高速缓存

Cache Memories

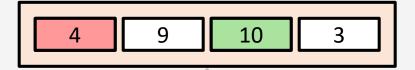


- □ 高速缓存的结构和工作原理
 Cache memory organization and operation
- 高速缓存对软件性能的影响
 Performance impact of caches

Cache memory organization and operation

缓存的基本概念 (回顾) General Cache Concepts (Reminder)



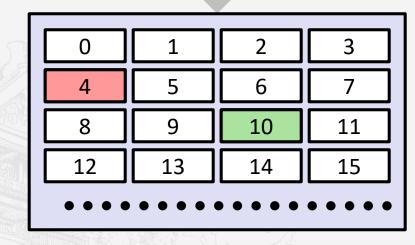


更小,更快,成本更高,缓存内存数据块的子集 Smaller, faster, more expensive memory caches a subset of the blocks

10

数据复制时,以"块"作为基本传输单元 Data is copied in block-sized transfer units

主存 Memory



更大,更慢,成本更低的内存,在逻辑上内存可以被划分为多个数据块 Larger, slower, cheaper memory viewed as partitioned into "blocks"

Cache memory organization and operation

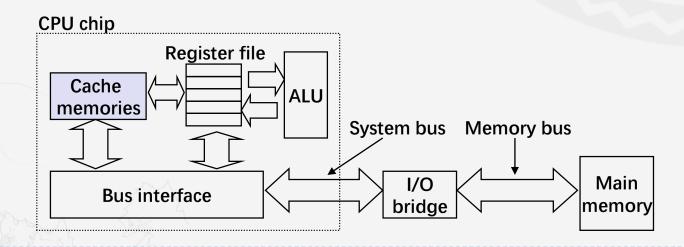
几个缓存设计原则 Many common design issues

- 每一个缓存项都要包含"标签" (ID) 和"内容" Each cached item has a "tag" (an ID) plus contents
- 需要一种快速有效的机制用来判断给定的数据是否被缓存 Need a mechanism to efficiently determine whether given item is cached
 - 通过对有效位置建立索引和约束规则
 Combinations of indices and constraints on valid locations
- ■未命中时,通常要选择一个现有缓存项,并被新缓存项所替代 On a miss, usually need to pick something to replace with the new item
 - 称之为"替换策略" called a "replacement policy"
- 一在写入时,需要传播更改的内容,或将该缓存项标记为"脏" On writes, need to either propagate change or mark item as "dirty"
 - 直写与回写 write-through vs. write-back
- 一不同的缓存场景采用不同的解决方案。我们以CPU中的高速缓存为例进行说明...... Different solutions for different caches. Lets talk about CPU caches as a concrete example…

Cache memory organization and operation

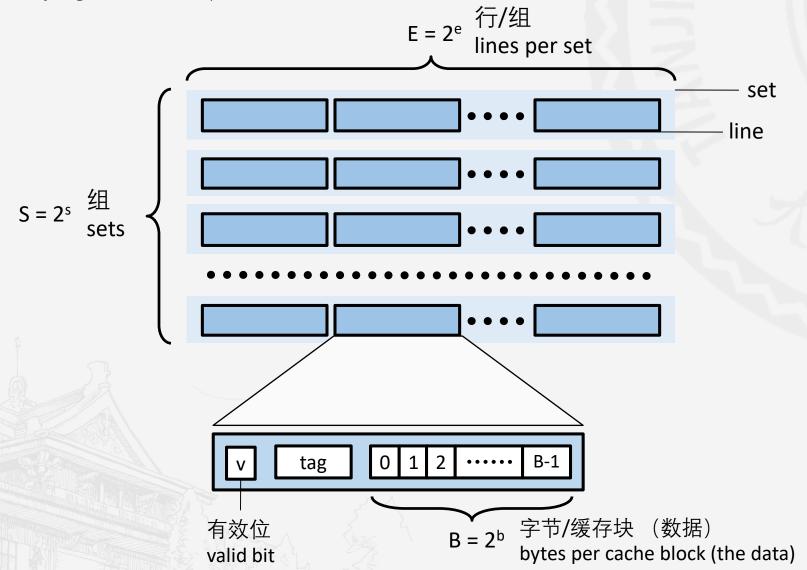
CPU高速缓存 CPU Cache Memories

- ■CPU高速缓存是一个小型的,快速的,基于SRAM技术的存储器,由硬件自动控制(对用户透明) CPU Cache memories are small, fast SRAM-based memories managed automatically in hardware
 - 用于保存频繁访问的主存数据块
 Hold frequently accessed blocks of main memory
- ■CPU首先在缓存(例如, L1、L2和L3)中查找数据, 然后才会在主存中查找数据 CPU looks first for data in caches (e.g., L1, L2, and L3), then in main memory
- 典型的系统结构:
 Typical system structure:



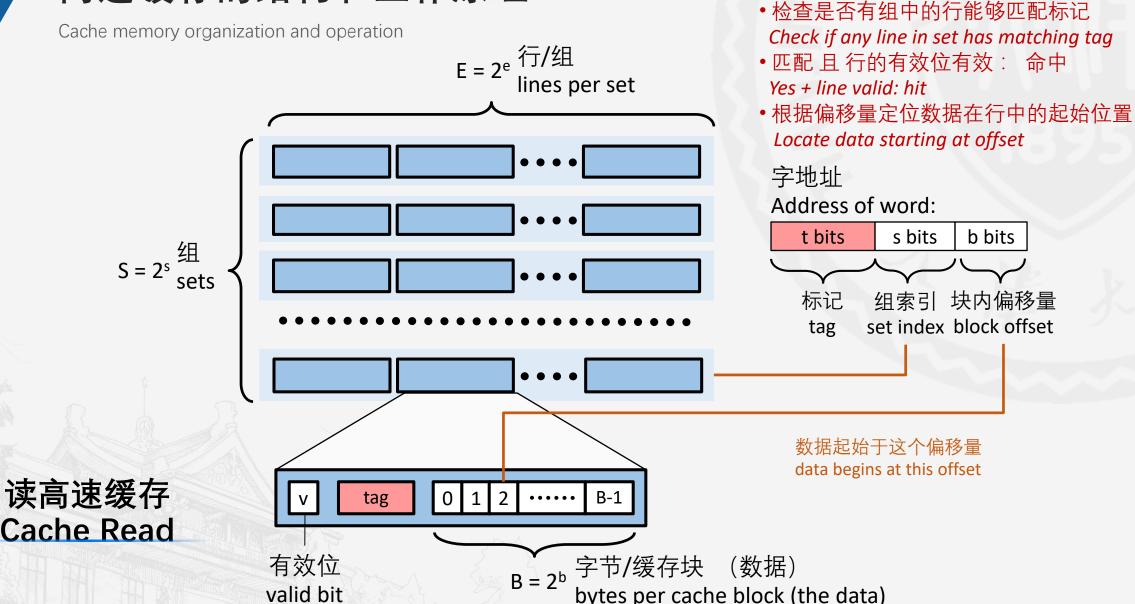
通用的高速缓存组织结构 (S, E, B) General Cache Organization (S, E, B)

Cache memory organization and operation



缓存容量 Cache size: C = S x E x B bytes

Cache memory organization and operation



• 确定组的位置

Locate set



Cache memory organization and operation

示例: 直接映射高速缓存 (E=1)

Example: Direct Mapped Cache (E = 1)

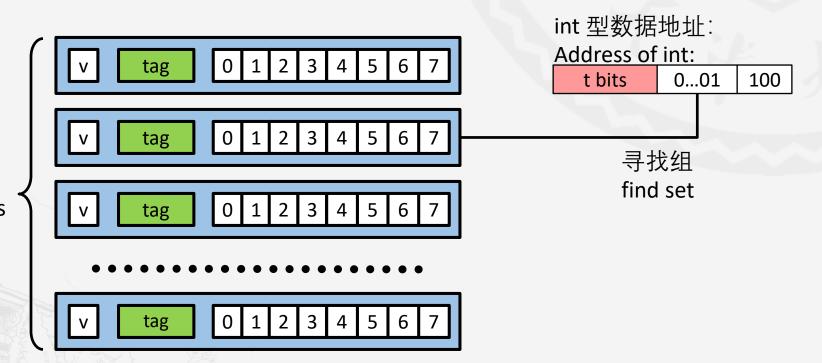
直接映射: 每组只有一行

Direct mapped: One line per set

假设:缓存块大小为8字节

Assume: cache block size 8 bytes

S = 2^s 组





Cache memory organization and operation

示例: 直接映射高速缓存 (E=1)

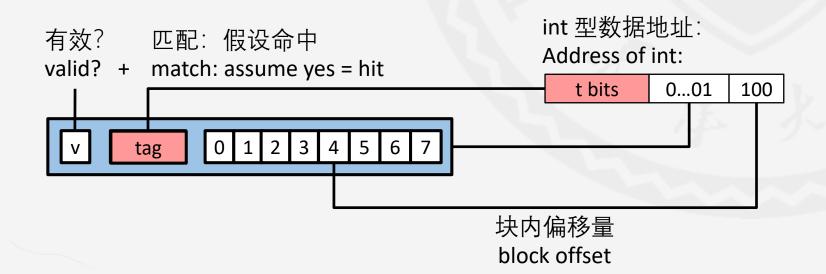
Example: Direct Mapped Cache (E = 1)

直接映射: 每组只有一行

Direct mapped: One line per set

假设:缓存块大小为8字节

Assume: cache block size 8 bytes





Cache memory organization and operation

示例: 直接映射高速缓存 (E=1)

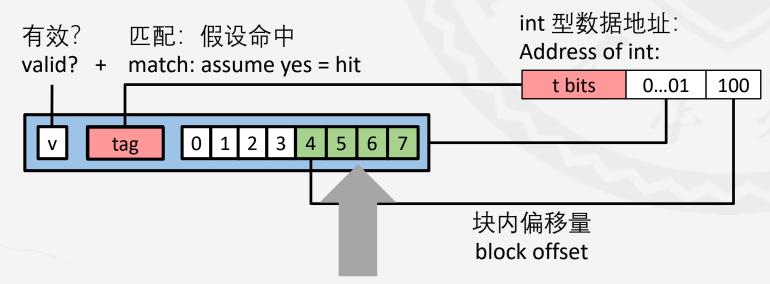
Example: Direct Mapped Cache (E = 1)

直接映射:每组只有一行

Direct mapped: One line per set

假设:缓存块大小为8字节

Assume: cache block size 8 bytes



int型数据(4字节)的位置 int (4 Bytes) is here

如果标记未匹配:原有的行将会被回收并替换 If tag doesn't match: old line is evicted and replaced

Cache memory organization and operation

直接映射高速缓存模拟 Direct Mapped Cache Simulation

Assume (假设):

- 4-bit addresses
- M=16 bytes
- B=2 bytes/block,
- S=4 sets
- E=1 Blocks/set

地址跟踪(读操作,每次读1字节) Address trace (reads, one byte per read):

0	$[0000_2],$	miss
1	$[0\underline{00}1_2],$	hit
7	$[0111_2],$	miss
8	$[1000_{2}],$	miss
0	$[0000_{2}]$	miss

	V	Tag	Block
Set 0	1	0	M[0-1]
Set 1			
Set 2			
Set 3	1	0	M[6-7]

Cache memory organization and operation

示例: E路组相联高速缓存 (假设: E=2)

Example: E-way Set Associative Cache (Assume: E=2)





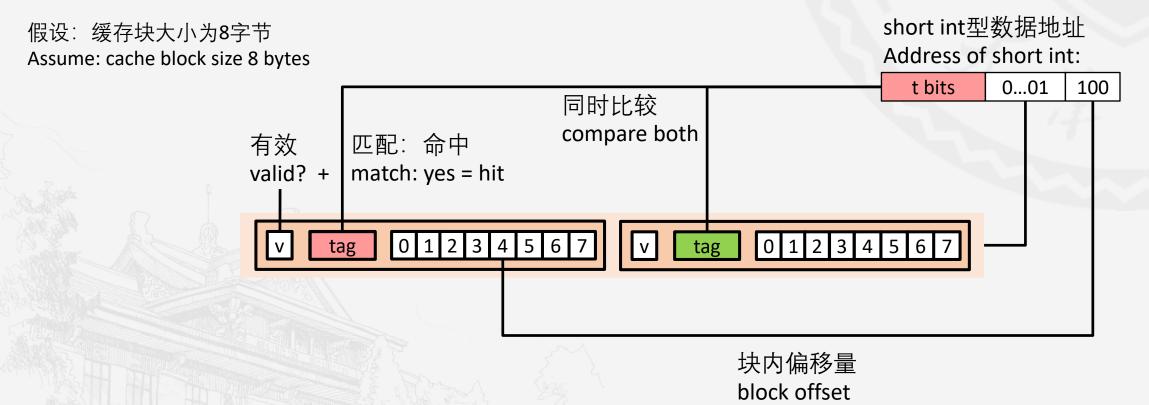
Cache memory organization and operation

示例: E路组相联高速缓存 (假设: E=2)

Example: E-way Set Associative Cache (Assume: E=2)

E = 2: 每组两行

E = 2: Two lines per set





Cache memory organization and operation

示例: E路组相联高速缓存 (假设: E=2)

Example: E-way Set Associative Cache (Assume: E=2)

short int (2 Bytes) is here

E = 2: 每组两行

E = 2: Two lines per set

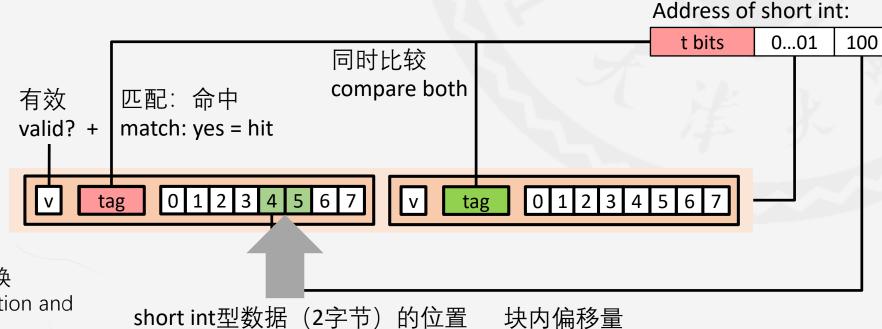
假设:缓存块大小为8字节

Assume: cache block size 8 bytes

没有成功匹配:

No match:

- 选择当前组中的一行被回收和替换
 One line in set is selected for eviction and replacement
- 替换策略: 随机, 最近最少使用 (LRU)
- Replacement policies: random, least recently used (LRU), ...



block offset

short int型数据地址

Cache memory organization and operation

2路组相联高速缓存模拟 2-Way Set Associative Cache Simulation

t=2	s=1	b=1
XX	Х	Х

Assume (假设):

- 4-bit addresses
- M=16 bytes
- B=2 bytes/block,
- S=2 sets
- E=2 Blocks/set

地址跟踪(读操作,每次读1字节) Address trace (reads, one byte per read):

0	$[00\underline{0}0_{2}],$	miss
1	$[00\underline{0}1_2],$	hit
7	$[01\underline{1}1_{2}],$	miss
8	$[10\underline{0}0_{2}],$	miss
0	$[00\underline{0}0_{2}]$	hit

·	V	Tag	Block
Set 0	1	00	M[0-1]
	1	10	M[8-9]

Set 1	1	01	M[6-7]
	0		



Cache memory organization and operation

- ■数据在存储系统中存在多份副本: Multiple copies of data exist:
 - ■一级缓存,二级缓存,主存和磁盘 L1, L2, Main Memory and Disk
- ■怎么处理写命中的情况? What to do on a write-hit?
 - 直写 (立即写入主存)
 Write-through (write immediately to memory)
 - ■回写 (至行被替换时才写入主存)
 Write-back (defer write to memory until replacement of line)
- ■怎么处理写未命中的情况? What to do on a write-miss?
 - 写分配 (加载至缓存, 然后更新缓存中的行)
 Write-allocate (load into cache, update line in cache)
 - 如果随后有更多在这个位置附近的写操作,会显著提升性能 Good if more writes to the location follow
 - 非写分配 (直接写入内存,不加载数据块至缓存)
 No-write-allocate (writes straight to memory, does not load into cache)

怎么处理写操作? What about writes?

典型的策略组合: Typical policy combination:

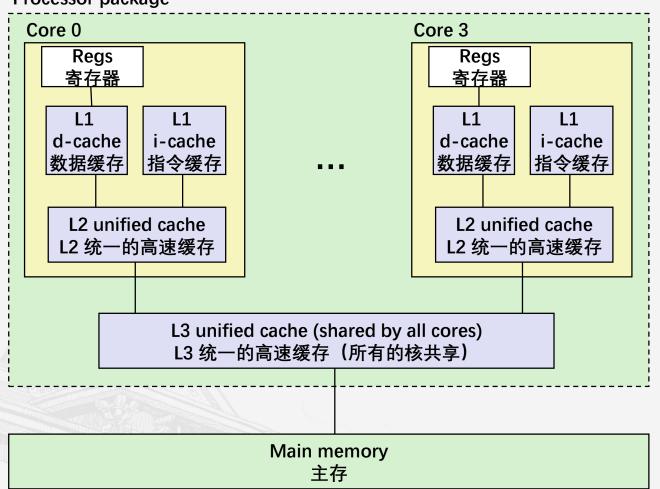
	写命中 Write-hit	写未命中 Write-miss
效率优先	回写	写分配
Efficiency first	Write-back	Write-allocate
可靠性优先	直写	非写分配
Reliability first	Write-through	No-write-allocate

Intel 酷睿 i7处理器高速缓存层次结构 Intel Core i7 Cache Hierarchy

Cache memory organization and operation

处理器封装

Processor package



L1 i-cache and d-cache:

32 KB, 8-way (8 lines per set), Access: 4 cycles

L2 unified cache:

256 KB, 8-way,

Access: 11 cycles

L3 unified cache:

8 MB, 16-way,

Access: 30-40 cycles

Block size: 64 bytes for all caches.



Cache memory organization and operation

■未命中率

Miss Rate

- 在缓存中找不到所引用的内存数据的百分比(未命中次数/总访问次数)= 1 命中率
 Fraction of memory references not found in cache
 (misses / accesses) = 1 hit rate
- ■典型值(百分数):
 Typical numbers (in percentages):
 - 一级缓存: **3% ~ 10%** 3-10% for L1
 - 在二级缓存中这个值非常小(例如: <1%),取决于缓存容量等因素 can be quite small (e.g., < 1%) for L2, depending on size, etc.

高速缓存的性能指标 Cache Performance Metrics

■命中时间

Hit Time

- 将缓存中的行数据发送到处理器所需的时间
 Time to deliver a line in the cache to the processor
 - 包括判定该行是否在缓存中的时间 includes time to determine whether the line is in the cache

典型值:

Typical numbers:

- 一级缓存: **1-2**个周期 1-2 clock cycle for L1
- 二级缓存: **5-20**个周期 1-2 clock cycle for L1



高速缓存的性能指标 Cache Performance Metrics

Cache memory organization and operation

■未命中惩罚 Miss Penalty

- ■由于缓存未命中所需要的额外数据访问时间 Additional time required because of a miss
- ■典型值:

Typical numbers:

- 主存: 50-200个时钟周期 50-200 cycles for main memory
- 趋势还在扩大! Trend: increasing!

这就是为什么用"未命中率"而不使用"命中率"作为性能指标的原因了

This is why "miss rate" is used instead of "hit rate"

■命中与未命中的巨大性能差异
Huge difference between a hit and a miss

- ■如果仅比较一级缓存和内存的话,可能相差达到100倍 Could be 100x, if just L1 and main memory
- ■你相信吗?99%命中率的缓存系统效率,两倍于97%命中率的缓存系统

Would you believe 99% hits is twice as good as 97%?

- 考虑下面的情况: 命中时间1个周期,未命中惩罚100个周期 Consider: cache hit time of 1 cycle, miss penalty of 100 cycles
- ■平均访问时间: Average access time

97% hits: 1 cycle + 0.03 * 100 cycles = **4 cycles**

99% hits: 1 cycle + 0.01 * 100 cycles = **2 cycles**



Cache memory organization and operation

编写缓存友好的代码 Writing Cache Friendly Code

- ■可以让程序在常见的场景下更快的运行 Make the common case go fast
 - 关注核心函数的内部循环 Focus on the inner loops of the core functions
- ■减少内部循环中的缓存未命中 Minimize the misses in the inner loops
 - ■对变量更好的重复利用(时间局部性)
 Repeated references to variables are good (temporal locality)
 - ■尽量使用步长为1的模式访问存储器(空间局部性) Stride-1 (步长为1) reference patterns are good (spatial locality)
- ■核心思想:通过理解高速缓存的工作机制,量化我们对局部性原理的定性认知 Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories

本章内容

- 高速缓存的结构和工作原理
 Cache memory organization and operation
- □ 高速缓存对软件性能的影响 Performance impact of caches
 - □通过循环重排提高空间局部性特征
 Rearranging loops to improve spatial locality
 - ■通过分块提高时间局部性特征
 Using blocking to improve temporal locality
 - □存储器山

The memory mountain

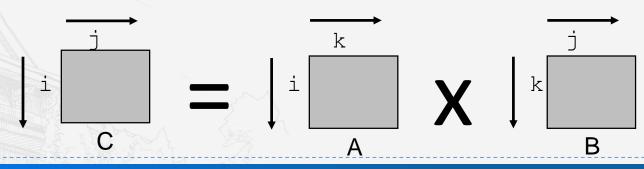
矩阵乘法的未命中率分析 Miss Rate Analysis for Matrix Multiply

Performance impact of caches

假设:

Assume:

- 每个矩阵是一个n×n的数组,数据类型为double, sizeof(double)==8
 Each matrix is an n×n array of double, with sizeof(double) == 8
- 缓存块大小为32字节(可以容纳4个64位数据) Cache block size = 32Bytes (big enough for four 64-bit words)
- 矩阵的维度(n)是一个非常大的值: 1/N趋近于0 Matrix dimension (N) is very large: Approximate 1/N as 0.0
- 缓存的容量较小,不足以同时缓存矩阵中的多行数据 Cache is not even big enough to hold multiple rows
- 一分析方法: 观察内部循环中的内存访问模式 Analysis Method: Look at access pattern of inner loop



Performance impact of caches

举例: 矩阵乘法 Matrix Multiplication Example

- ■n x n 矩阵相乘 Multiply N x N matrices
- ■共O(N³) 次操作(时间复杂度) O(N³) total operations
- 每个元素都需要进行N次读操作 N reads per source element
- ■每个目标元素都需要进行N次累加 N values summed per destination
 - 这些累加可能会在寄存器中进行 but may be able to hold in register

```
/* ijk */

/* ijk */

for (i=0; i<n; i++) {

for (j=0; j<n; j++) {

    sum = 0.0;

    for (k=0; k<n; k++)

        sum += a[i][k] * b[k][j];

    c[i][j] = sum;

}
```

C语言数组在内存中的布局(回顾) Layout of C Arrays in Memory (review)

Performance impact of caches

- C语言数组以"行优先"方式分配内存 C arrays allocated in row-major order
 - 每一行的元素在内存中的位置都是连续的 Each row in contiguous memory locations
- ■在一行中,逐列进行访问
 Stepping through columns in one row:

- 访问连续的元素
 accesses successive elements
- 如果块大小B大于8字节,则可利用空间局部性 if block size (B) > 8 bytes, exploit spatial locality
- 未命中率 = 8/B miss rate = 8 bytes / B

■在一列中,逐行进行访问
Stepping through rows in one column:

- 依次访问元素之间距离很远 accesses distant elements
- 没有空间局部性! no spatial locality!
- 未命中率 = 1 (即100%) miss rate = 1 (i.e. 100%)

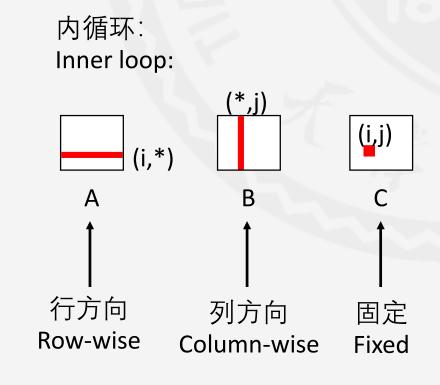
Performance impact of caches

矩阵乘法(ijk) Matrix Multiplication (ijk)

```
/* ijk */
for (i=0; i<n; i++) {
  for (j=0; j<n; j++) {
    sum = 0.0;
    for (k=0; k<n; k++)
        sum += a[i][k] * b[k][j];
    c[i][j] = sum;
  }
}</pre>
```

每次内循环迭代的未命中次数 Misses per inner loop iteration:

```
<u>A</u> <u>B</u> <u>C</u> 0.25 1.0 0.0
```



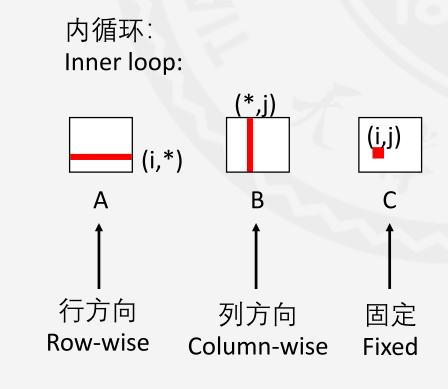
Performance impact of caches

矩阵乘法(jik) Matrix Multiplication (jik)

```
/* jik */
for (j=0; j<n; j++) {
  for (i=0; i<n; i++) {
    sum = 0.0;
    for (k=0; k<n; k++)
        sum += a[i][k] * b[k][j];
    c[i][j] = sum
  }
}</pre>
```

每次内循环迭代的未命中次数 Misses per inner loop iteration:

```
<u>A</u> <u>B</u> <u>C</u> 0.25 1.0 0.0
```



Performance impact of caches

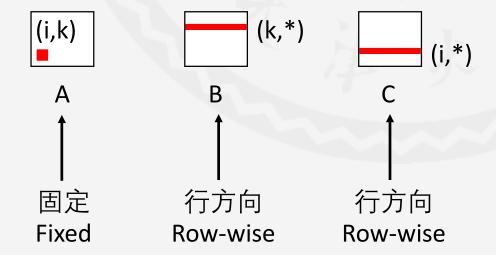
矩阵乘法(kij) Matrix Multiplication (kij)

```
/* kij */
for (k=0; k<n; k++) {
  for (i=0; i<n; i++) {
    r = a[i][k];
    for (j=0; j<n; j++)
       c[i][j] += r * b[k][j];
  }
}</pre>
```

每次内循环迭代的未命中次数 Misses per inner loop iteration:

```
<u>A</u> <u>B</u> <u>C</u> 0.0 0.25 0.25
```

内循环: Inner loop:



Performance impact of caches

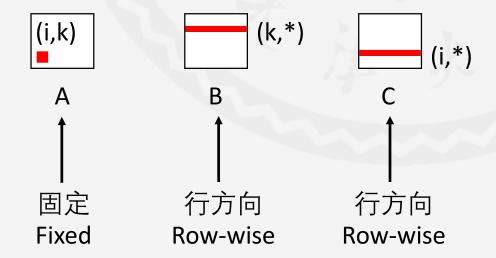
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```
/* ikj */
for (i=0; i<n; i++) {
  for (k=0; k<n; k++) {
    r = a[i][k];
    for (j=0; j<n; j++)
       c[i][j] += r * b[k][j];
  }
}</pre>
```

每次内循环迭代的未命中次数 Misses per inner loop iteration:

<u>A</u> <u>B</u> <u>C</u> 0.0 0.25 0.25

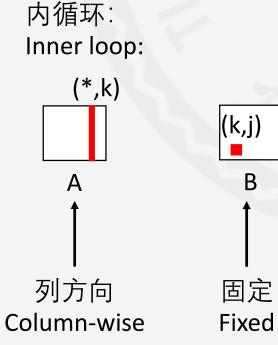
内循环: Inner loop:

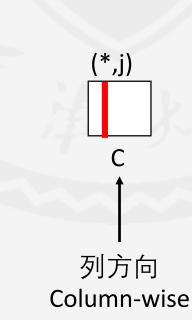


Performance impact of caches

矩阵乘法(jki) Matrix Multiplication (jki)

```
/* jki */
for (j=0; j<n; j++) {
  for (k=0; k<n; k++) {
    r = b[k][j];
    for (i=0; i<n; i++)
        c[i][j] += a[i][k] * r;
  }
}</pre>
```





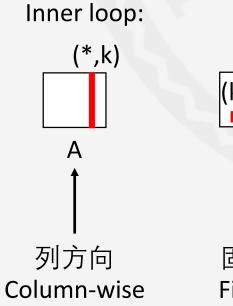
每次内循环迭代的未命中次数 Misses per inner loop iteration:

<u>A</u> <u>B</u> <u>C</u> 1.0 0.0 1.0

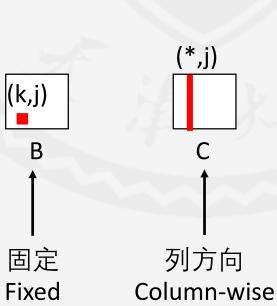
Performance impact of caches

矩阵乘法(kji) Matrix Multiplication (kji)

```
/* kji */
for (k=0; k<n; k++) {
  for (j=0; j<n; j++) {
    r = b[k][j];
    for (i=0; i<n; i++)
        c[i][j] += a[i][k] * r;
  }
}</pre>
```



内循环:



每次内循环迭代的未命中次数 Misses per inner loop iteration:

<u>A</u> <u>B</u> <u>C</u> 1.0 1.0

Performance impact of caches

矩阵乘法小结 Summary of Matrix Multiplication

```
for (i=0; i<n; i++) {
  for (j=0; j<n; j++) {
    sum = 0.0;
    for (k=0; k<n; k++)
       sum += a[i][k] * b[k][j];
    c[i][j] = sum;
  }
}</pre>
```

```
for (k=0; k<n; k++) {
  for (i=0; i<n; i++) {
    r = a[i][k];
  for (j=0; j<n; j++)
    c[i][j] += r * b[k][j];
  }
}</pre>
```

```
for (j=0; j<n; j++) {
  for (k=0; k<n; k++) {
    r = b[k][j];
    for (i=0; i<n; i++)
        c[i][j] += a[i][k] * r;
  }
}</pre>
```

ijk (& jik):

- 2次内存加载,0次存储 2 loads, 0 stores
- 未命中次数/循环 = 1.25 misses/iter = 1.25

kij (& ikj):

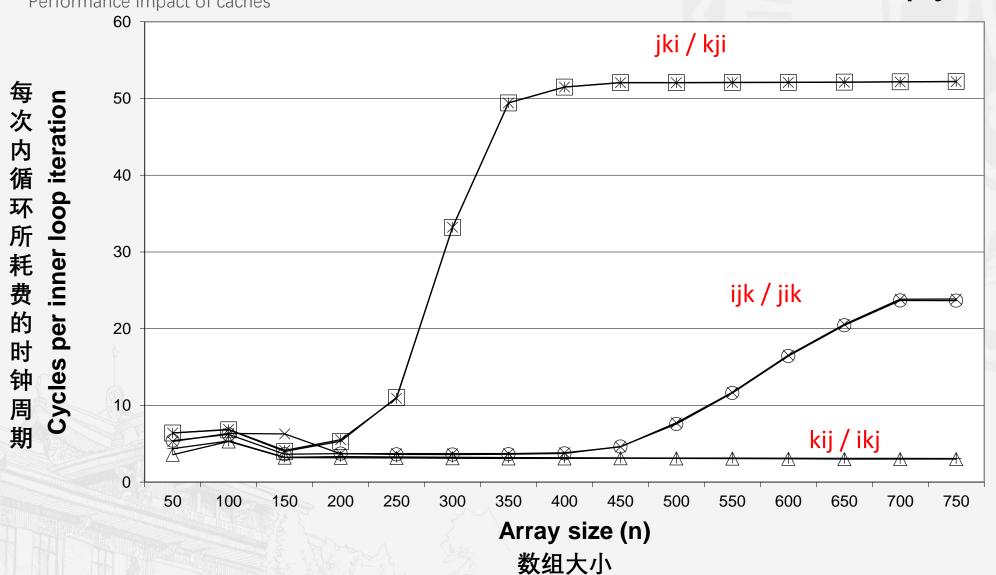
- 2次内存加载, 1次存储2 loads, 1 store
- 未命中次数/循环 = 0.5 misses/iter = 0.5

jki (& kji):

- 2次内存加载, 1次存储2 loads, 1 store
- 未命中次数/循环 = 2.0 misses/iter = 2.0

酷睿i7处理器矩阵乘法性能 Core i7 Matrix Multiply Performance







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The memory mountain



Performance impact of caches

矩阵乘法 Matrix Multiplication

```
c = (double *) calloc(sizeof(double), n*n);

/* Multiply n x n matrices a and b */
void mmm(double *a, double *b, double *c, int n) {
   int i, j, k;
   for (i = 0; i < n; i++)
        for (j = 0; j < n; j++)
        for (k = 0; k < n; k++)
        c[i*n+j] += a[i*n + k] * b[k*n + j];
}</pre>
```



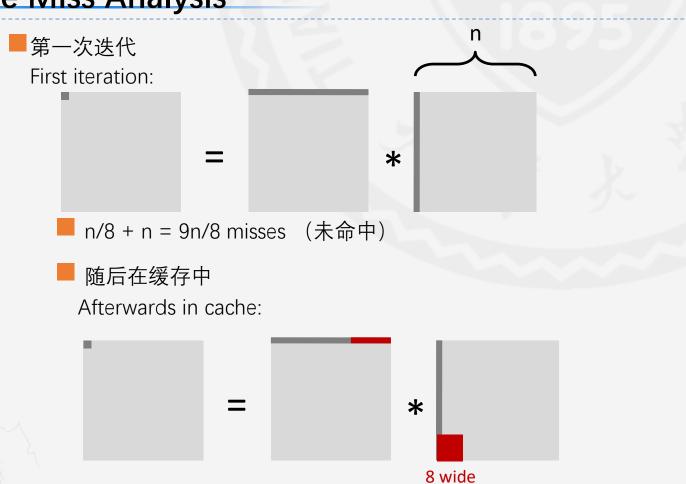
Performance impact of caches

缓存未命中分析 Cache Miss Analysis

假设:

Assume:

- 矩阵中的元素是double类型 Matrix elements are doubles
- 缓存块容量是8个double类型数据(64字节) Cache block = 8 doubles
- ■缓存总的容量 C << n (远远小于n)
 Cache size C << n (much smaller than n)

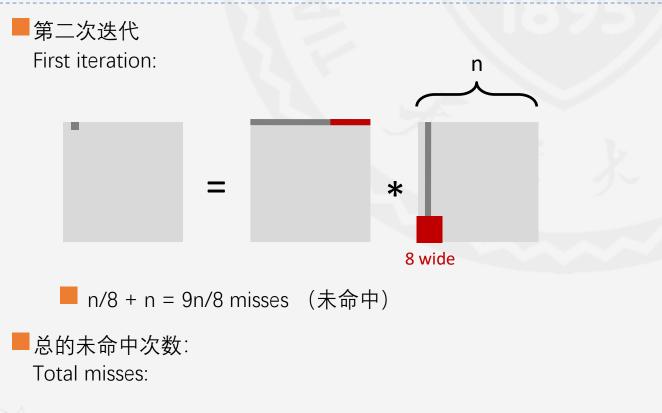




Performance impact of caches

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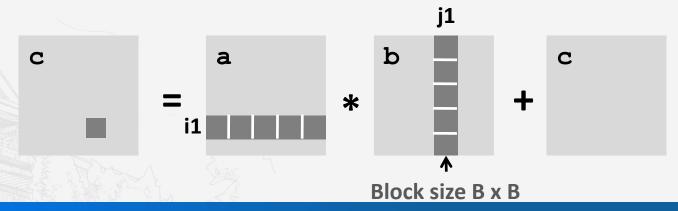


 $9n/8 * n^2 = (9/8) * n^3$



分块矩阵乘法 Blocked Matrix Multiplication

Performance impact of caches





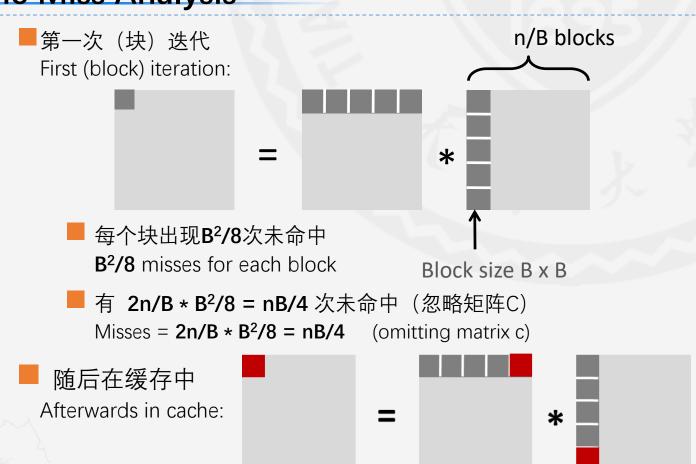
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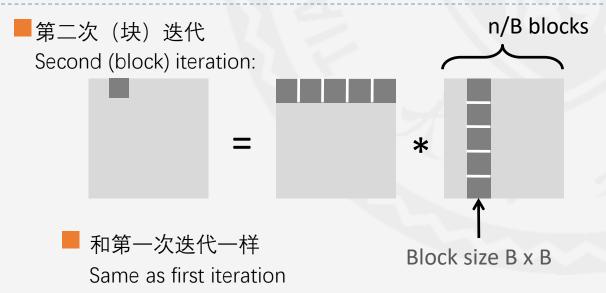




Performance impact of caches

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- 有 2n/B * B²/8 = nB/4 次未命中 Misses = 2n/B * B²/8 = nB/4
- 总未命中次数: ↑ Total misses: nB/4 * (n/B)² = n³/(4B)



Performance impact of caches

小结 Summary

- 未分块: n³ * (9/8)
 No blocking::
- ■分块: Blocking:: n³/(4B)
- B的值越大,未命中次数越少。但要 注意限制 **3B**² < **C** Suggest largest possible block size B, but limit **3B**² < **C**

- ■导致这些显著差异的原因:
 Reason for dramatic difference:
 - ■矩阵乘法中具有内在的时间局部性特征
 Matrix multiplication has inherent temporal locality:
 - ■输入数据: 3n², 计算次数: 2n³ Input data: 3n2, computation 2n3
 - ■每个数组元素需要使用O(n)次 Every array elements used O(n) times
 - ■必须要恰当的编写程序,才能够实现这种局部性特征 But program has to be written properly

本章内容

- 高速缓存的结构和工作原理 Cache memory organization and operation
- □ 高速缓存对软件性能的影响 Performance impact of caches
 - ■通过循环重排提高空间局部性特征
 Rearranging loops to improve spatial locality
 - ■通过分块提高时间局部性特征
 Using blocking to improve temporal locality
 - □存储器山

The memory mountain

Performance impact of caches

存储器山 The Memory Mountain

- ■读吞吐量(读带宽)
 Read throughput (read bandwidth)
 - 从存储系统中读取数据的速率 (MB/S)
 Number of bytes read from memory per second (MB/s)

- ■存储器山:一个读吞吐量关于时间和空间局部性的函数关系
 Memory mountain: Measured read throughput as a function of spatial and temporal locality
 - ■一种表征存储系统性能的简洁方法
 Compact way to characterize memory system performance



Performance impact of caches

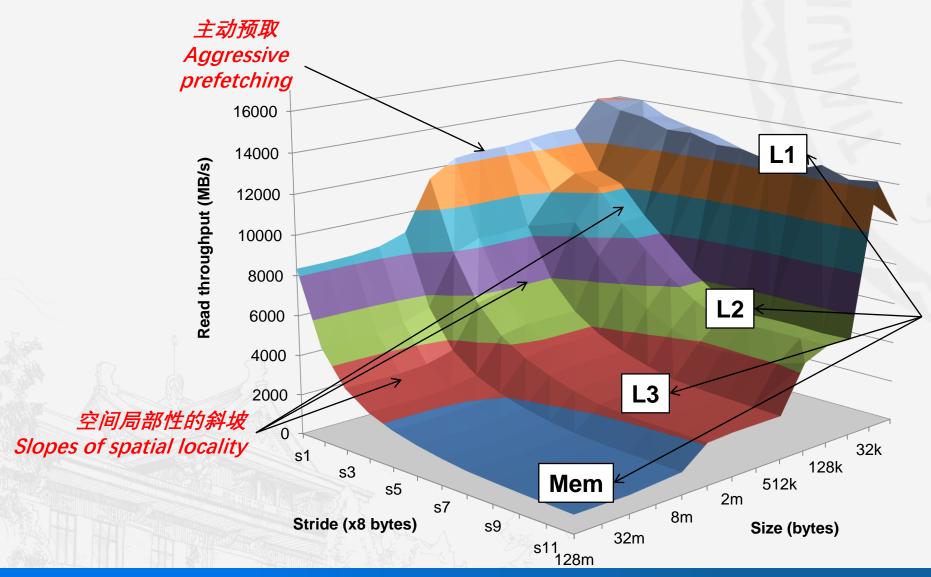
- 使用不同的elems和stride的参数组合,调用 test()函数 Call test() with many combinations of elems and stride
- ■对于每一个 elems 和 stride 参数 For each elems and stride:
 - ■首先,调用一次test(),对缓存进行"预热" First, call test() once to warm up the caches:
 - ■然后,再次调用test(),然后测量读吞吐量 Then, call test() again and measure the read throughput

测量存储器山的函数 Memory Mountain Test Function

```
long data[MAXELEMS]; /* Global array to traverse */
/* test - Iterate over first "elems" elements of
          array "data" with stride of "stride", using
          using 4x4 loop unrolling.
int test(int elems, int stride) {
    long i, sx2=stride*2, sx3=stride*3, sx4=stride*4;
    long acc0 = 0, acc1 = 0, acc2 = 0, acc3 = 0;
    long length = elems, limit = length - sx4;
    /* Combine 4 elements at a time */
    for (i = 0; i < limit; i += sx4) {
        acc0 = acc0 + data[i];
        acc1 = acc1 + data[i+stride];
        acc2 = acc2 + data[i+sx2];
        acc3 = acc3 + data[i+sx3];
    /* Finish any remaining elements */
    for (; i < length; i+=stride) {</pre>
        acc0 = acc0 + data[i];
    return ((acc0 + acc1) + (acc2 + acc3));
```

存储器山 The Memory Mountain

Performance impact of caches



Core i7 Haswell 2.1 GHz 32 KB L1 d-cache 256 KB L2 cache 8 MB L3 cache 64 B block size

时间局部性的山脊 Ridges of temporal locality