data are kept on a long-term basis. Common secondary storage devices are the hard disk and optical disks.

→ The hard disk has enormous storage capacity compared to main memory.

→ The hard disk is usually contained inside the case of a computer.

→ The hard disk is used for long-term storage of programs and data.