

# UNIT-III PROJECTIONS OF PLANES

26/11/20

→ A plane figure (or) surface is a two dimensional object having 2 Dimensions length and breadth. It has negligible thickness.

→ A plane may be of any shape such as triangular, square, pentagonal, hexagonal, circular etc.

Types of planes:  
Planes may be divided into two types.

- (a)  $\perp^r$  planes
- (b) oblique planes

(a) perpendicular plane:

Planes which are  $\perp^r$  to one of the reference plane and  $\parallel^l$  to the other reference plane are called  $\perp^r$  planes

- ① plane  $\perp^r$  to  $H.P$  &  $\parallel^l$  to  $V.P$
  - ② plane  $\perp^r$  to  $V.P$  &  $\parallel^l$  to  $H.P$
  - ③ plane  $\perp^r$  to both  $H.P$  &  $V.P$  ( $\parallel^l$  to both  $H.P$  &  $V.P$ )
  - ④ plane  $\perp^r$  to  $V.P$  and inclined to  $H.P$
  - ⑤ plane  $\perp^r$  to  $H.P$  and inclined to  $V.P$
- (b) oblique planes:  
Planes which are inclined to both  $H.P$  &  $V.P$  are known as oblique planes.

Important points:  
→ when a plane is parallel to one of the reference plane then the projection on that plane to which it is  $\parallel^l$  will be its "true shape".

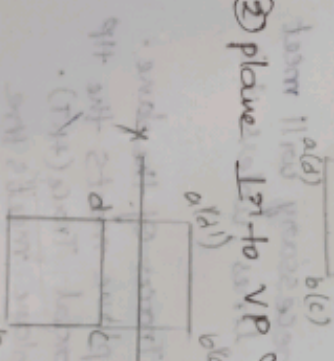
→ When a plane is  $\perp^r$  to one of the reference plane then the projection on that plane to which it is  $\perp^r$  is a "st. line".  
→ when a plane is inclined to one of the reference plane then the projection on that plane to which it is inclined will be in "apparent shape".

Positions:

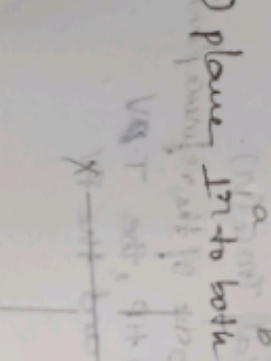
- ① plane  $\parallel^l$  to  $V.P$  &  $\perp^r$  to  $H.P$



- ② plane  $\perp^r$  to  $V.P$  &  $\parallel^l$  to  $H.P$



- ③ plane  $\perp^r$  to both  $H.P$  &  $V.P$



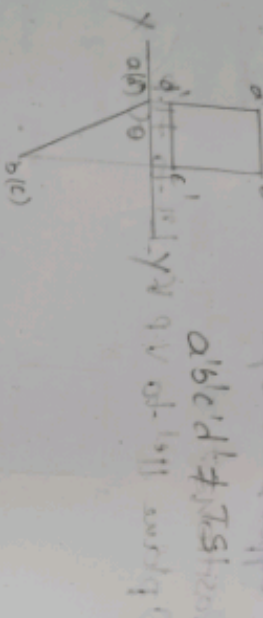


④ plane  $\perp$  to VP & inclined to HP

Let a plane be inclined to HP at an angle  $\theta$  and be perpendicular to VP. The reference line XY is drawn. The plane is represented by a line perpendicular to XY at a distance of 20 mm from XY. The front view (FV) is a point on this line, and the top view (TV) is a line perpendicular to XY at a distance of 20 mm from XY. The angle  $\theta$  is shown between the XY line and the line representing the plane.

⑤ plane  $\perp$  to HP & inclined to VP

Let a plane be inclined to VP at an angle  $\phi$  and be perpendicular to HP. The reference line XY is drawn. The plane is represented by a line perpendicular to XY at a distance of 20 mm from XY. The front view (FV) is a line perpendicular to XY at a distance of 20 mm from XY, and the top view (TV) is a point on this line. The angle  $\phi$  is shown between the XY line and the line representing the plane.



### Traces of planes:

A plane, extended if necessary will meet the reference planes in lines, unless it is parallel to any of them.

→ These lines are called Traces of the plane.

→ The line in which the plane meets the HP is called the Horizontal Trace (H.T.).

→ The line in which the plane meets the VP is called the Vertical Trace (V.T.).

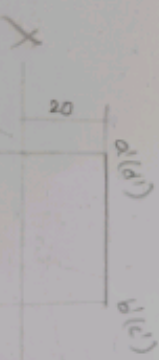
Projections of planes  $\parallel$  to one of the reference planes

→ When the plane is  $\parallel$  to HP, the T.V. should be drawn first and the F.V. projected from it.

→ When the plane is  $\perp$  to both HP & VP (i.e. to profile plane) the side view must be drawn first. The F.V. and T.V. are projected from the side view.

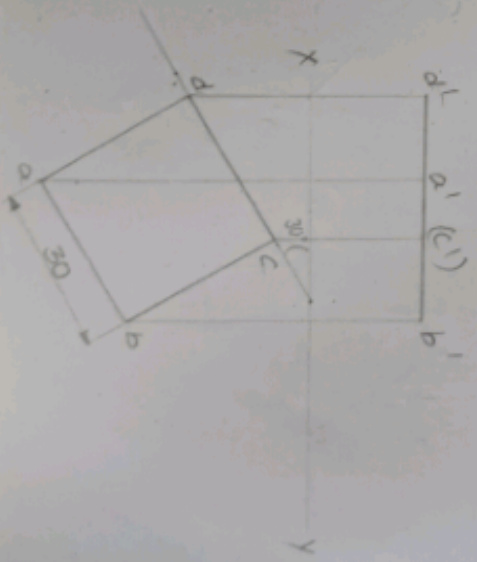
### Problems:

1) A Square plane ABCD of side 30 mm. has its plane  $\parallel$  to HP and 20 mm away from it. Draw the projections of the plane when 2 of its sides are  $\parallel$  to VP (b) inclined at  $30^\circ$  to VP

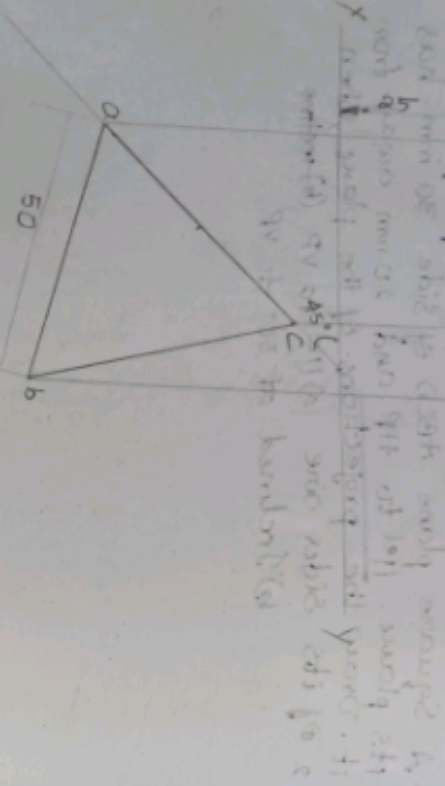


2) A square plane ABCD of side 30 mm. has its plane  $\parallel$  to HP and 20 mm away from it. Draw the projections of the plane when 2 of its sides are  $\parallel$  to VP (b) inclined at  $30^\circ$  to VP

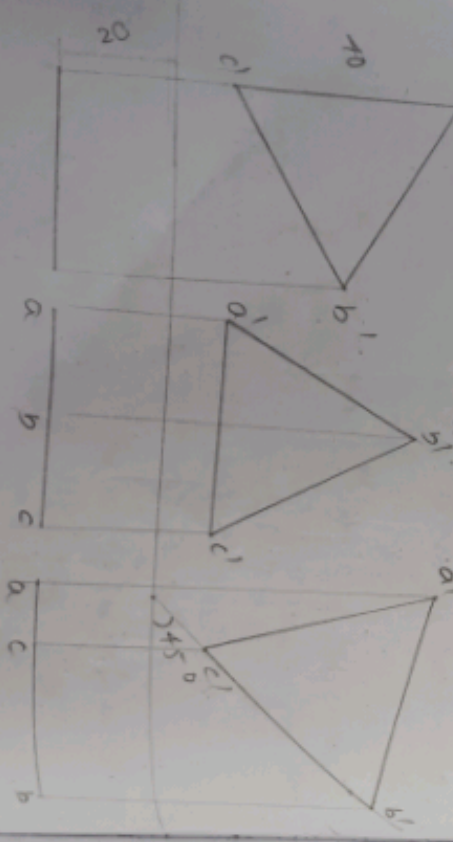
3) A square plane ABCD of side 30 mm. has its plane  $\parallel$  to HP and 20 mm away from it. Draw the projections of the plane when 2 of its sides are  $\parallel$  to VP (b) inclined at  $30^\circ$  to VP



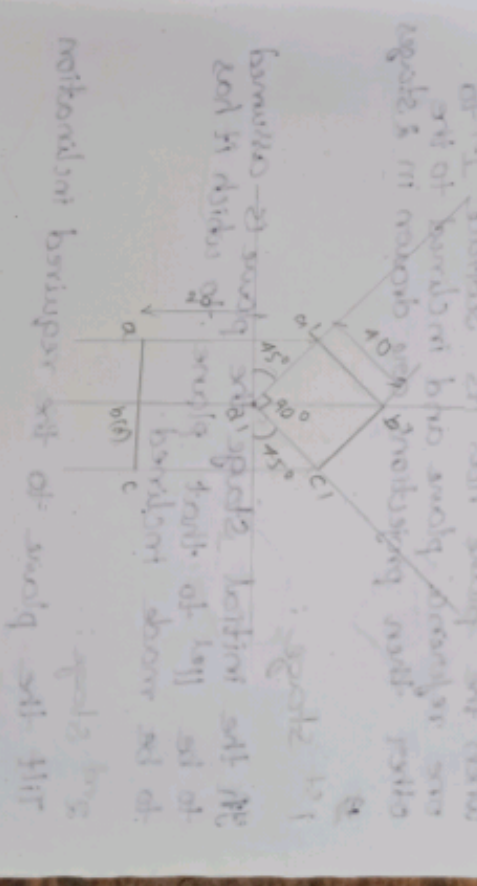
2) An Equilateral Triangle of 50 mm Side has its Vertical Trace parallel to and 25 mm above XY. It has no horizontal Trace. Draw its projection when one of its Sides is inclined at  $45^\circ$  to VP.



3) An Equilateral ~~and~~ Triangular plate ABC of Side 40 mm has its plane  $\parallel$  to VP and 20 mm away from it. Draw the projections of the plate when one of its Side is (a)  $\perp$  to HP (b)  $\parallel$  to HP (c) Inclined at  $45^\circ$  to HP.



4) A Square ABCD of 40 mm side has a Corner on HP and 20 mm in front of VP. All sides of the square are equally inclined to HP and  $\parallel$  to VP. Draw its projections and show its traces.



5) A hexagon of 30 mm side has one of its corners on the top HP. The plane of the hexagon is  $\perp$  to both HP and VP. The longest Diagonal passing through the corner which is on the HP is  $\perp$  to HP. Draw its projections.





Projections of plane  $L_1$  to one reference plane and inclined to the other when the plane has its surface  $L_1$  to one reference plane and inclined to the other then projections are drawn in 2 stages

1<sup>st</sup> stage:

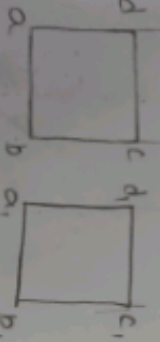
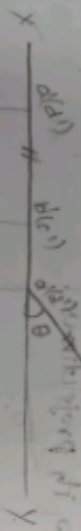
If the initial stage the plane is assumed to be  $\parallel$  to that plane to which it has to be made inclined.

2<sup>nd</sup> stage:

Tilt the plane to the required inclination

Positions:

① plane  $L_1$  to VP and inclined to HP



② plane  $L_1$  to HP & inclined to VP



Important points:

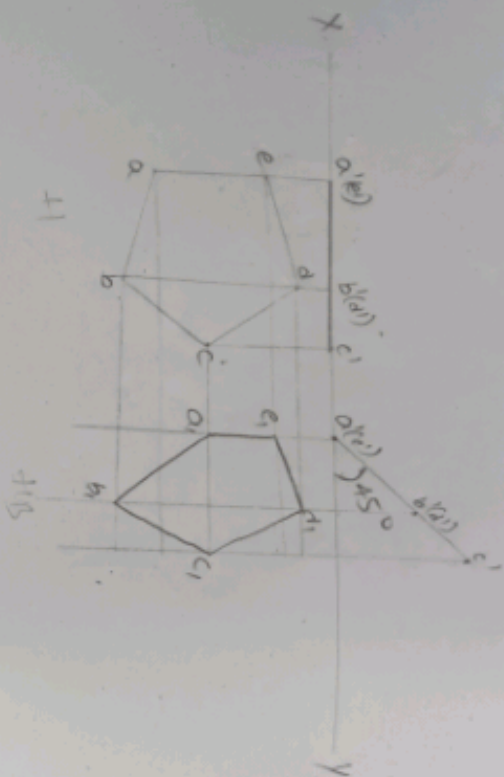
Side on HP/VP

Corners on HP/VP

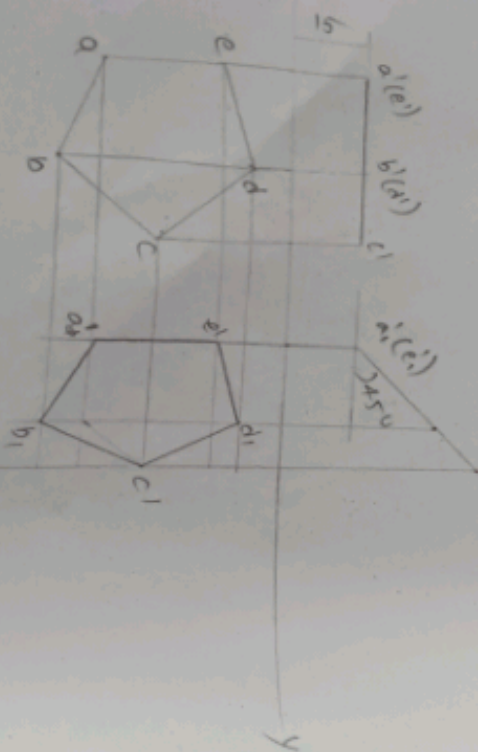


Problems:

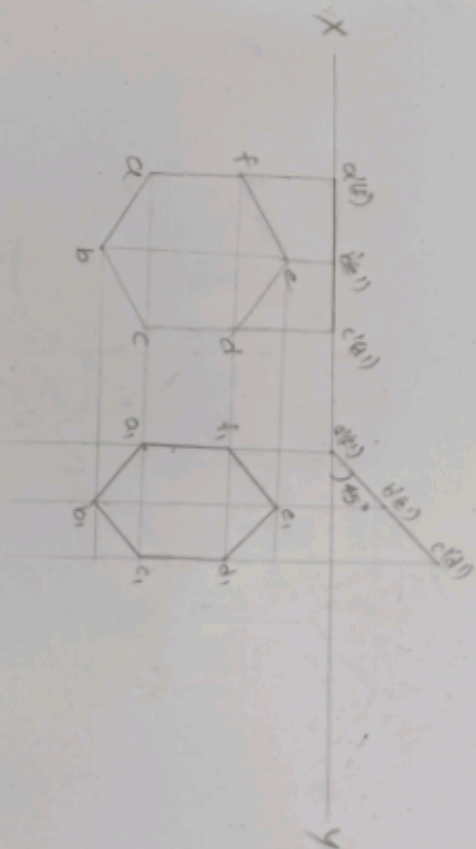
- ① A regular pentagon of 25 mm has one side  $\perp$  to VP. Its plane is inclined at  $45^\circ$  to H.P.  $\perp$  to VP. Draw its projections.



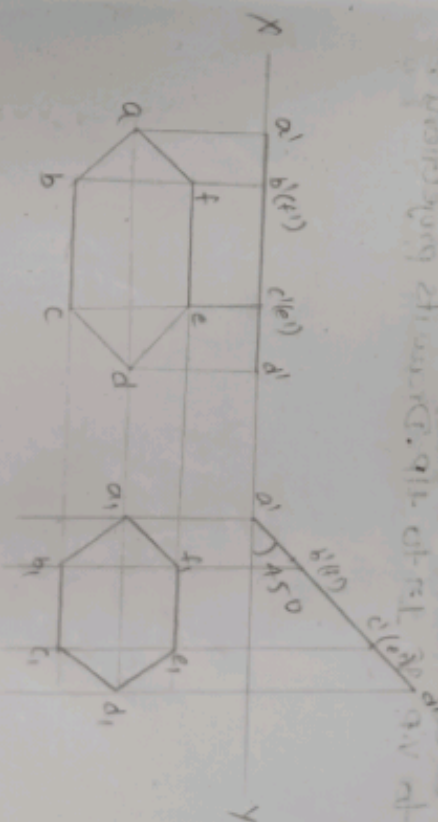
- ② Draw the projections of a regular pentagon of 25 mm side with its surface making an angle of  $45^\circ$  with H.P. one of its sides of pentagon is  $\parallel$  to H.P. and 15 mm away from it. The plane is  $\perp$  to V.P.



- ③ A regular hexagon of 40 mm side has a side in the H.P. Its surface is inclined at  $45^\circ$  to H.P. and  $\perp$  to V.P. draw its projections.

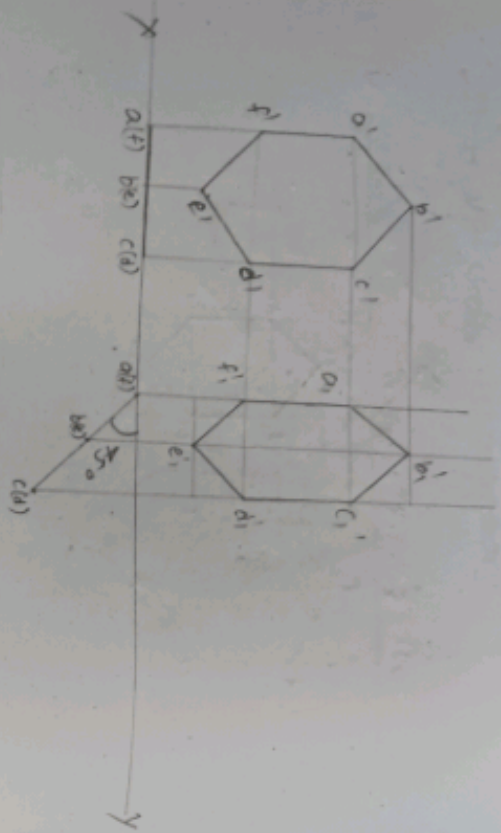


- ④ A regular hexagon of 30 mm side has a corner in the H.P. its surface is inclined at  $45^\circ$  to H.P. and  $\perp$  to V.P. Draw its projections.

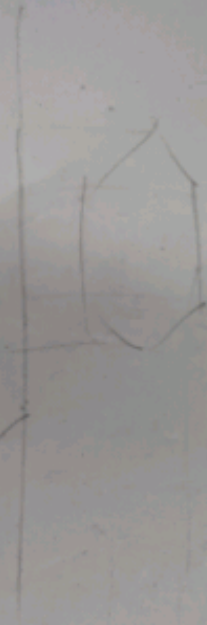




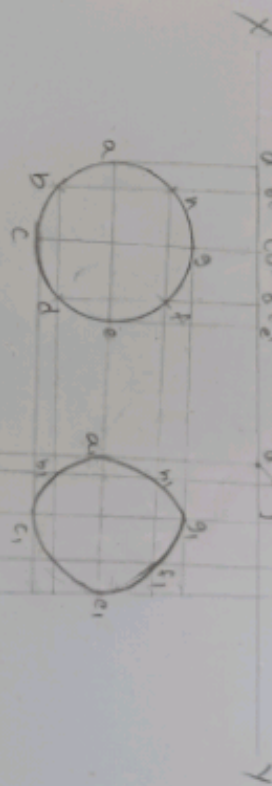
3) A Hexagonal plate of size 30 mm is placed with a side on V.P and surface inclined at  $45^\circ$  to V.P and  $17^\circ$  to H.P. draw its projections.



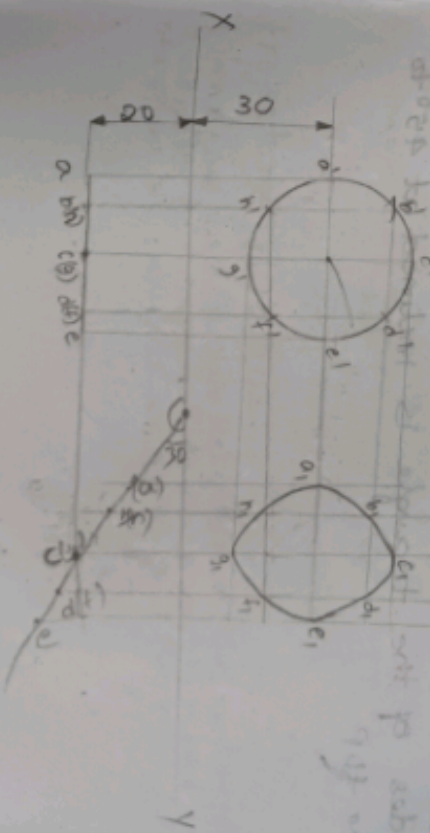
4) A Hexagonal plate of size 30 mm is resting with a corner on V.P and surface inclined at  $45^\circ$  to V.P &  $17^\circ$  to H.P. Draw its projections.



5) A Circular plate of diameter 50 mm is resting on H.P. on a pt on the circumference with its surface inclined at  $45^\circ$  to H.P. and  $17^\circ$  to V.P. Draw its projections.



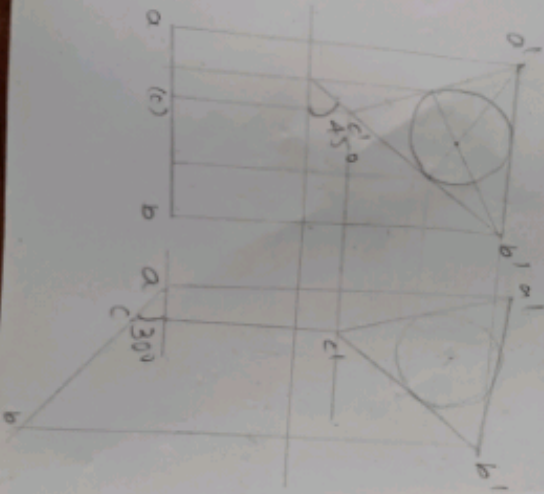
6) Draw the projections of a circle of 50 mm diameter, having its plane vertical and inclined at  $30^\circ$  to the V.P. its Centre is 30 mm above the H.P. and 20 mm in front of the V.P.



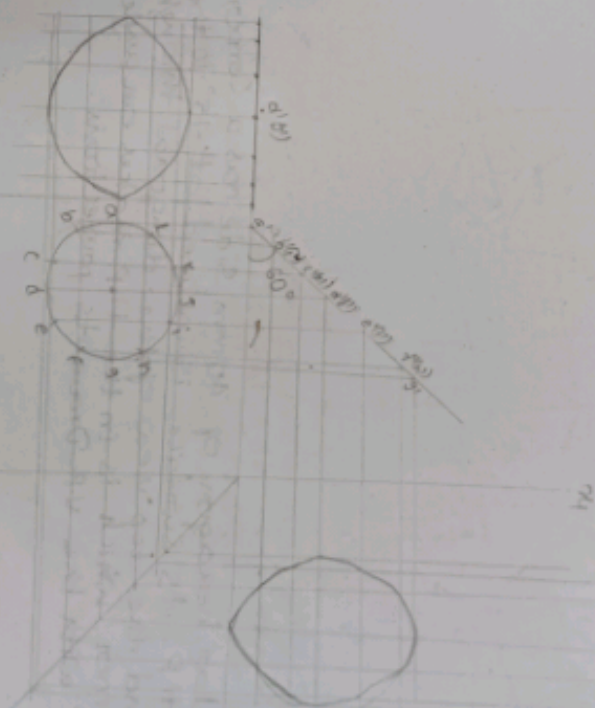
9) ND Blatt Ex-12-5 prob  
 Draw a regular hexagon of 40mm side, with its two sides vertical. Draw a circle of 40mm diameter in its centre. The fig represents a hexagonal plate with a hole in it and having its surface parallel to the V.P. Draw its projections when the surface is vertical and inclined at  $30^\circ$  to the V.P. Assume the thickness of the plate to be equal to that of a line.



10) ND Blatt Ex-12-2 prob  
 Draw an Equilateral triangle of 15mm side and inscribe a circle in it. Draw the projection of the figure when its plane is vertical and inclined at  $30^\circ$  to the V.P. and one of the sides of the triangle is inclined at  $45^\circ$  to the H.P.



11) ND Blatt Ex-12-8  
 The top view of a plate, the surface of which is  $\perp$  to the V.P. and inclined at  $60^\circ$  to the H.P. is a circle of 60mm diameter. Draw its 3 views.



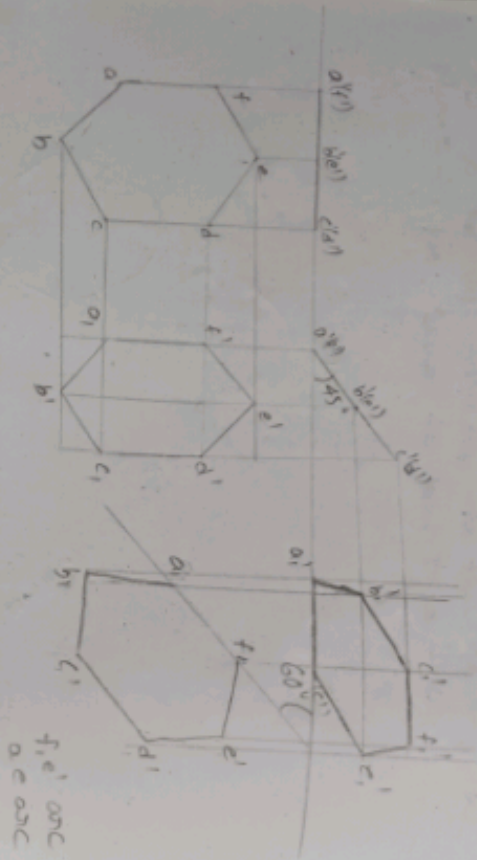
### Projections of Oblique:

When a plane has its surface inclined to one plane and an edge (or) a diameter (or) a diagonal  $\parallel$  to that plane and inclined to the other plane, its projections are drawn in 3 steps.

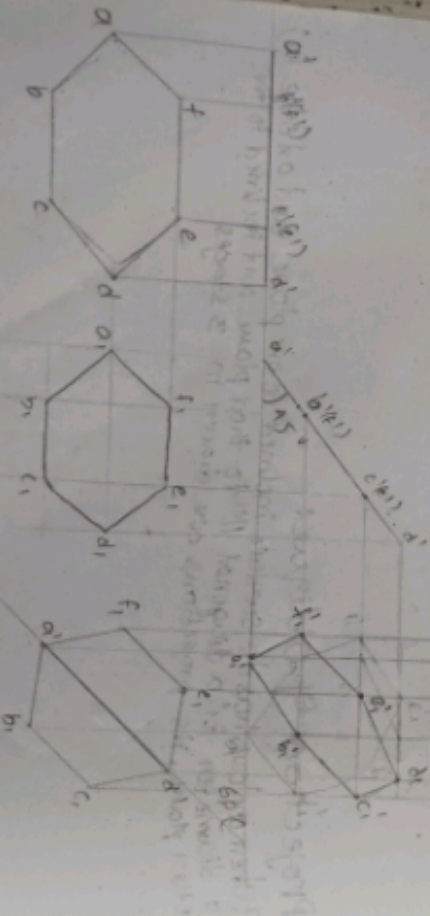


Problems on projections of Oblique Solids

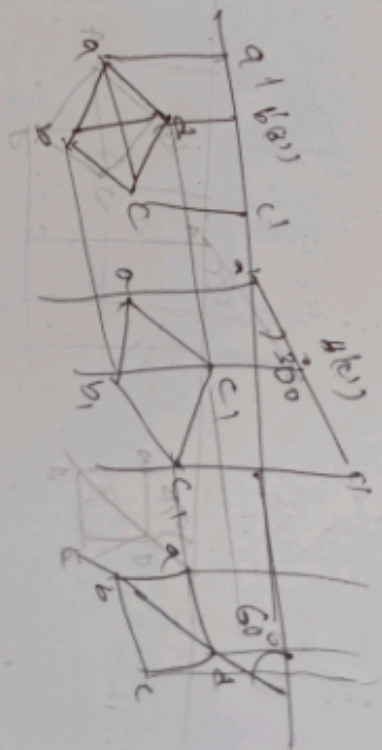
1) Draw the projections of a regular hexagon of 25 mm side, having one of its sides in the H.P. and inclined @  $60^\circ$  to the V.P. and its surface making an angle of  $45^\circ$  with the H.P.



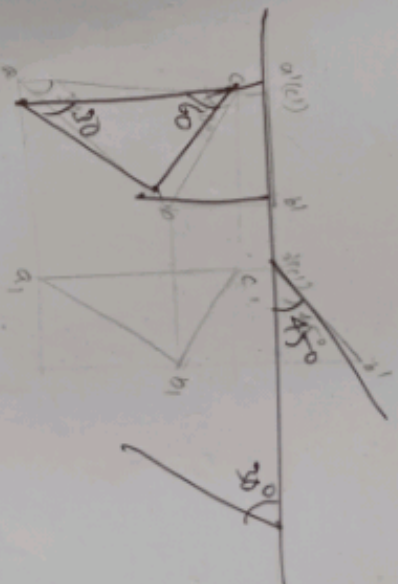
2) A regular hexagon of 40 mm side has a corner in the H.P. its surface is inclined at  $45^\circ$  to the H.P. and the top view of the diagonal through the corner which is in the H.P. makes an angle of  $60^\circ$  with the V.P. Draw its projections.



3) A Square ABCD of 50 mm side has its corner A in the H.P. its diagonal AC inclined @  $30^\circ$  to the H.P. and the diagonal BD inclined @  $45^\circ$  to the V.P. || to the H.P. Draw its projections.

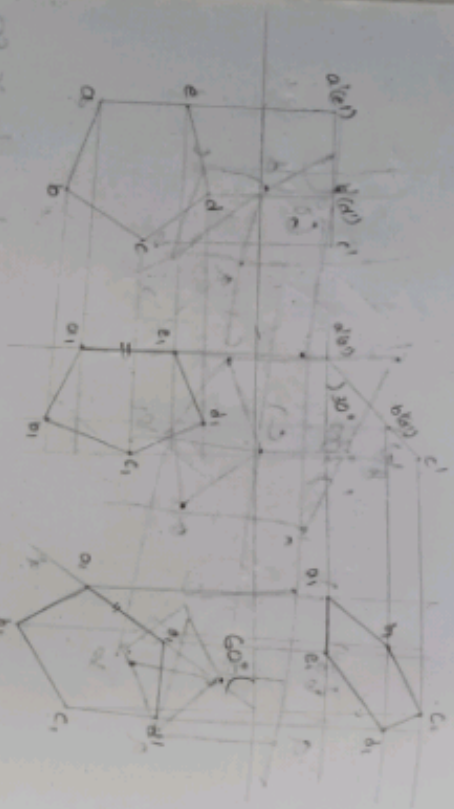


4) A 60° Set Square of 125 mm longest side is 50 kept. that the longest side is in the H.P. making an angle  $30^\circ$  with the V.P. and the Set Square itself inclined @  $45^\circ$  to the H.P. Draw the projections.

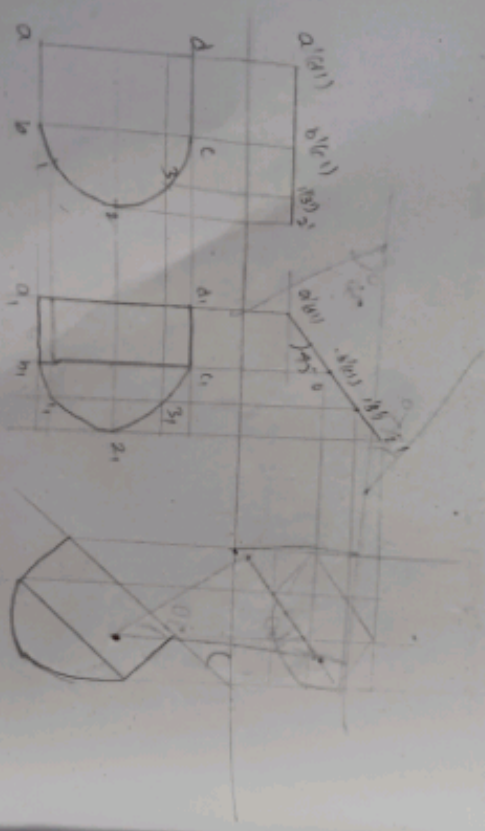




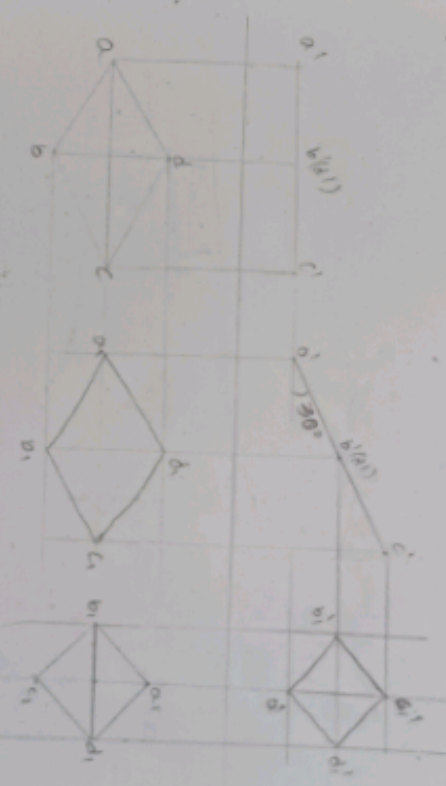
2) Draw the projections of a regular pentagon of 40 mm side, having its surface inclined @  $30^\circ$  to the H.P. and a side || to the H.P. and inclined @ an angle of  $60^\circ$  to the V.P.



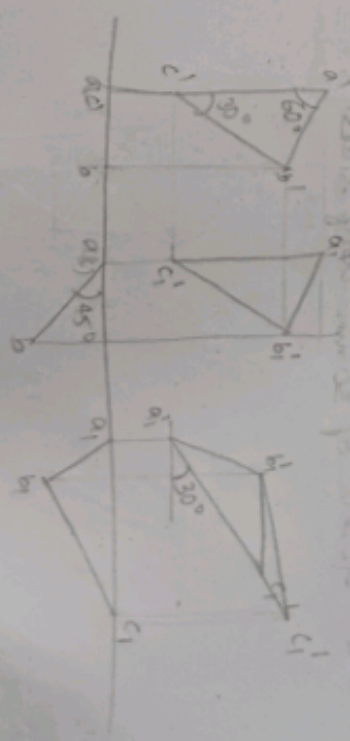
3) A Composite plate of negligible thickness is made up of a rectangle  $60\text{ mm} \times 40\text{ mm}$  and a semi-circle on its longer side. Draw its projections when the longer side is || to the H.P., and inclined @  $45^\circ$  to the V.P. The surface of the plate making  $30^\circ$  angle with the H.P.



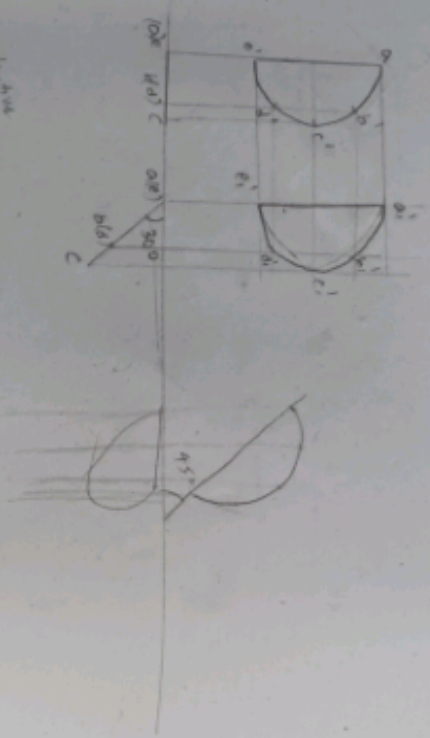
3) Draw the projections of a rhombus having diagonals 125 mm and 50 mm long, the smaller diagonal of which is || to both the principal planes, while the other is inclined @  $30^\circ$  to the H.P.



3) A thin  $30^\circ-60^\circ$  Set Square has its longest edge in the V.P. and inclined @  $30^\circ$  to the H.P. Its surface makes an angle of  $45^\circ$  with the V.P. draw its projections.



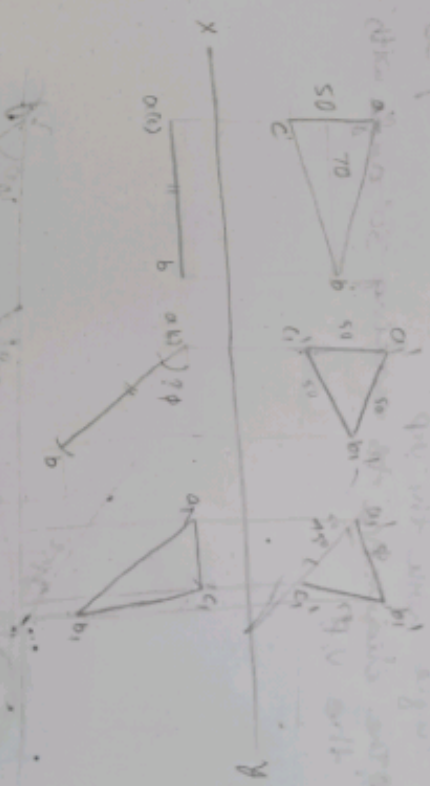
- 9) A Semi circular plate of 80 mm diameter has its straight edge in the V.P. and inclined @  $45^\circ$  to the H.P. The surface of the plate makes an angle of  $30^\circ$  with the V.P. Draw its projections.



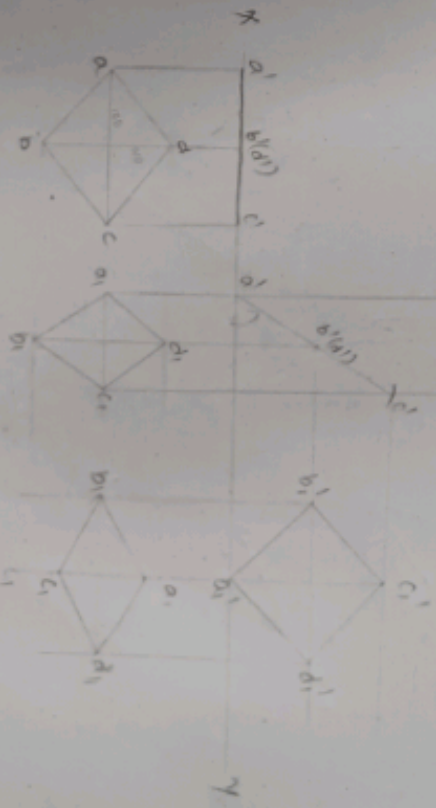
- 10) A thin rectangular plate of sides 60 mm x 30 mm has its shortest side in the V.P. and inclined @  $30^\circ$  to the H.P. project its top view if its FV is a square of 30 mm long sides.



- 11) A plate having shape of an isosceles triangle has base 50 mm long and altitude 70 mm. It is placed flat in the FV it is seen as an Equilateral triangle of 50 mm sides and one side inclined @  $45^\circ$  to XY. Draw its TV.

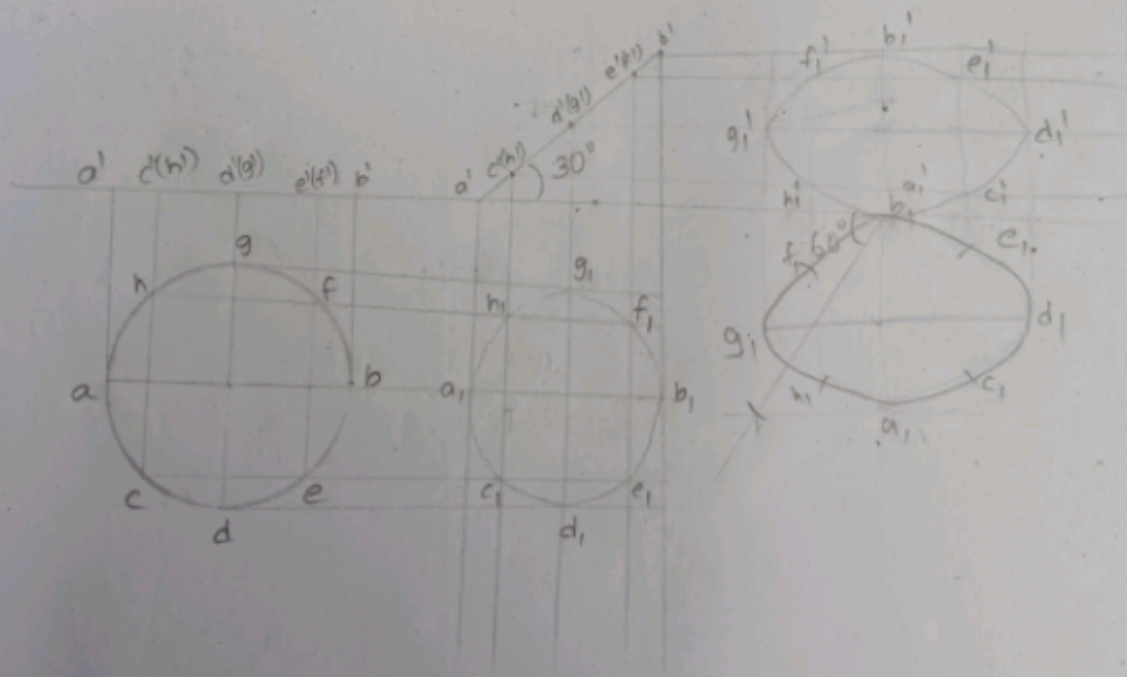


- 12) Draw a rhombus of diagonals 100 mm and 60 mm long, with the longer diagonal horizontal. The figure is the top view of a square of 100 mm long diagonals, with a corner on the ground. Draw its FV and determine the angle which its surface makes with the ground.





14) Draw the projections of a circle of 75 mm diameter appears as an ellipse in the FV, having the end 'A' of the diameter AB in the HP, the end B in the V.P, and the surface inclined @  $30^\circ$  to the H.P and @  $60^\circ$  to the V.P



as the arc on 60° line  
a, b, on locus

75

13) A steel plate of negligible thickness and 50 mm diameter appears as an ellipse in the FV, having its major axis 50 mm long and minor axis 30 mm long. Draw its TV when the major axis of the ellipse is horizontal.

