





Key Concepts of a Quantum State





ENTANGLEMENT





MEASUREMENT



PROBABILITY AND AMPLITUDES



Mathematical Representation of a Quantum State

A quantum state $|\psi\rangle$ is generally expressed as a combination of basis states:

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

where:

- α and β are complex probability amplitudes.
- The total probability must always be 1:

$$|\alpha|^2 + |\beta|^2 = 1$$

For larger systems, quantum states can describe **multi-qubit** systems or even entire quantum systems in **higher dimensions**.



Example of a Quantum State

Single-Qubit State: A qubit in a superposition might be:

$$rac{1}{\sqrt{2}}|0
angle+rac{1}{\sqrt{2}}|1
angle$$

This means the qubit has equal probability (50%) of being measured as |0\) or |1\).

• Entangled State: Two entangled qubits could be in the Bell state:

$$rac{1}{\sqrt{2}}(\ket{00}+\ket{11})$$

This means that if one qubit is measured as |0⟩, the other must also be |0⟩, and the same for |1⟩.

Why Is the Quantum State Important?



