

CS 584  
MACHINE LEARNING  
Assignment 3:  
Discriminative Learning

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## Logistic Regression:

### Introduction:

Logistic regression is a classification model which classifies data according to the probability of occurrence and this classification takes parameters generated by sigmoid function or logistic function.

### Iris Dataset (continuous dataset)

This is the multivariate dataset with 4 features and 150 samples in which 3 classes are there. Each class has 50 samples. The classification using logistic regression model is done for these 3 classes. This dataset is used for first question of the assignment.

### 1] 2 class Logistic Regression

#### a) Loading the dataset:

The dataset is taken from the sklearn datasets. The features are taken in the x as input and the labels are taken in the y. As 2 class dataset was required and iris is 3 class dataset so, only first 100 samples are considered as input.

#### b) Estimating the model parameters:

Theta is the parameter we need to estimate for classification.

Assume theta initially.

#### Sigmoid function:

$$\text{Sigmoid}(x) = \frac{1}{1 + \exp(-x)}$$

For prediction of y values:

$$\text{Sigmoid}(\theta^T x) = \frac{1}{1 + \exp(-(\theta^T x))}$$

Using this function  $h(\theta^T x)$  is calculated which is then used in gradient descent to update the value of theta. Then if  $h(\theta^T x)$  is greater than 0.5 then it is considered as class 1 otherwise 0.

Gradient Descent to update theta:

$$\theta = \theta - Learning\ rate * \sum_{i=1}^m (h(\theta x^{(i)}) - y^{(i)}) X^{(i)}$$

In this way classification is done using Logistic regression.

c) Performance:

Performance with 10 fold (For Some folds)

LOGISTIC REGRESSION FOR 2 CLASS

('FOR FOLD', 1)

y\_pred y\_test

0 1 1

1 1 1

2 1 1

3 1 1

4 1 1

5 1 1

6 1 1

7 1 1

8 0 0

9 0 0

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 2)

y\_pred y\_test

0 1 1

1 1 1

2 1 1

3 1 1

4 0 0

5 0 0

6 0 0

7 0 0

8 0 0

9 0 0

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 3)

y\_pred y\_test

0 1 1

1 1 1

2 1 1

3	1	1
4	1	1
5	1	1
6	0	0
7	0	0
8	0	0
9	0	0

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 4)

	y_pred	y_test
--	--------	--------

0	1	1
1	1	1
2	1	1
3	0	0
4	0	0
5	0	0
6	0	0
7	0	0
8	0	0
9	0	0

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 5)

	y_pred	y_test
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0	1	1
1	1	1
2	1	1
3	1	1
4	1	1
5	0	0
6	0	0
7	0	0
8	0	0
9	0	0

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 6)

	y_pred	y_test
--	--------	--------

0	1	1
1	1	1
2	1	1
3	1	1
4	1	1
5	1	1
6	0	0

7	0	0
8	0	0
9	0	0

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 7)

	y_pred	y_test
--	--------	--------

0	1	1
---	---	---

1	1	1
---	---	---

2	1	1
---	---	---

3	1	1
---	---	---

4	1	1
---	---	---

5	0	0
---	---	---

6	0	0
---	---	---

7	0	0
---	---	---

8	0	0
---	---	---

9	0	0
---	---	---

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 8)

	y_pred	y_test
--	--------	--------

0	1	1
---	---	---

1	1	1
---	---	---

2	1	1
---	---	---

3	0	0
---	---	---

4	0	0
---	---	---

5	0	0
---	---	---

6	0	0
---	---	---

7	0	0
---	---	---

8	0	0
---	---	---

9	0	0
---	---	---

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0

('FOR FOLD', 9)

	y_pred	y_test
--	--------	--------

0	1	1
---	---	---

1	1	1
---	---	---

2	1	1
---	---	---

3	1	1
---	---	---

4	0	0
---	---	---

5	0	0
---	---	---

6	0	0
---	---	---

7	0	0
---	---	---

8	0	0
---	---	---

9	0	0
---	---	---

ACCURACY BY MY MODEL 1.0

ACCURACY BY FUNCTION 1.0  
(‘FOR FOLD’, 10)

	y_pred	y_test
0	1	1
1	1	1
2	1	1
3	1	1
4	1	1
5	1	1
6	0	0
7	0	0
8	0	0
9	0	0

ACCURACY BY MY MODEL 1.0  
ACCURACY BY FUNCTION 1.0

The Accuracy helps in understanding the performance of the classification. Hence, we can get know what percent of input is misclassified.

By looking at the accuracies and the predicted values above we can say that the data was classified accurately for all folds in 10 fold cross validation.

Using Non-linear combinations of inputs to increase the capacity of the classifier:

For this, we take multivariate data to get more features. By increasing number of features we map data from low dimension feature space to high dimension feature space.

## 2] 3 class Logistic Regression

a) Loading the dataset: (4 features)

The dataset is taken from the sklearn datasets. All the features are taken in the x as input and the labels are taken in the y. All the samples are considered as input.

b) Estimating the model parameters:

Theta is the parameter we need to estimate for classification.

Assume theta initially.

Sigmoid function:

$$\text{Sigmoid}(x) = \frac{1}{1 + \exp(-x)}$$

For prediction of y values:

$$\text{Sigmoid}(\theta_j^T x) = \frac{\exp(\theta_j^T x)}{\sum \exp(\theta_j^T x)}$$

Using this function  $h(\theta^T x)$  is calculated which is then used in gradient descent to update the value of theta. Then if  $h(\theta^T x)$  is greater than 0 then it is considered as classes j otherwise k.

Stochastic Gradient Descent to update theta:

$$\theta_j = \theta_j - \text{Learning rate} * (h\theta_j(x) - \text{Indicator}(y = j))X^i$$

In this way classification is done using Logistic regression.

c) Performance:

Performance with 10 fold (For one of the folds)

LOGISTIC REGRESSION FOR K CLASS

FOR FOLD: 1

Predicted Y : [0 0 1 1 0 2 0 0 2 0 2 0 0 0 0]

Actual Y : [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]

ACCURACY BY MY MODEL 0.666666666667

ACCURACY BY FUNCTION 1.0

FOR FOLD: 2

Predicted Y : [0 0 0 1 1 0 0 0 0 0 0 1 0 0 1]

Actual Y : [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]

ACCURACY BY MY MODEL 0.733333333333

ACCURACY BY FUNCTION 1.0

FOR FOLD: 3

Predicted Y : [0 0 1 0 0 0 2 0 1 0 0 0 1 0 0]

Actual Y : [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]

ACCURACY BY MY MODEL 0.733333333333

ACCURACY BY FUNCTION 1.0

FOR FOLD: 6

Predicted Y : [1 1 0 0 0 1 0 0 1 0 0 1 0 2 1]

Actual Y : [1 1 1 1 1 1 1 1 1 1 1 1 1 1 1]

ACCURACY BY MY MODEL 0.4

ACCURACY BY FUNCTION 0.666666666667

The Accuracy helps in understanding the performance of the classification. Hence, we can get know what percent of input is misclassified.

By looking at the accuracies and the predicted values above we can say that the data was classified accurately for some folds in 10 fold cross validation.

3] Two layer feedforward MLP with error function: