

# EE2703: Applied Programming Lab

## Week3: Forier Approximation

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### 1 Objectives

- Finding Forier coefficients using Integral method
- Finding Forier coefficients using "Least square fit model" and comparing with original coefficients
- Plotting coefficients in semilog and log-log scale
- plotting estimated functions with original functions

### 2 Theory

The Forier series is given by

$$f(x) = a_0 + \sum_{k=1}^{\infty} a_k \cos(kx) + b_k \sin(kx) \quad (1)$$

The coefficients  $a_k$  and  $b_k$  are calculated by

$$a_0 = \frac{1}{2\pi} \int_0^{2\pi} f(x) dx \quad (2)$$

$$a_k = \frac{1}{\pi} \int_0^{2\pi} f(x) \cos(kx) dx$$
$$b_k = \frac{1}{\pi} \int_0^{2\pi} f(x) \sin(kx) dx \quad (3)$$

- The above equations use the Direct Integration method of finding the Fourier series
- We shall also use the Least Squares method to find the Fourier approximation.
- We will plot forier coefficients obtained through both methods and compare them
- Finally we will re-create the functions using second method and compare with original functions

### 3 Plots

#### 3.1 Creating the functions

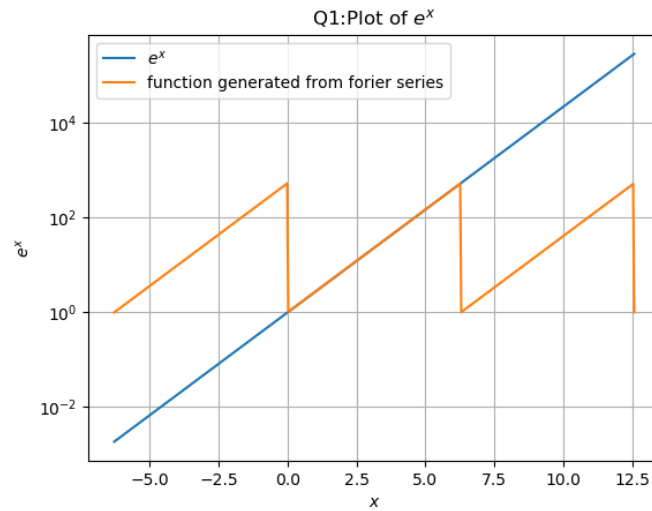


Figure 1: Plot of  $e^x$  in periodic and normal form using forier transform

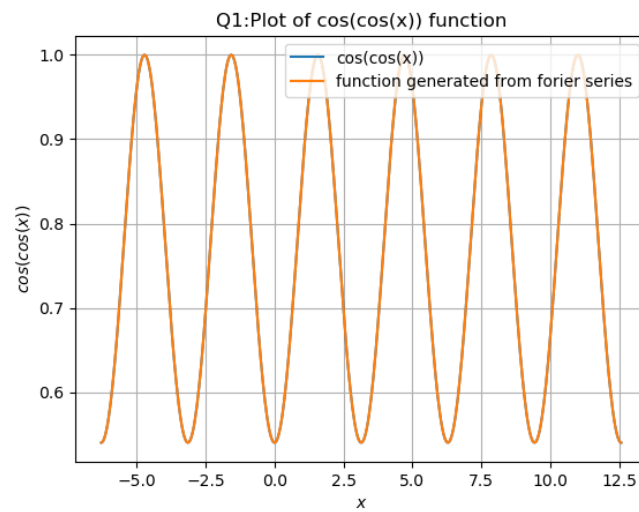


Figure 2: Plot of  $\cos(\cos(x))$  in periodic and normal form using forier transform

As we can see, there is no difference in the plot of  $\text{periodic}(\cos(\cos(x)))$  and  $\cos(\cos(x))$ . This is because the period of  $\cos(\cos(x))$  is  $\pi$

### 3.2 Obtaining Fourier Series Coefficients

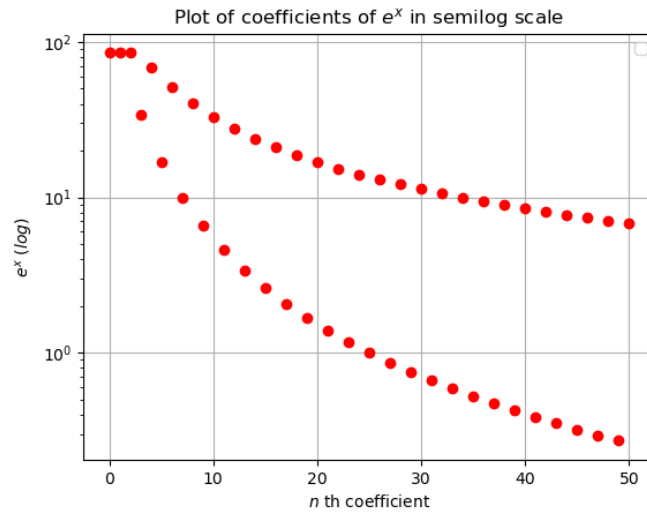


Figure 3: semilog plot of coefficients of  $e^x$

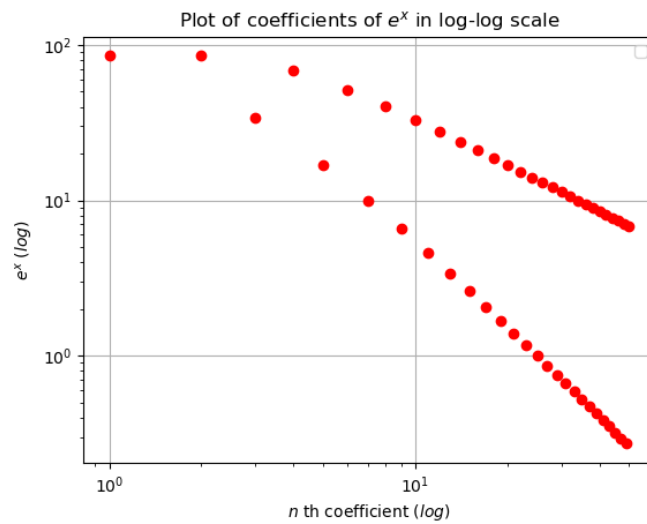


Figure 4: Log-Log plot of coefficients of  $e^x$

In case of  $e^x$  log of the coefficients is approximately proportional to log of kth index. Hence log-log plot is almost linear in case of  $e^x$ .

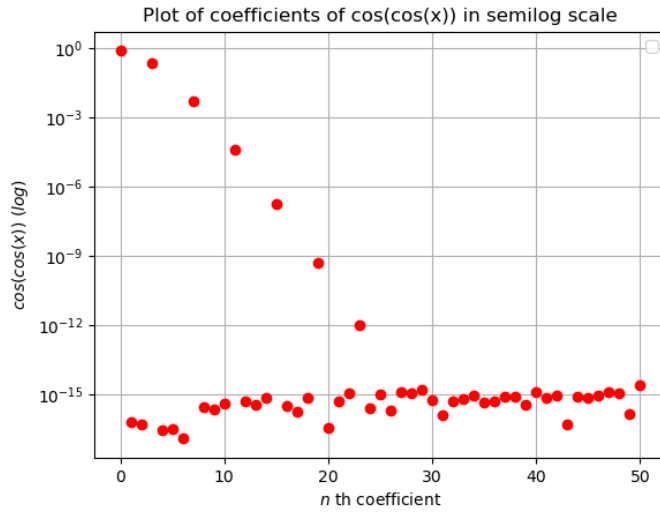


Figure 5: Semilog plot of coefficients of  $\cos(\cos(x))$

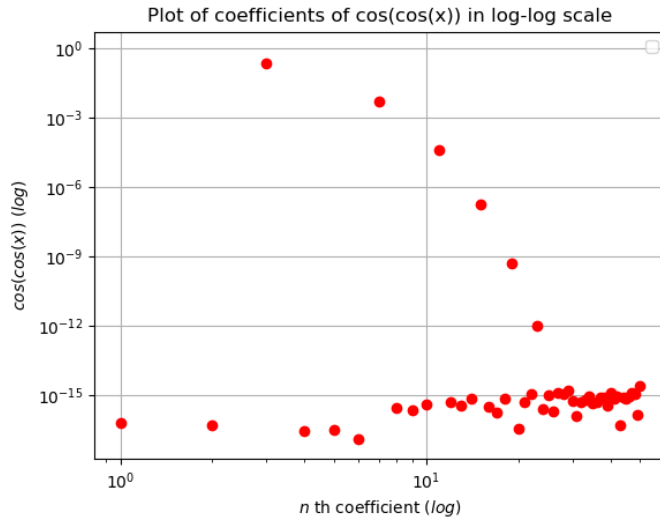


Figure 6: Log-Log plot of coefficients of  $\cos(\cos(x))$

The semilogy plot of  $\cos(\cos(x))$  coefficients are almost linear. bn coefficients of  $\cos(\cos(x))$  are nearly zero because  $\cos(\cos(x))$  is an even function. From the plot of  $\cos(\cos(x))$ , we can see that it is approximately sinusoidal with period of  $2\pi$ . Hence the value converges more quickly as compared to  $e^x$

### 3.3 Obtaining Fourier Series Coefficients using Least Squares Approach

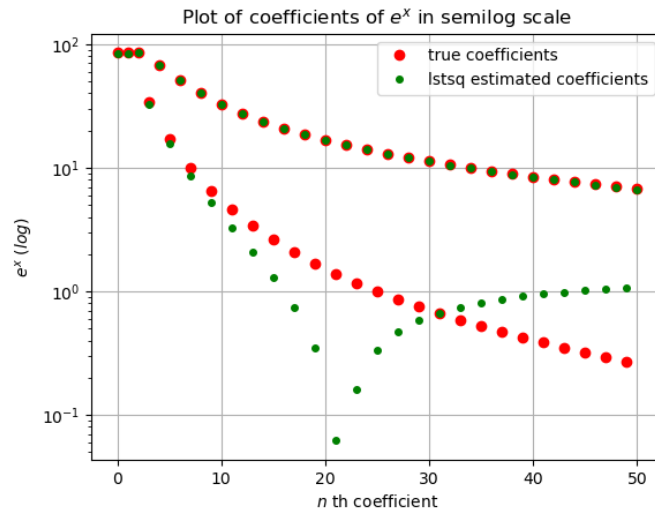


Figure 7: Semilog plot of lstsq estimated coefficients of  $e^x$

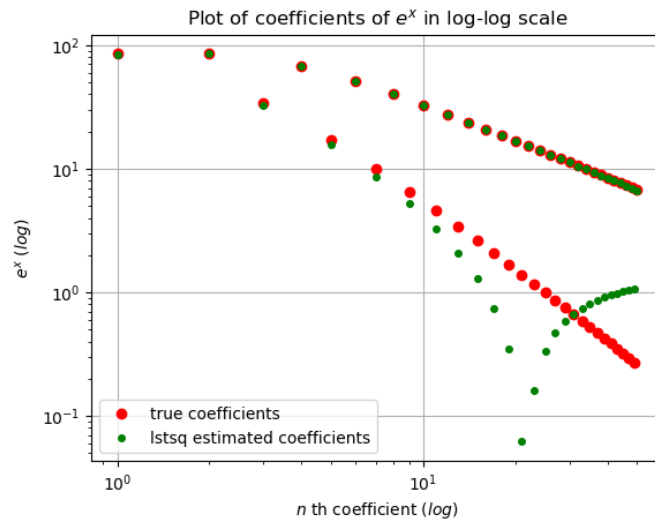


Figure 8: log-log plot of lstsq estimated coefficients of  $e^x$

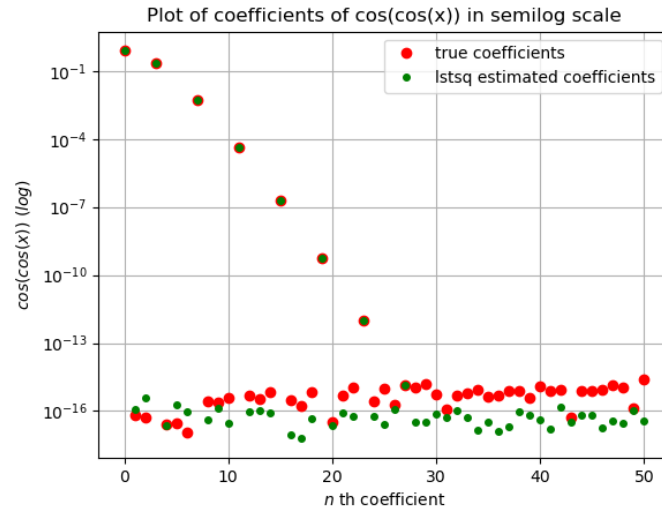


Figure 9: Semilog plot of lstsq estimated coefficients of  $\cos(\cos(x))$

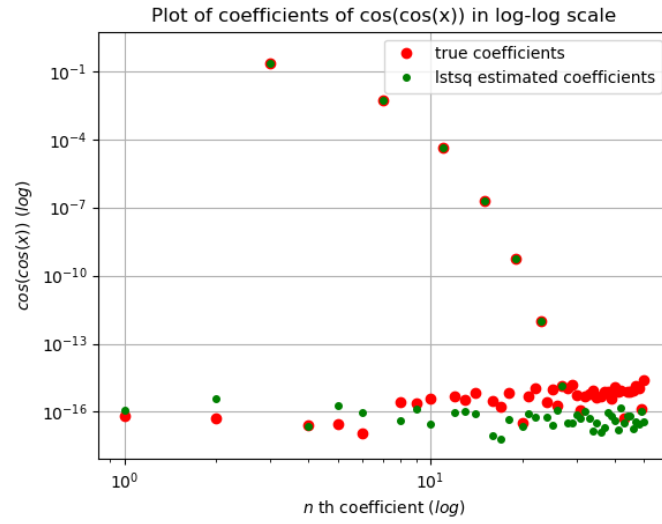


Figure 10: log-log plot of lstsq estimated coefficients of  $\cos(\cos(x))$

### 3.4 Plotting the estimated functions

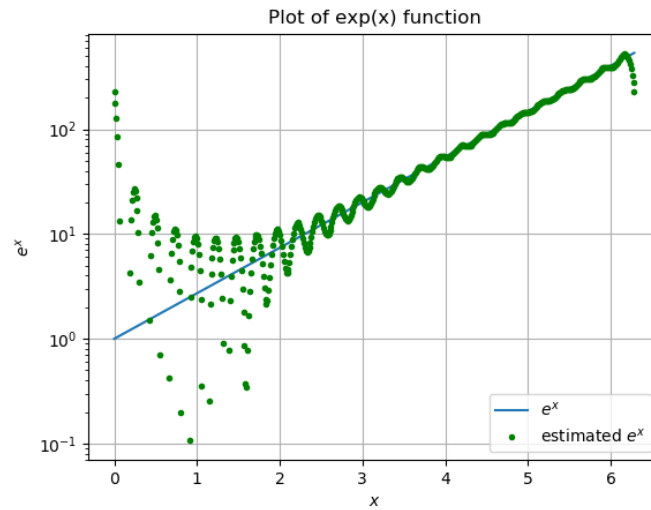


Figure 11: plot of estimated  $e^x$  function

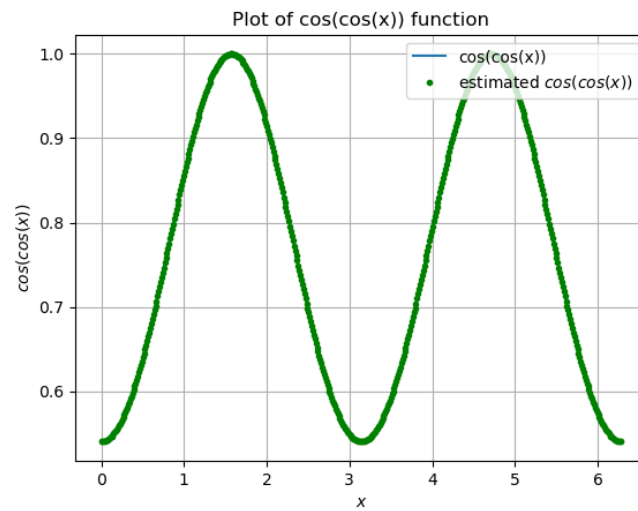


Figure 12: plot of estimated  $\cos(\cos(x))$  function

## 4 Conclusion

We plotted and analysed the two ways of generating Fourier coefficients for the given two functions  $e^x$  and  $\cos(\cos(x))$ . The methods used are the direct evaluation of the Fourier Series formula and the Least Square approach's best fit. The Least Square approach's values fit well for  $\cos(\cos(x))$  but diverge for  $e^x$