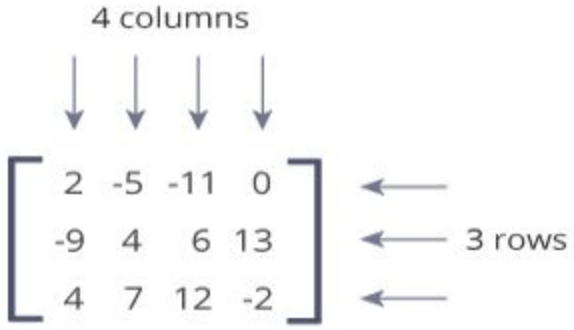
Python Matrices and NumPy Arrays

we will learn about Python matrices using nested lists, and NumPy package.
A matrix is a two-dimensional data structure where numbers are arranged into rows and columns. For example:



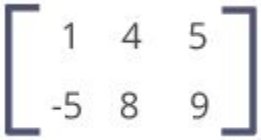
This matrix is a 3x4 (pronounced "three by four") matrix because it has 3 rows and 4 columns.

Python Matrix

Python doesn't have a built-in type for matrices. However, we can treat list of a list as a matrix. For example:

```
A = [[1, 4, 5],
     [-5, 8, 9]]
```

We can treat this list of a list as a matrix having 2 rows and 3 columns.



Let's see how to work with a nested list.

```
A = [[1, 4, 5, 12],
     [-5, 8, 9, 0],
     [-6, 7, 11, 19]]

print("A =", A)
print("A[1] =", A[1])      # 2nd row
print("A[1][2] =", A[1][2])   # 3rd element of 2nd row
```

```
print("A[0][-1] =", A[0][-1])   # Last element of 1st Row

column = [];        # empty list
for row in A:
 column.append(row[2])

print("3rd column =", column)
```

When we run the program, the output will be:

```
A = [[1, 4, 5, 12], [-5, 8, 9, 0], [-6, 7, 11, 19]]
A[1] = [-5, 8, 9, 0]
A[1][2] = 9
A[0][-1] = 12
3rd column = [5, 9, 11]
```

NumPy Array

NumPy is a package for scientific computing which has support for a powerful N-dimensional array object. Before you can use NumPy, you need to install it. For more info,

Once NumPy is installed, you can import and use it.

NumPy provides multidimensional array of numbers (which is actually an object). Let's take an example:

```
import numpy as np
a = np.array([1, 2, 3])
print(a)             # Output: [1, 2, 3]
print(type(a))       # Output: <class 'numpy.ndarray'>
```

As you can see, NumPy's array class is called ndarray.

How to create a NumPy array?

There are several ways to create NumPy arrays.

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1. Array of integers, floats and complex Numbers

```
import numpy as np
```

```
3.
4.  A = np.array([[1, 2, 3], [3, 4, 5]])
5.  print(A)
6.
7.  A = np.array([[1.1, 2, 3], [3, 4, 5]]) # Array of floats
8.  print(A)
9.
10. A = np.array([[1, 2, 3], [3, 4, 5]], dtype = complex) # Array of complex numbers
11. print(A)
```

When you run the program, the output will be:

```
[[1 2 3]
 [3 4 5]]

[[1.1 2.  3. ]
 [3.  4.  5. ]]

[[1.+0.j 2.+0.j 3.+0.j]
 [3.+0.j 4.+0.j 5.+0.j]]
```

---

2. Array of zeros and ones

```
1.
2.  import numpy as np
3.
4.  zeors_array = np.zeros( (2, 3) )
5.  print(zeors_array)
6.
7.  '''
8.  Output:
9.  [[0. 0. 0.]
10.  [0. 0. 0.]]
11. '''
12.
13. ones_array = np.ones( (1, 5), dtype=np.int32 ) // specifying dtype
14. print(ones_array)      # Output: [[1 1 1 1 1]]
```

Here, we have specified dtype to 32 bits (4 bytes). Hence, this array can take values from -2^{-31} to $2^{-31}-1$.

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3. Using arange() and shape()

```
1.
2.  import numpy as np
3.
4.  A = np.arange(4)
5.  print('A =', A)
6.
7.  B = np.arange(12).reshape(2, 6)
8.  print('B =', B)
9.
10. '''
11. Output:
12. A = [0 1 2 3]
13. B = [[ 0  1  2  3  4  5]
14. [ 6  7  8  9 10 11]]
15. '''
```

Learn more about other ways of creating a NumPy array.

Matrix Operations

Above, we gave you 3 examples: addition of two matrices, multiplication of two matrices and transpose of a matrix. We used nested lists before to write those programs. Let's see how we can do the same task using NumPy array.

Addition of Two Matrices

We use + operator to add corresponding elements of two NumPy matrices.

```
1.
2.  import numpy as np
3.
4.  A = np.array([[2, 4], [5, -6]])
5.  B = np.array([[9, -3], [3, 6]])
6.  C = A + B      # element wise addition
7.  print(C)
8.
9.  '''
10. Output:
11. [[11  1]
12. [ 8  0]]
13. '''
```

Multiplication of Two Matrices
To multiply two matrices, we use dot() method. Learn more about how numpy.dot works.
Note: * is used for array multiplication (multiplication of corresponding elements of two arrays) not matrix multiplication.

```
1.
2.  import numpy as np
3.
4.  A = np.array([[3, 6, 7], [5, -3, 0]])
5.  B = np.array([[1, 1], [2, 1], [3, -3]])
6.  C = a.dot(B)
7.  print(C)
8.
9.  '''
10. Output:
11. [[ 36 -12]
12. [ -1   2]]
13. '''
```

Transpose of a Matrix
We use numpy.transpose to compute transpose of a matrix.

```
1.
2.  import numpy as np
3.
4.  A = np.array([[1, 1], [2, 1], [3, -3]])
5.  print(A.transpose())
6.
7.  '''
8.  Output:
9.  [[ 1  2  3]
10. [ 1  1 -3]]
11. '''
```

As you can see, NumPy made our task much easier.

Access matrix elements, rows and columns

Access matrix elements
Similar like lists, we can access matrix elements using index. Let's start with a one-dimensional NumPy array.

```
1.
2.  import numpy as np
3.  A = np.array([2, 4, 6, 8, 10])
4.
5.  print("A[0] =", A[0])     # First element
6.  print("A[2] =", A[2])     # Third element
7.  print("A[-1] =", A[-1])   # Last element
```

When you run the program, the output will be:
A[0] = 2
A[2] = 6
A[-1] = 10

Now, let's see how we can access elements of a two-dimensional array (which is basically a matrix).

```
1.
2.  import numpy as np
3.
4.  A = np.array([[1, 4, 5, 12],
5.     [-5, 8, 9, 0],
6.     [-6, 7, 11, 19]])
7.
8.  #  First element of first row
9.  print("A[0][0] =", A[0][0])
10.
11. # Third element of second row
12. print("A[1][2] =", A[1][2])
13.
14. # Last element of last row
15. print("A[-1][-1] =", A[-1][-1])
```

When we run the program, the output will be:
A[0][0] = 1
A[1][2] = 9
A[-1][-1] = 19

Access rows of a Matrix

```
1.
2.  import numpy as np
3.
4.  A = np.array([[1, 4, 5, 12],
5.     [-5, 8, 9, 0],
```

```
    [-6, 7, 11, 19]])

print("A[0] =", A[0]) # First Row
print("A[2] =", A[2]) # Third Row
print("A[-1] =", A[-1]) # Last Row (3rd row in this case)
```

When we run the program, the output will be:

```
A[0] = [1, 4, 5, 12]
A[2] = [-6, 7, 11, 19]
A[-1] = [-6, 7, 11, 19]
```

Access columns of a Matrix

```
import numpy as np

A = np.array([[1, 4, 5, 12],
    [-5, 8, 9, 0],
    [-6, 7, 11, 19]])

print("A[:,0] =",A[:,0]) # First Column
print("A[:,3] =", A[:,3]) # Fourth Column
print("A[:,-1] =", A[:,-1]) # Last Column (4th column in this case)
```

When we run the program, the output will be:

```
A[:,0] = [ 1 -5 -6]
A[:,3] = [12  0 19]
A[:,-1] = [12  0 19]
```

If you don't know how this above code works, read slicing of a matrix section of this article.

Slicing of a Matrix

Slicing of a one-dimensional NumPy array is similar to a list. If you don't know how slicing for a list works, Let's take an example:

```
import numpy as np
letters = np.array([1, 3, 5, 7, 9, 7, 5])

# 3rd to 5th elements
```

```
print(letters[2:5])        # Output: [5, 7, 9]

# 1st to 4th elements
print(letters[:-5])        # Output: [1, 3]

# 6th to last elements
print(letters[5:])         # Output:[7, 5]

# 1st to last elements
print(letters[:])          # Output:[1, 3, 5, 7, 9, 7, 5]

# reversing a list
print(letters[::-1])          # Output:[5, 7, 9, 7, 5, 3, 1]
```

Now, let's see how we can slice a matrix.

```
import numpy as np

A = np.array([[1, 4, 5, 12, 14],
   [-5, 8, 9, 0, 17],
   [-6, 7, 11, 19, 21]])

print(A[:2, :4])  # two rows, four columns

''' Output:
[[ 1  4  5 12]
[-5  8  9  0]]
'''


print(A[:1,])  # first row, all columns

''' Output:
[[ 1  4  5 12 14]]
'''

print(A[:,2])  # all rows, second column

''' Output:
[ 5  9 11]
'''

print(A[:, 2:5])  # all rows, third to fifth column
```

```
29.
30. '''Output:
31. [[ 5 12 14]
32. [ 9  0 17]
33. [11 19 21]]
34. '''
```

As you can see, using NumPy (instead of nested lists) makes it a lot easier to work with matrices, and we haven't even scratched the basics. We suggest you to explore NumPy package in detail especially if you trying to use Python for data science/analytics.