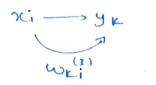
9.6.1.2

Ex 5.18

from D layer to k-dimensional output layer we introduce DMK (skip layer) which is



so we can write yx for forward propagation with skip layer.

yk = 
$$\frac{H}{J=0}$$
 w<sub>kj</sub>z<sub>j</sub> +  $\frac{D}{Z}$  w<sub>ki</sub>x<sub>i</sub>.

skiplayer

The Derivation of E(w) with wij and wij remain same since these weights are not dependent on the wij so, differentiating with whi gives

$$\frac{\partial \epsilon_n}{\omega_{ki}^{(1)}} = (y_n - t_n) \partial_{\omega_{ki}} (3) y_k$$

$$= (y_n - t_n) \pi_i = S_k \pi_i$$

9.6.2.1

Ex Q. 23.1

as A fundamental theorm in Linear Algebra states that If viw are finite dimensional Nector spaces, and let T be a linear transformation from V to withen the Image of T is a finite-dimensional subspace of wand

dim(v)= dim(null(T))+dim(image(T)).

we can say dim(null(A)) 21. thus

-> Au=Au

b) let f be recovery function, let  $u \neq v \in \mathbb{R}^{D} \Rightarrow Au = Av$ Hence f(Au) = f(Au) so at least one of the vector  $u_{i}v$  is not recovered. let assume feature space is of finite dimensions let x where  $\psi(xj)$  is jth column

So, we can find spectral decomposition of xix.

We can find Efficient solution in case of d>>100,500 the tigen decomposition of xTx can also be find in polynomial fine.

Let V be matrix with n leading Eigenvector of xTx as column and D be a diagonal non matrix whose diagonal consist of the corresponding Eigen values.

V is the matrix whose column are n leading figen vector of  $x \times T$  go, for  $x \in X$  the  $U^T \varphi(x)$  is  $D^{V_2} V T \varphi(x)$ 

$$= D^{-1/2} V^{T} X^{T} \emptyset(X) = D^{1/2} V^{T} \begin{bmatrix} K(x_{1}, X) \\ K(x_{1}, X) \end{bmatrix}$$

23.4

as Note that for every Unit Vector WE Rd, IE (m)

(KW, xi>>= tr (WTxi-xIW).

Hence, the Optimization problem here wincides with the Optimization problem objective of n=1 pcA. Hence the Optimal solution of our varience Maximization problem is the first principle vector of x1....xm.

$$w^* = arginax^* \qquad \frac{1}{m} \sum_{i=1}^{m} (\langle w_i, v_i \rangle)^*$$

$$||w|| = 1, \langle w_i, w_i \rangle = 0$$

11W11=1, <w, wis=0

PCA problem in case of n=2 is Equivalent to finding a Unity matrix we Rdx2

WIE WZ optimal matrix w's column and two first principal Vectors of x1 ... xm

$$= W_{1}^{T} \int_{m}^{m} \sum_{i=1}^{m} z_{i} x_{i}^{T} w_{i} + W_{2}^{T} \int_{m}^{m} \sum_{i=1}^{m} x_{i} x_{i}^{T} w_{i}$$

Since w' & w, are orthonormal, we get

$$= w_{1}^{T} + \sum_{m=1}^{m} x_{1}^{T} x_{1}^{T} w_{1} + w^{+} + \sum_{m=1}^{m} x_{1}^{T} x_{1}^{T} w^{+} - 2$$

9.6.2.2

6x 20.5

@ we have ,

$$C = \frac{1}{n} \left( \left[ I - v_1 v_1^T \right] x^T x \left[ I - v_1 v_1^T \right] \right)$$

$$= \frac{1}{n} \left( \left( x^T x - v_1 v_1^T x^T x \right) \left( I - v_1 v_1^T \right) \right)$$

$$= \frac{1}{n} \left[ x^T x - v_1 \left( v_1^T x^T x \right) - \left( x^T x v_1 \right) v_1^T + v_1 \left( v_1^T v_1 x_1 v_1 \right) v_1^T \right]$$

$$= \frac{1}{n} \left[ x^T x - n x v_1 v_1^T - n x v_1 v_1^T + n x v_1 v_1^T \right]$$

$$C \Rightarrow \frac{1}{n} \left[ x^T x - n x v_1 v_1^T \right] = \frac{1}{n} x^T x - \lambda v_1 v_1^T$$
Hence proved.

(b) since & liver in d-1 subspace orthogonauto v, the vectors u must be orthogonauto v1, Hence

utvi=0 4 utu=1 30, u=12

( we have

d = length(c)

2 = Zeros (d, K)

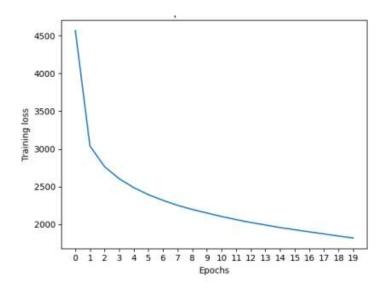
for j = 1: K

[lambda (1), V (:, J) = f(c);

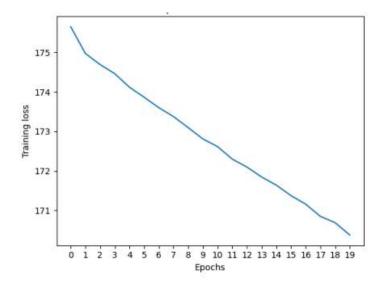
C= C- lambda (1) · (V(:,1)); 1. depration

erd.

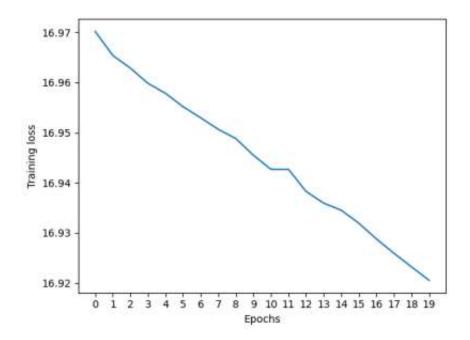
Plot for training loss over epochs Depth : 1 , Batch Size : 10 With accuracy : 87.2%



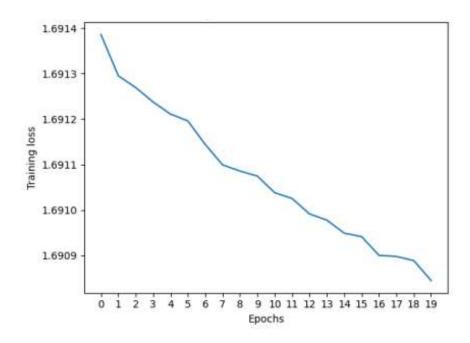
Plot for training loss over epochs Depth : 1 , Batch Size : 100 With accuracy : 87.5%



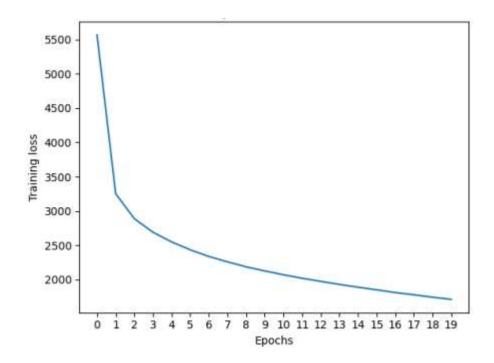
Plot for training loss over epochs Depth : 1 , Batch Size : 1000 With accuracy : 87.61%



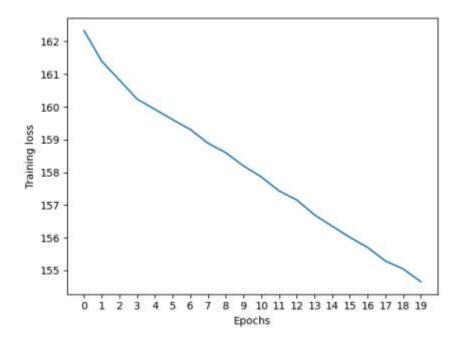
Plot for training loss over epochs Depth : 1 , Batch Size : 10000 Accuracy is : 87.55%



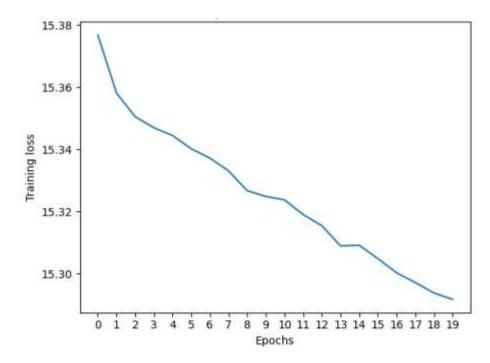
Plot for training loss over epochs Depth : 2 , Batch Size : 10 With accuracy : 87.4%



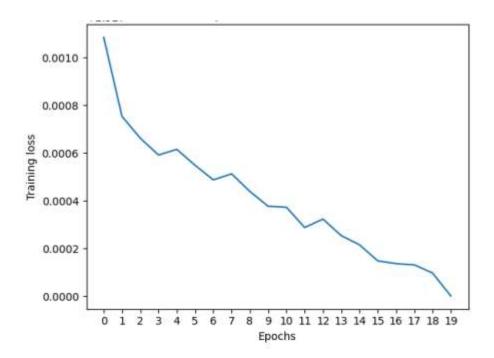
Plot for training loss over epochs Depth : 2 , Batch Size : 100 With accuracy : 88.01%



Plot for training loss over epochs Depth : 2 , Batch Size : 1000 With accuracy : 88.04%

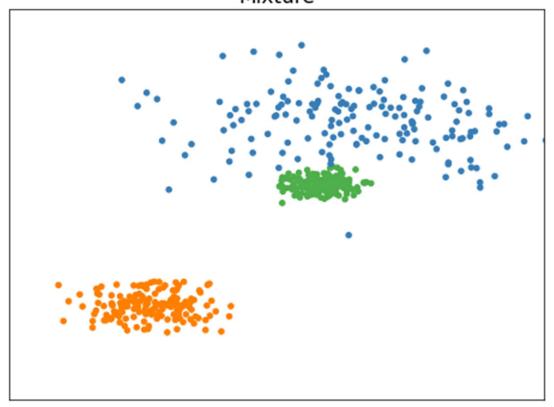


Plot for training loss over epochs Depth : 2 , Batch Size : 10000 With accuracy : 88.12%



```
Trained SVM: sigma = 0.1, C = 0.01: accuracy = 0.10302734375
Trained SVM: sigma = 0.1, C = 0.1: accuracy = 0.10302734375
Trained SVM: sigma = 0.1, C = 1: accuracy = 0.10302734375
Trained SVM: sigma = 0.1, C = 10: accuracy = 0.10302734375
Trained SVM: sigma = 0.1, C = 100: accuracy = 0.10302734375
Trained SVM: sigma = 1, C = 0.01: accuracy = 0.10302734375
Trained SVM: sigma = 1, C = 0.1: accuracy = 0.10302734375
Trained SVM: sigma = 1, C = 1: accuracy = 0.10302734375
Trained SVM: sigma = 1, C = 10: accuracy = 0.10302734375
Trained SVM: sigma = 1, C = 100: accuracy = 0.10302734375
Trained SVM: sigma = 10, C = 0.01: accuracy = 0.10302734375
Trained SVM: sigma = 10, C = 0.1: accuracy = 0.19921875
Trained SVM: sigma = 10, C = 1: accuracy = 0.8125
Trained SVM: sigma = 10, C = 10: accuracy = 0.82421875
Trained SVM: sigma = 10, C = 100: accuracy = 0.82421875
Trained SVM: sigma = 33.24893569946289, C = 0.01: accuracy = 0.395751953
Trained SVM: sigma = 33.24893569946289, C = 0.1: accuracy = 0.9086914062
Trained SVM: sigma = 33.24893569946289, C = 1: accuracy = 0.9365234375
Trained SVM: sigma = 33.24893569946289, C = 10: accuracy = 0.94555664062
Trained SVM: sigma = 33.24893569946289, C = 100: accuracy = 0.9448242187
```

Gaussian Mixture



Here 0,1,2 are clusters

## True parameters :

Mean of 0 : [-1.174,-1.288]
Mean of 1 : [0.755 , 1.039]
Mean of 2 : [0.409 , 0.2511]

Variance of 0:

[[ 0.1019269 -0.00029818] [-0.00029818 0.02493694]]

```
Variance of 1 :

[[ 0.73527736 -0.04720549] [-0.04720549     0.15766104]]

Variance of 2 :

[[ 0.03158649     0.00019285] [ 0.00019285     0.00730099]]

MLE Parameters :

Mean of 0 : [-1.174,-1.288]

Mean of 1 : [ 0.755     , 1.041]

Mean of 2 : [ 0.422     , 0.2540]

Variance of 0 :

[[ 0.1019279     -0.00029818][-0.00029818     0.02493794]]

Variance of 1 :

[[ 0.74108496     -0.04699152][-0.04699152      0.15890399]]

Variance of 2 :

[[ 0.03092742      0.00041713] [ 0.00041713      0.00753385]]]
```

The Obtained parameters and the true parameters are almost same