

# CS-449 Project Milestone 3: Optimizing, Scaling, and Economics

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**Last Updated:** 2021/05/17 17:04:57 +02'00'

**Due Date:** 04-06-2021 23:59 CET

**Submission URL:** <https://cs449-sds-2021-sub.epfl.ch:8083/m3>

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## Abstract

In this milestone, you will parallelize the computation of similarities by leveraging the Breeze linear algebra library for Scala, effectively using more efficient low-level routines. You will also measure how well your Spark implementation scales when adding more executors. You will finally compute economic ratios to help you choose the most appropriate infrastructure for your needs.

## 1 Motivation: Growing Pains

Your movie recommendation service is growing in number of users and movies rated, beyond the hobby side project you had started with. As your service is growing, the time to compute the *k-nearest neighbours* is growing also. If left unchecked, this may exceed the time your users are willing to wait to obtain high-quality suggestions.

In this last Milestone you are going to keep computation time within reasonable bounds in two steps: (1) you will first optimize your implementation for a single executor, aiming for a speedup of at least 10x compared to Milestone 2 (Section 3); (2) you will parallelize the execution of both the *k-NN* implementation and the predictions with Spark, using simple parallelization methods you have already used in the exercises (Section 4). The optimization will keep your technical requirements lower, and the scaling will enable you follow the growth of your users easily.

As your service is growing, so does the cost of the infrastructure you are using. In order to plan for future growth, in the most affordable way possible,

you will compute a few simple economic ratios to compare some currently available options for the supporting hardware infrastructure, either in a private or public cloud, to select one that provides you with the best bang for your buck (Section 5).

After completing this Milestone and the project, you will have had a basic but complete experience in implementing useful data analytics algorithms, measuring and analyzing their computing time and memory usage, optimizing their performance both on a single machine and in a distributed fashion, and planning required resources for future growth. You should therefore have a good foundation for pursuing a research career in distributed systems, doing more advanced development on real-world infrastructure, as well as leading a technical team in a startup.

## 2 Dataset

For the optimization part of this milestone, you will again use the MovieLens 100K dataset [3]. Again, for the sake of simplicity, you will only test on the `ml-100k/u1.test` dataset (with the corresponding `ml-100k/u1.base`). This will enable you to evaluate performance gains compared to your implementation of Milestone 2.

For the scaling part of this milestone, you will use a larger dataset in order to simulate a larger computation load on your service. Using the techniques of this Milestone, you could easily scale to 10M or 25M ratings while retaining a computation time that is within the bounds of a real-world service. However, to make your (busy) student life easier, you will test with the smaller 1M MovieLens dataset, which should take at most a minute to process (once optimized). You can find it here:

<https://grouplens.org/datasets/movielens/1m/>

However, the 1M dataset does not provide pre-split training and test sets, as the 100K, so you will use the scripts of the 10M dataset to split the ratings into a `ml-1m/ra.train` and `ml-1m/ra.test` datasets. Instructions for downloading the dataset, copying the scripts, and performing the split are provided in the template. As for the 100K dataset, in a real-life setting you would test on multiple splits of the dataset to ensure your results are not specific to one split and most likely generalize. But for the sake of the pedagogical exercise, it will be sufficient to only test on the `ml-1m/ra.train` and `ml-1m/ra.test` split.

## 3 Optimizing with Breeze, a Linear Algebra Library

Before throwing more computing resources at the problem, e.g. Spark Executors running on additional cluster machines, it is always worth verifying whether a single machine would actually be sufficient for the task. In some cases, as is the case for your recommender, a drastic reduction in computation time can be

achieved with slightly different, but mathematically equivalent, implementation techniques.

In the case of the recommender of this project, the performance of the same prediction algorithm in Python/Numpy shows that there is major room for improvement: we obtained computation times of 0.05s for computing all similarities and k-nearest neighbours on the `ml-100k/u1.base` dataset and 0.15s for computing all predictions on the `ml-100k/u1.test` dataset. Compared to students' reported execution times in Scala/Spark for Milestone 2, that were in the order of 20s of seconds for computing similarities and close to a minute for computing predictions, this represents potential for speedups of 400x. The major difference with Python/Numpy compared to using Spark's RDDs and DataFrame APIs, is the use of mature linear algebra libraries with efficient multi-core vectorized implementations.

As far as we are aware of, Scala does not offer complete and efficient equivalents to the Numpy libraries yet. The Breeze library<sup>1</sup> does however come somewhat close on a subset of operations and datatypes. Breeze is the recommended interface for Scala/Spark to the underlying netlib-java library<sup>2</sup>, itself a wrapper for low-level linear algebra libraries such as BLAS and LAPACK, that is used internally by the Spark mllib library. In this section, you will therefore use Breeze directly to reimplement the prediction algorithm of Milestone 2 and measure the speedup you can obtain. With relatively simple implementation techniques, you should obtain at least a 10x reduction in execution time. This can translate in at least a 10x reduction in the number of executors required to obtain the same computation time, potentially more depending on the overhead of RDD and Dataframe libraries and their parallization behaviour.

Note that to best leverage a linear algebra library, your implementation should compute *all* k-nearest neighbours prior to making predictions, instead of lazily based on which predictions to make, as the RDD API might have encouraged you to do in Milestone 2. You will notice that the speed up you obtain this way stays quite large even if you are actually computing more similarities than previously.

### 3.1 Overview of some Breeze Operations

Unfortunately, the breeze library has been on minimal maintenance mode for a couple of years<sup>3</sup> and the documentation is somewhat lacking<sup>4</sup>. To get you started, here is an overview of some operations we found useful in our reference implementation.

For all of them you should first import:

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<sup>1</sup><https://github.com/scalanlp/breeze>

<sup>2</sup><https://github.com/fommil/netlib-java>

<sup>3</sup><https://github.com/scalanlp/breeze/commits/master>

<sup>4</sup>This is no fault of the author, as the library does quite a lot as a labor of (volunteer) love, and as such is already quite an accomplishment. This highlights the issue of funding to maintain core open source infrastructure. If you ever work for a company that makes money using open source software, do remember to pay the benefits forward and sustain the open source commons by funnelling some funding towards the projects you depend on.

```
import breeze.linalg._
import breeze.numbers._
```

### 3.1.1 Dense Vector and Matrix

If all the data can fit in memory, the most efficient numerical operations are usually based around the `DenseVector` and `DenseMatrix` data types. There is a fairly comprehensive library for linear algebra, which supports efficient slicing, element-wise operations, and matrix multiplication. The set of operations and their equivalence in other numerical languages is listed here: <https://github.com/scalanlp/breeze/wiki/Linear-Algebra-Cheat-Sheet>.

When working with the `ml-100k/u1.base` dataset, a `DenseMatrix` can easily fit all the ratings in memory, even if they are sparse compared to `users * items`. Prefer a sparse matrix anyway since it makes it easier to try larger datasets with the same implementation.

### 3.1.2 Sparse Matrix

If a matrix, e.g. user-item ratings, does not fit in memory using a `DenseMatrix`, as is necessarily the case for the largest MovieLens datasets, you can use a `SparseMatrix` representation. The Breeze library only supports the Compressed Sparse Column (CSC) format<sup>5</sup>. Here is a summary of operations you might find useful.

#### Creation

You can efficiently create a `CSCMatrix` with the `CSCMatrix.Builder` as follows:

```
val builder = new CSCMatrix.Builder[Double](rows=943, cols=1682)
builder.add(row, col, value)
...
val x = builder.result()
```

The template already does this for the ratings, both for training and testing.

#### Slicing

You can obtain a `SliceVector` of rows  $i$  to  $j$  of column  $m$  with `x(i to j, m)` or a `SliceMatrix` of row  $i$  to  $j$  of columns  $m$  to  $n$  with `x(i to j, m to n)`. Note that if you slice to obtain a single row  $i$  between columns  $m$  and  $n$  you will obtain a "transposed" vector, which you may have to transpose again for some operations as they may not support the transposed version. Note also that the `::` operator (ex: `x(i, ::)`), which provides all elements along the corresponding dimension, is not supported on `SparseMatrix`. You have to explicitly provide a range  $i$  to  $j$  for that dimension.

<sup>5</sup>See Wikipedia for an overview of other formats: [https://en.wikipedia.org/wiki/Sparse\\_matrix](https://en.wikipedia.org/wiki/Sparse_matrix)

### Iteration

You can efficiently iterate through all non-zero elements of a `CSCMatrix` matrix  $x$  with:

```
for ((k,v) <- x.activeIterator) {  
  val row = k._1  
  val col = k._2  
  // Do something with row, col, v  
}
```

### Matrix multiplication

You can multiply matrix  $x$  by matrix  $y$  (both can also be slices with compatible dimensions) with  $x * y$ . You can use it to implement the  $s_{u,v}$  computation with pre-processed ratings of Milestone 2:

$$s_{u,v} = \sum_{i \in (I(u) \cap I(v))} \check{r}_{u,i} * \check{r}_{v,i} \quad (1)$$

Operating on slices of two `CSCMatrix` (or the same) is however slower than performing a matrix-vector multiplication, see below.

### Matrix-Vector multiplication

After a fair amount of experimentation, it seems that a `CSCMatrix-DenseVector` multiplication in Breeze is significantly faster than operating on `SliceMatrix` of a `CSCMatrix`, even when taking into account the conversion of a `SliceVector` to a `DenseVector` prior to the multiplication and the explicit iteration through rows/columns. I therefore recommend you organize the main  $k$ -NN computation, as defined in Eq. 1, around this primitive. To still keep a little bit of the fun in experimenting with different possible implementations, you will have to figure out yourself whether it is best to assign users to rows and items to columns of a `CSCMatrix` (or the opposite!) when preparing the  $\check{r}_{u,i}$  sparse matrix.

### Reduction

The reduction along a given dimension, such as performing a `sum(x, Axis._1)` is not supported. You can either explicitly create a `DenseVector` with the correct size for that dimension then iterate through all active (non-zero) elements as shown above. You can also do a matrix multiplication: for a matrix  $X$ , you can reduce the columns by multiplying  $X_{m,n} * 1_{n,1}$  or the rows by multiplying  $1_{1,m} * X_{m,n}$ , where  $1_{1,n}$  is an  $n$ -by-1 matrix of all 1 and  $1_{1,m}$  is a 1-by- $m$  matrix of all 1. Either options are useful for pre-processing the ratings, i.e. computing  $\check{r}_{u,i}$ , prior to computing  $s_{u,v}$ , you will have to measure which one is fastest.

### top-k elements

You can find the indices of the top  $k$  elements of a (non-transposed) `SliceVector`  $s$  with `argtopk(s, k)` and iterate through them with:

```
for (i <- argtopk(s,k)) {
  // do something with s(i)
}
```

It can sometimes be faster to call `argtopk` with a `DenseVector` instead of a `SliceVector`. You will have to measure whether this is significant.

### Element-wise operations

Many element-wise operations and boolean operations from <https://github.com/scalanlp/breeze/wiki/Linear-Algebra-Cheat-Sheet> are supported on `CSCMatrix`. Unsupported operations will result in compilation errors. You can quickly and interactively identify and test those that are supported with `sbt console` on a small test `CSCMatrix`, which you may create as such:

```
> val x = CSCMatrix[Double]((1.0, 2.0, 3.0), (4.0, 5.0, 0.0))
// x.<tab> for autocompletion of supported operations
```

### Others

See <https://github.com/scalanlp/breeze/blob/06b23cfa837c53e025bb70f0f4bc1f241986d0ba/math/src/test/scala/breeze/linalg/CSCMatrixTest.scala> for example usage of other supported operations on `CSCMatrix`. If you find success with additional operations, please share examples as above on the forum (but without giving away a complete solution) to help others.

## 3.2 Questions

1. Reimplement the `Predictor` of Milestone 2 using the Breeze library and without using Spark. Test your implementation on the 'ml-100k/u1.base' as a training set, and the 'ml-100k/u1.test' as a test dataset, and  $k = 200$ . Ensure your implementation gives a MAE of 0.7485 (within 0.0001). Output the MAE for  $k = 100$  and  $k = 200$  (We will use both for grading). (Make sure to make self-similarities equal to 0, i.e.  $s_{u,u} = 0$ , prior to computing the  $k$ -nearest neighbours.)
2. Measure the time for computing all *k-nearest neighbours* (even if not all are used to make predictions) for all users on the 'ml-100k/u1.base' dataset. Output the min, max, average, and standard-deviation over 5 runs in your implementation.
3. Measure the time for computing all 20,000 predictions of the 'ml-100k/u1.test'. Output the min, max, average, and standard-deviation over 5 runs in your implementation.
4. Compare the time for computing all *k-nearest neighbours* of 'ml-100k/u1.base' to the one you obtained in Milestone 2 (Q.2.2.7). What is the speedup of your new implementation (as a ratio  $\frac{t_{old}}{t_{new}}$ )? Why do you think that is the case? (Ensure you have obtained at least a 10x decrease in execution time)

for the *k-nearest neighbours* and predictions compared to Milestone 2. If you did not compute all *k-NN* in Milestone 2, use the time you reported for computing similarities.).

### 3.3 Tips

1. For any kind of optimization work, always make sure to first have a correct (and often simpler) implementation to compare against, to ensure your optimizations do not affect the correctness of the results. As you develop, compare the answers for both and ensure they answers stay the same. Your implementation of Milestone 2 can serve for this.
2. Prior to optimizing, make sure to measure how long each part of your program takes. Our intuitions of what is fast and slow is (most) often wrong, so always measure first to focus you attention on the parts that matter most.
3. Always tackle the slowest parts first, then move to the others. As you optimize, the bottlenecks, i.e. the parts that slow your program the most, will change.
4. Optimization work can be addictive. It also suffers from diminishing returns, i.e. the biggest gains can be obtained with relatively little work but further gains will take increasingly larger amounts of work. For the sake of the project, we are aiming for a  $10x$  reduction in computation time for both the *k-NN* computations and the prediction time. For a more precise reference see below.
5. As a reference, without using Spark and running on the `iccluster041.iccluster.epfl.ch`, we have obtained a time of  $\approx 1s$  for computing all *k-NNs* on `ml-100k/u1.base`, prior to making predictions, and less than 4s for making all 20,000 predictions. You should be able to obtain similar results with a reasonable and systematic effort. If in doubts, share your running times on the forum.

## 4 Scaling with Spark

In a real-world setting, your number of users may outgrow the capabilities of a single machine, even after extensive optimization work. In that case, distributing the execution on multiple machines allows your implementation to grow with the number of users. The two main parts worth parallelizing are *k-NN* and making predictions.

For this Milestone, you will use a simple parallelization strategy in which every worker (Spark executor) will obtain a copy of the input data and they will compute different parts of the output. The distribution of the shared input data is done efficiently with Spark's *broadcast variables*.

For  $k$ -NN, workers will compute the top  $k$  users for different subsets of users. The results are then reassembled on the driver node in a sparse  $k$ -NN `CSCMatrix`. A high-level presentation of the parallelization strategy is given in Algorithm 1. A similar pattern can be used to make predictions by parallelizing over pairs of user-items  $(u, i)$  to output a tuple user-item-prediction  $(u, i, p_{u,i})$  and storing them in a `CSCMatrix`. The MAE is then simply `sum(abs(pred-test))/test.activeSize`.

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**Algorithm 1** Parallel k-NN Computations with Replicated Ratings (Spark)

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```

1: Input  $r_{\bullet,\bullet}$  (ratings),  $sc$  (SparkContext),  $k$  (number of nearest neighbours)
2:  $\check{r}_{\bullet,\bullet} \leftarrow \text{preprocess}(r_{\bullet,\bullet})$  ▷ Similar to Milestone 2
3:  $br \leftarrow sc.\text{broadcast}(\check{r}_{\bullet,\bullet})$ 
4: procedure  $\text{topk}(u)$ 
5:    $\check{r}_{\bullet,\bullet} \leftarrow br.\text{value}$  ▷ Retrieve broadcast variable
6:    $s_{u,\bullet} \leftarrow \text{similarities}(u, \check{r}_{\bullet,\bullet})$  ▷ Using Matrix-Vector multiplication
7:   return  $(u, \text{argtopk}(s_{u,\bullet}, k).map(v \rightarrow (v, s_{u,v})))$  ▷ Compute k-NN for user  $u$ 
8: end procedure
9:  $\text{topks} \leftarrow sc.\text{parallelize}(0 \text{ to } nb\_users).map(\text{topk}).collect()$ 
10:  $knn \leftarrow knnBuilder(\text{topks})$  ▷ Using the CSCMatrix.Builder
11: return  $knn$ 

```

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## 4.1 Questions

In the following questions, you will ensure this distributed version gives the same results you obtained previously and assess its scalability and resource usage.

1. Test your spark implementation with the `ml-1m/ra.train` as a training set, and the `ml-1m/ra.test` as a test dataset, and  $k = 200$  (the command to do so is provided in the README of the template). Output the MAE you obtain.
2. Manually run your implementation on the cluster 5 times and compute the average. Compare the average  $kNN$  and *prediction* time to your optimized (non-Spark) version of Section 3 on the `ml-1m/ra.train` dataset. For the Spark version of this section, use a single executor, i.e. `--master "local[1]"` when using `spark-submit`. Are they similar? If not, how much overhead does Spark add? Answer both questions in your report.
3. Measure and report  $kNN$  and *prediction* time when using 1, 2, 4, 8, 16 executors on the IC Cluster in a table. Perform each experiment 3 times and report the average, min, and max for both  $kNN$  and *predictions*. Do you observe a speedup? Does this speedup grow linearly with the number of executors, i.e. is the running time  $X$  times faster when using  $X$  executors compared to using a single executor? Answer both questions in your report.



## 4.2 Tips

1. Use the following command to vary the number of executors on the IC-Cluster (once connected on the `iccluster041.iccluster.epfl.ch` driver node): `spark-submit --master yarn --num-executors X ...` where `X` is the number of executors to use.

## 5 Economics

You have seen that the optimizations of Section 3 may translate in lower needs for additional hardware. In this section, you will quantify the economics of buying/renting hardware to execute your recommender. You will, in the process, obtain insights into the economic benefits of optimization as well as develop an ability to estimate the running costs of a given implementation.

These days, you have many choices of hardware infrastructure. The landscape and particular tradeoffs of each point, are too broad to cover in this project. But since it may affect some design decisions, let's quickly review three representative examples of currently available hardware, summarized in Table 1, and provide some context in which they may be useful.

First, you may choose not to distribute your similarity computations and instead replace your re-purposed desktop machine, with a more powerful one, i.e. with increased RAM and better processor performance. One representative example is a powerful server. For example, the server in the IC IT Cluster with the largest amount of main memory, at 1.5TB of RAM, is listed in Table 1. The main advantage of this approach is that you don't have to change your software implementation, which sometimes is not possible because your particular algorithms are not easily distributed, and other times might be too complex for the skills or development time you currently have. However, the main drawback is that higher-end machines are usually more expensive because they are produced in lower volumes and sold at higher margins. The running costs at idle are also higher because all the added circuitry needs to be powered, even if not used.

Second, if your algorithms can be distributed, which fortunately is the case for k-NN [5, 4], you may elect to distribute them on virtualized cloud infrastructure. Today's cloud providers have many virtualization offerings, with one example based on containers, i.e. isolated processes running within the same operating system. Virtualization makes available the underlying hardware at a finer granularity, e.g. per CPU per second, as listed in the second line of Table 1. The pricing structure for the IC IT cluster suggests that the same hardware is rented in both cases, the previous case being equivalent to renting upfront all the capabilities of the hardware for an entire day. The main advantages of virtualized cloud offerings are potentially reduced maintenance costs, as the maintenance of the hardware is centralized and shared between multiple

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<sup>6</sup>From EUR to CHF, as listed here (Jan. 20th 2021) <https://buyzero.de/products/compute-module-4-cm4?variant=32090358612070&src=raspberrypi>

<sup>7</sup>Electricity (3W (idle) - 15W (max)) <https://www.raspberrypi.org/documentation/hardware/raspberrypi/power/README.md>, 0.15CHF/kWh)

Hardware	RAM	CPU	Buying Costs	Operating Costs
ICC.M7	24x64GB DDR4 -2666: 1.5 TB	2x Intel Xeon Gold 6132 (Skylake) 2x 14 cores, 2.6 GHz, 19.25 MB L3 cache	–	20.40CHF/day
				1 GB-s: $1.5e^{-7}$ CHF/s (0.012CHF/day)
Containers	Unspec.	Unspec.	–	1 vCPU-s: $1.02e^{-6}$ CHF/s (0.092CHF/day)
				1 vGPU-s: $6.583e^{-5}$ CHF/s (5.68CHF/day)
RPi 4 Compute Module	8GB LPDDR4 -3200 SDRAM	Broadcom BCM2711 quad-core Cortex-A72 ARMv8 64-bit SoC@1.5GHz	94.83CHF <sup>6</sup>	0.0108CHF/day - 0.054CHF/day <sup>7</sup> + Maintenance

Table 1: Technical specifications and cost of IC IT cloud offerings, compared to the highest performing Raspberry Pi available in 2021, a cheap and widely available consumer computing device.

cloud users, and offloading the risks associated with under- or over-provisioning hardware infrastructure compared to actual business needs (you only pay what you use). However, if the actual maintenance costs for some applications are low, and computing needs are stable and foreseeable, the cost of acquiring hardware may actually be recouped in a few years. Moreover, if user data is subject to stringent privacy limitations, it may sometimes not be possible to process it in a cloud (although there are plenty of ongoing research and industrial developments aiming to provide better privacy guarantees). Also, the electronic waste, carbon emissions, and energy usage, of cloud providers may be higher than what you could obtain with privately-operated infrastructure [2].

Third, you may distribute your algorithms on hardware you acquire and maintain yourself, by favouring cheap, energy-efficient, and widely available commodity hardware, an approach that was pioneered by Google in 1998. For example, the highest performing Raspberry Pis are increasingly closing the gap with Desktop and Server performance at a really low price point. The specification and costs, as of January 2021, are listed in the third line of Table 1. While there is still a significant gap in performance with the most powerful hardware of today, RaspberryPi 4 Compute Modules are on par or more powerful than the servers used by Google in 2005, are more energy efficient by a factor of 4-5x, and probably less expensive by a factor at least 4-5x [1]! They provide the same advantages as Hardware-as-a-Service, in having full access to the hardware and their operating costs (when only taking electricity into account) are lower than equivalent virtualized offerings for the same performance. Moreover, private data never leaves the organization, the hardware can be used for longer than the typical 2-3 years turn-around time of cloud servers (lowering e-waste and grey energy), and they can be setup to operate on renewable energy at reasonable costs [2]. However, setting up the infrastructure and maintaining the software up-to-date requires labor time, which may more than offset the lower operating costs. They also have higher initial costs compared to cloud offerings, but, given the low price of individual devices, that cost may be spread over time and engaged as computing needs grow.

The following questions will help you analyze how technical capabilities relate to application needs, and acquire or rent the right amount of hardware resources for your current and future needs.

## 5.1 Questions

For the following questions, make the following assumptions<sup>8</sup>:

- Throughput of 1 single Intel CPU core  $\approx$  4 Cortex-A72 (16 cores total)<sup>9</sup>

<sup>8</sup>For real deployments, you would have to empirically verify these assumptions, and revise them as the application, the landscape of hardware offerings, and your software implementation evolve.

<sup>9</sup>Rough estimate based on the performance of the more recent Intel Xeon E3-1230 v6, which has 4 cores instead of 14, on the following benchmark: <https://truebenchmark-the-toffee-project.org/>. Note that the Intel cores have hyper-threading, which doubles some of hardware to obtain twice the number of virtual CPUs and is clocked almost twice

- Containers use the same CPU and RAM as the ICC.M7 machine
- The ICC.M7 costs 35,000 CHF (based on a 39,000\$USD quote from the Dell website in the US, created on Jan. 21st 2021)
- Users rate on average 100 movies
- A good  $k$  for k-NN, to obtain a significant gain in accuracy compared to average global deviation, is 200
- The nodes should hold in memory both (1) the similarity values obtained from k-NN and (2) all movie ratings for all users, by distributing them roughly equally between many nodes, while still leaving 50% of memory free for computation and other tasks
- Use floats (32-bit floating point numbers) for similarity values  $s_{u,v}$  and 8-bit unsigned ints for ratings  $(r_{u,i})$
- 1 GB =  $10^9$  Bytes (manufacturers sometimes use  $1\text{GB} = 1024^3$ )
- Assume a year is always 365 days (no leap years)

Answer the following questions:

1. How many days of renting does it take to make buying the ICC.M7 less expensive? How many years does that represent?
2. What is the daily cost of an IC container with the same amount of RAM and CPUs (1 vCPU = 1 core) as the ICC.M7 machine? What is the ratio of  $\frac{ICC.m7(CHF/day)}{Container(CHF/day)}$ ? Is the container cheaper (consider a difference of less than 5% to be negligible)?
3. Idem, but compared to 4 Raspberry Pis (to obtain the same CPU throughput)? What is the ratio  $\frac{4RPis(CHF/day)}{Container(CHF/day)}$  at max power for the RPi? at min power for RPi? Is the container cheaper than the 4RPis (consider a difference of less than 5% to be negligible)?
4. After how many days of renting a container, is the cost higher than buying and running 4 Raspberry Pis? (1) Assuming optimistically no maintenance at minimum power usage, and (2) no maintenance at maximum power usage, to obtain a likely range. (Round up days)
5. For the same buying price as an ICC.M7, how many Raspberry Pis can you get? Assuming perfect scaling, would you obtain a larger overall throughput and RAM from these? If so, by how much (ratio)?
6. How many users can be held in memory per GB? Per RPi? Per ICC.M7?
7. Based on your answers, which would be your preferred option of the three? Would you buy or rent? Why?

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higher, so the actual performance per ARM core is actually much better than it may seem at first sight.

## 5.2 Tips

1. Write down the full equation with units for every term when calculating ratios.

## 6 Deliverables

You can start from the latest version of the template:

- Zip Archive: <https://gitlab.epfl.ch/sacs/cs-449-sds-public/project/cs449-Template-M3/-/archive/master/cs449-Template-M3-master.zip>
- Git Repository:

```
git clone
```

```
https://gitlab.epfl.ch/sacs/cs-449-sds-public/project/cs449-Template-M3.  
git
```

We may update the template to clarify or simplify some aspects based on student feedback during the next weeks, so please refer back to <https://gitlab.epfl.ch/sacs/cs-449-sds-public/project/cs449-Template-M3> to see the latest changes.

Provide answers to the previous questions in a **pdf** report (if your document saves in any other format, export/print to a pdf for the submission). Use the sub-section numbers of this document to group your answers, i.e. Section 3.2 and 5.1. Also, provide your source code (in Scala):

```
CS449-YourID-M3/  
report-YourID-M3.pdf  
optimizing/build.sbt  
optimizing/src/main/scala/Predictor.scala  
scaling/build.sbt  
scaling/src/main/scala/Predictor.scala  
scaling/project/plugins.sbt  
economics/build.sbt  
economics/src/main/scala/Economics.scala
```

Your executables should output their numerical answers and timing measurements in the JSON format, following the conventions for keys and data types provided in the template.

Add any other packages or source files you have created. Remove all other unnecessary folders (ex: `project/project`, `project/target`, and `target`). Ensure your project automatically and correctly downloads the missing dependencies and correctly compile from only the files you are providing. Ensure the `optimizing.json`, `scaling-100k.json`, `scaling-1m.json`, and `economics.json` files are re-generated correctly using the commands listed in `README.md`. If in doubt, refer to the `README.md` file for more detail.

Once you have ensured the previous, remove again all unnecessary folders, as well as the datasets (`data/ml-100k`, `data/ml-100k.zip`, `data/ml-1m`, `data/ml-1m.zip`, and `data/ml-10M100K`, `data/ml-10m.zip`, if present), zip your archive (`CS449-YourID-M3.zip`), and submit to the TA. Your archive should be around or less than 1MB.

## 7 Grading

We will use the following grading scheme:

	Points
Questions	35
Source Code Quality & Organisation	5
<b>Total</b>	<b>40</b>

Points for 'Source Code' will reflect how easy it was for the TA to run your code and check your answers. Grading for answers to the questions without accompanying executable code will be 0. We will enforce the minimal project structure of the previous section, as well as the JSON output format: deviations will cost points. If you really need to change any of those, please ask on the Moodle forum first.

### 7.1 Collaboration vs Plagiarism

You are encouraged to help each other better understand the material of the course and the project by asking questions and sharing answers. You are also very much encouraged to help each other learn the Scala syntax, semantics, standard library, and idioms and Spark's Resilient Distributed Data types and APIs. It is also fine if you compare answers to the questions before submitting your report and code for grading. The dynamics of peer learning can enable the entire class to go much further than each person could have gone individually, so it is very welcome.

However, you should write the report and code individually. You should also compare answers *only after having attempted the best shot you can do alone*, well ahead of the deadline, and after doing your best to understand the material and hone your skills. The main reason is pedagogical: we have done our best to prepare a project that removes much of the accidental complexity of the topic, would be much more accessible than learning directly from the research literature, and would be deeper and more balanced than marketing material for the latest technologies. But for that pedagogical experience to give its fruits, you have to put enough efforts to have it grow on you.

To make grading simpler and scalable, so you will have feedback in a timely manner, we have opened the possibility to short-cutting the entire learning process and go for maximal grade with minimal effort. If you do so, you will not only completely waste a great personal opportunity to develop useful skills, you will lower the reputation of an EPFL education for all your colleagues,

and you will be wasting the resources Society is collectively investing in your education. So we will be remorseless and drastically give 0 to all submissions that are copies of one another.

## 8 Updates

None yet!

## References

- [1] Google machine. <https://google-services.blogspot.com/2006/07/google-machine.html>, 2006. Accessed: 2021-01-21.
- [2] DE DECKER, K. Low-tech magazine: Solar-powered website. <https://solar.lowtechmagazine.com/about.html>, 2019. Accessed: 2021-01-21.
- [3] HARPER, F. M., AND KONSTAN, J. A. The MovieLens datasets: History and context. *ACM Transactions on Interactive Intelligent Systems* 5, 4 (Dec. 2015), 19:1–19:19.
- [4] KARYDI, E., AND MARGARITIS, K. Parallel and distributed collaborative filtering: A survey. *ACM Comput. Surv.* 49, 2 (Aug. 2016).
- [5] SCHELTER, S., BODEN, C., AND MARKL, V. Scalable similarity-based neighborhood methods with mapreduce. In *Proceedings of the Sixth ACM Conference on Recommender Systems* (New York, NY, USA, 2012), RecSys ’12, Association for Computing Machinery, p. 163–170.

## A Notation

- $u$  and  $v$ : *users* identifiers
- $i$  and  $j$ : *items* identifiers
- $\bar{r}_{\bullet,\bullet}$ : average over a range, with  $\bullet$  representing all possible identifiers, either *users*, *items*, or both (ex:  $\bar{r}_{\bullet,i}, \bar{r}_{u,\bullet}, \bar{r}_{\bullet,\bullet}$ ), ex:  $\bar{r}_{u,\bullet} = \frac{\sum_{r_{u,i} \in \text{Train}} r_{u,i}}{\sum_{r_{u,i} \in \text{Train}} 1}$
- $\hat{r}_{u,i}$ : deviation from the average  $\bar{r}_{u,\bullet}$
- $r_{u,i}$ : rating of user  $u$  on item  $i$ , ( $u$  is always written before  $i$ )
- $p_{u,i}$ : predicted rating of user  $u$  on item  $i$
- $|X|$ : number of items in set  $X$
- $*$ : scalar multiplication
- $r_{u,i}, r_{v,i} \in \text{Train}$ : both  $r_{u,i}$  and  $r_{v,i}$  are elements of *Train* for the same  $i$

- $1_x$ : indicator function,  $\begin{cases} 1 & \text{if } x \text{ is true} \\ 0 & \text{otherwise} \end{cases}$
- $u, v \in U$ : shorthand for  $\forall u \in U, \forall v \in U$
- $R(u, n)$ : top  $n$  recommendations for user  $u$  as a list
- $sorted_{\searrow}(x)$ : sort the list  $x$  in decreasing order
- $[x|y]$ : create a list with elements  $x$  such that  $y$  is true for each of them
- $top(n, l)$ : return the highest  $n$  elements of list  $l$
- $U$ : set of users
- $I$ : set of items
- $U(i)$ : is the set of users with a rating for item  $i$  ( $\{u | r_{u,i} \in \text{Train}\}$ )
- $I(u)$ : is the set of items for which user  $u$  has a rating ( $\{i | r_{u,i} \in \text{Train}\}$ )