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### 1 Data structures

# 1.1 Segment Tree

```
1 | struct Node{
    ll val = 0;
3 };
  Node operator+(Node a, Node b) {return {a.val+b.val};}
  class Segment_Tree{
   public:
     int n;
    vector<Node> tree;
    Segment_Tree(int x = 1e5+10){
10
      n = x;
11
       tree.resize(2*n+1);
12
    }
13
14
    void build(vi &arr){
15
      for(int i=0;i<n;i++)tree[n+i] = {arr[i]};</pre>
      for(int i = n-1; i>0;i--)tree[i] = tree[i*2]+tree[i*2+1];
17
    }
18
19
    void update(int p, ll val){
20
       for(t[p+=n] = {val};p>1;p>>=1)tree[p>>1] = tree[p]+t[p^1];
21
    }
22
23
    11 query(int 1,int r){
24
      Node s;
25
      for(l+=n,r+=n; l<r; l>>=1, r>>=1)
        if(l\&1)s = s+ tree[l++];
         if(r\&1)s = s+ tree[--r];
28
       }
29
      return s.val;
30
31
32 };
```

# 1.2 Merge Sort Tree

```
struct Node{
     vi val;
2
     int search(int x){
       int 1 = 0, r = sz(val)-1;
       while(l<=r){</pre>
         int m = 1+(r-1)/2;
         if(val[m] < x)l = m+1;
         else r = m-1;
9
10
       return sz(val)-l;
11
12
13
14
   Node operator+(Node a, Node b){
15
     int i=0, j=0;
16
     Node aux;
     while (i < sz(a.val) \&\& j < sz(b.val)){
18
       if (a.val[i] < b.val[j] ) aux.val.pb(a.val[i++]);</pre>
19
       else aux.val.pb(b.val[j++]);
20
21
     while (i<sz(a.val)) aux.val.pb(a.val[i++]);</pre>
     while (j<sz(b.val)) aux.val.pb(b.val[j++]);</pre>
23
     return aux:
24
25
   class Segment_Tree{
26
     public:
27
     int n,k=0;
28
     vector<Node> tree;
29
     Segment_Tree(int x = 1e5+10){
30
       n = x;
31
       while((1<<k)<n)k++;
32
       tree.resize(2*(1<<k)+1);
33
34
     void build(vi &arr){
35
       for(int i=0;i<n;i++)tree[(1<<k)+i].val.pb(arr[i]);</pre>
36
       for(int i = (1<<k)-1; i>0;i--)tree[i] = tree[i*2]+tree[i*2+1];
37
     }
38
39
     void query(int a,int b,ll &ans,int i){
40
       a += (1 << k);
41
```

```
b += (1 << k);
42
        while(a<=b){</pre>
43
          if(a%2 == 1)ans += tree[a++].search(i);
44
          if(b%2 == 0)ans += tree[b--].search(i);
45
           a/=2;
46
           b/=2;
47
48
     }
49
<sub>50</sub> | };
```

#### 1.3 Fenwick Tree

```
1 | struct Node{
     11 n = 0;
     Node operator+(Node b){return {n+b.n};}
   };
4
5
   class Fenwick_Tree{
   public:
     vector<Node> tree;
     int n:
     Fenwick_Tree(int x){
       n = x+1;tree.resize(n);
11
     }
12
13
     11 sum(int r){
14
       r++:
15
       Node ans = \{0\};
16
       while(r){
17
         ans = ans + tree[r];
18
         r -= r&-r;
19
20
       return ans.n;
21
22
23
     void update(int id, Node val){
24
       id++;
25
       while(id < n){
26
         tree[id] = tree[id]+val;
27
         id += id&-id;
28
29
    }
30
31 };
```

# 1.4 Sparse Table

```
1 | struct Node{
     int val = 0;
     Node operator+(Node b){return {__gcd(val,b.val)};}
   };
4
   class SparseTable{
     public:
     vector<vector<Node>> sparse;
8
9
     SparseTable(int n=2e5+10){
10
       sparse.assign(n , vector<Node> (log2(n)+1));
11
12
13
     void build(const vi &a){
14
       for(int i=0;i<sz(a);i++)
15
         sparse[i][0] = {a[i]};
16
17
       for(int j=1;(1<<j)<=sz(a);j++)
18
         for(int i=0;i+(1<<j)-1 <sz(a);i++)
19
           sparse[i][j]= sparse[i][j-1]+sparse[i+(1<<(j-1))][j-1];
20
     }
21
22
     int query(int 1, int r){
23
       int len = r-l+1;
24
       int k = log2(len);
25
       return (sparse[l][k]+sparse[r-(1<<k)+1][k]).val;
26
     }
27
28
29 };
```

# 1.5 Disjoint Set Union

```
class DSU{
     private:
     vi parent,rank,size;
     int c;
     public:
     int mx = 0;
     DSU(int n):parent(n+1),rank(n+1,0),size(n+1,1),c(n){
       iota(all(parent),0);
8
     }
9
10
     int find(int u){return parent[u] == u?u:parent[u] = find(parent[u]) ;}
11
12
     bool same(int u,int v){return find(u)==find(v);}
13
14
     int get_size(int u){return size[find(u)];}
15
16
     int count(){return c;}
17
18
     void merge(int u,int v){
19
       u = find(u);
20
       v = find(v);
21
       if(u!=v){
22
         c--;
23
         if(rank[u] > rank[v])swap(u,v);
24
         parent[u] = v;
25
         size[v] += size[u];
26
         if(rank[u] == rank[v])rank[v]++;
         mx = max(mx, size[v]);
28
29
30
31 };
```

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# 2 Graphs

### 2.1 DFS

```
void dfs(int u){
vis[u] = 1;
for(auto v:adj[u]){
if(!vis[v])dfs(v);
}
}
```

#### 2.2 BFS

```
1  queue<int> q;
2  q.push(0);
3  while(!q.empty()){
4   int u = q.front();
5  q.pop();
6  for(int v:adj[u]){
7   if (!vis[v]) {
8    vis[v] = 1;
9   q.push(v);
10  }
11  }
12 }
```

# 2.3 Topological Sort

```
vi ts;
   queue<int> q;
   for (int i = 1; i < n+1; i++)
     if(!in[i])q.push(i);
5
   while (!q.empty()) {
6
     int u=q.front();
     q.pop();
8
     ts.pb(u);
9
     for (int v : adj[u]) {
10
       in[v]--;
11
       if(!in[v])q.push(i);
12
     }
13
   }
14
15
if(sz(ts)!=n)cout <<"IMPOSSIBLE";</pre>
```

- 2.4 Dijkstra
- 2.5 Bellman-Ford
- 2.6 Floyd-Warshall
- 2.7 SCC Kosaraju

```
class SCC{
   private:
     int n;
     vector<vi> adj;
     vector<vi> adj_t;
     vector<vi> adj_cond;
     vi order;
     vector<bool> vis;
     vi who;
     int comp;
   public:
11
     SCC(int n,vector<vi> &a,vector<vi>&b):n(n),adj(a),adj_t(b){
       comp = -1;
       who.resize(n);
       vis.resize(n);
15
       for(int i=0;i<n;i++)</pre>
16
         if(!vis[i])dfs1(i);
17
18
       vis.assign(n,0);
19
       for(int i=n-1;i>=0;i--)
20
         if(!vis[order[i]]){
21
            comp++;
22
           dfs2(order[i]);
23
24
       adj_cond.resize(comp+1);
25
       for(int u=0;u<n;u++)</pre>
26
         for(auto v:adj[u])
27
           if(who[v]!=who[u])
28
              adj_cond[who[u]].pb(who[v]);
29
     }
30
31
     void dfs1(int u) {
32
       vis[u] = true;
33
       for (int v:adj[u])
34
         if (!vis[v])dfs1(v);
35
       order.pb(u);
36
```

dfs2(order[i]);

74

```
}
                                                                                               if (!vis[v])dfs2(v);
37
                                                                                     32
                                                                                             who[u] = comp;
                                                                                     33
38
     void dfs2(int u) {
                                                                                           }
39
                                                                                     34
       vis[u] = 1;
40
                                                                                     35
       for (int v : adj_t[u])
                                                                                           //~a->b ~b->a
                                                                                     36
41
         if (!vis[v])dfs2(v);
                                                                                           void addOR(int a, bool af, int b, bool bf) {
42
                                                                                     37
                                                                                             a += a + (af ^ 1);
       who [u] = comp;
43
                                                                                     38
                                                                                             b += b + (bf ^ 1);
     }
44
                                                                                     39
45 };
                                                                                             adj[a ^ 1].push_back(b);
                                                                                             adj[b ^ 1].push_back(a);
2.8
     2	ext{-SAT}
                                                                                             adj_t[b].push_back(a ^ 1);
                                                                                     42
                                                                                             adj_t[a].push_back(b ^ 1);
                                                                                     43
                                                                                          }
1 | class SAT{
                                                                                     44
   private:
                                                                                     45
                                                                                           //( a OR b ) ^ (~a or ~b)
     int n;
                                                                                     46
                                                                                           void addXOR(int a, bool af, int b, bool bf) {
     vector<vi> adj;
                                                                                     47
                                                                                             addOR(a, af, b, bf);
     vector<vi> adj_t;
                                                                                     48
5
                                                                                             addOR(a, !af, b, !bf);
     vector<vi> adj_cond;
                                                                                     49
6
                                                                                          }
     vi order;
                                                                                     50
7
                                                                                          //(a -> b)
     vector<bool> vis;
                                                                                           void _add(int a,bool af,int b,bool bf) {
     vi who:
                                                                                             a += a + (af ^ 1);
     vector<bool> ans;
                                                                                     53
10
                                                                                             b += b + (bf ^ 1);
     int comp;
                                                                                     54
11
                                                                                             adj[a].push_back(b);
   public:
                                                                                     55
12
                                                                                             adj_t[b].push_back(a);
                                                                                     56
13
                                                                                           }
     SAT(int m=0){
                                                                                     57
14
       n = (m << 1);
                                                                                     58
15
                                                                                           //(a->b)^(b->a)
       adj.resize(n);
                                                                                     59
16
                                                                                           void add(int a,bool af,int b,bool bf) {
       adj_t.resize(n);
                                                                                     60
17
                                                                                             _add(a, af, b, bf);
                                                                                     61
       vis.assign(n,0);
18
                                                                                             _add(b, !bf, a, !af);
       who.assign(n,-1);
                                                                                     62
19
                                                                                           }
     }
                                                                                     63
20
                                                                                     64
21
                                                                                           bool solve_SAT(){
     void dfs1(int u) {
                                                                                     65
^{22}
                                                                                             for(int i=0;i<n;i++)</pre>
       vis[u] = true;
                                                                                     66
23
                                                                                               if(!vis[i])dfs1(i);
       for (int v:adj[u])
                                                                                     67
24
         if (!vis[v])dfs1(v);
                                                                                     68
^{25}
                                                                                             comp = -1;
       order.pb(u);
                                                                                     69
26
                                                                                             vis.assign(n,0);
     }
                                                                                     70
27
                                                                                             for(int i=sz(order)-1;i>=0;i--)
                                                                                     71
28
                                                                                               if(!vis[order[i]]){
     void dfs2(int u) {
                                                                                     72
29
                                                                                                 comp++;
       vis[u] = 1;
                                                                                     73
30
```

for (int v : adj\_t[u])

31

```
}
75
       ans.assign(n/2,0);
76
       for(int i=0;i<n;i+=2){</pre>
77
          if(who[i] == who[i+1])return 0;
78
          ans[i/2] = (who[i] > who[i+1]);
79
       }
80
       return 1;
81
82
83
     bool operator[](int i){
84
       return ans[i];
85
86
87
88
```

#### 2.9 Euler Paths and cycles

#### 2.9.1 Directed Graphs

```
struct EulerSolver
   private:
     vector<vector<pii>> adj;
     int n,edges;
     vi in,out;
5
     vi ans,edge_ans;
6
     int root;
7
     vi done:
8
     void dfs(int u){
9
       while(done[u] < sz(adj[u])){</pre>
10
         auto [v,id] = adj[u][done[u]++];
11
         dfs(v);
12
         edge_ans.pb(id);
13
14
       ans.pb(u);
15
16
   public:
17
     EulerSolver(vector<vector<pii>>> &a,int t):adj(a){
18
       n = t;
19
       edges = 0;
20
       in.assign(n,0);
21
       out.assign(n,0);
22
       done.assign(n,0);
23
       root = -1;
24
       for(int u=0;u< n;u++)
25
```

```
for(auto v:adj[u]){
26
            edges++;
27
            in[v.F]++;
28
            out[u]++;
29
         }
30
31
     }
32
33
     bool possible(){
34
       int cnt1 =0,cnt2 =0;
       bool ok = 1;
36
       for(int i=0;i<n;i++){
37
         if (in[i] - out[i] == 1) cnt1++:
38
         if (out[i] - in[i] == 1) cnt2++, root = i;
         if (abs(in[i] - out[i]) > 1) ok = 0;
40
41
       if(cnt1 > 1 || cnt2 > 1)ok = 0;
42
       if(!ok)return 0;
44
       if(root == -1)
         for(int i=0;i<n;i++)</pre>
46
            if(out[i])root = i;
47
48
       if(root == -1)return 1;
49
       dfs(root);
50
51
       if(sz(ans) != edges+1)return 0;
52
       reverse(all(ans));
53
       reverse(all(edge_ans));
54
       return 1;
55
     }
56
57
     int size(){
58
       return ans.size():
59
     }
60
61
     int operator()(int i,bool x){
62
       if(x)return ans[i];
63
       else return edge_ans[i];
64
     }
65
66 };
```

#### 2.9.2 Unirected Graphs

```
struct EulerSolver{
   private:
2
     vector<vector<pii>>> adj;
     int n,edges;
4
     vi ans,edge_ans;
     vi deg;
     int root;
     vi done;
     vector<bool> vis;
10
     void dfs(int u){
11
       while(done[u] < sz(adj[u])){</pre>
12
         auto [v,id] = adj[u][done[u]++];
13
          if(vis[id])continue;
         vis[id]=1;
15
         dfs(v);
16
         edge_ans.pb(id);
17
       }
18
       ans.pb(u);
19
20
   public:
21
     EulerSolver(vector<vector<pii>>> &a,int t):adj(a),n(t){
22
       edges = 0;
23
       done.assign(n,0);
^{24}
       deg.assign(n,0);
25
       root = -1;
26
       for(int u=0;u<n;u++)</pre>
27
         for(auto v:adj[u]){
28
            edges++;
29
           deg[v.F]++;
30
           deg[u]++;
31
32
       vis.assign(edges/2,0);
33
     }
34
35
     bool possible(){
36
       int odd = 0;
37
       for(int i=0;i<n;i++)</pre>
38
         if((deg[i]/2)&1){
39
            odd++;
40
           root = i;
41
^{42}
43
```

```
44
       if(odd>2)return 0;
45
46
       if(root == -1)
47
         for(int i=0;i<n;i++)</pre>
48
           if(deg[i]){root = i;break;}
49
50
       if(root == -1)return 1;
51
       dfs(root);
52
53
       if(sz(ans) != edges/2+1)return 0;
54
       reverse(all(ans));
55
       reverse(all(edge_ans));
56
       return 1;
57
     }
58
59
     int size(){
60
       return ans.size();
61
     }
62
63
     int operator()(int i,bool x){
64
       if(x)return ans[i];
65
       else return edge_ans[i];
66
67
68 };
```

3 TREES - Page 8 of 12

### 3 Trees

### 3.1 LCA - Binary Lifting

#### 3.1.1 Normal LCA

```
const int MAX = 1e5+5,LG=18;
   vi deep(MAX);//Si tiene peso vi cost(MAX)
   int par[MAX] [LG+1];
   void dfs(int u = 1,int p=0){// U = raiz del arbol}
     par[u][0] = p;
     deep[u] = deep[p]+1;//cost[u] += cost[p]
7
     for(int i=1;i<=LG;i++)par[u][i]=par[par[u][i-1]][i-1];</pre>
     for(int v:adj[u]){
9
       if(v!=p){
10
          dfs(v,u);
11
12
13
14
15
   int lca(int u,int v){
16
     if(deep[u] < deep[v])swap(u,v);</pre>
17
     for(int k=LG:k>=0:k--)
18
       if(deep[par[u][k]] >= deep[v])
19
          u = par[u][k];
20
     if(u==v)return u;
21
     for(int k=LG; k>=0; k--)
22
       if(par[u][k]!=par[v][k])
23
         u=par[u][k],v=par[v][k];
24
     return par[u][0];
25
26
27
   int dist(int u,int v){
28
     int lc = lca(u,v);
29
     return deep[u]+deep[v]-(deep[lc]<<1);</pre>
30
31
32
   int kth(int u.int k){
33
     assert(k>=0);
34
     for(int i=0;i<=LG;i++)</pre>
35
       if(k&(1<<i))u = par[u][i];
36
     return u;
37
```

38 }

#### 3.1.2 Min/Max weight on the path

```
const int MAX = 1e5+5.LG=18:
   vector<vector<pii>>> adj(MAX,vector<pii> ());
   vi deep(MAX);
   int par[MAX] [LG+1];
   int mn[MAX][LG+1];
   int mx[MAX][LG+1];
   void dfs(int u=1,int p=0,int costmn = INF,int costmx = -INF){
     par[u][0] = p;
     deep[u] = deep[p]+1;
11
     if(p!=0){
12
       mn[u][0] = costmn;
13
       mx[u][0] = costmx;
14
15
     for(int i=1;i<=LG;i++){</pre>
       par[u][i]=par[par[u][i-1]][i-1];
       mn[u][i]=min(mn[u][i-1],mn[par[u][i-1]][i-1]);
18
       mx[u][i]=max(mx[u][i-1], mx[par[u][i-1]][i-1]);
19
     }
20
21
     for(auto [v,t]:adj[u]){
22
       if(v!=p){
23
         dfs(v,u,t,t);
24
25
     }
26
27
28
   pii minmax(int u,int v){
     pii ans = {INF,-INF};
30
     if(deep[u] < deep[v])swap(u,v);</pre>
31
     for(int k=LG;k>=0;k--)if(deep[par[u][k]] >= deep[v]){
32
       ans.F = min(ans.F,mn[u][k]);
33
       ans.S = max(ans.S, mx[u][k]);
34
       u = par[u][k];
35
     }
36
     if(u==v)return ans;
37
     for(int k=LG;k>=0;k--)if(par[u][k]!=par[v][k]){
38
       ans.F = min(\{ans.F, mn[u][k], mn[v][k]\});
39
```

```
ans.S = max({ans.S,mx[u][k],mx[v][k]});
u=par[u][k],v=par[v][k];
}
ans.F = min({ans.F,mn[u][0],mn[v][0]});
ans.S = max({ans.S,mx[u][0],mx[v][0]});
return ans;
}
```

## 3.2 Centroid Decomposition

```
class Centroid{
   private:
     vector<vi> tree;
     vi par;
4
     vi sub;
5
     vector<bool> check;
6
     int n;
7
   public:
8
     Centroid(vector<vi> &t):tree(t){
       n = tree.size();
10
       par.resize(n);
11
       sub.resize(n);
12
       check.resize(n);
13
       build();
14
     }
15
16
     void build(int u = 0, int p = -1){
17
       dfs(u, p);
18
       int c = get_centroid(u,p,sub[u]);
19
       check[c] = 1;
20
       par[c] = p+1;
21
^{22}
       for (auto v : tree[c]){
23
         if(!check[v])
24
            build(v, c);
^{25}
       }
26
27
     }
28
29
     int dfs(int u,int p){
30
       if(check[u])return 0;
31
       sub[u] = 1;
32
```

```
for(int v:tree[u])
33
         if(v!=p)sub[u]+=dfs(v,u);
34
35
       return sub[u];
36
     }
37
38
     int get_centroid(int u,int p,int x){
39
       for(auto v:tree[u])
40
         if(v!=p && sub[v]*2>x && !check[v])return get_centroid(v,u,x);
41
42
       return u;
43
     }
44
45
     int operator[](int i){
46
       return par[i];
47
     }
48
49 };
```

# 3.3 Euler Tour Technique

### 3.4 Tree Matching

#### 3.5 Diameter

```
vector<vector<pii>>> adj;
   vector<bool> vis;
   int bfs(int n,vll &d,int v = 0){
     vis.assign(n,0);
     d.assign(n,0);
     d[v] = 0;
     queue<int> q;
     q.push(v);
     pll last = \{v,0\};
10
     vis[v] = 1;
11
     while(!q.empty()){
12
       int u = q.front();q.pop();
13
       for(auto [w,c]:adj[u]){
14
         if(vis[w])continue:
15
         d[w] = d[u] + c;
16
         q.push(w);
17
         vis[w] = 1;
18
         if(d[w]>last.S)last = {w,d[w]};
19
20
```

18

```
}
21
     return int(last.F);
^{22}
   }
23
^{24}
    void solve(){
25
      int n;cin >> n;
26
      adj.assign(n,vector<pii> ());
27
     for(int i=1;i<n;i++){</pre>
28
        int a,b;ll c;
29
        cin >> a >> b >> c;
30
        adi[--a].pb(\{--b,c\});
31
        adj[b].pb({a,c});
32
     }
33
     vll dx(n), dy(n);
      int a =bfs(n,dx);
      int b =bfs(n,dy,a);
36
      bfs(n,dx,b);
37
38
     for(int i=0;i<n;i++){</pre>
39
        cout << \max(dx[i], dy[i]) << "_\n"[i==(n-1)];
40
     }
41
42
43
```

### 3.6 Heavy Light Decomposition

```
class HLD
   private:
2
     int n;
     vector<vi> adj;
     vi parent;
5
     vi heavy;
     vi depth;
     vi root;
     vi treePos;
9
     Segment_Tree tree;
10
11
     int dfs(int u =0){
12
       int size = 1, mx_sub = 0;
13
       for(auto v:adj[u])
14
         if(v!=parent[u]){
15
           parent[v] = u;
16
           depth[v] = depth[u]+1;
17
```

```
if(sub > mx_sub){
19
              heavy[u] = v;
20
              mx_sub = sub;
21
22
            size += sub;
23
         }
24
       return size;
25
     }
26
27
     template <class BinaryOperation>
28
     void processPath(int u, int v, BinaryOperation op) {
29
       for (; root[u] != root[v]; v = parent[root[v]]) {
30
         if (depth[root[u]] > depth[root[v]]) swap(u, v);
31
          op(treePos[root[v]], treePos[v] + 1);
32
33
       if (depth[u] > depth[v]) swap(u, v);
34
       op(treePos[u], treePos[v] + 1);
     }
36
37
     void init(vi &a){
38
       for(int i=0,crt=0;i<n;++i){</pre>
39
         if(parent[i] == -1 || heavy[parent[i]]!=i){
40
           for(int j = i; j!=-1; j = heavy[j]){
41
              root[j] = i;
42
              treePos[i] = crt++;
43
44
         }
45
46
       tree = Segment_Tree(n);
47
       for(int i=0;i<n;i++){</pre>
48
          tree.update(treePos[i],a[i]);
49
       }
50
     }
51
   public:
54
     HLD(int n,vector<vi> &vale,vi &a):n(n),adj(vale){
55
       parent.assign(n,0);
56
       heavy.assign(n,-1);
57
       depth.assign(n,0);
58
       root.resize(n);
59
       treePos.assign(n,0);
60
```

int sub = dfs(v);

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```
parent[0] = -1;
61
       dfs();
62
       init(a);
63
64
65
     void update(int u,int &val){
66
       tree.update(treePos[u],val);
67
68
69
     void updatePath(int u, int v, int value) {
70
       processPath(u, v, [this, &value](int 1, int r) {
71
         tree.update_range(1, r, value);
72
       });
73
     }
74
75
     int query(int u,int v){
76
       int ans = 0:
77
       processPath(u,v,[this,&ans](int l,int r){
78
         ans = \max(ans,tree.query(1,r));
79
       });
80
       return ans;
81
82
83 | };
```

# 4 Math

#### 4.1 Identities

```
\begin{split} C_n &= \frac{2(2n-1)}{n+1} C_{n-1} \\ C_n &= \frac{1}{n+1} \binom{2n}{n} \\ C_n &\sim \frac{4^n}{n^{3/2} \sqrt{\pi}} \\ \sigma(n) &= O(\log(\log(n))) \text{ (number of divisors of } n) \\ F_{2n+1} &= F_n^2 + F_{n+1}^2 \\ F_{2n} &= F_{n+1}^2 - F_{n-1}^2 \\ \sum_{i=1}^n F_i &= F_{n+2} - 1 \\ F_{n+i} F_{n+j} - F_n F_{n+i+j} &= (-1)^n F_i F_j \\ \text{(M\"obius Inv. Formula) Let } g(n) &= \sum_{d \mid n} f(d), \text{ then } f(n) &= \sum_{d} d \mid ng(d) \mu\left(\frac{n}{d}\right) \right). \end{split}
```

#### 4.2 Theorems

# 5 Strings

# 5.1 Suffix Array

```
1 struct suffix{
     int index;
     pii rank;
     bool operator<(suffix b){return rank<b.rank;}</pre>
     bool operator>(suffix b){return rank>b.rank;}
 6
7
   class Suffix_Array{
     public:
     string s; int n;
     vector<suffix> suffixes;
11
     vi lcp;
12
     Suffix_Array(string x){
       s = x + "$":
       n = sz(s);
15
       suffixes.resize(n);
     }
17
18
19
     void radix sort(vector<suffix> &suff){
20
       for(int i: vi{2,1}){
21
          auto key = [&](const suffix &x){
22
            return i == 1?x.rank.F:x.rank.S;
23
         };
24
25
         int mx = 0;
26
         for (const auto &i:suff) { mx = max(mx, key(i)); }
27
         vector<int> occs(mx + 1);
28
         for (const auto &i:suff)occs[kev(i)]++;
29
          vector<int> start(mx + 1);
30
         for (int i=1;i<=mx; i++) start[i] = start[i-1]+occs[i-1];</pre>
31
32
         vector<suffix> new_arr(suff.size());
33
         for (const auto &i : suff) {
34
            new_arr[start[key(i)]] = i;
35
            start[key(i)]++;
36
         }
37
```

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```
suff = new_arr;
38
       }
39
     }
40
41
     void build(){
42
       for(int i=0;i<n;i++)suffixes[i].index = i , suffixes[i].rank = {s[i</pre>
43
           ],(i+1<n?s[i+1]:-1)};
       sort(all(suffixes));
44
       vi equiv(n);
45
46
       for(int i=1;i<n;i++){</pre>
47
          auto c_val = suffixes[i].rank;
48
          int cs = suffixes[i].index:
49
         auto p_val = suffixes[i - 1].rank;
         int ps = suffixes[i-1].index;
51
         equiv[cs] = equiv[ps] + (c_val > p_val);
52
       }
53
54
       for(int cmp_ant = 1;cmp_ant <n; cmp_ant <<=1){</pre>
55
         for(auto &x:suffixes)
56
           x.rank = {equiv[x.index],equiv[(x.index+cmp_ant)%n]};
57
58
         //Std sort O(nlognlogn) Radix Sort O(nlogn)
59
         radix_sort(suffixes);
60
61
         for(int i=1;i<n;i++){</pre>
62
           auto c_val = suffixes[i].rank;
63
            int cs = suffixes[i].index;
64
           auto p_val = suffixes[i - 1].rank;
65
           int ps = suffixes[i-1].index;
66
           equiv[cs] = equiv[ps] + (c_val > p_val);
67
         }
68
       }
69
     }
70
71
     void build_lcp(){
72
       vector<int> suff_ind(n);
73
       for (int i = 0; i < n; i++)suff_ind[suffixes[i].index] = i;</pre>
74
       lcp.resize(n-1);
75
       int start_at = 0;
76
       for (int i = 0; i < n - 1; i++) {
77
         int prev = suffixes[suff_ind[i] - 1].index;
78
          int curr_cmp = start_at;
79
```

```
while (s[i + curr_cmp] == s[prev + curr_cmp])curr_cmp++;
80
         lcp[suff_ind[i] - 1] = curr_cmp;
81
         start_at = max(curr_cmp - 1, 0);
82
83
    }
84
85
     void show(){
86
       for(int i=0;i<n;i++)cout << suffixes[i].index << "\"[(i+1)==n];
87
    }
88
89 };
```

### 6 Others