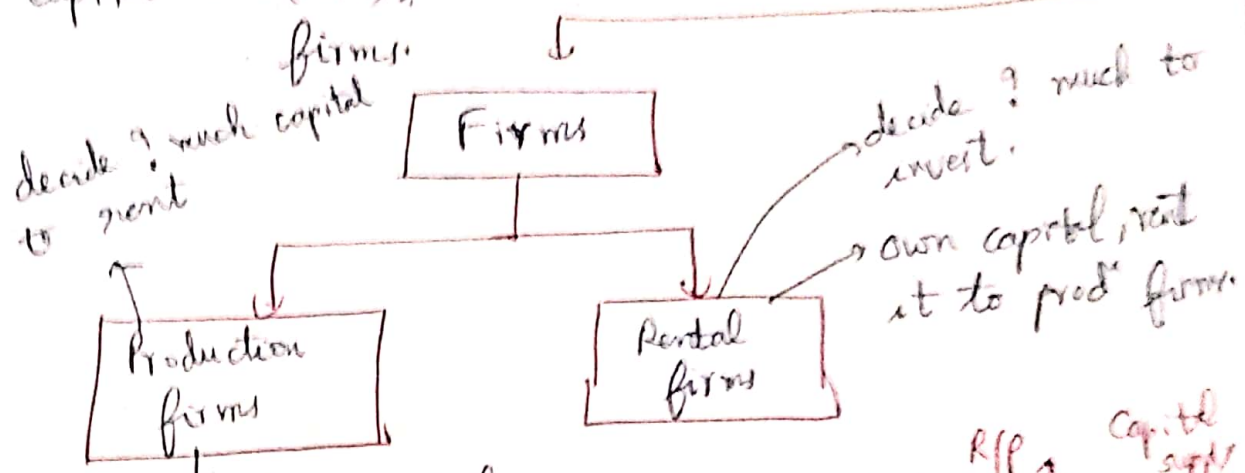


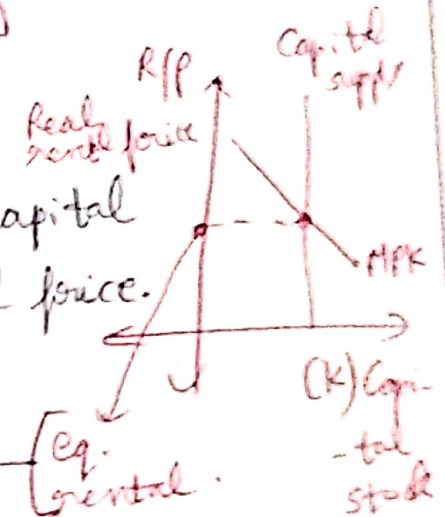
Business - fixed investment: *assumes that firms can borrow to buy capital when they feel that's profitable*

→ Std. model: Neoclassical model of investment

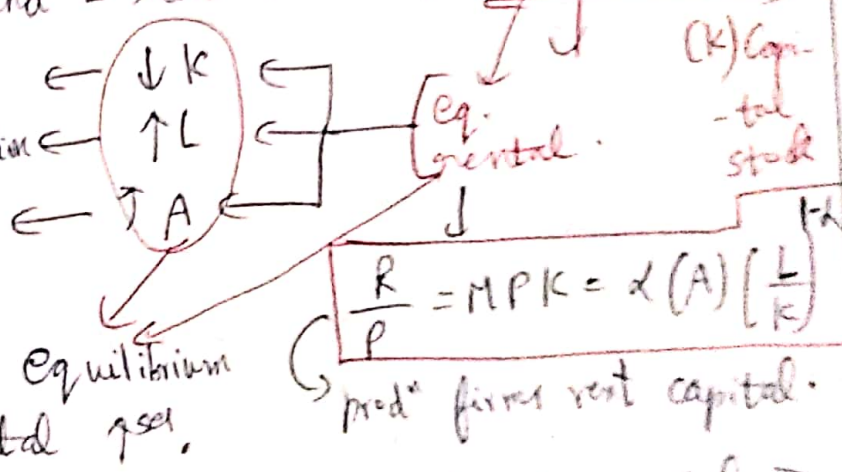
→ shows how investment depends on Capital demand (MPK), interest rate & tax rules affecting



they use to produce goods & services. Production firms rent capital until capital demand = real rental price.



earthquake / war → $\downarrow K$
 popⁿ growth / immigration → $\uparrow L$
 Technological ↑ment → $\uparrow A$



$$\frac{R}{P} = MPK = A \left(\frac{L}{K} \right)$$

Equilibrium rental price.

prodⁿ firms rent capital.

→ Rental firms → rent when benefit/unit capital > cost.

Benefit (per unit capital) → $\frac{R}{P}$ → the income that rental firms earn from renting 1 unit of capital to production firms.

↳ The Cost of capital:

- Interest cost: Opportunity cost equal to the interest firms could have earned if they had purchased P_K worth of bonds instead of spending P_K from their own funds.

$$\boxed{\text{Interest cost rate}} = i \times P_K \quad P_K = \text{nominal price of capital.}$$

- Depreciation cost:

Depreciation rate = % of cost that wears out each (D) period.

Firm's capital = $(1 - D)$ (Worth of capital) after the depreciation period.

$$\boxed{\text{Depreciation cost}} = s \times P_K$$

→ s = rate of depreciation.
→ current price of capital.

- Capital Loss: $= -\Delta P_K$.

A capital gain, $\Delta P_K > 0$ reduces cost of K .

$$\boxed{\text{Nominal cost of capital}} = \text{Interest + depreciation costs} + \text{Capital loss}$$

$$= i \times P_K + s \times P_K - \Delta P_K$$

$$= P_K \left(i + s - \frac{\Delta P_K}{P_K} \right)$$

Real price of capital = P , $\frac{\Delta P_K}{P_K} = \pi$.

\therefore Nominal ^{Cost} price of capital = $P_K (i + s - \pi)$
 $= P_K (r + s)$

Real cost of capital = $\left(\frac{P_K}{P}\right)(r + s)$

relative
price
of
capital.

real
interest
rate

depreciation
rate

Profit rate = $SP - CP = \frac{R}{P} - \frac{P_K}{P}(r + s) = MPK - \frac{P_K}{P}(r + s)$

- $\rightarrow > 0 \rightarrow$ firm rents \uparrow capital ($\uparrow K$)
- $\rightarrow < 0 \rightarrow$ firm $\downarrow K$ by not replacing it as it depreciates.
- \rightarrow determines a firm's net ~~interest~~ rate.
investment.

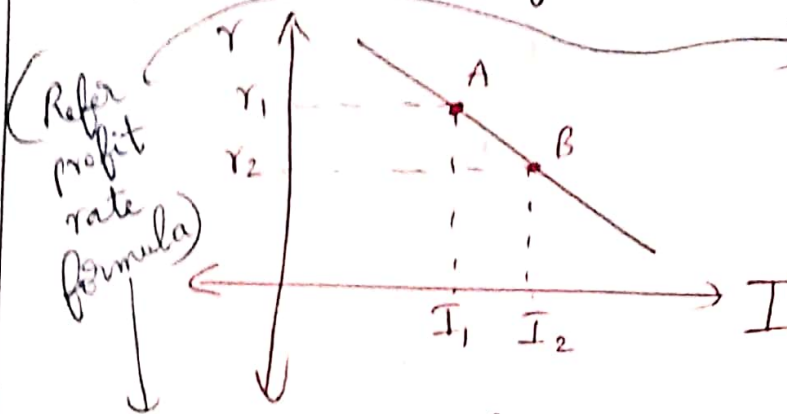
\rightarrow Net investment = $\Delta K = I \left[MPK - \frac{P_K}{P}(r + s) \right]$
 $I[\]$ is a funcⁿ

\rightarrow Gross investment = net investment + δK
(replacement of depreciated K)

$$I = I_n \left[MPK - \frac{P_K}{P}(r + s) \right] + \delta K \quad \text{--- (1)}$$

$$= \Delta K + \delta K$$

↳ The investment funcⁿ: (① prev. page)



↳ $r \uparrow^{set} \Rightarrow$

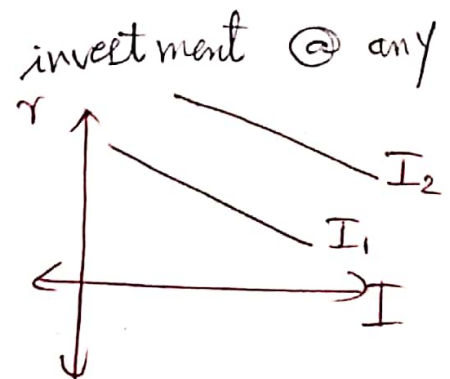
(i) \uparrow in cost of capital

(ii) \downarrow in profit rate & thus \downarrow in investment.

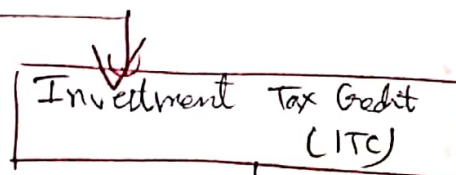
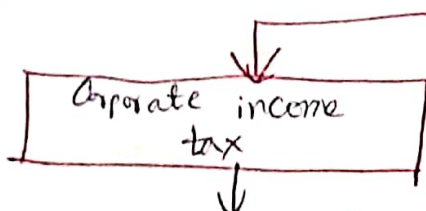
↳ $MPK \uparrow^{set}$ or $\frac{P_K}{P} \downarrow^{set}$:

$\rightarrow \uparrow$ in profit rate $\rightarrow \uparrow$ in interest rate.

\rightarrow Shifts I curve to rt.



↳ Taxes affecting investment



Tax on profits.

Conventional price of capital \rightarrow used to compute profit. If P_K over time, profit is overstated. So, even if economic profit of firm $= 0 \Rightarrow$ corporate income tax \checkmark .

DISCOURAGES INVESTMENTS.

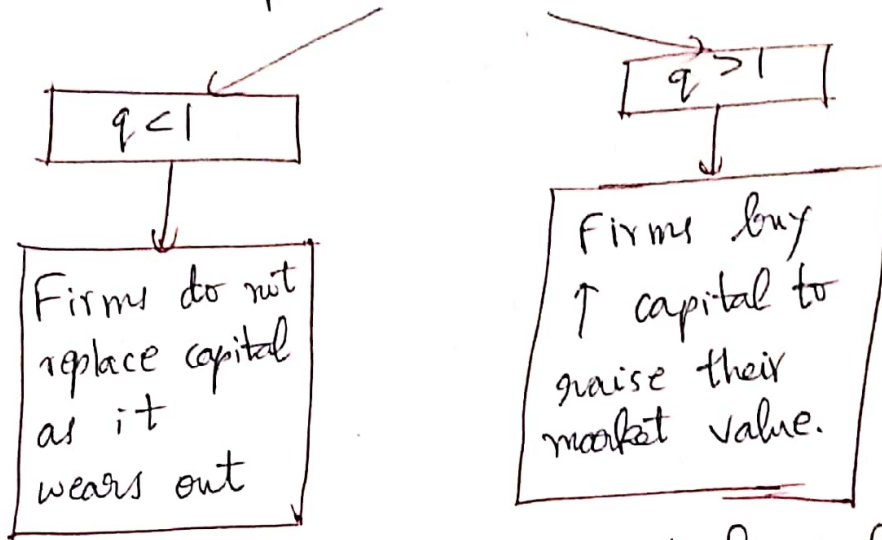
\rightarrow reduces the firm's taxes by certain amt. for every \$ it spends on capital.

$\Rightarrow P_K \downarrow$

\Rightarrow Profit rate \uparrow^{set}
 \Downarrow
investment \uparrow .

Tobin's q :

$$q = \frac{\text{Market value of installed capital}}{\text{Replacement cost of installed capital}}$$



Relation b/w q theory & Neoclassical model:

→ stock market value of capital depends on current & expected future profits of capital.

→ $MPK \begin{cases} > \text{cost of capital} \rightarrow \text{profit rate} \uparrow \rightarrow q \uparrow \\ < \text{cost of capital} \rightarrow \text{profit rate} \downarrow \rightarrow q \downarrow \end{cases}$

Efficient Markets Hypothesis (EMH):

→ Market price of a company's stock is the fully rational valuation of the company, given current info about the company's business prospects.

→ EMH \Rightarrow stock prices should only change as new info arrives. (random-walk / stock prices are un-predictable)

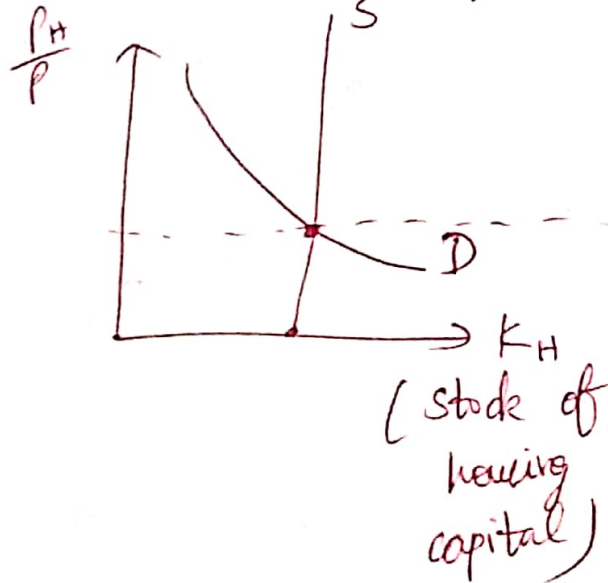
→ Stock prices $\downarrow^{ser} \Rightarrow \downarrow$ in technological progression.
 $\downarrow \Rightarrow \downarrow$ in household wealth
 $\downarrow \Rightarrow \downarrow$ in household consumption etc;

Residential - fixed investment:

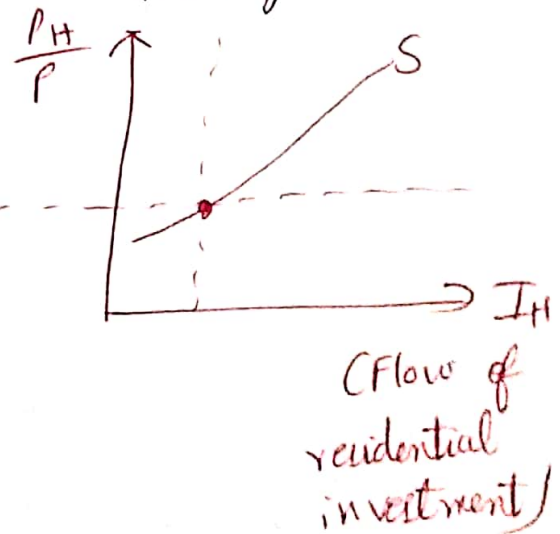
→ depends of $\left(\frac{P_H}{P} \right) = \frac{\text{Nominal price of houses}}{\text{Real " " " "}}$
 \swarrow depends on supply & demand of existing houses.

→ determined as follows:

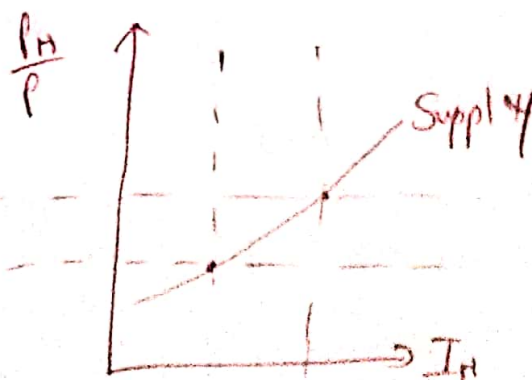
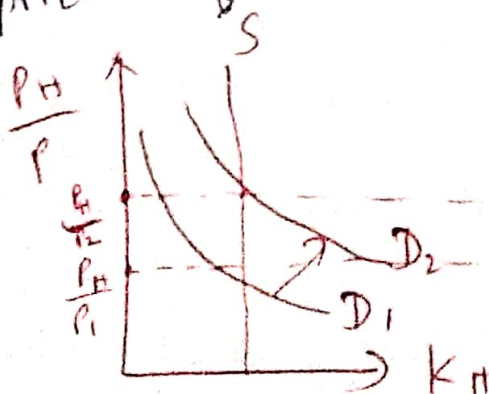
Market for housing



Supply of new housing



Interest rate $\downarrow \Rightarrow$ demand for houses $\uparrow \Rightarrow \uparrow$ relative price
 $\uparrow^{ser} \Rightarrow \uparrow^{ser}$ residential investment.



D_1 to D_2
 curve shift.

Tax treatment of housing:

Subsidises home ownership by allowing ppl to deduct mortgage interest.
 (applies to nominal mortgage rate \Rightarrow subsidy $\uparrow \Rightarrow$ IRT & Mortgage rate \uparrow (nominal))

Inventory investment:

$\sim 1\%$ of GDP.

\rightarrow Reasons: (Motives of investment)

- ① Prodⁿ Smoothing \rightarrow Sales $<$ prodⁿ \rightarrow inventories \uparrow
 \rightarrow Sales $>$ prodⁿ \rightarrow inventories \downarrow .
- ② Factor of prodⁿ \rightarrow spare parts when machines break down.
- ③ Stock-out avoidance \rightarrow avoid lost sales when demand $>$ expected.
- ④ Work in progress \rightarrow Works not yet completed \rightarrow goods still under construction \rightarrow inventory.

Accelerator Model:

\rightarrow A simple theory that explains the behaviour of inventory investment without focussing on any 1 particular investment.

→ N = stock of inventories, ΔN = inventory investment
 Assuming that firms hold a stock of inventories
 & o/p, $N = \beta Y$

β = exogenous parameter

$$\Rightarrow \Delta N = \beta \Delta Y \Rightarrow \text{Inventory investment} \propto \text{change in o/p.}$$

→ o/p \uparrow^{ses} ⇒ inventory investment \uparrow^{ses}
 → o/p \downarrow^{ses} ⇒ " " \downarrow^{ses}

→ opportunity cost of holding goods in the inventory = $\frac{\text{Interest earned on revenue from selling the goods.}}{\text{selling the goods.}}$

real interest \uparrow

opportunity cost of maintaining inventories \uparrow

firms \downarrow inventories & produce only when required.

So, inventory depends of interest rates.